

# Simultaneous-source seismic data acquisition and processing with compressive sensing

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# Introduction

Seismic data acquisition

- marine surveys
- static vs. dynamic geometries
- time-lapse surveys

# Marine seismic surveys

**S** : seismic source (air-gun arrays)

• : receivers (hydrophones and/or geophones)

**1** : towed-streamer geometry (**moving receivers => dynamic geometry**)

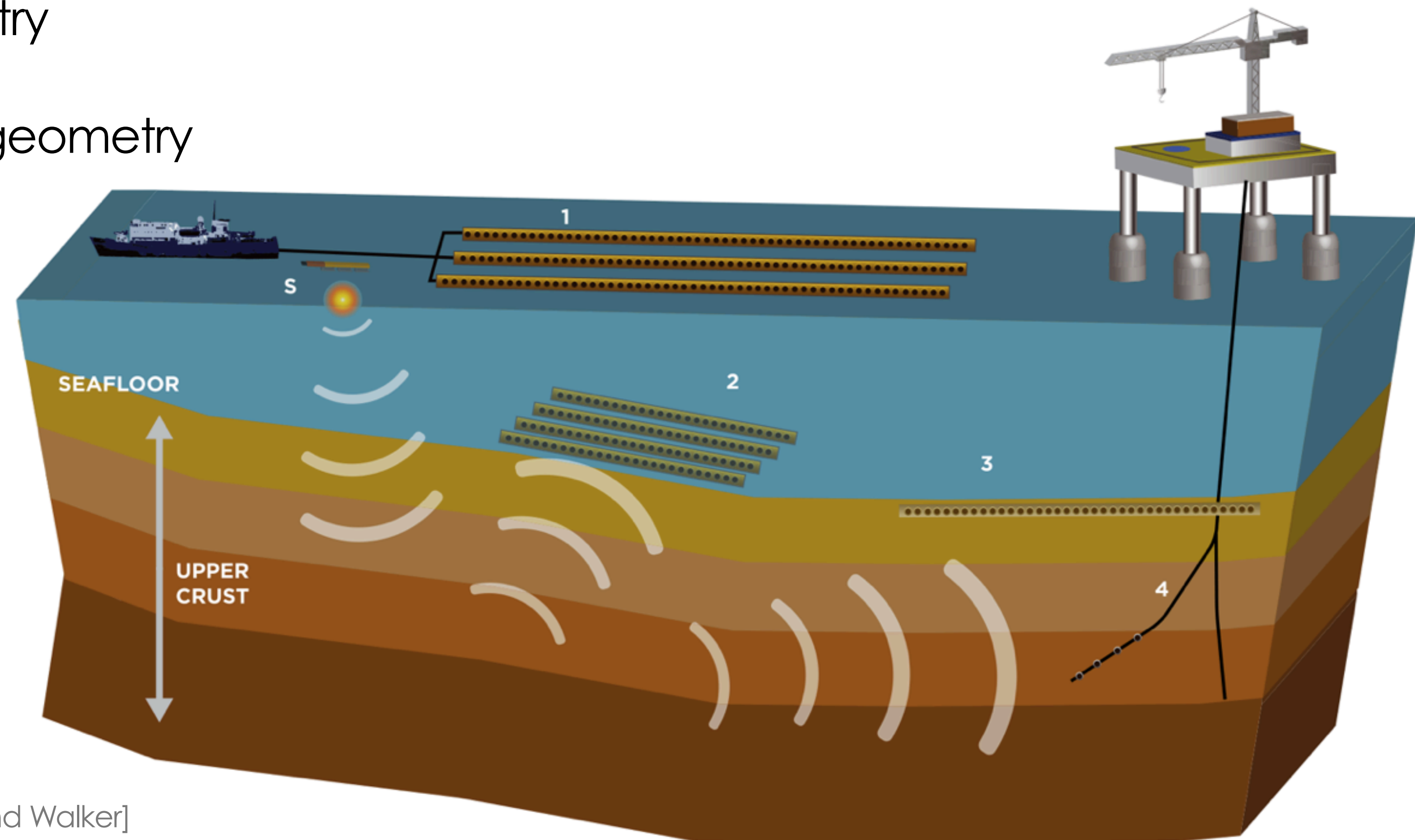
**2** : ocean-bottom geometry

**3** : buried seafloor array

**4** : vertical seismic profile geometry

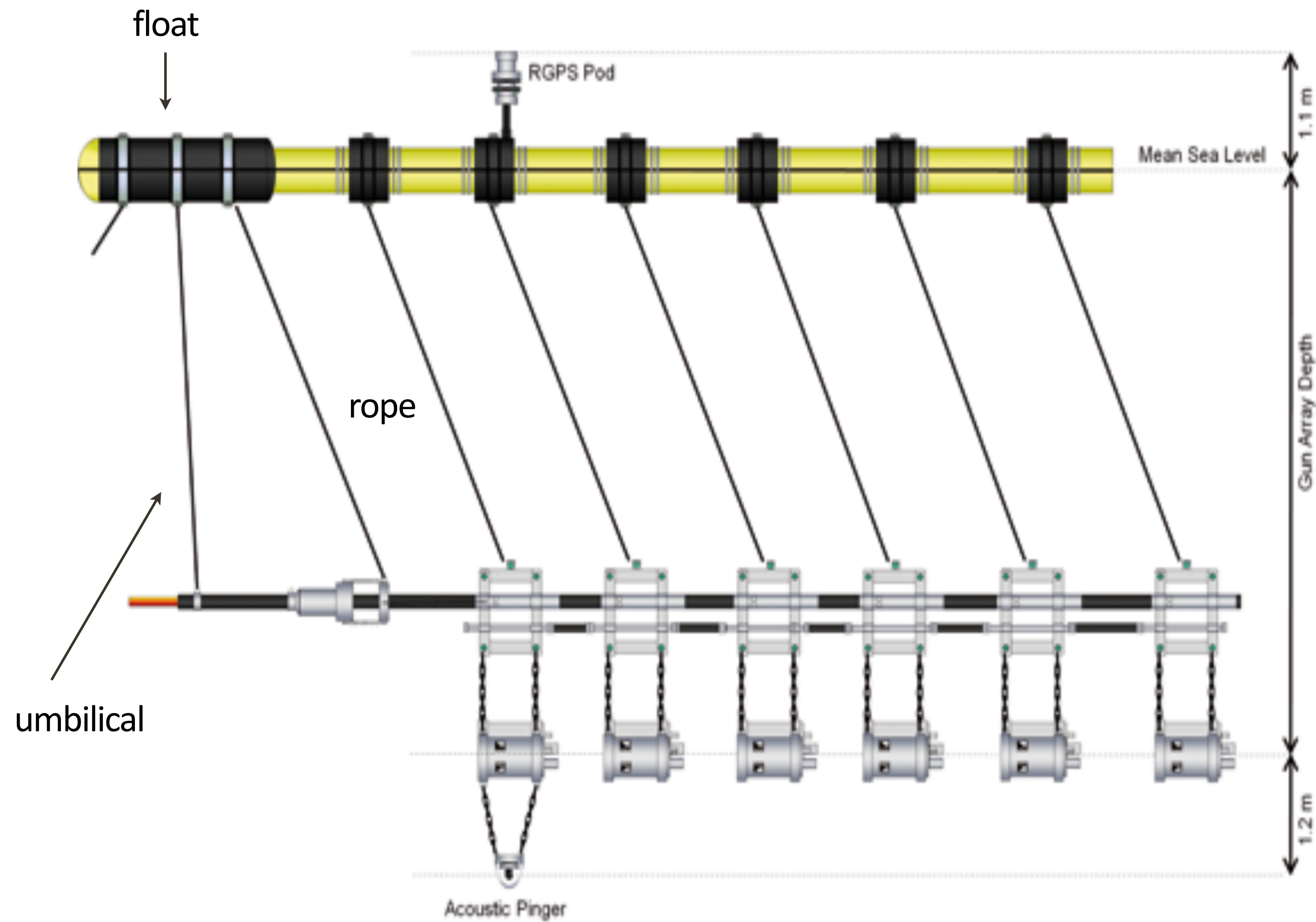
**2 - 4: fixed receivers**

**=> static geometries**

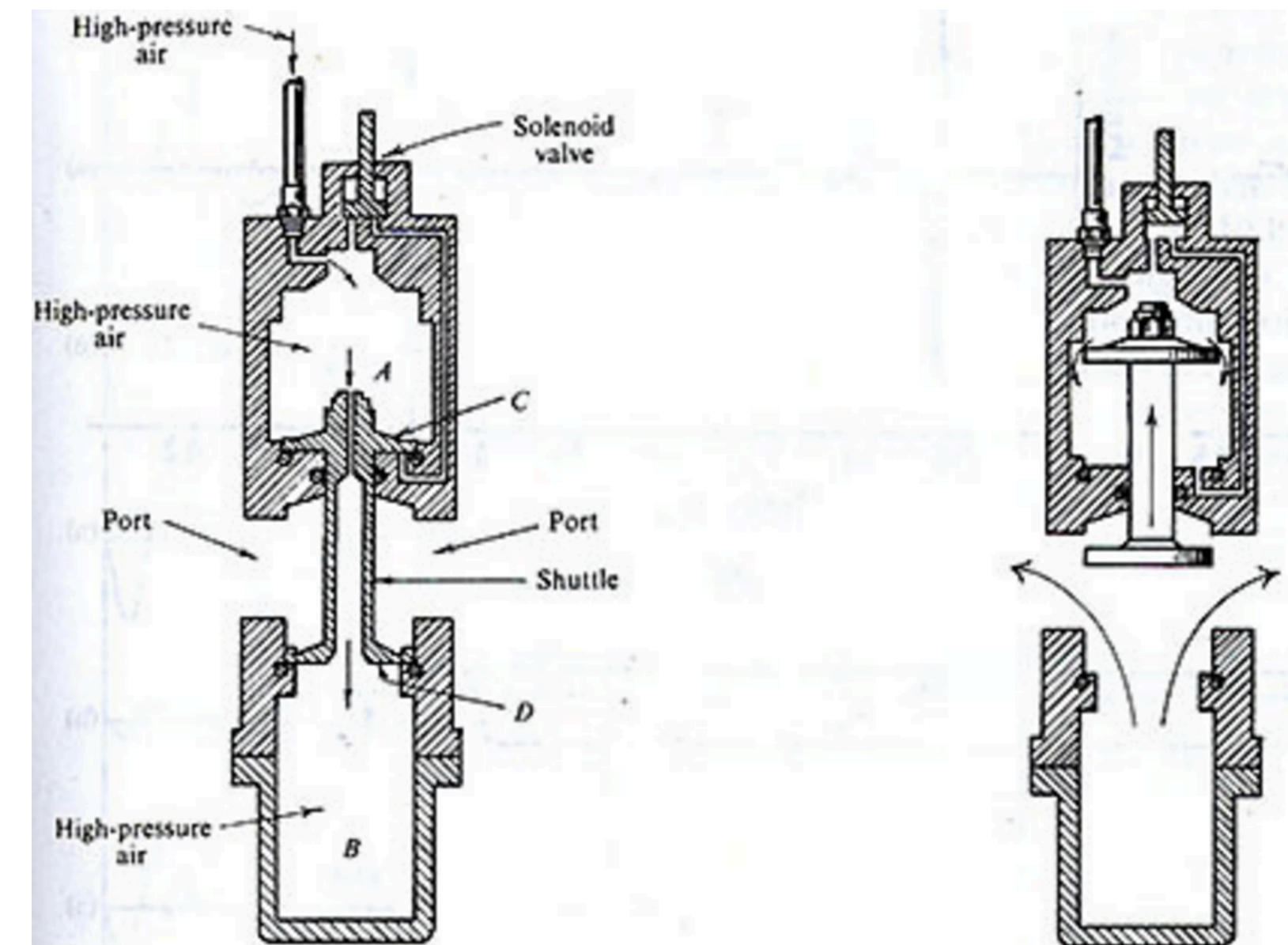




# Marine seismic source



side view of an air-gun array

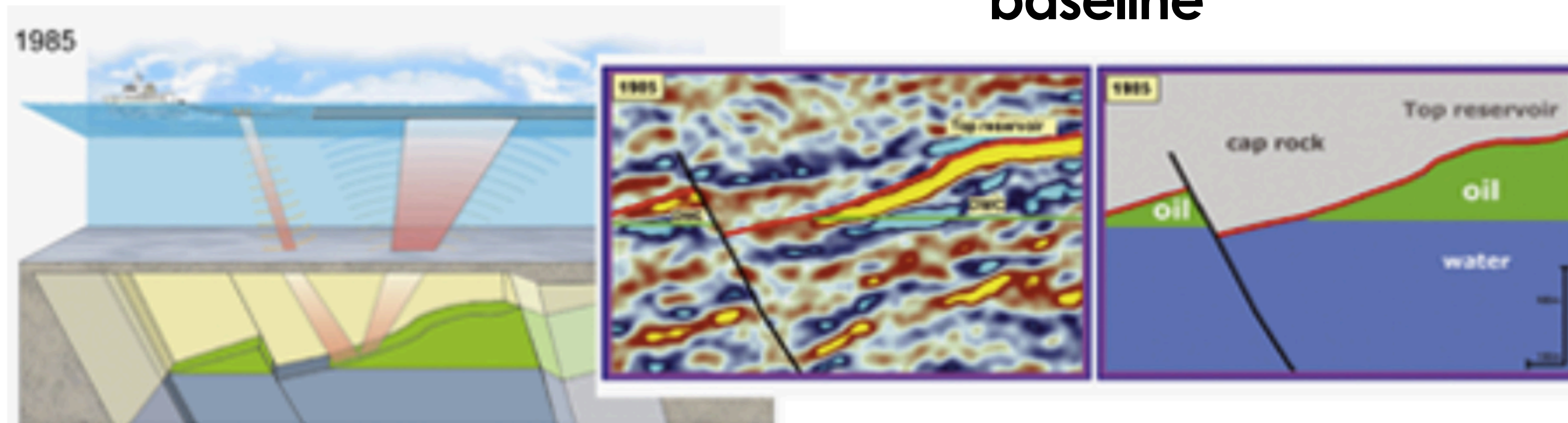


schematic of air gun primed (left)  
and firing (right)

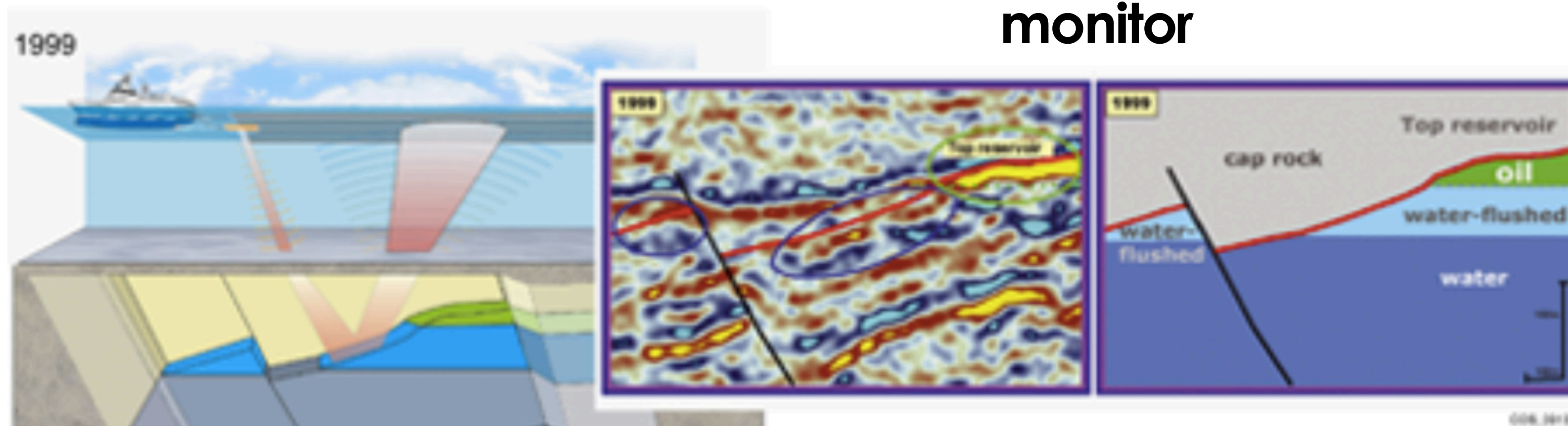


# Time-lapse (or 4D) surveys

## baseline



## monitor



Principle of 4D acquisition

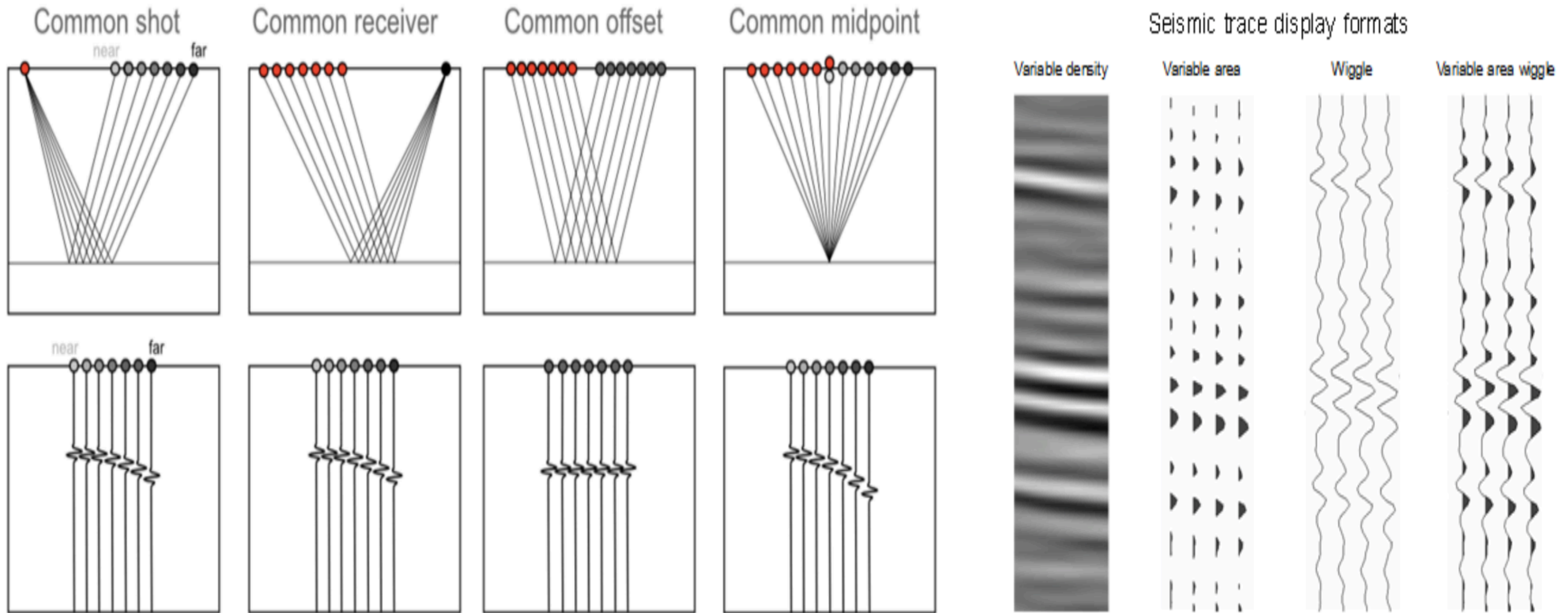
Gullfaks field

## Seismic reservoir monitoring

- compare seismic surveys re-run some time apart (order of months or years) over the same area
- monitor changes in the reservoir over time due to production



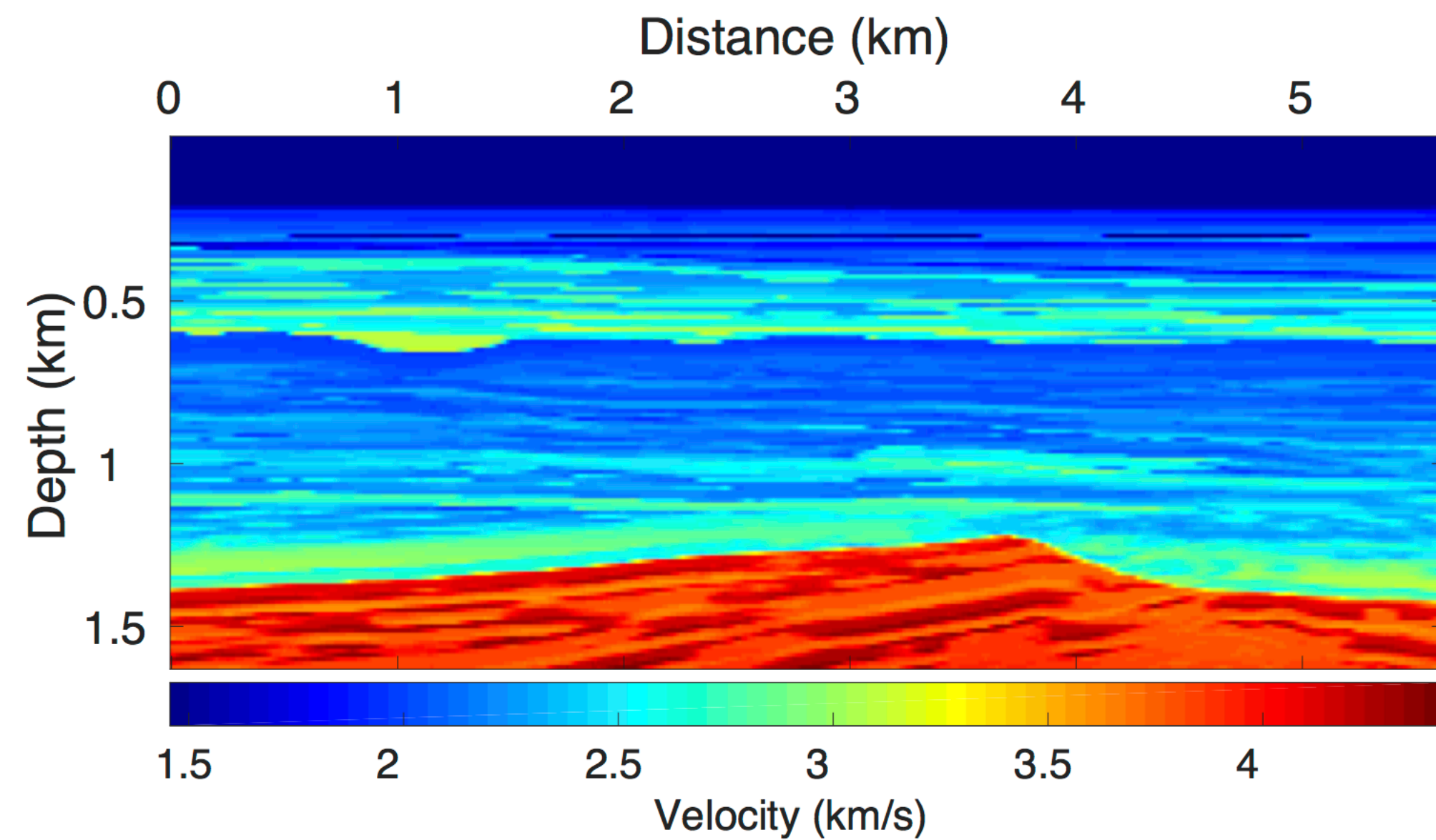
# Types of gathers & trace display formats



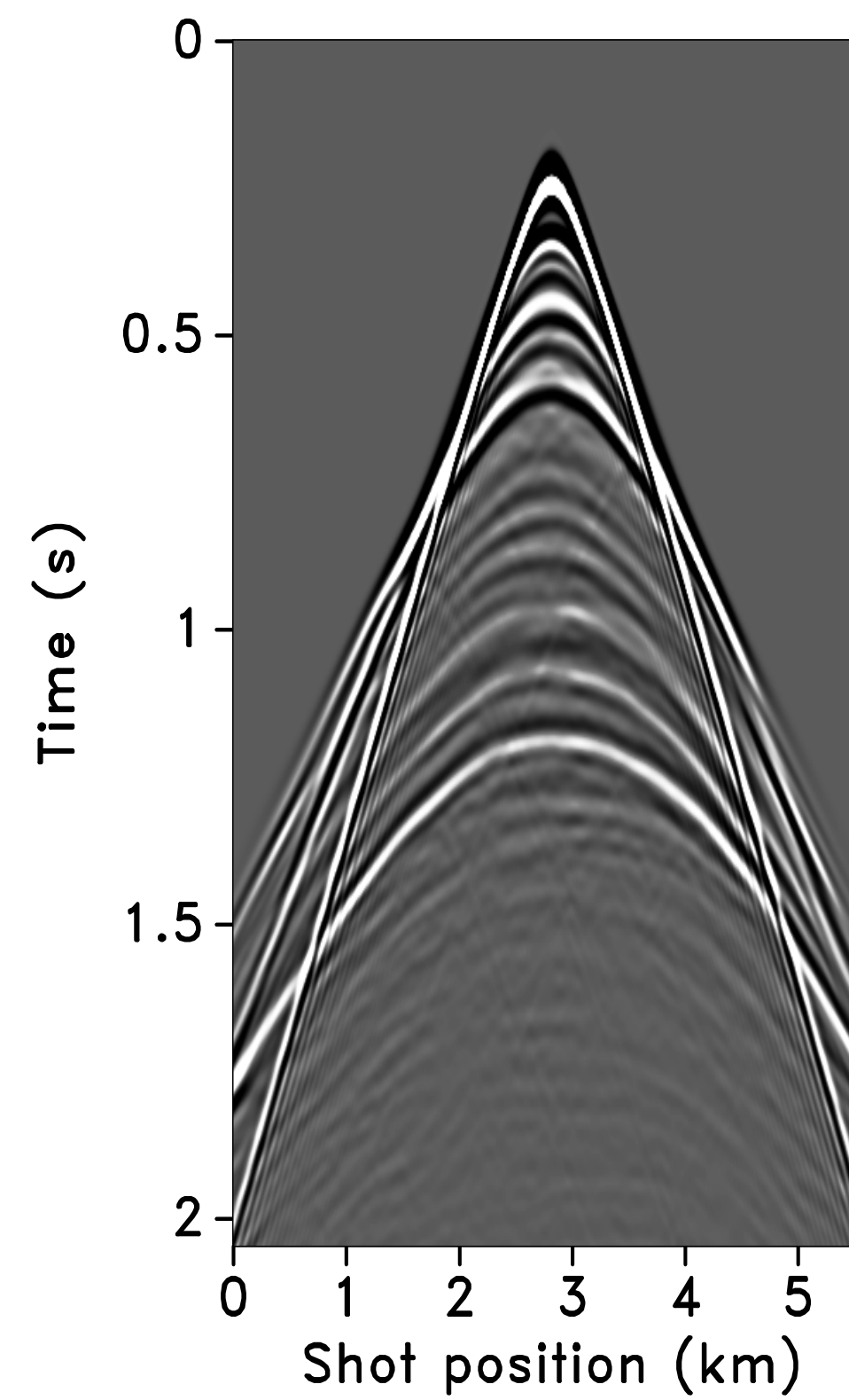


# Types of gathers

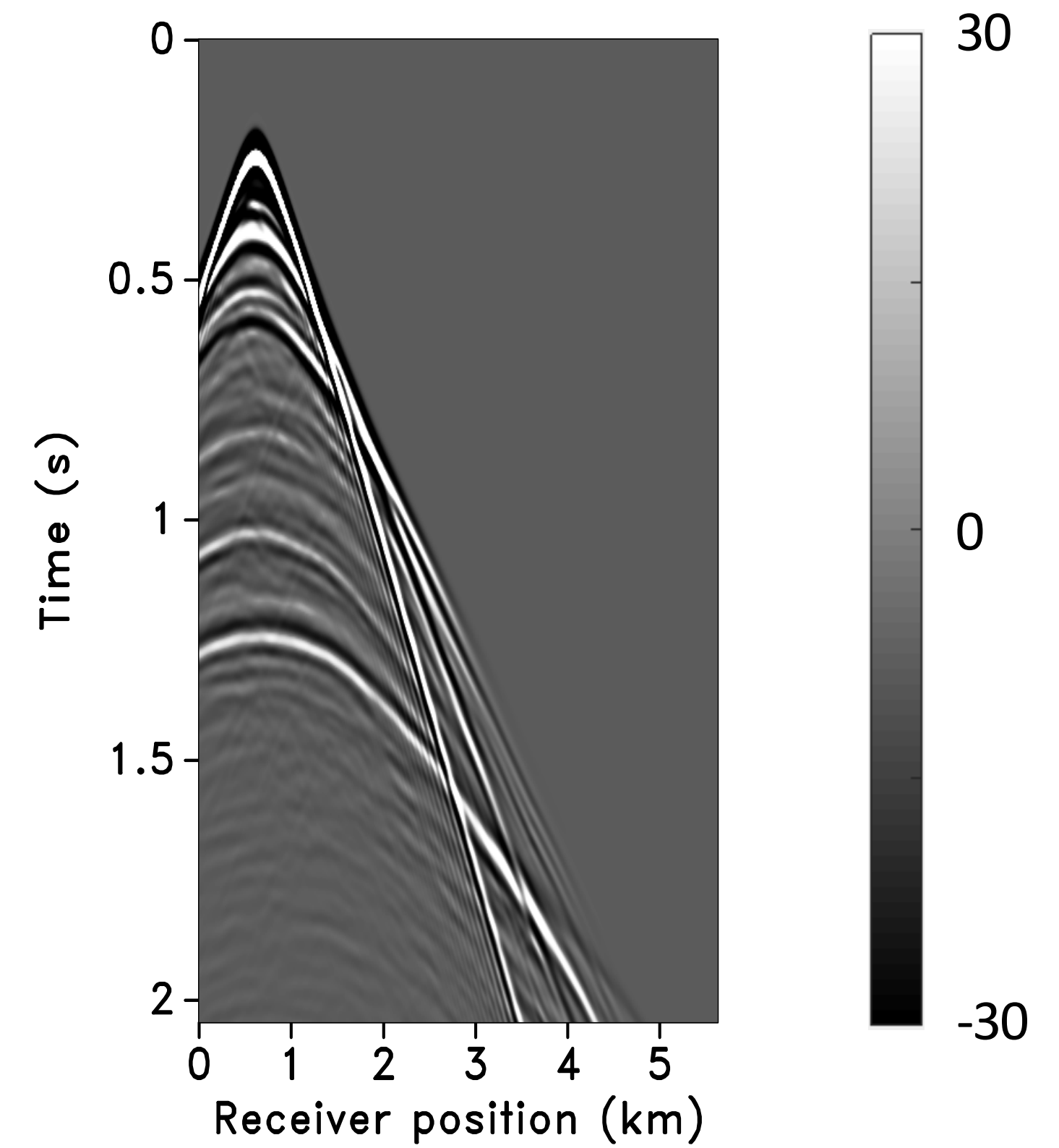
## Earth model



## Receiver gather

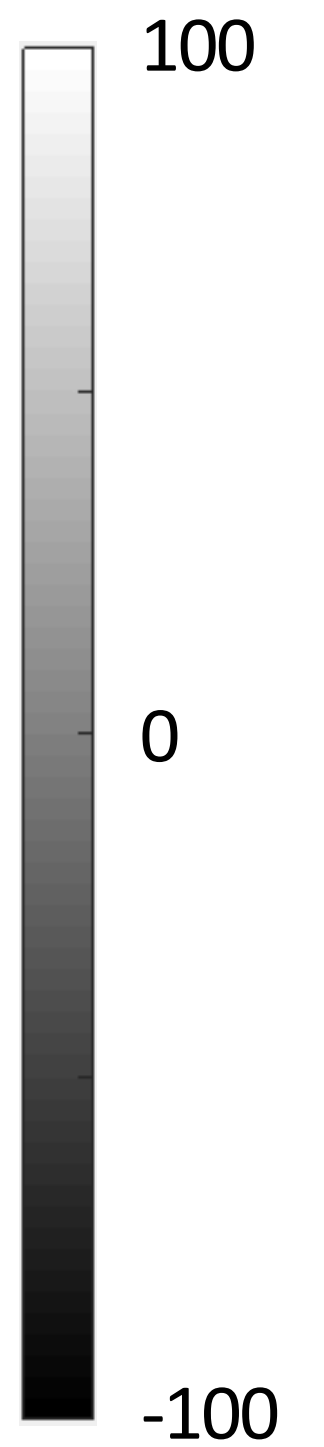
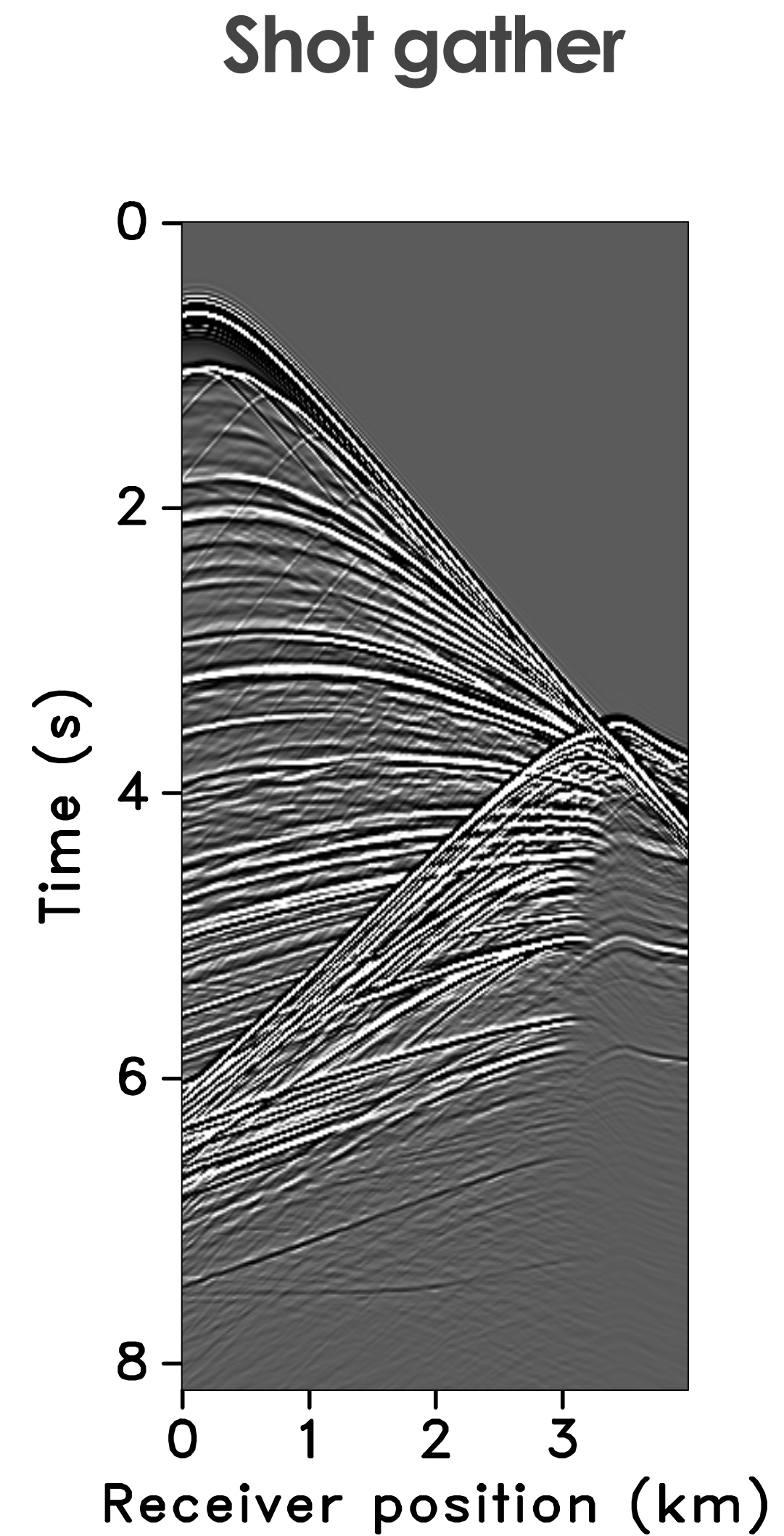
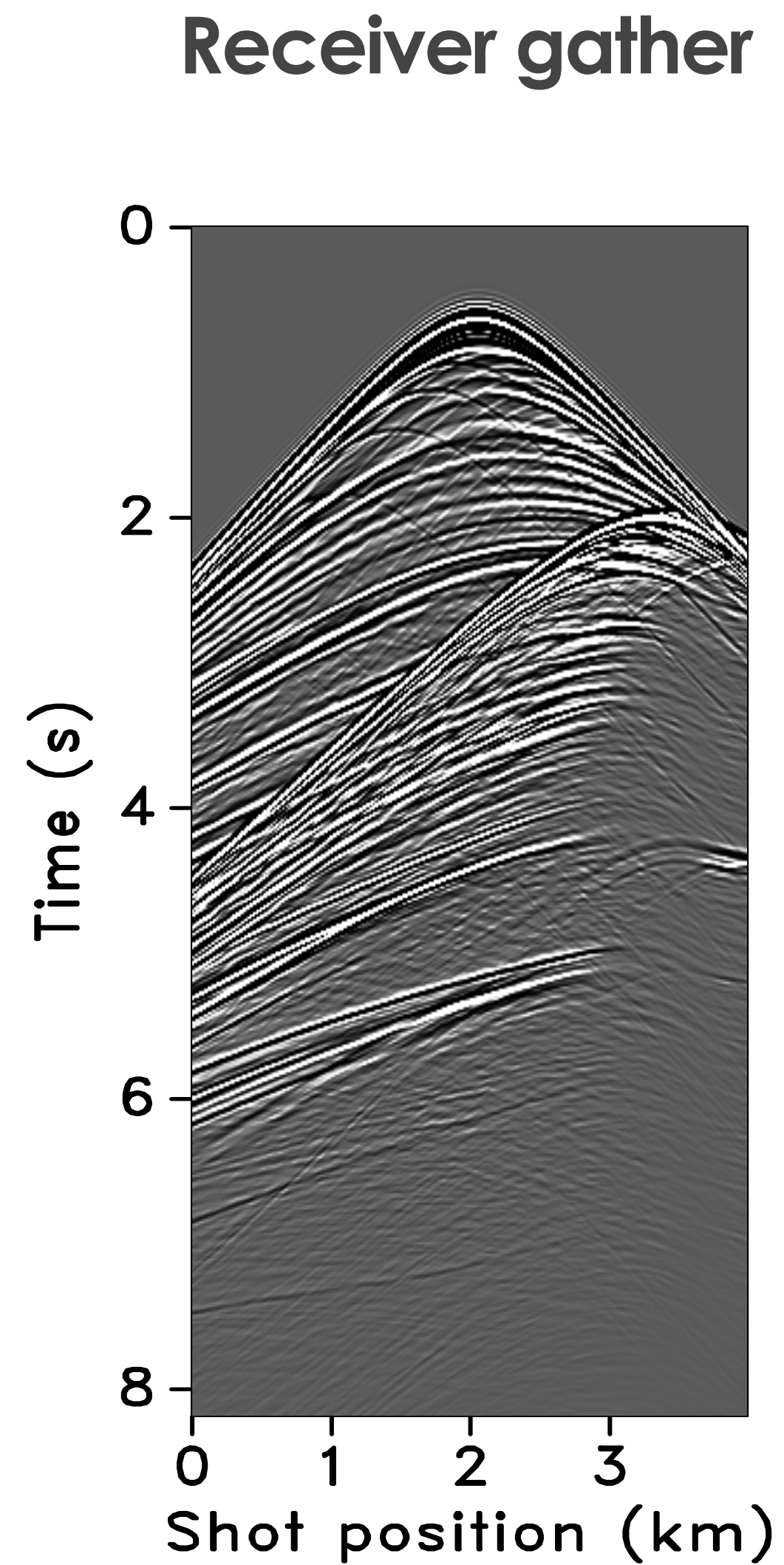
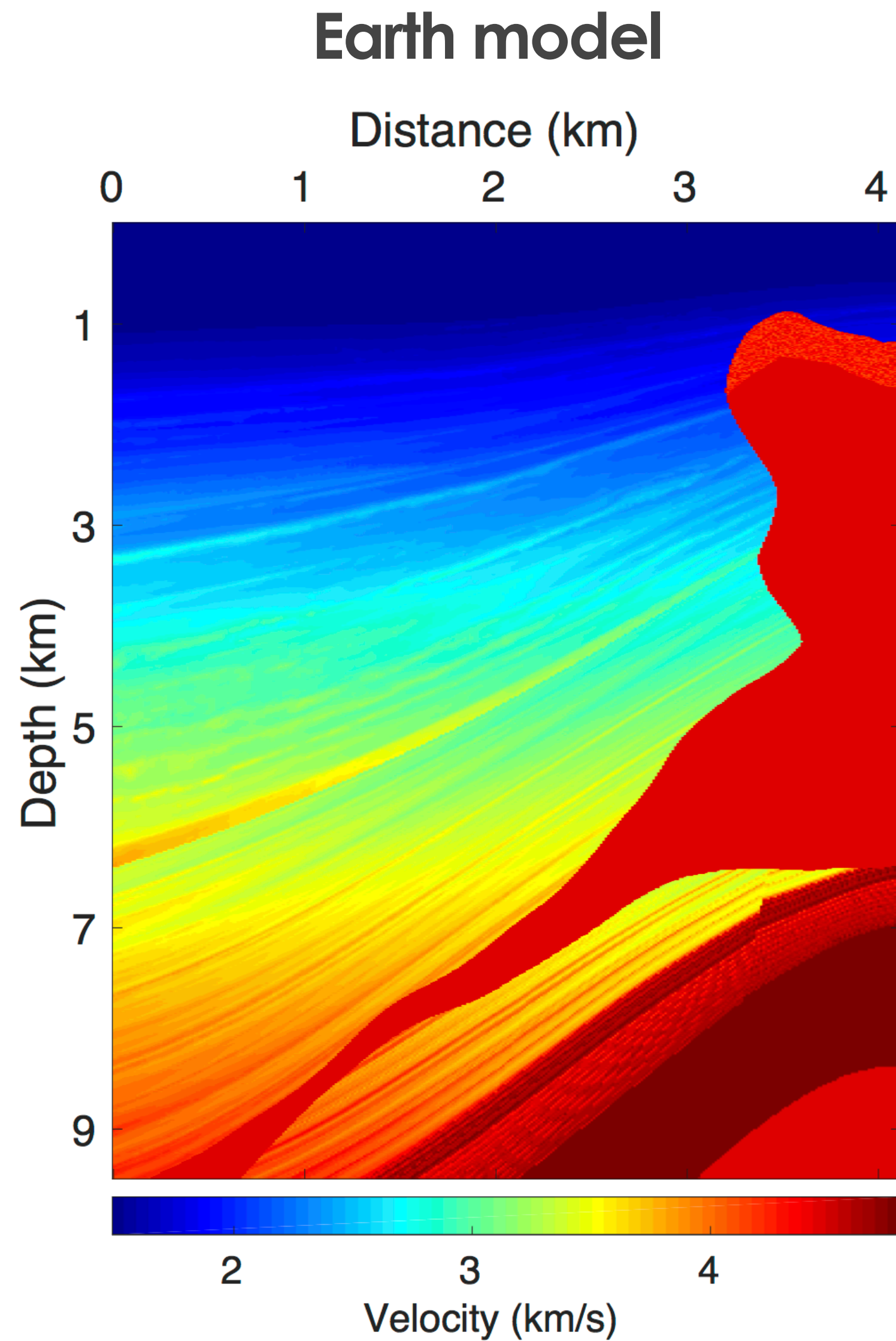


## Shot gather





# Types of gathers





# Challenges

**Expensive dense and full-azimuthal** sampling to produce high-resolution images of the subsurface

- deploy multiple source vessels for full azimuthal coverage
- simultaneous-source (or blended) acquisition; **problem:** source separation
- leads to uneven sampling: coarse source and dense receiver sampling or vice-versa

Time-lapse seismic acquisition

- **repeat expensive** dense acquisitions & “independent” processing
- hampered by practical challenges to ensure repetition

## Our solutions

Adapt ideas from Compressive Sensing (CS)

- **design economic** (or low-cost), **randomly subsampled** acquisitions
- surveys acquired with **small** environmental **imprint**
- **recover** dense, periodically sampled data via **structure promotion**

Adapt ideas from Distributed Compressive Sensing (DCS)

- **economic**, randomly subsampled **time-lapse** acquisition
- offers possibility to **relax** insistence on survey **replicability**
- **recover** dense, periodically sampled time-lapse vintages and difference by **exploiting common information** among the vintages



# The impact

## Special Section: Impact of compressive sensing on seismic data acquisition and processing

- 640**.....Introduction to this special section: Impact of compressive sensing on seismic data acquisition and processing, N. Allegar, F. J. Herrmann, and C. C. Mosher
- 642**.....Compressive sensing: A new approach to seismic data acquisition, R. G. Baraniuk and P. Steeghs
- 646**..... Sparsity in compressive sensing, J. Ma and S. Yu
- 654**.....Sparse seismic wavefield sampling, X. Campman, Z. Tang, H. Jamali-Rad, B. Kuvshinov, M. Danilouchkine, Y. Ji, W. Walk, and D. Smit
- 661**..... Operational deployment of compressive sensing systems for seismic data acquisition, C. C. Mosher, C. Li, F. D. Janiszewski, L. S. Williams, T. C. Carey, and Y. Ji
- 670**.....Application of compressive seismic imaging at Lookout Field, Alaska, L. Brown, C. C. Mosher, C. Li, R. Olson, J. Doherty, T. C. Carey, L. Williams, J. Chang, and E. Staples
- 677**.....Highly repeatable 3D compressive full-azimuth towed-streamer time-lapse acquisition — A numerical feasibility study at scale, R. Kumar, H. Wason, S. Sharan, and F. J. Herrmann
- 688**..... Highly repeatable time-lapse seismic with distributed compressive sensing — Mitigating effects of calibration errors, F. Oghenekohwo and F. J. Herrmann

# The Leading Edge®

Special Section: Impact of compressive sensing on seismic data acquisition and processing

Annual Meeting preview



INTERNATIONAL EXPOSITION AND 87TH  
ANNUAL MEETING  
HOUSTON, TEXAS  
24-29 SEPTEMBER 2017



SEG SOCIETY OF EXPLORATION  
GEOPHYSICISTS

August 2017 - Volume 36, No. 8  
ISSN 1070-485X

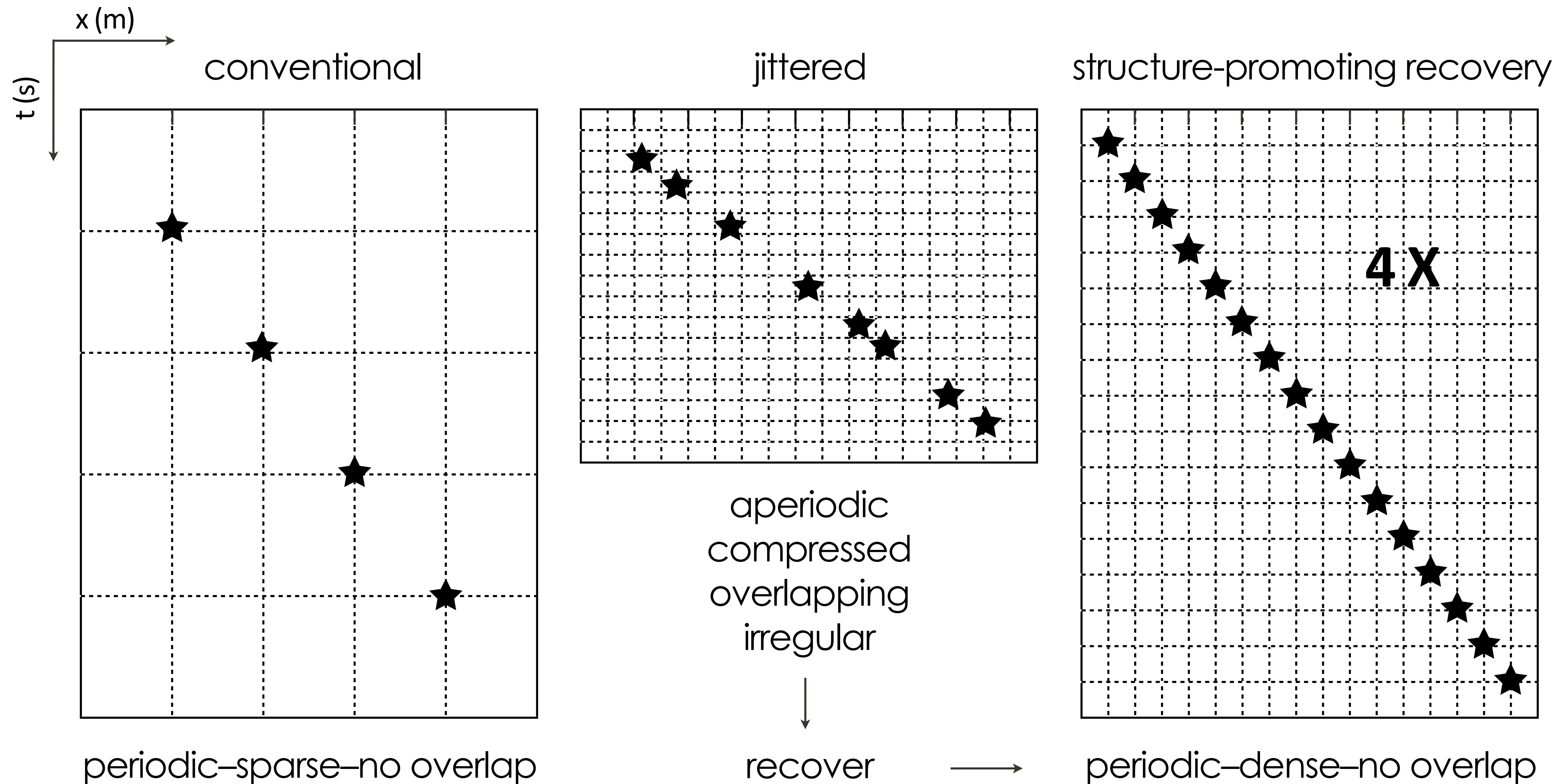


# Chapters 2 & 3

- Compressive sensing in seismic exploration
- simultaneous-source marine acquisition
  - static acquisition geometry



# Conventional vs. compressive acquisition



★ source

# Compressive sensing

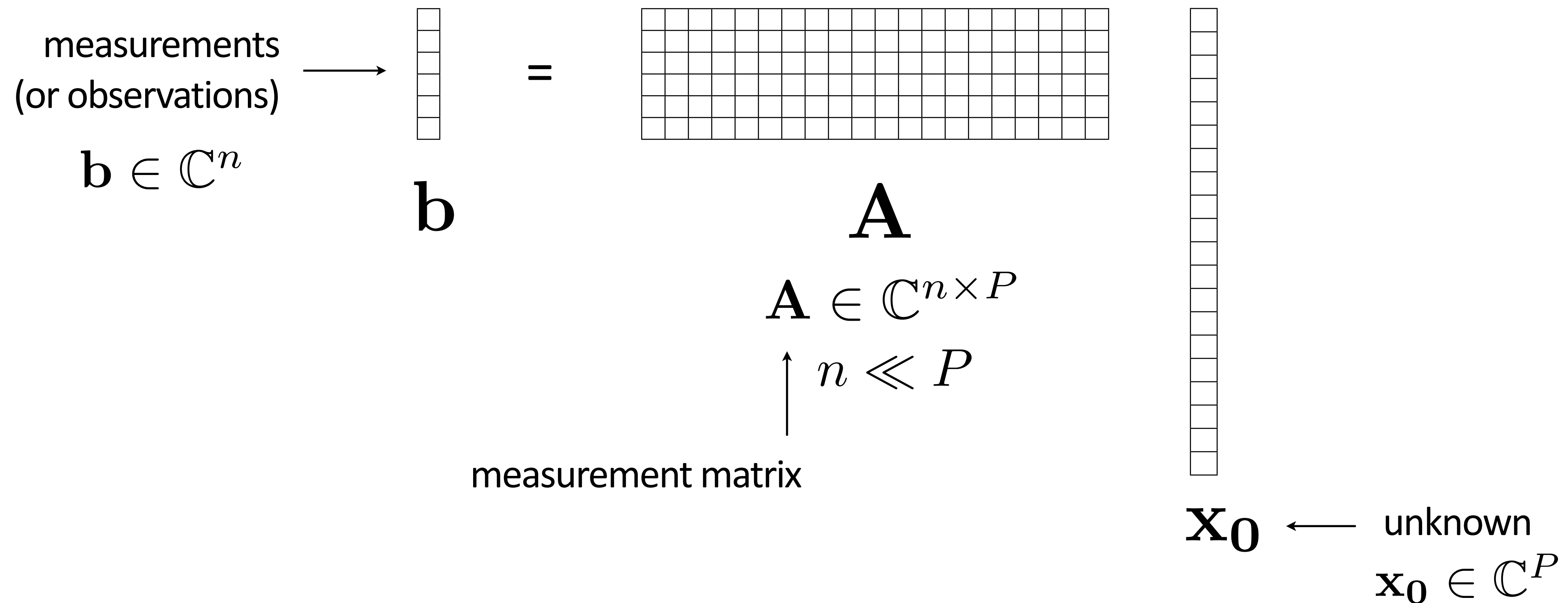
Powerful sensing paradigm

- ▶ **find representations that reveal structure**
  - transform-domain sparsity (e.g., Fourier, curvelets, etc.)
- ▶ **sample to break structure**
  - randomized acquisition (e.g., time-jittered, over/under, SLO, etc.)
  - destroys sparsity
- ▶ **recover by structure promotion**
  - sparsity via one-norm minimization

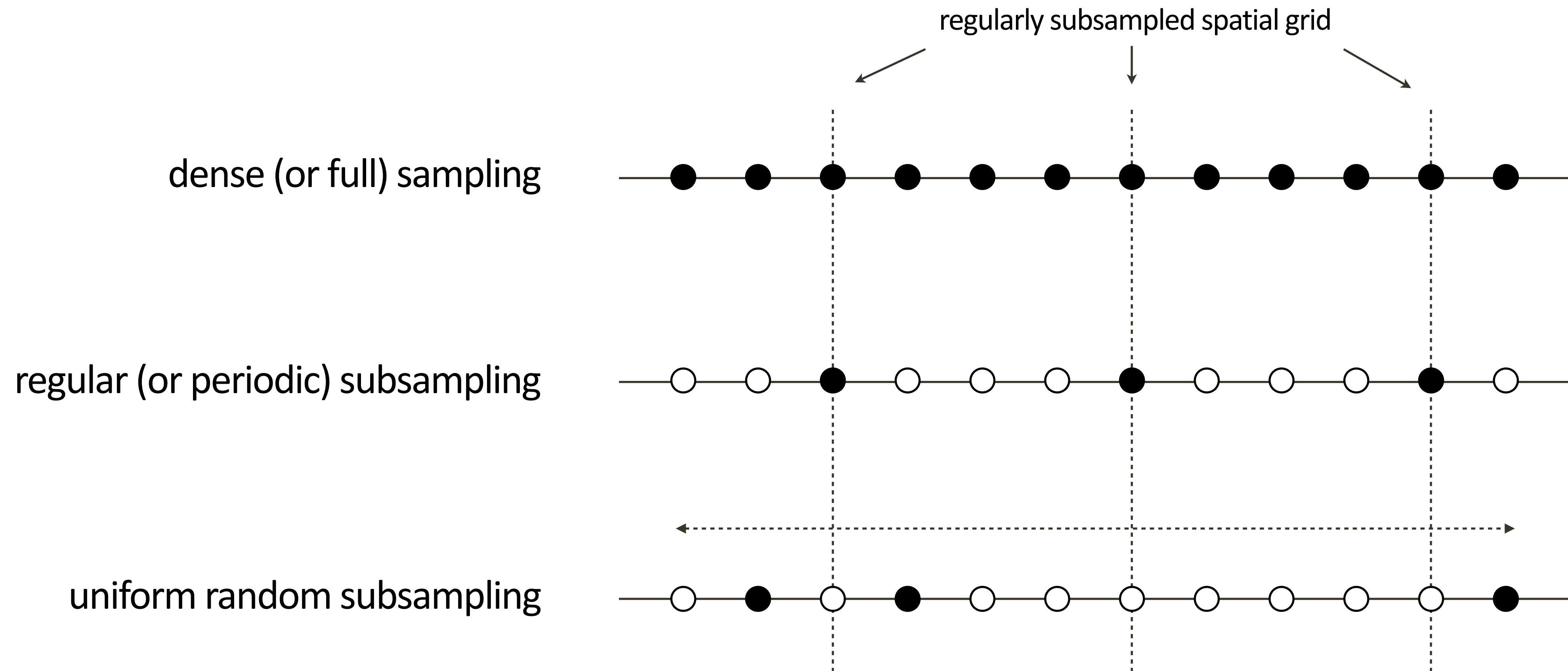


# Compressive sensing

Solve an underdetermined system of linear equations:



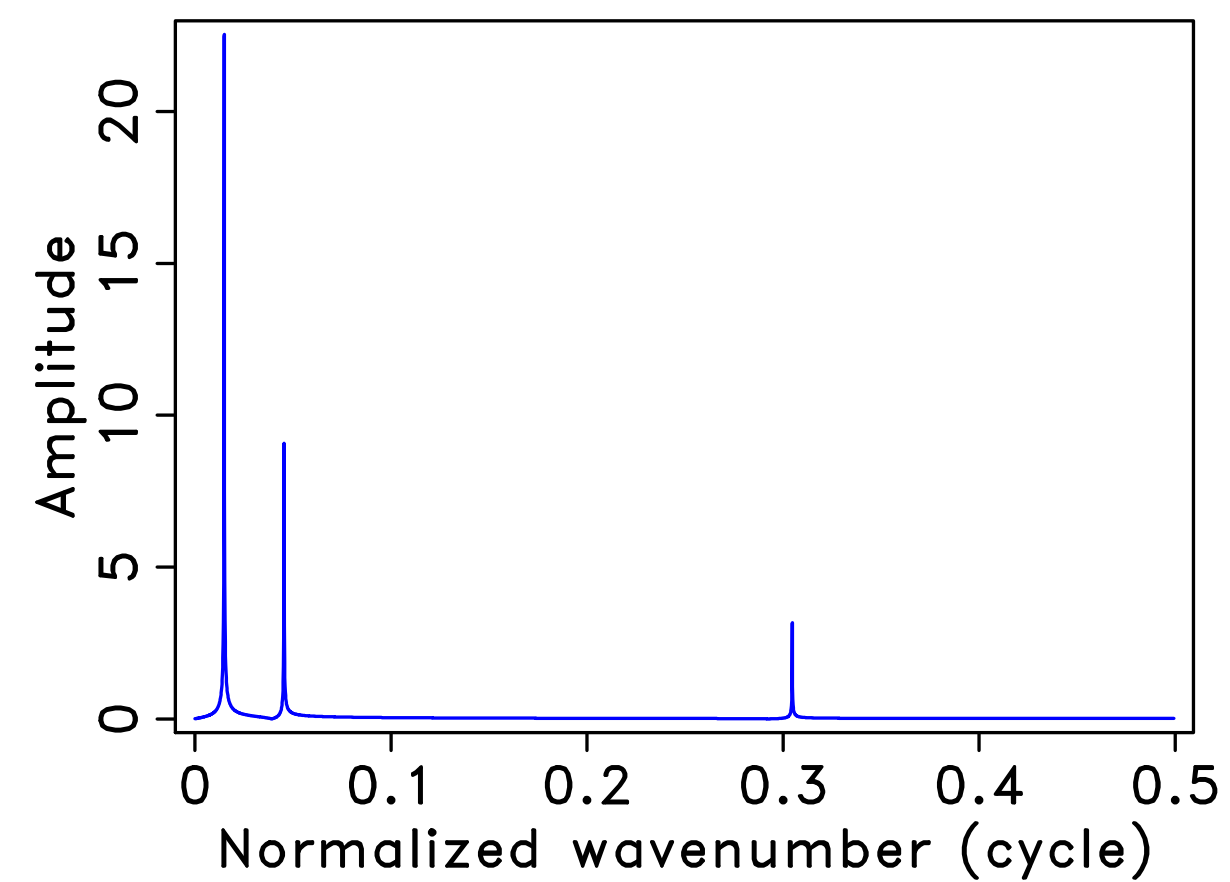
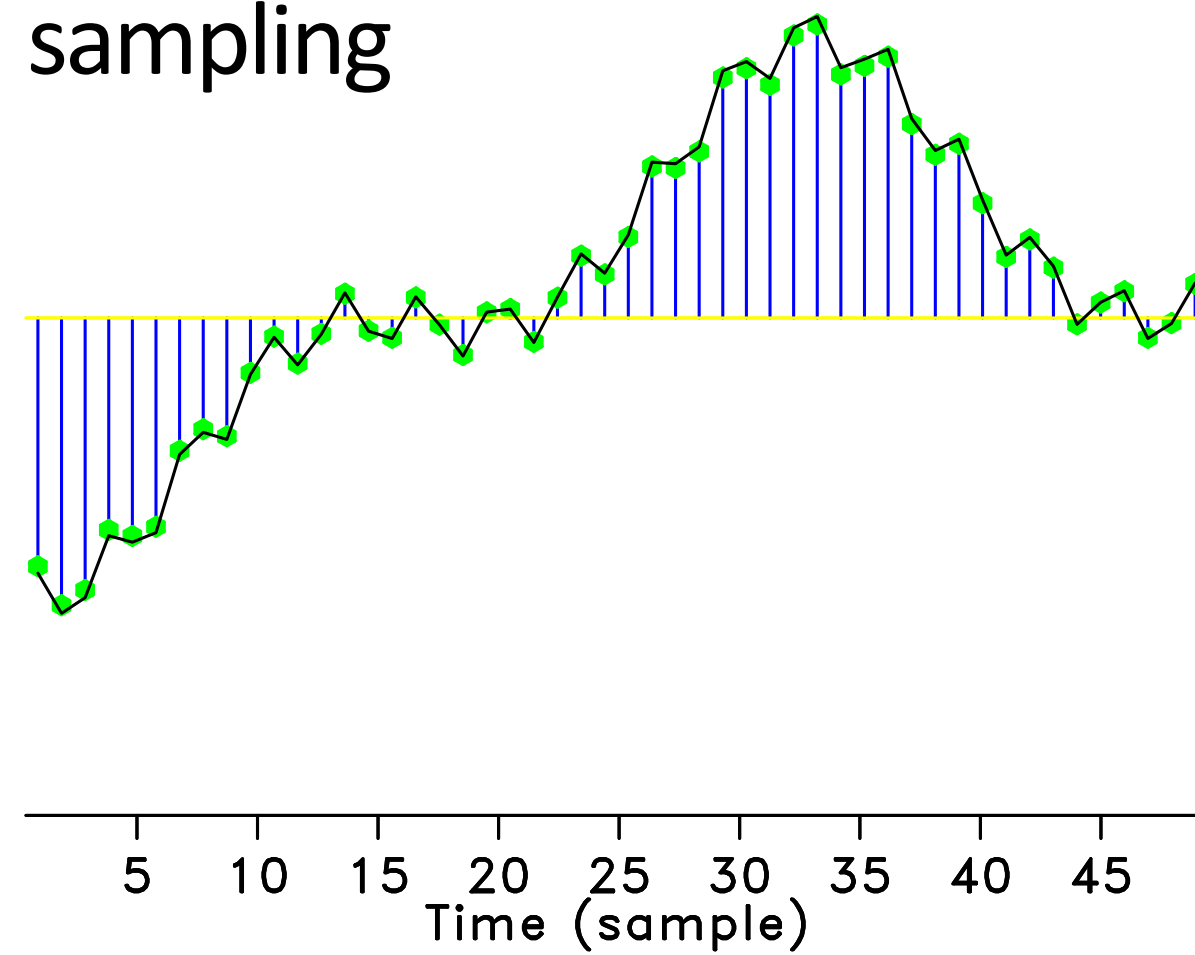
# Sampling schemes



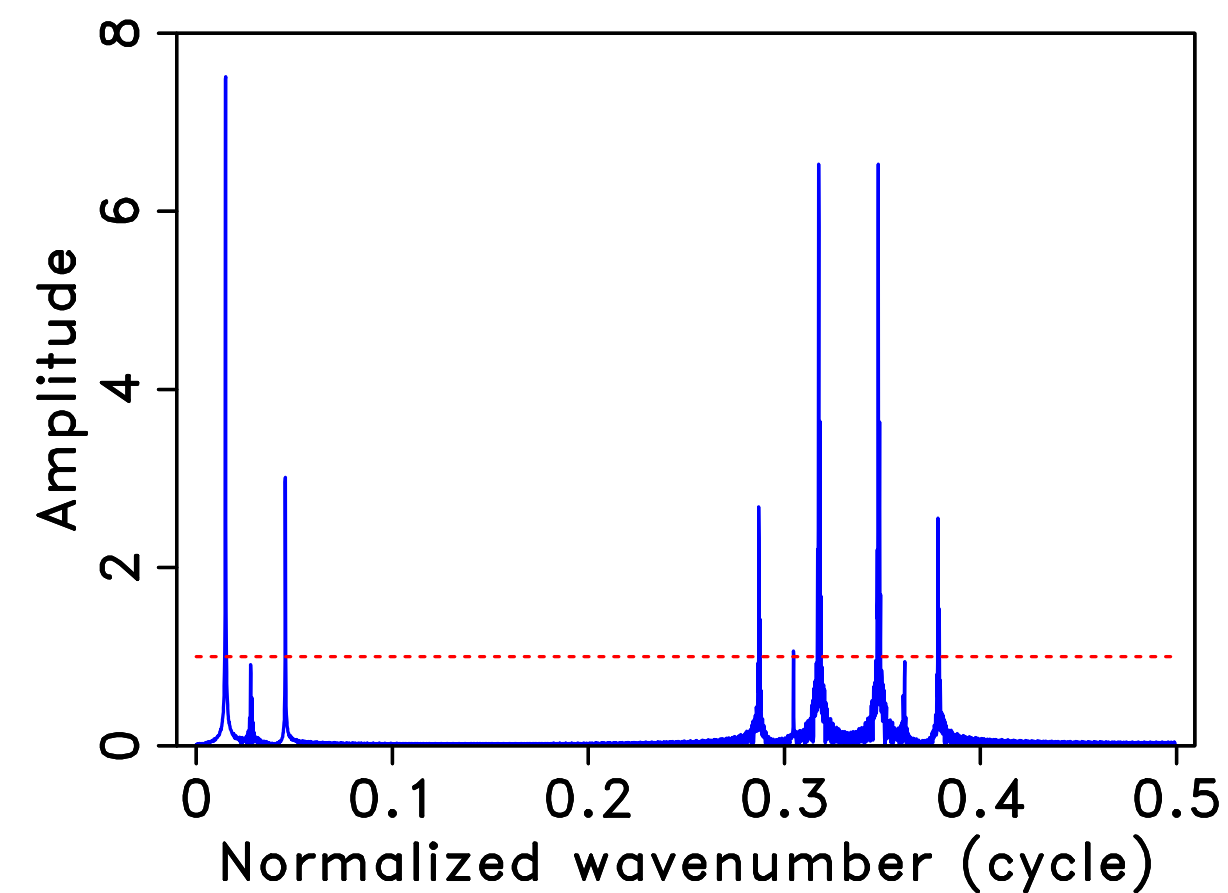
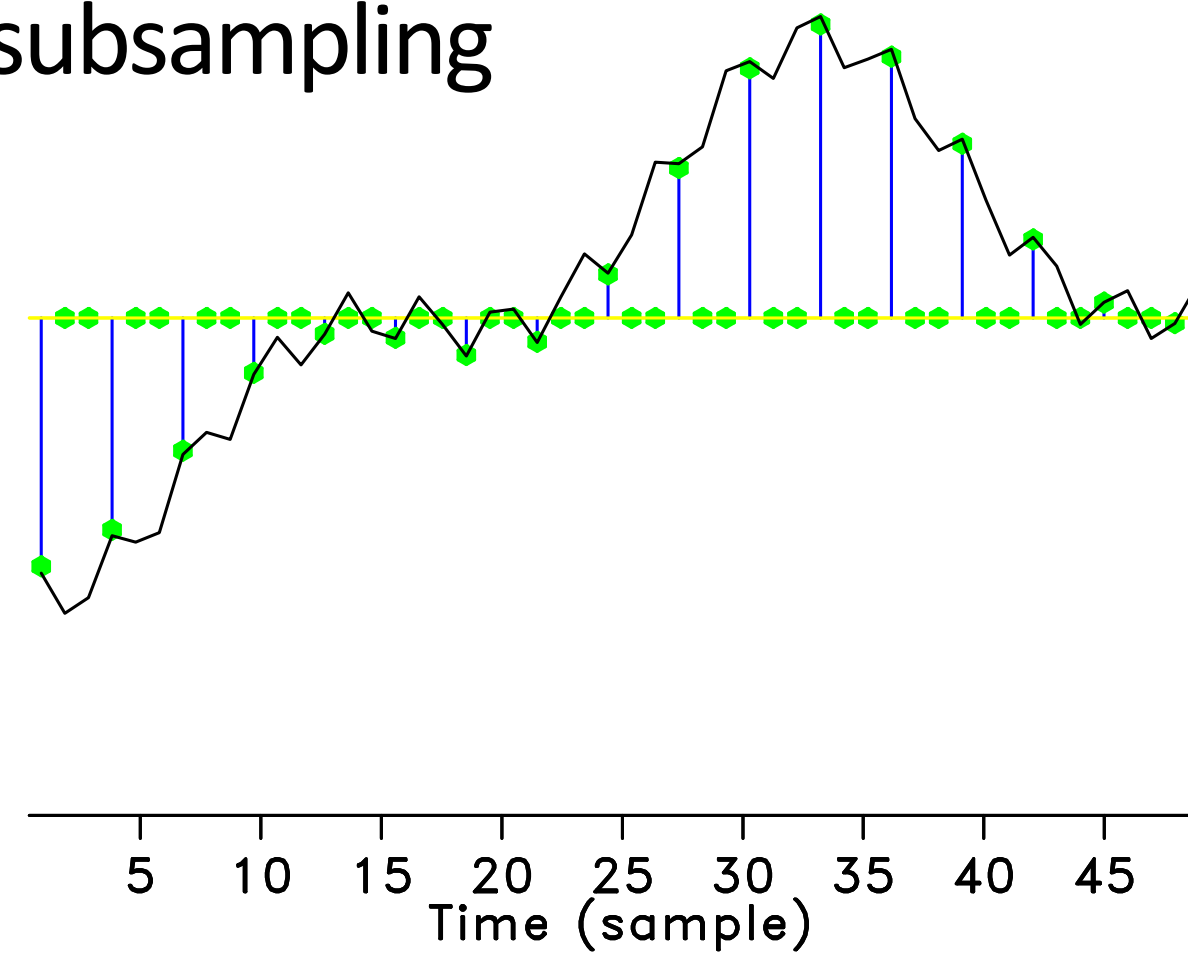


# Random vs. periodic subsampling

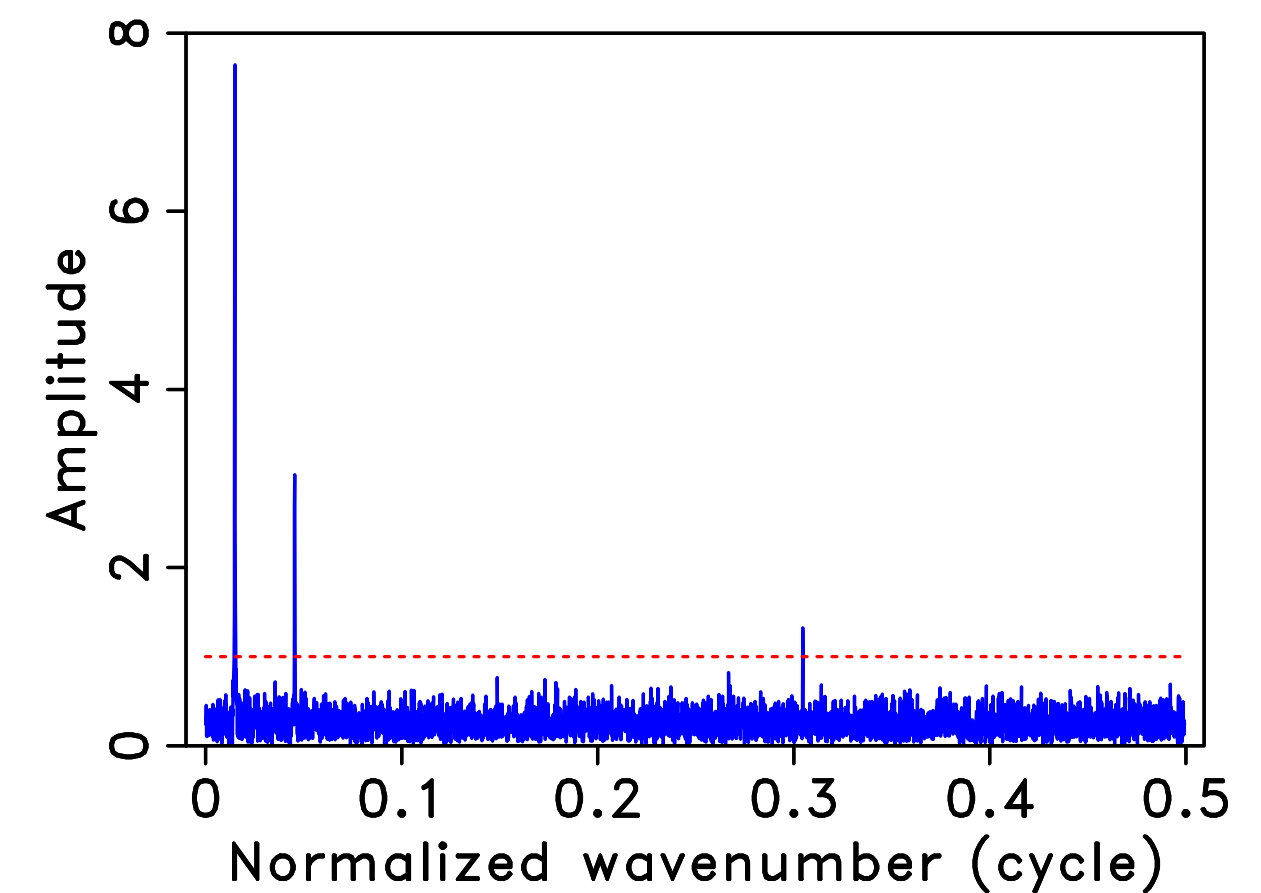
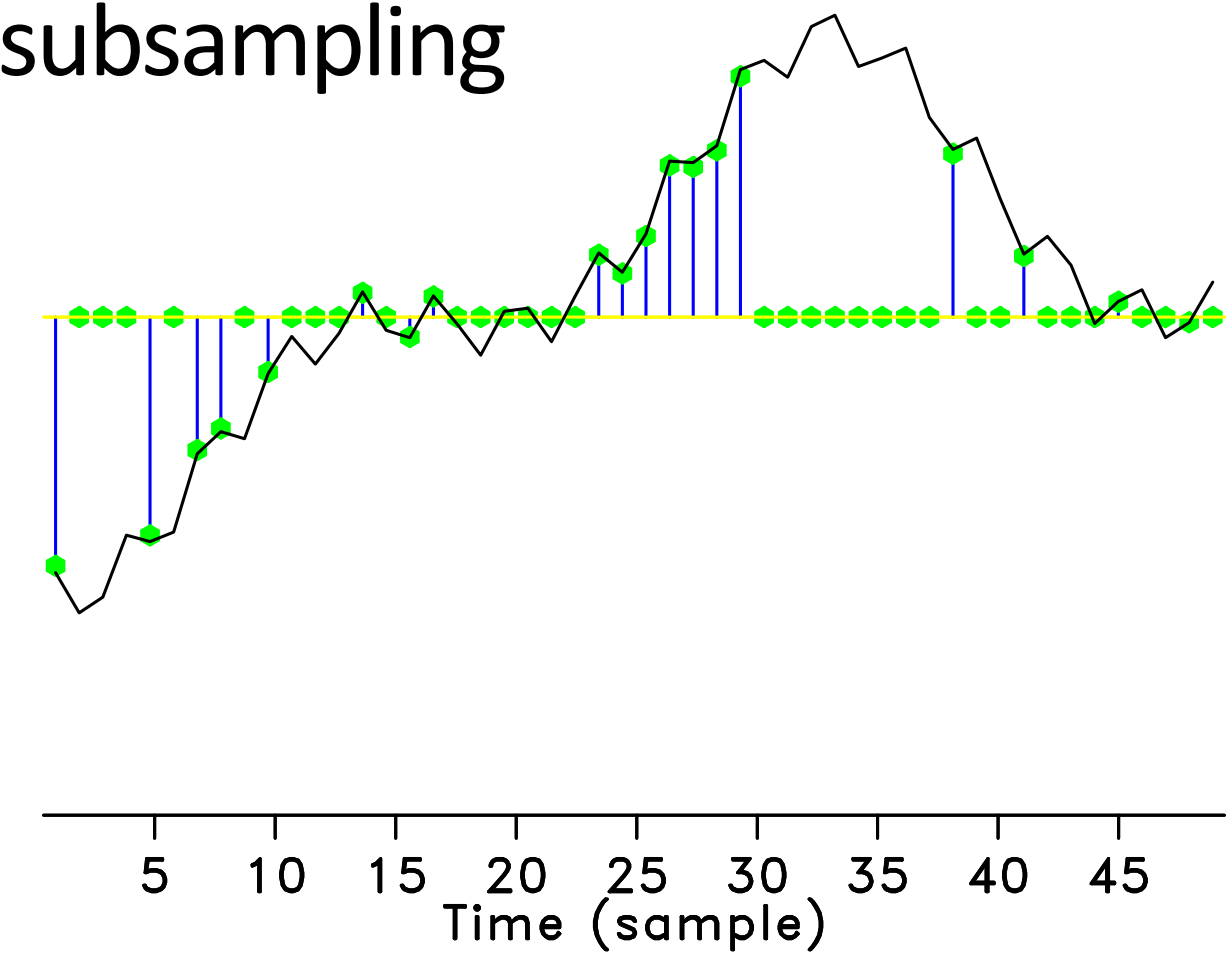
full  
sampling



periodic  
subsampling



random  
subsampling



# Adapt CS ideas to seismic acquisition

- design simultaneous-source marine acquisition
- source separation via structure (“sparsity”) promotion

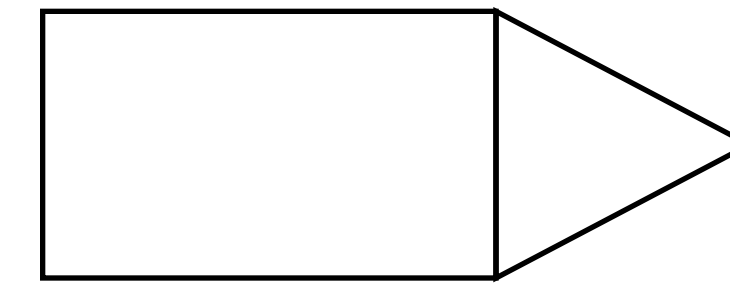
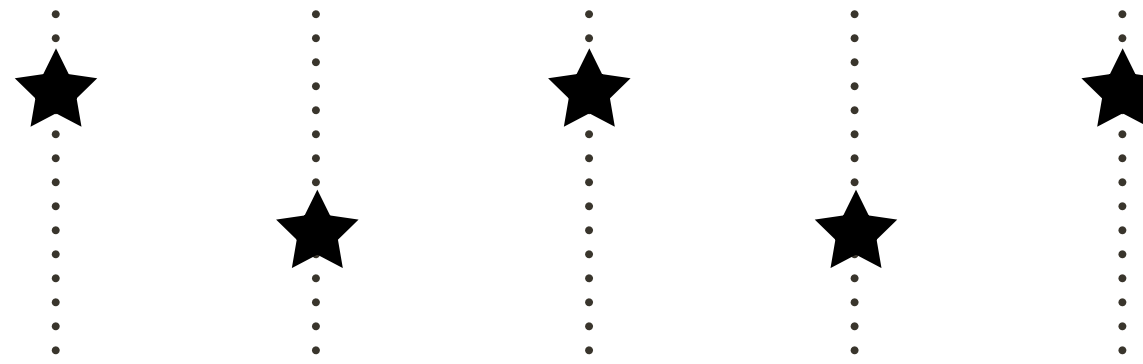


# Simultaneous-source marine acquisition

random vs. periodic

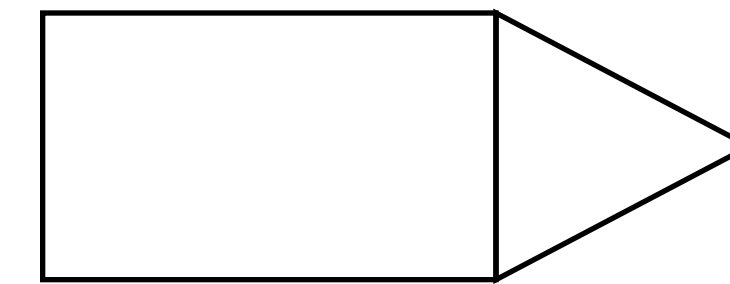
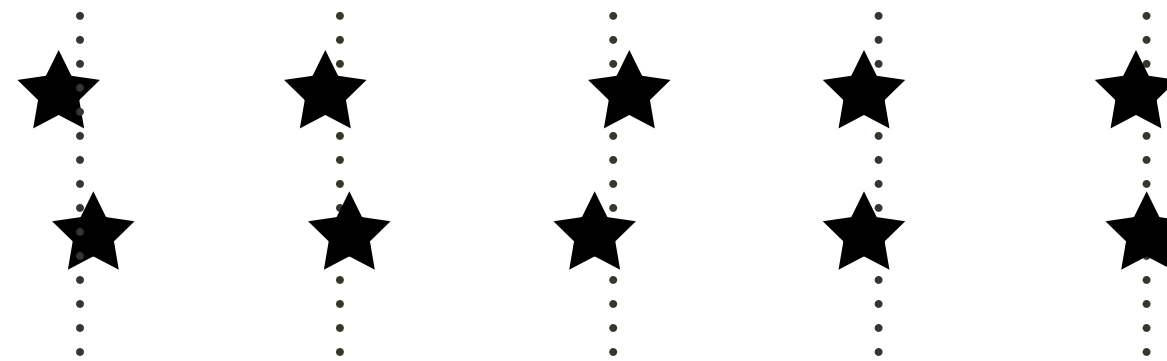
shot-time randomness

**periodically** sampled spatial grid  
(**static/dynamic** acquisition geometry:  
conventional acquisition)



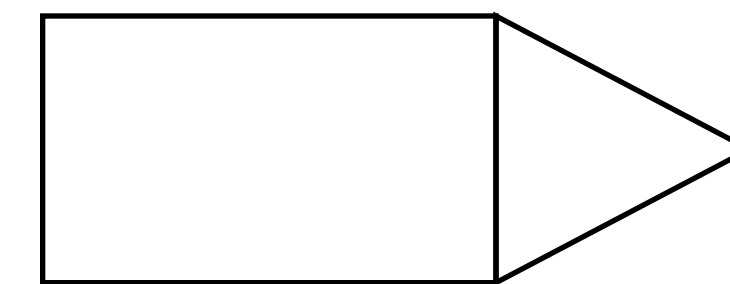
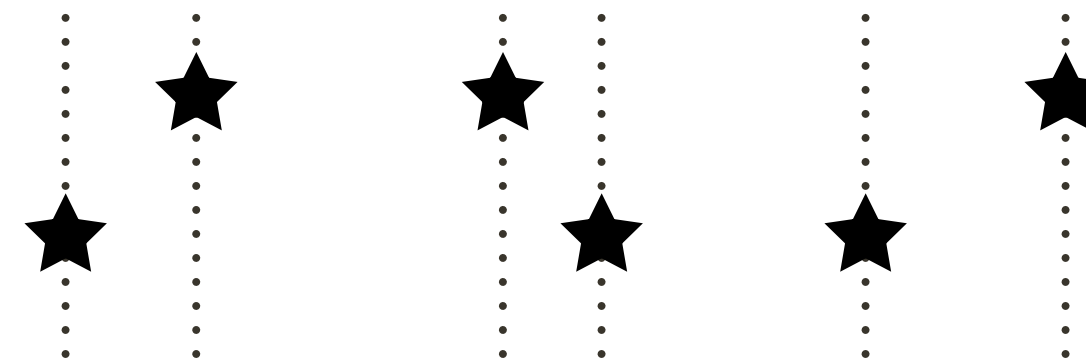
NONE

**almost periodically** sampled spatial grid  
(**dynamic** acquisition geometry:  
towed arrays)



SMALL

**randomly** jittered sampled spatial grid  
(**static** acquisition geometry: OBC/OBN;  
“time-jittered” acquisition)

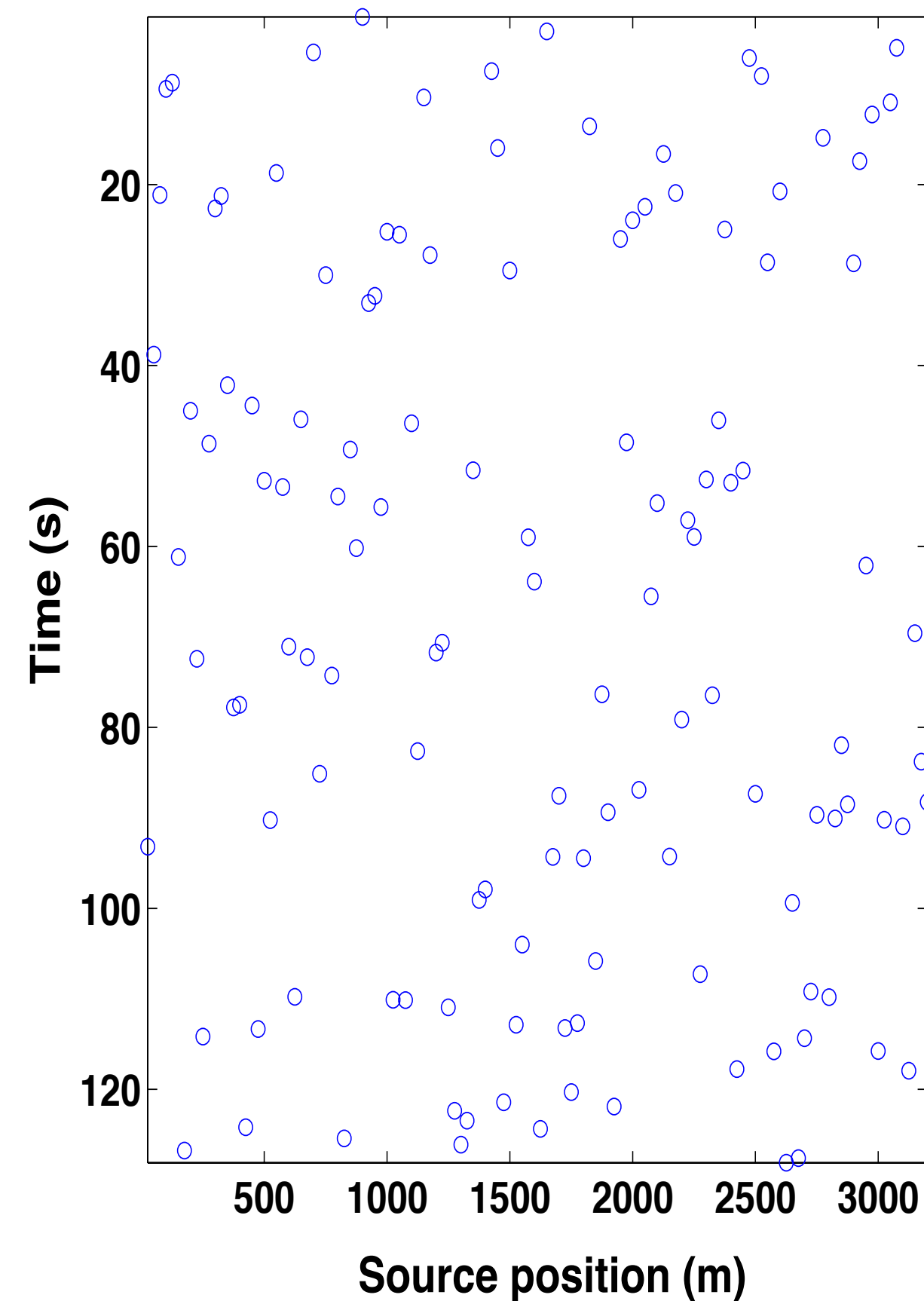


LARGE

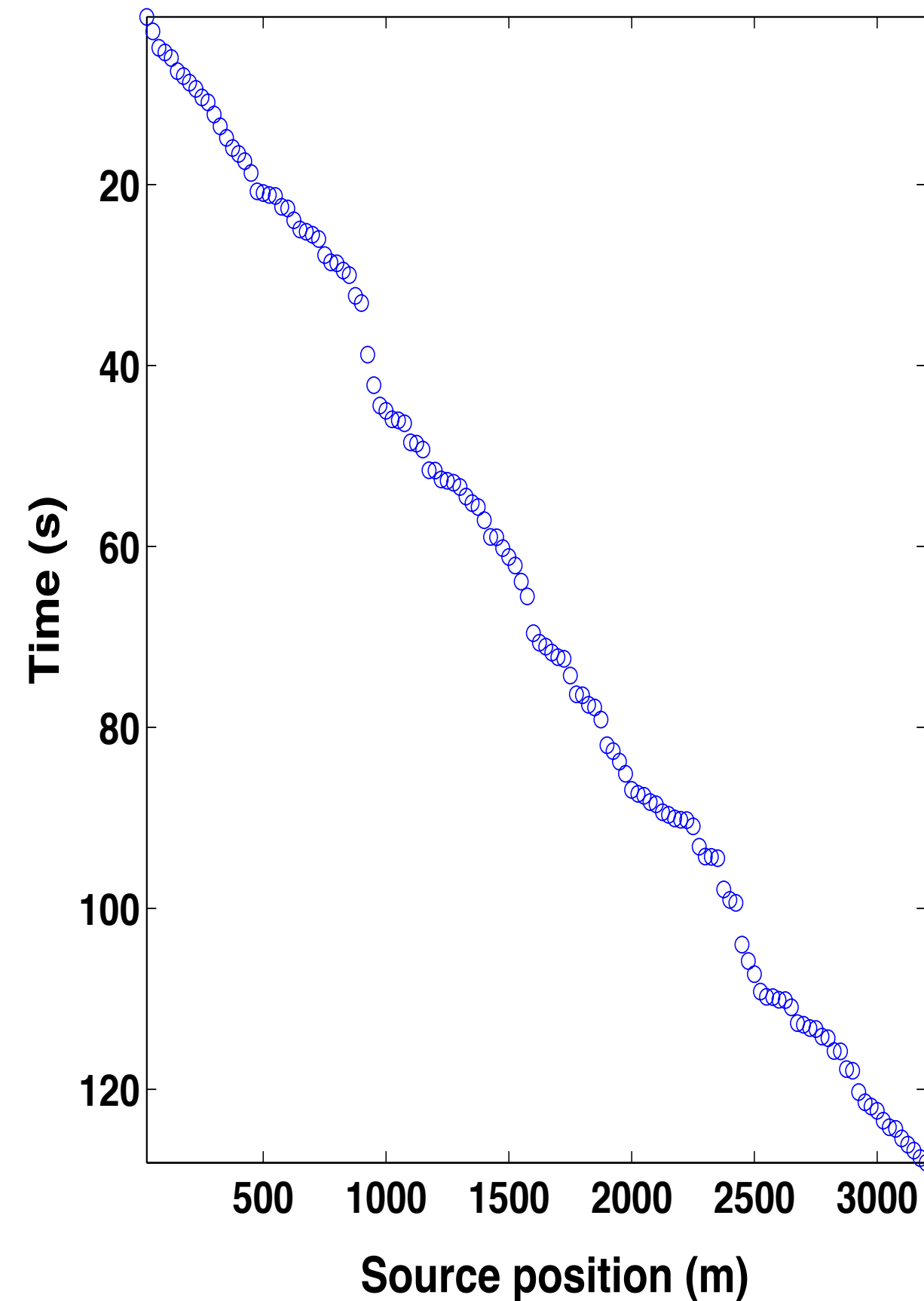
# Simultaneous-source marine acquisition

random vs. periodic

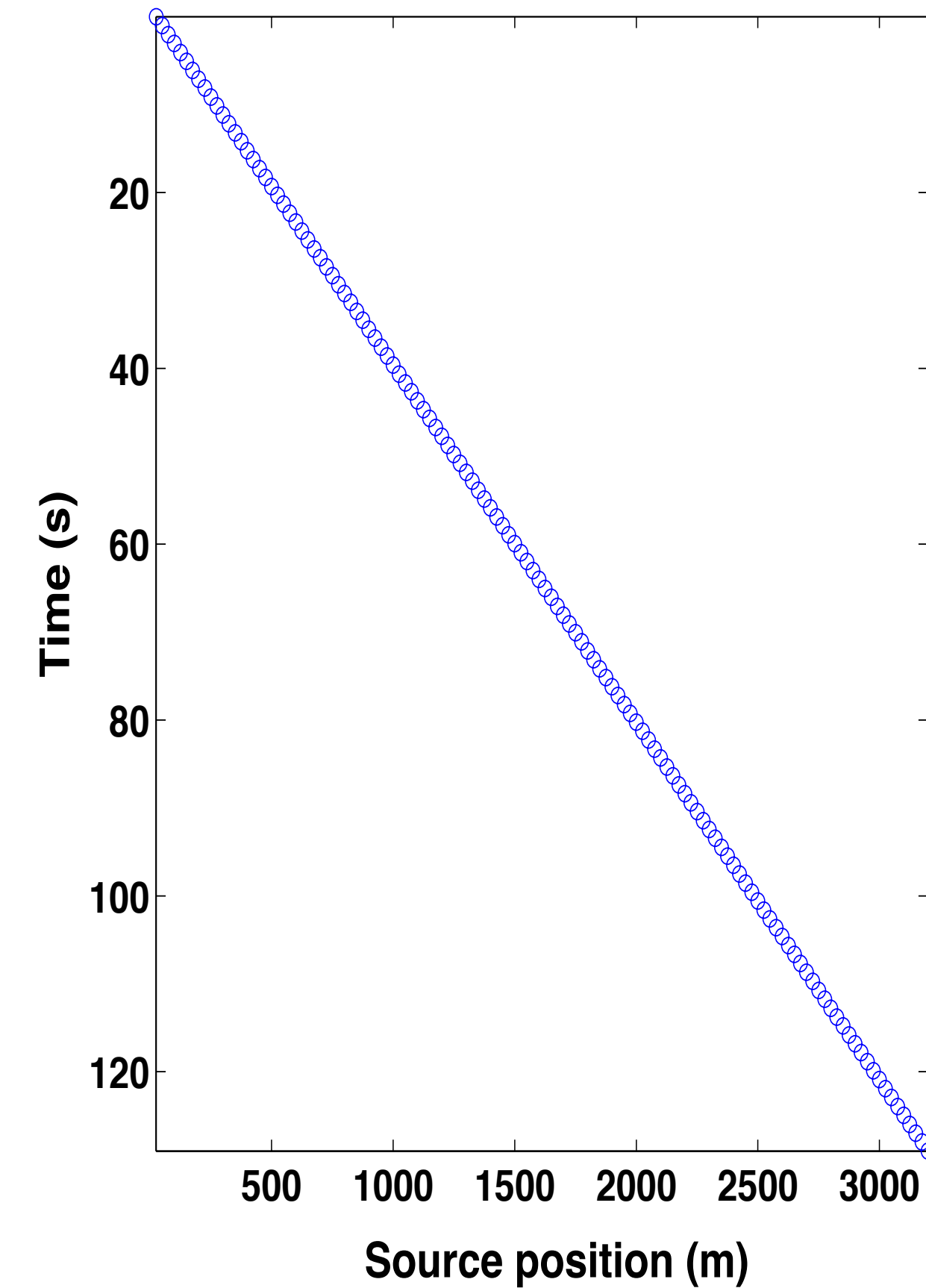
**“Ideal” simultaneous acquisition**



**Random time dithering**



**Periodic time dithering**

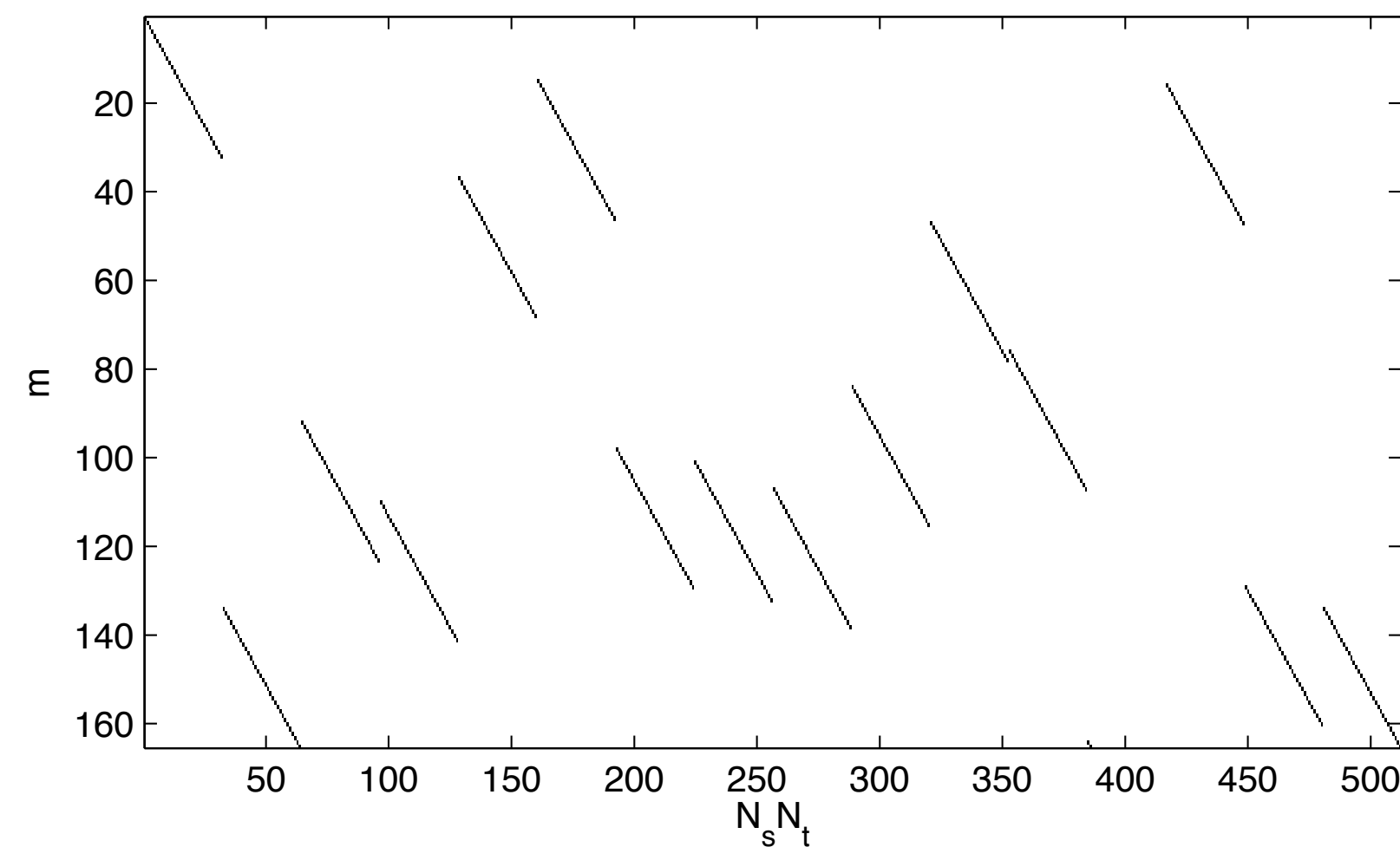




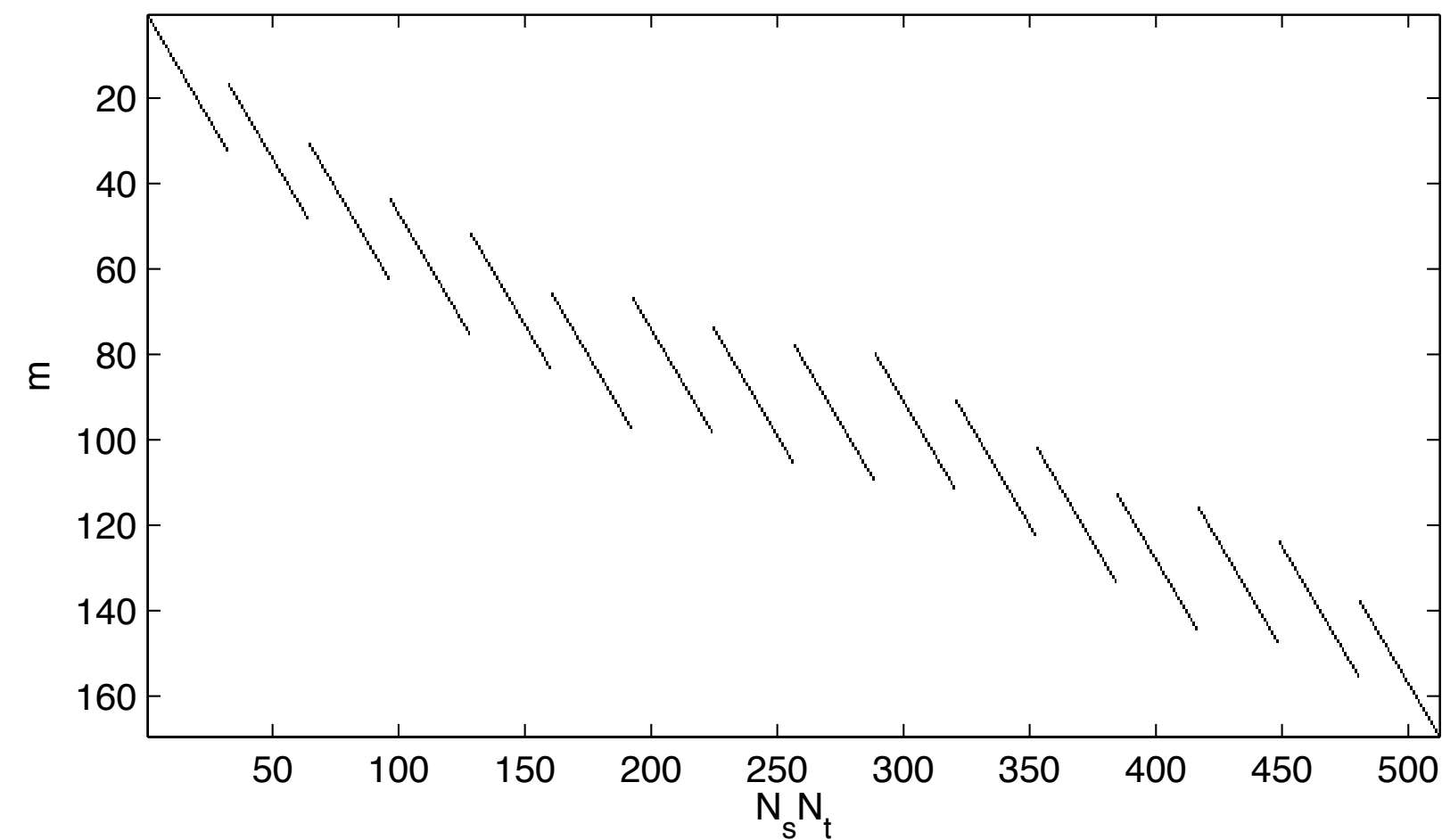
# Simultaneous-source sampling operators

random vs. periodic

“Ideal” simultaneous acquisition



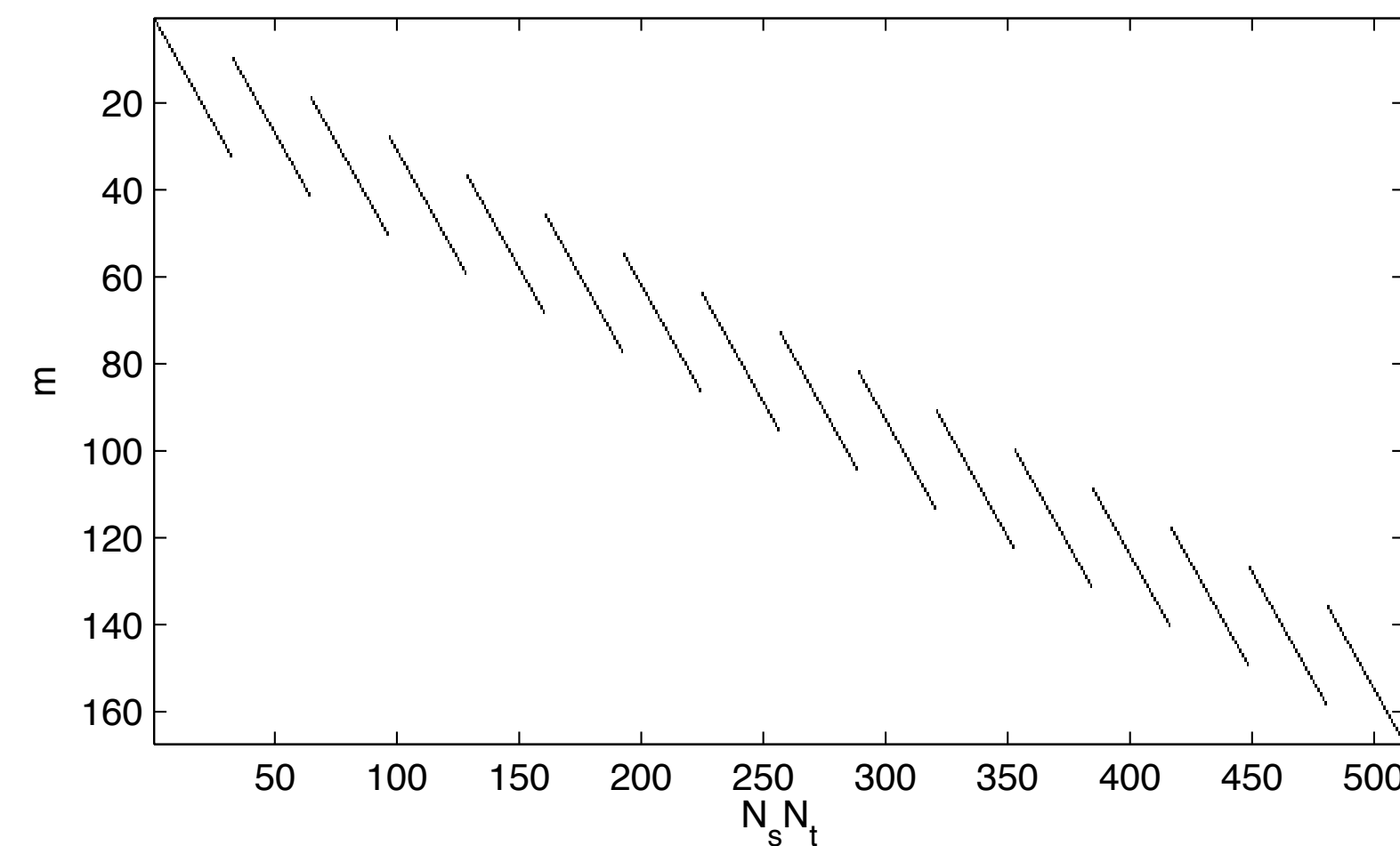
Random time dithering



samples recorded at each receiver  
during conventional acquisition

Periodic time dithering

samples recorded at each receiver  
during simultaneous acquisition

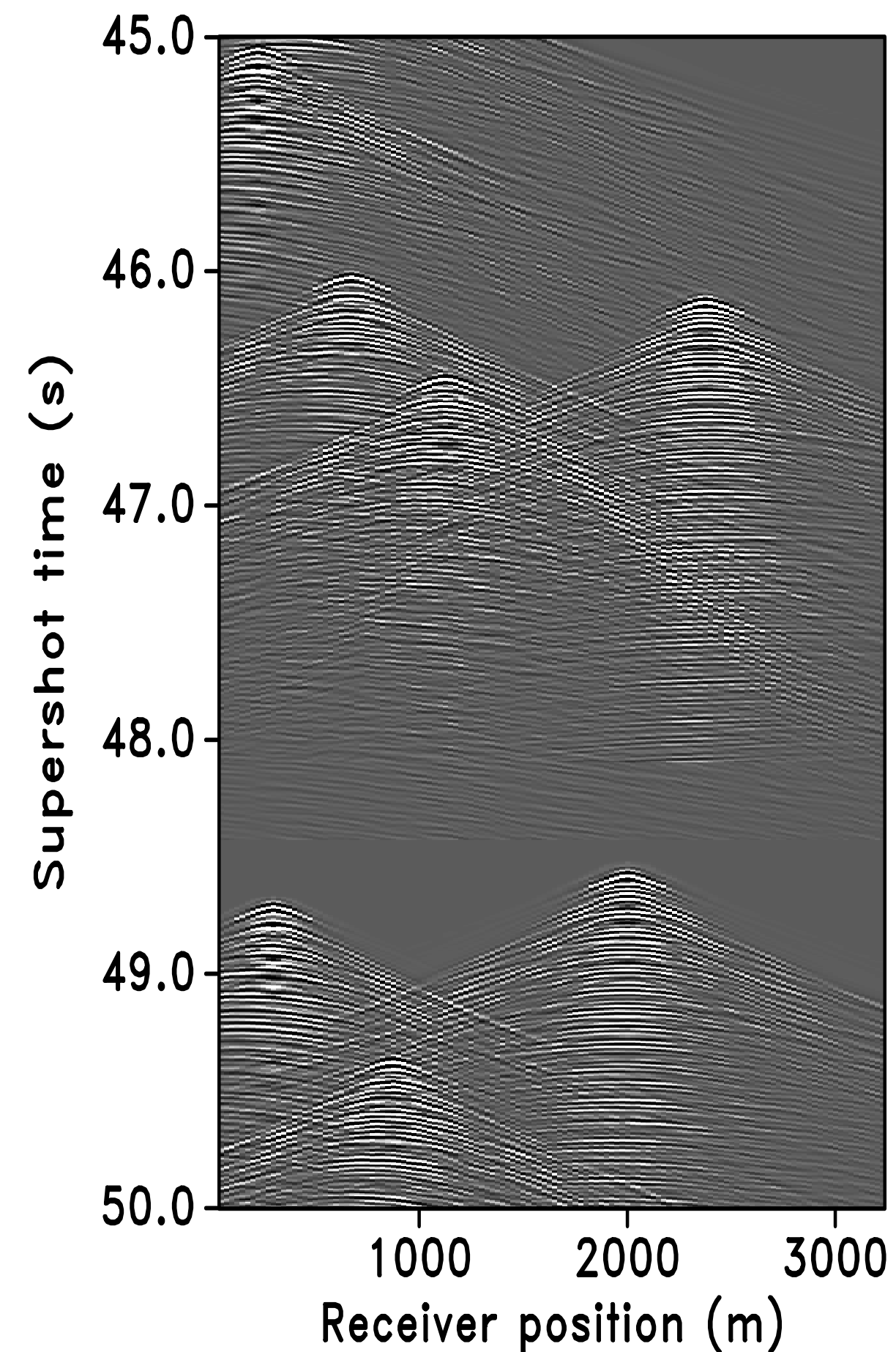


**$N_s$** : number of sources  
 **$N_t$** : number of time samples  
 **$N_r$** : number of receivers

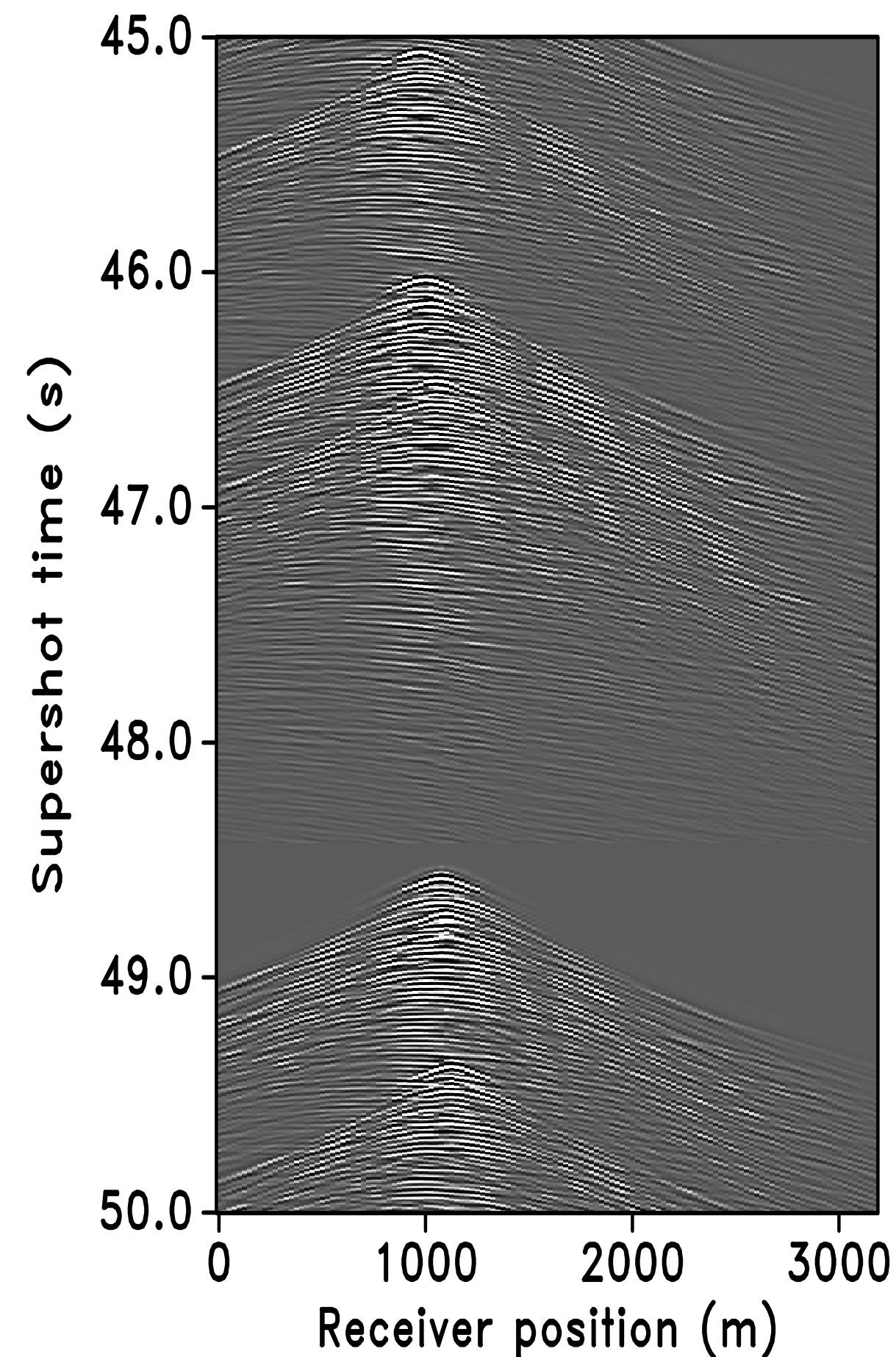
# Measurements

– overlapping shots

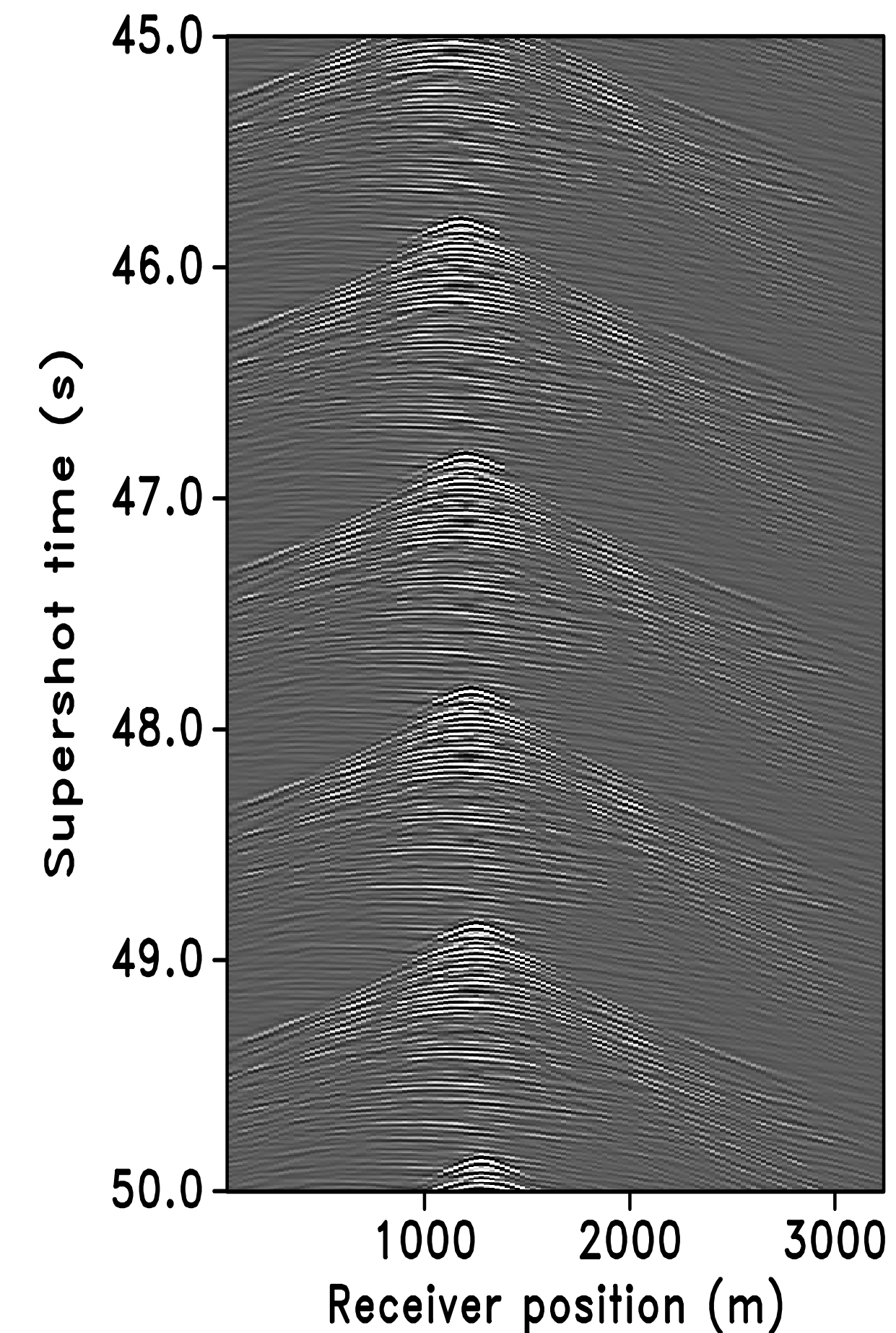
**“Ideal” simultaneous acquisition**



**Random time dithering**



**Periodic time dithering**





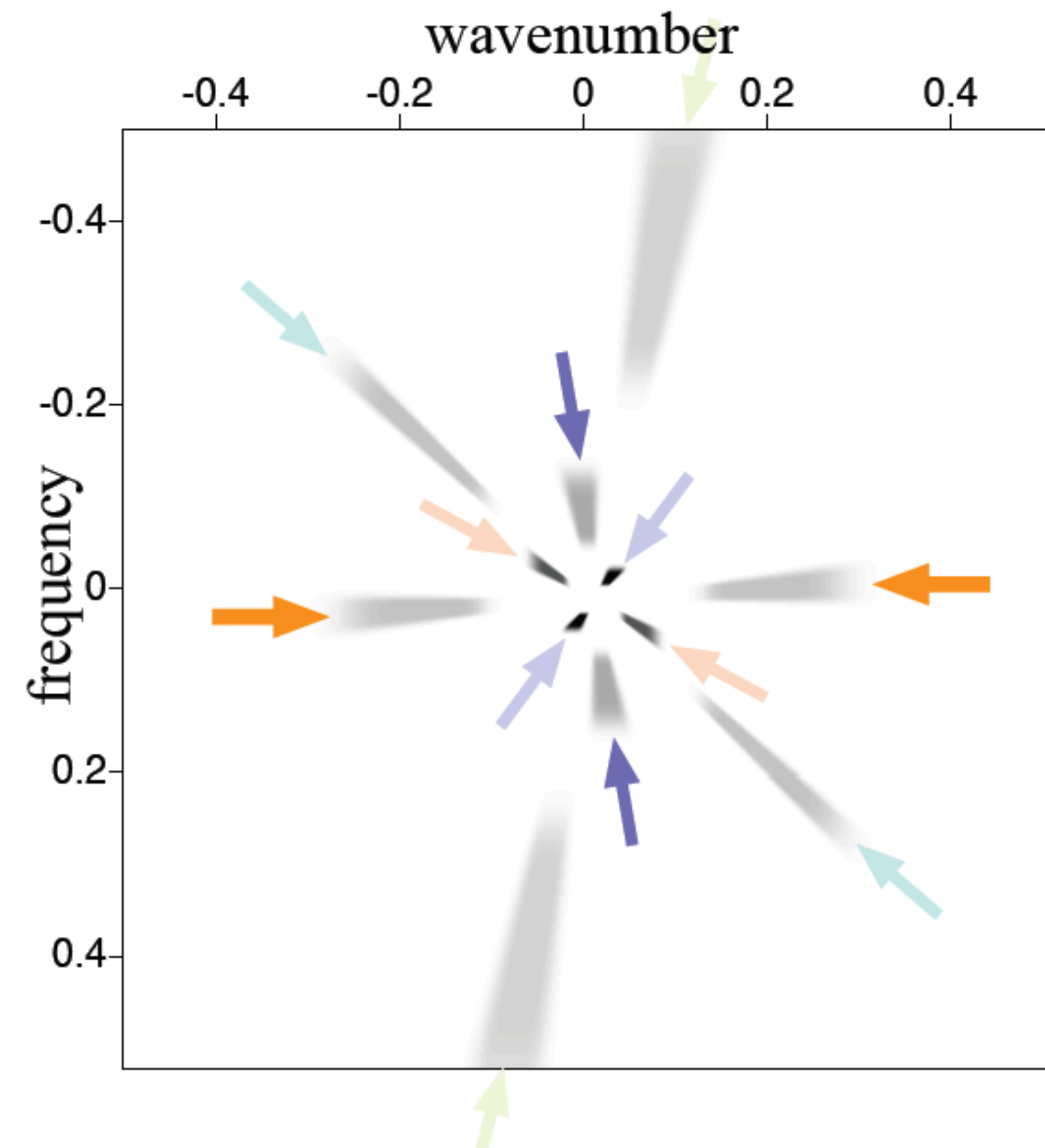
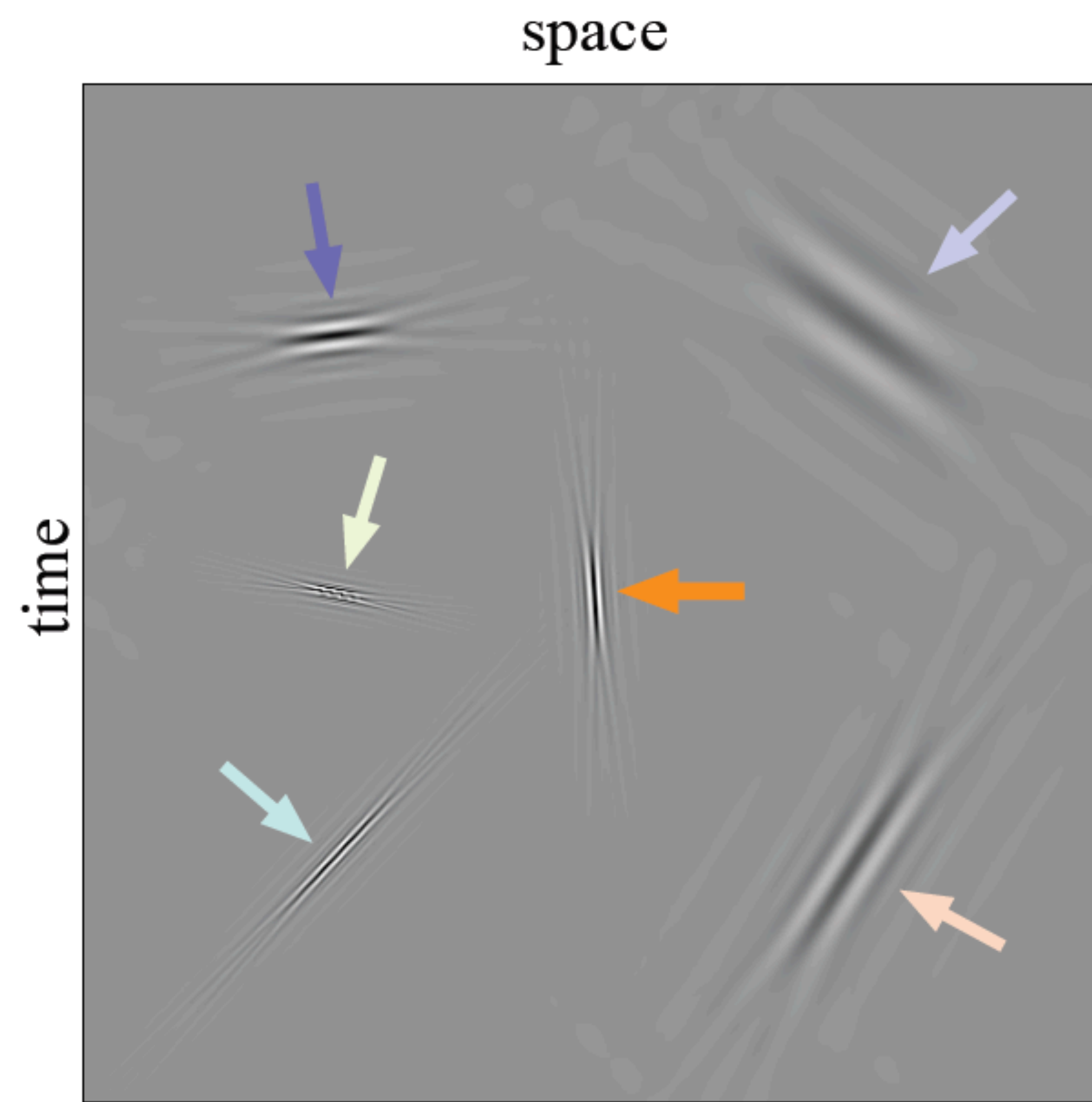
# Source separation via sparsity promotion

$$\mathbf{d} = \mathbf{S}^H \mathbf{x}$$

$$\tilde{\mathbf{x}} = \arg \min_{\mathbf{x}} \|\mathbf{x}\|_1 \quad \text{subject to} \quad \mathbf{A}\mathbf{x} = \mathbf{b}$$

$\mathbf{x}$	a choice of curvelet coefficients for $\mathbf{d}$
$\mathbf{S}^H$	a transform domain synthesis (curvelet)
$\mathbf{A}$	measurement operator : $\mathbf{M}\mathbf{S}^H$ , $\mathbf{M}$ : acquisition (or mixing) operator
$\mathbf{b}$	simultaneous data
$\tilde{\mathbf{x}}$	estimated curvelet coefficients for source separated wavefield
$\tilde{\mathbf{d}}$	( $= \mathbf{S}^H \tilde{\mathbf{x}}$ ) estimated source separated wavefield

# Curvelets

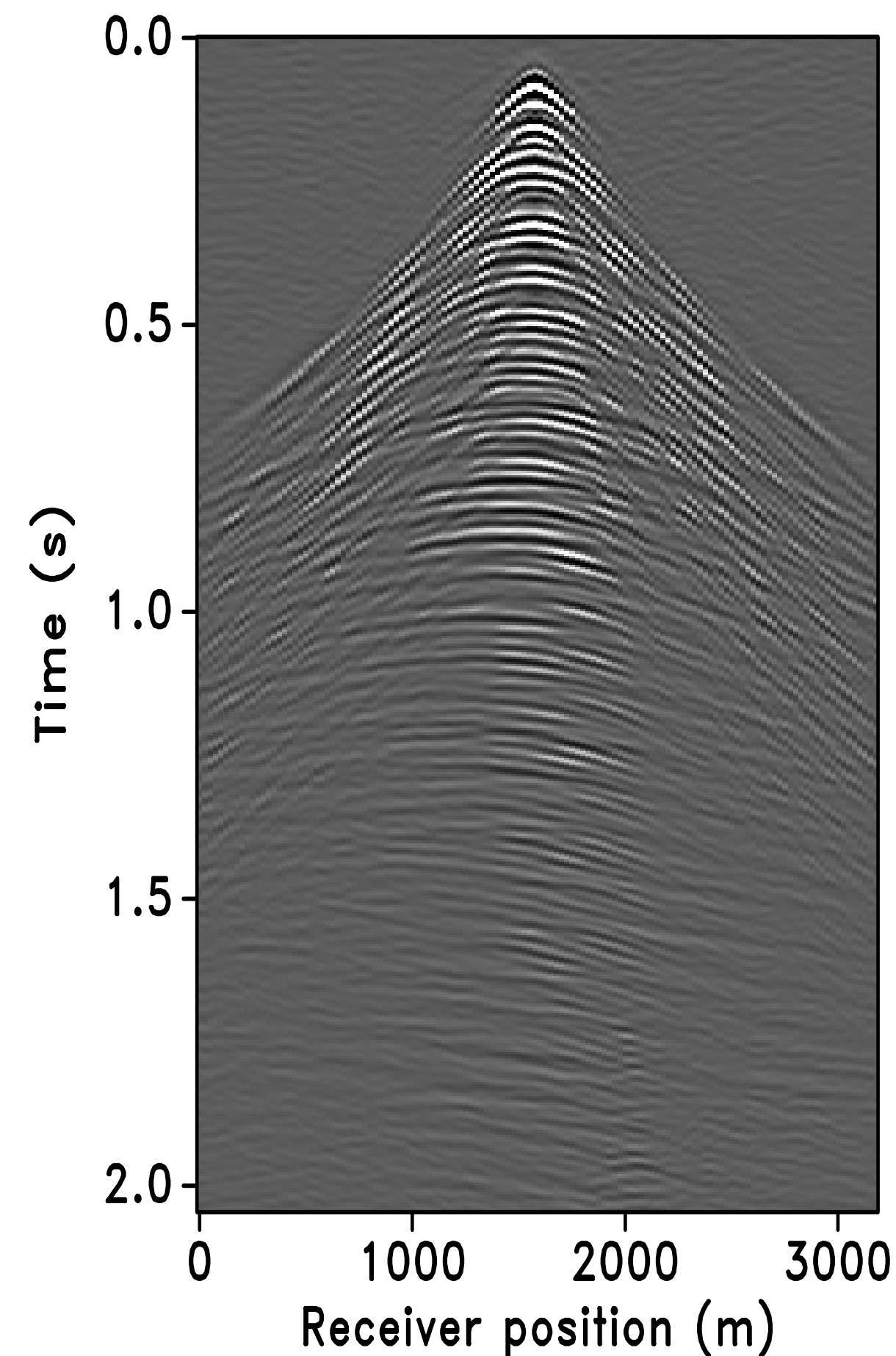




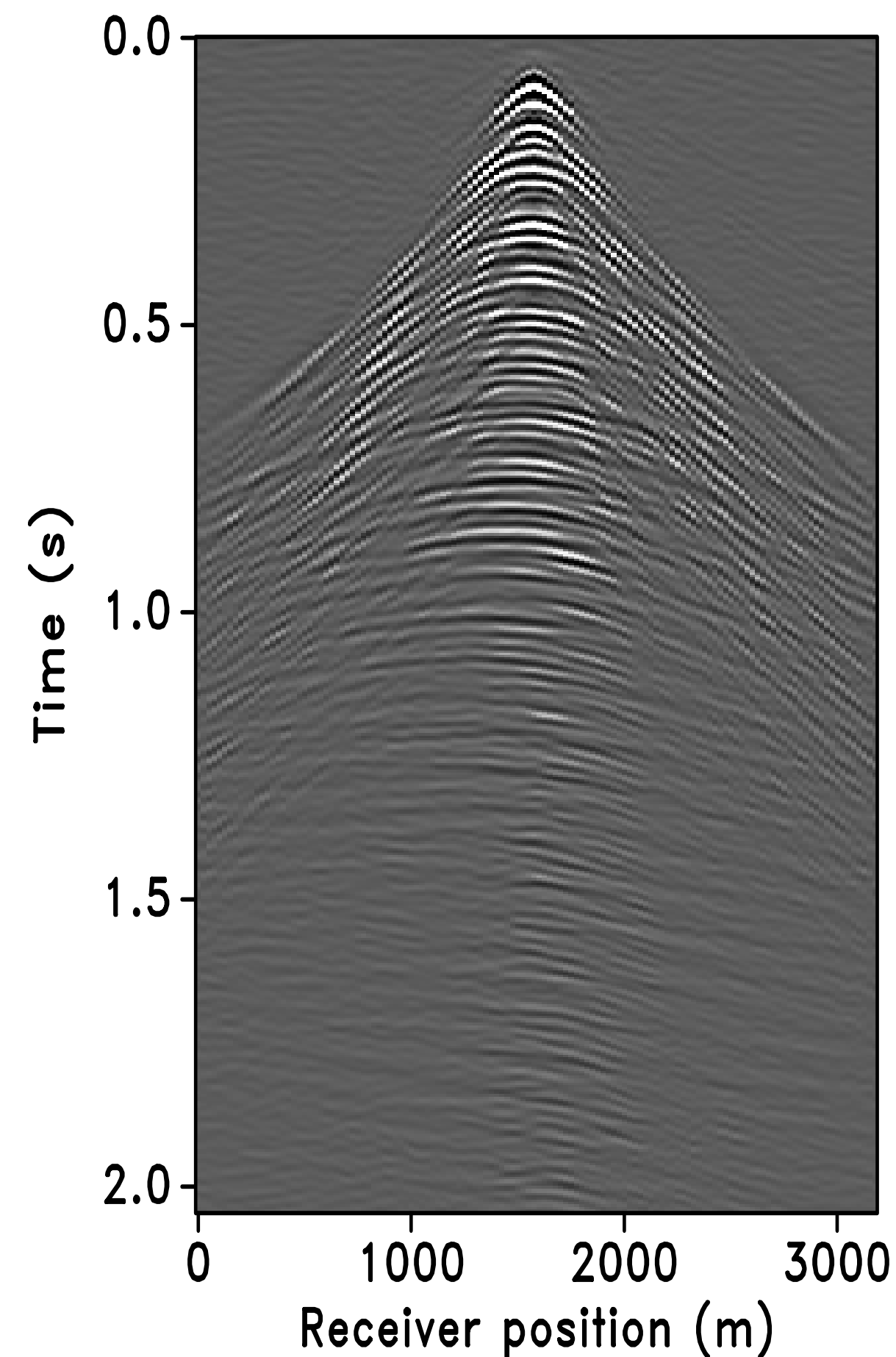
# Source separation

– subsampling factor = 2

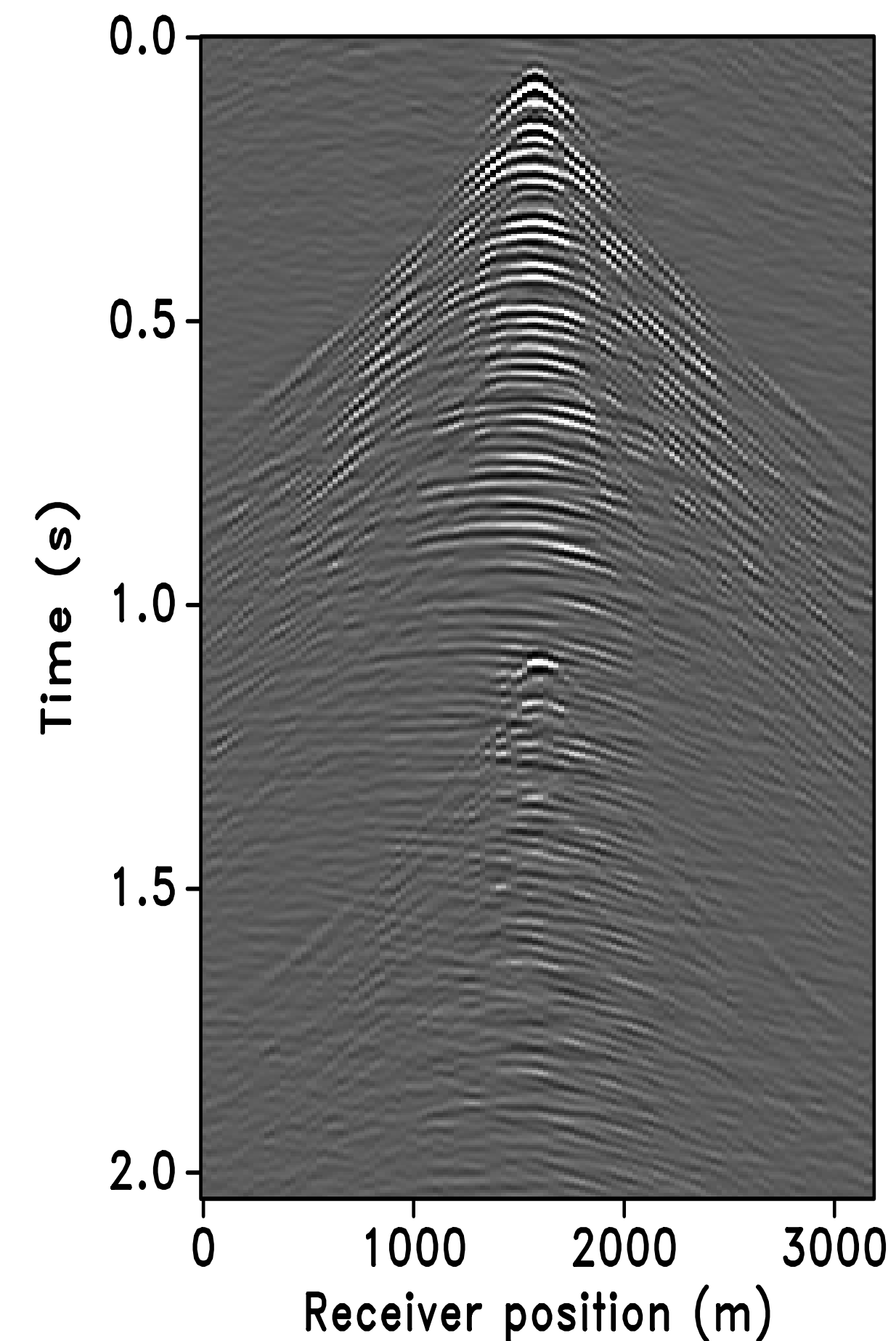
“Ideal” simultaneous acquisition



Random time dithering



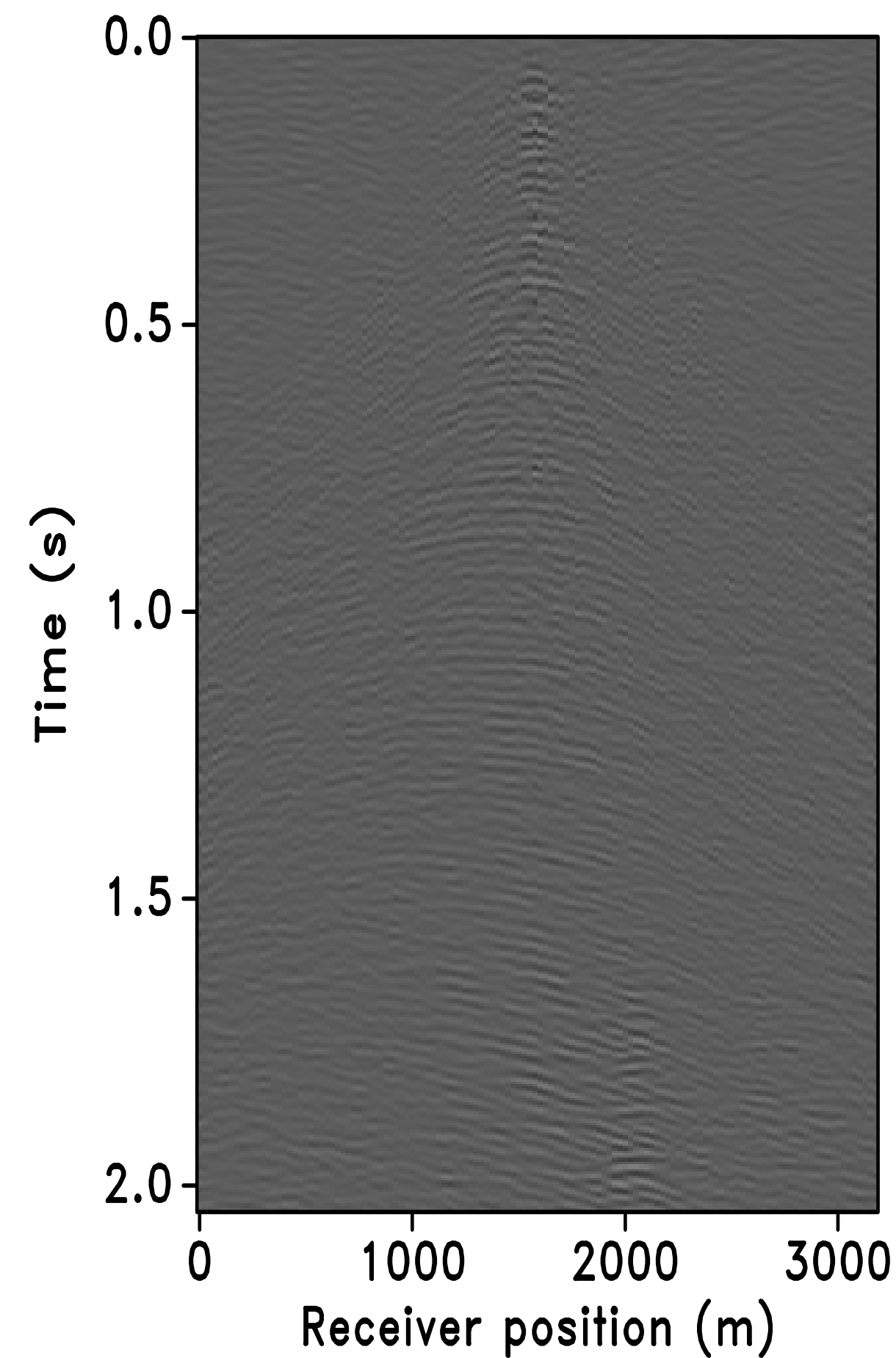
Periodic time dithering



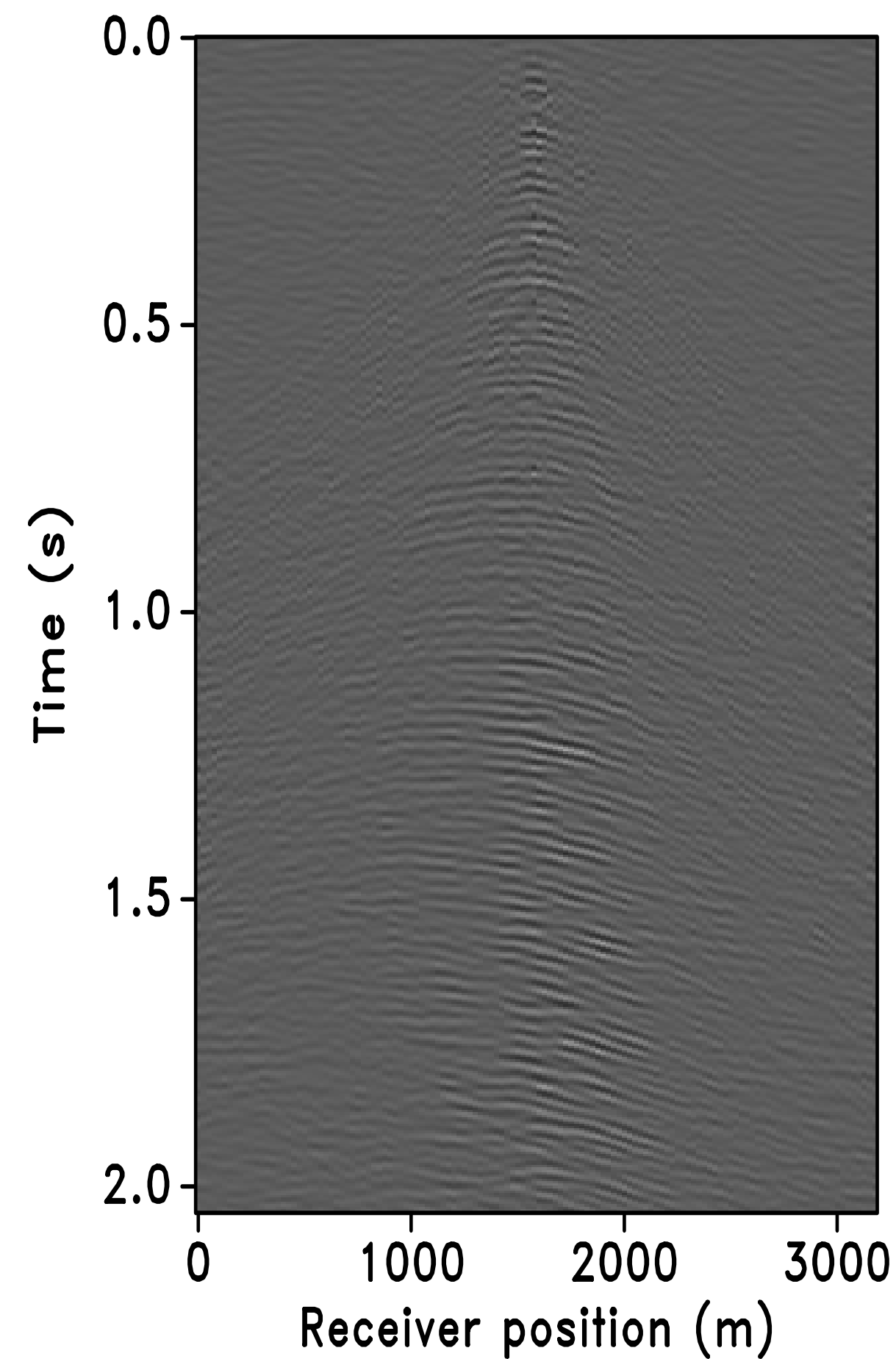
# Residual

– subsampling factor = 2

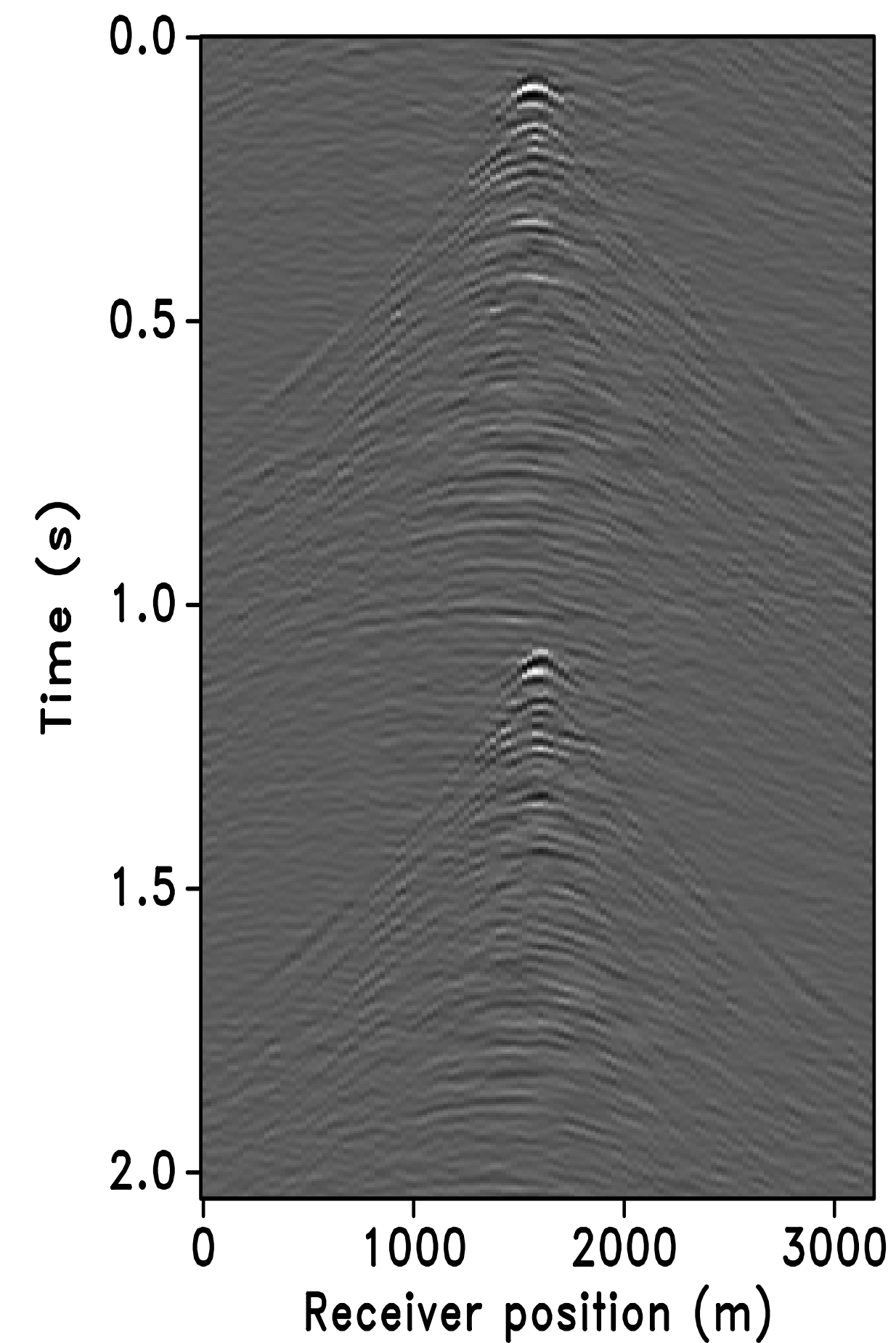
“Ideal” simultaneous acquisition



Random time dithering



Periodic time dithering





# Conclusions

CS ideas can be **successfully** adapted to seismic data acquisition

Three **key** components:

- find representations that reveal structure, e.g., transform-domain sparsity
- sample to break structure, e.g., randomized acquisitions
- recover by structure promotion, e.g., sparsity via one-norm minimization

**Curvelets** lead to compressible representation of seismic data

**Simultaneous-source acquisition** is an instance of compressive sensing

CS offers new **design** perspectives for seismic data acquisition schemes

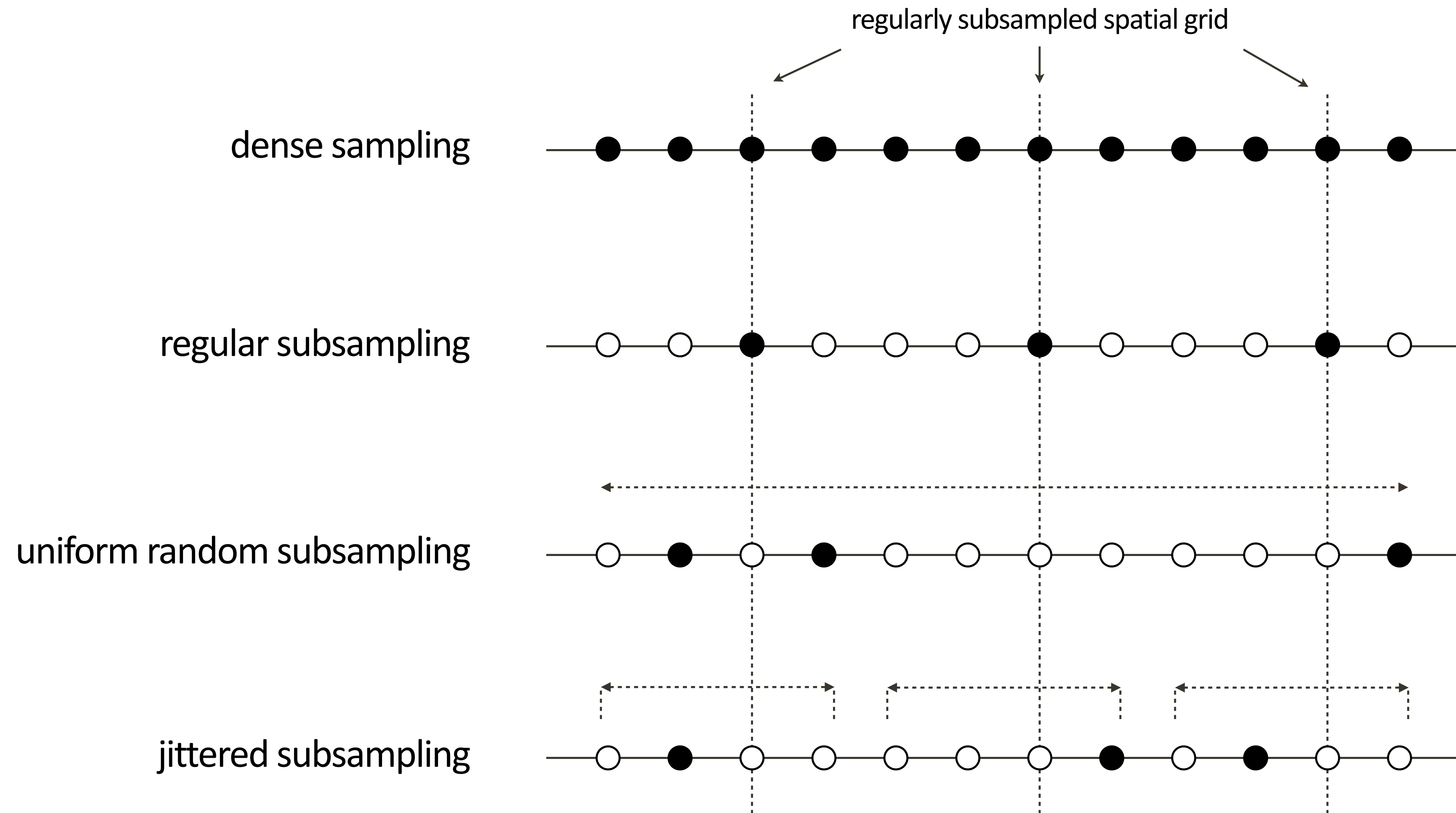
# Chapter 4

Compressive marine seismic acquisition

- **pragmatic** simultaneous-source “time-jittered” marine
- static acquisition geometry

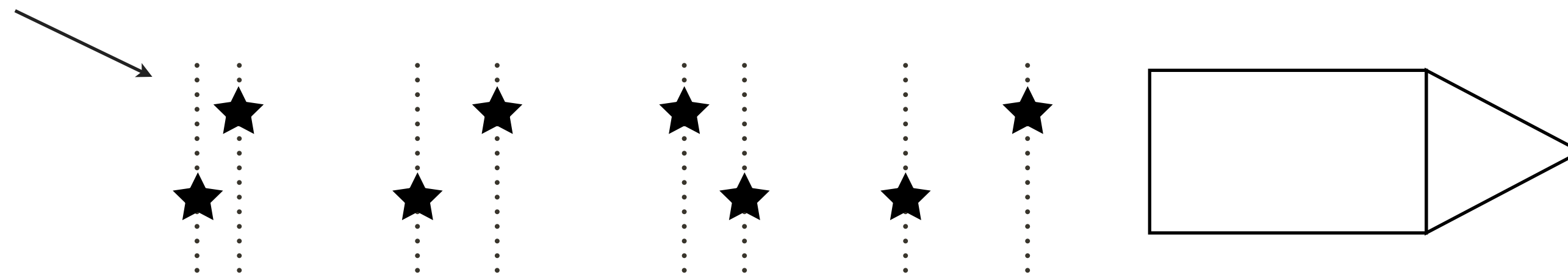


# Sampling schemes



# Time-jittered marine acquisition

shot-time randomness: **LARGE**  
irregularly sampled spatial grid



continuous recording  
*START*

continuous recording  
*STOP*

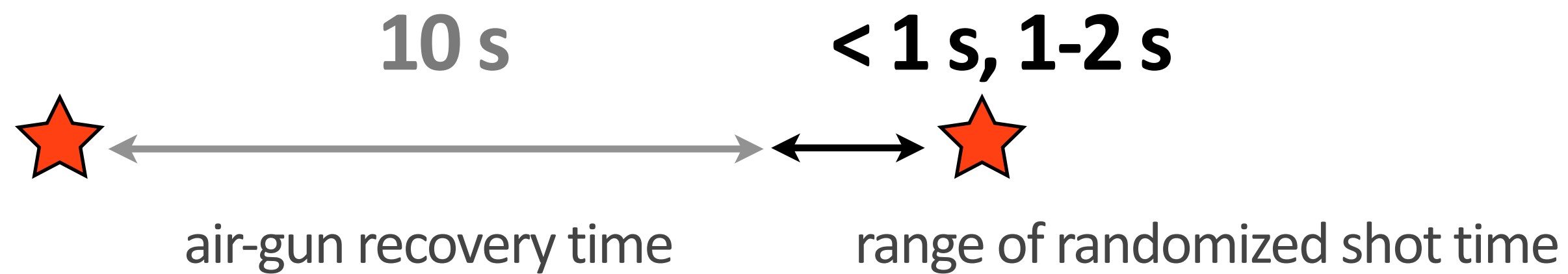


ocean-bottom cable

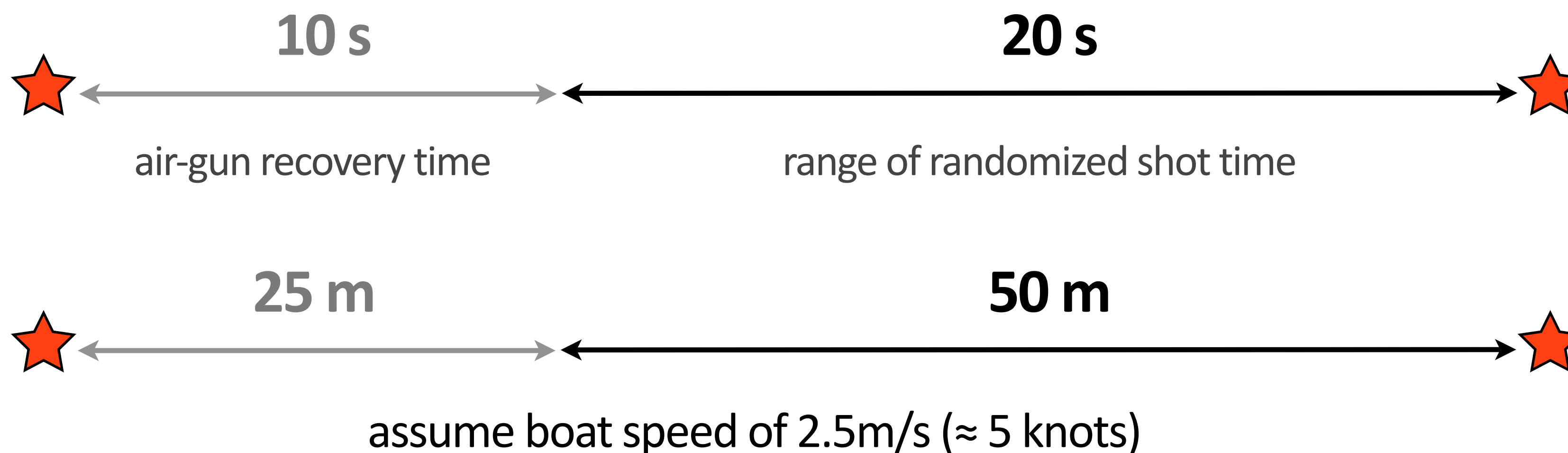


# Design of time-jittered shots

## Low variation

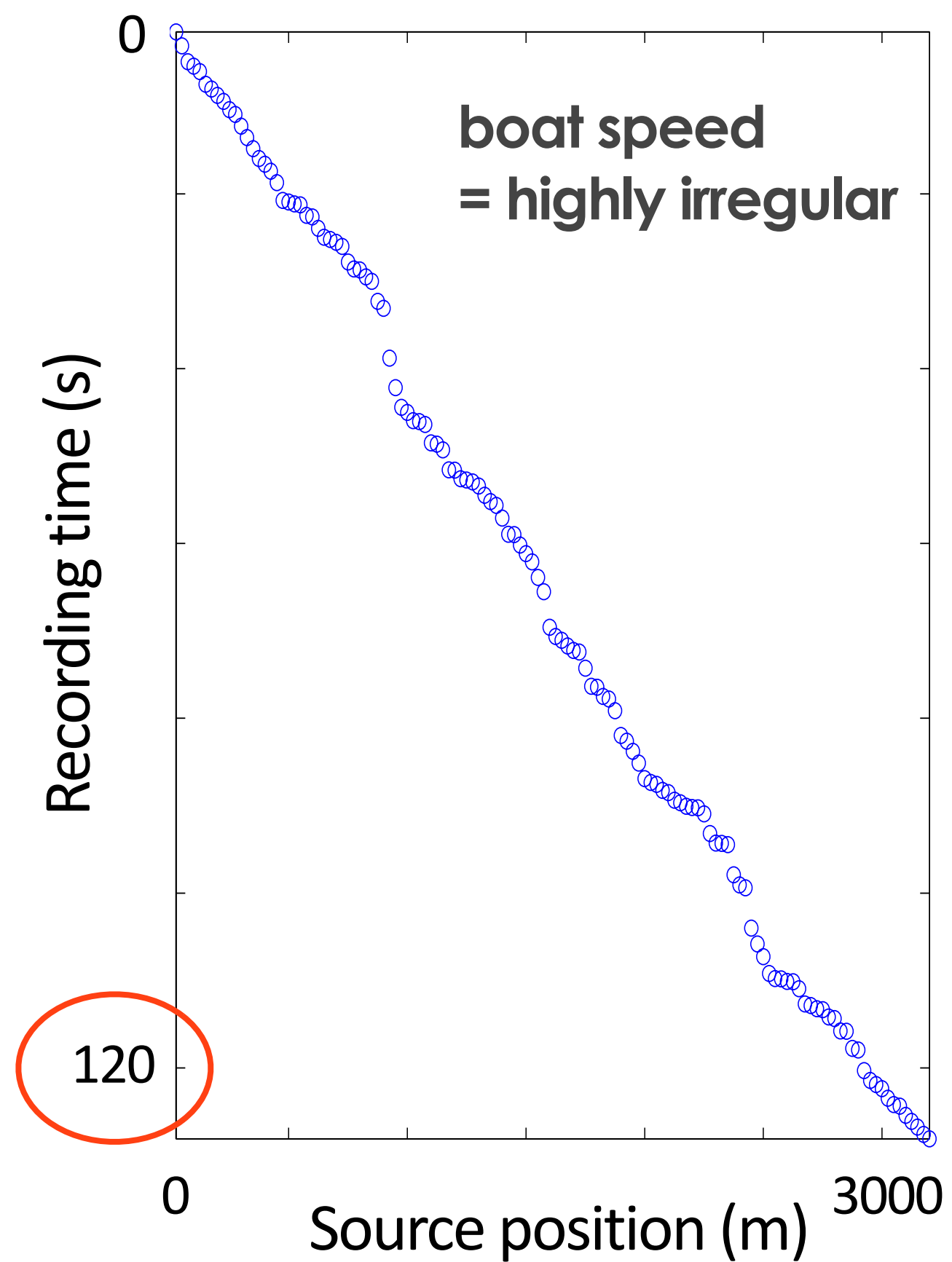


## High variation

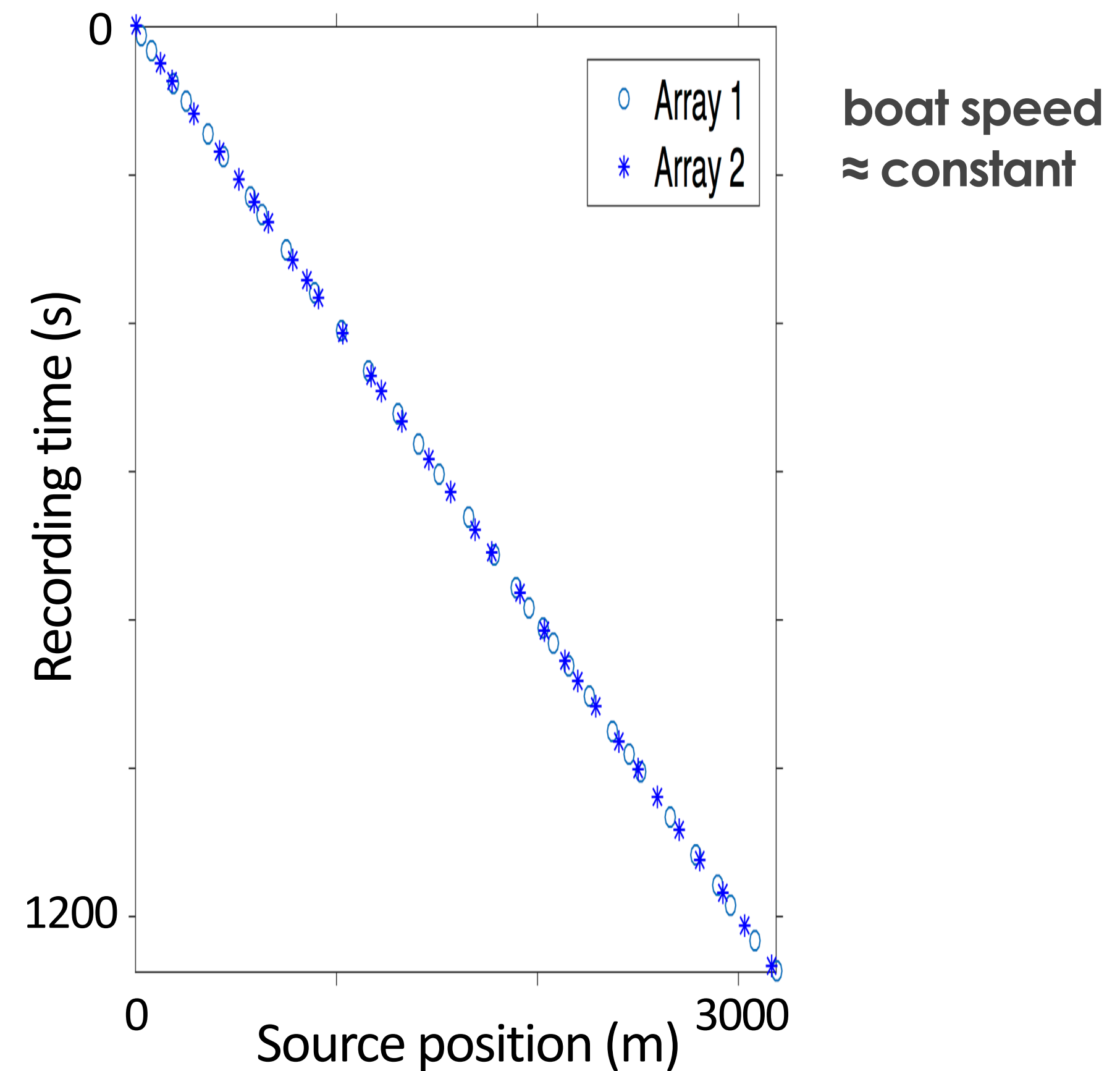


# Pragmatic compressive simultaneous acquisition

Random time dithering  
(**non**realistic)



Time-jittered marine  
(realistic)

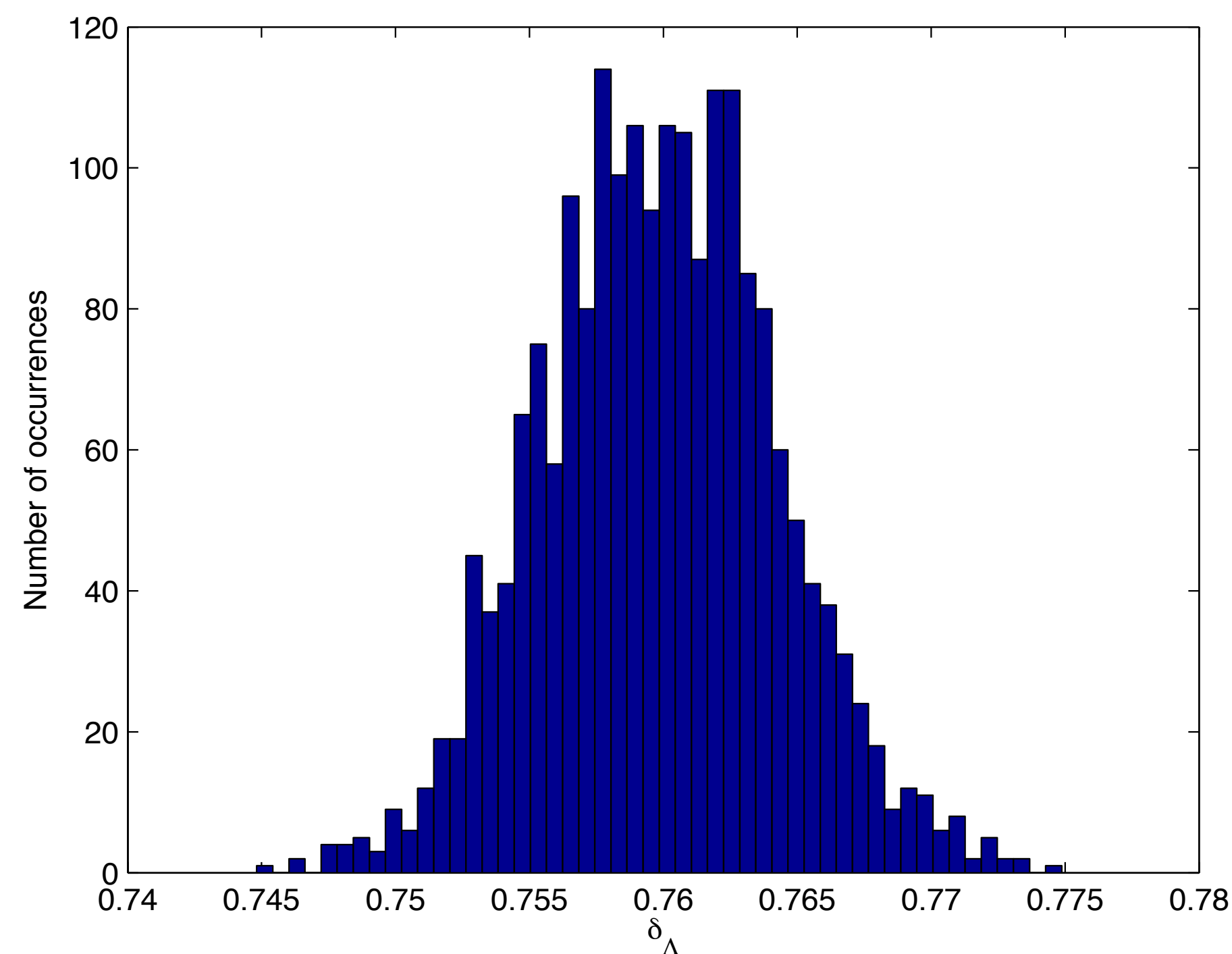




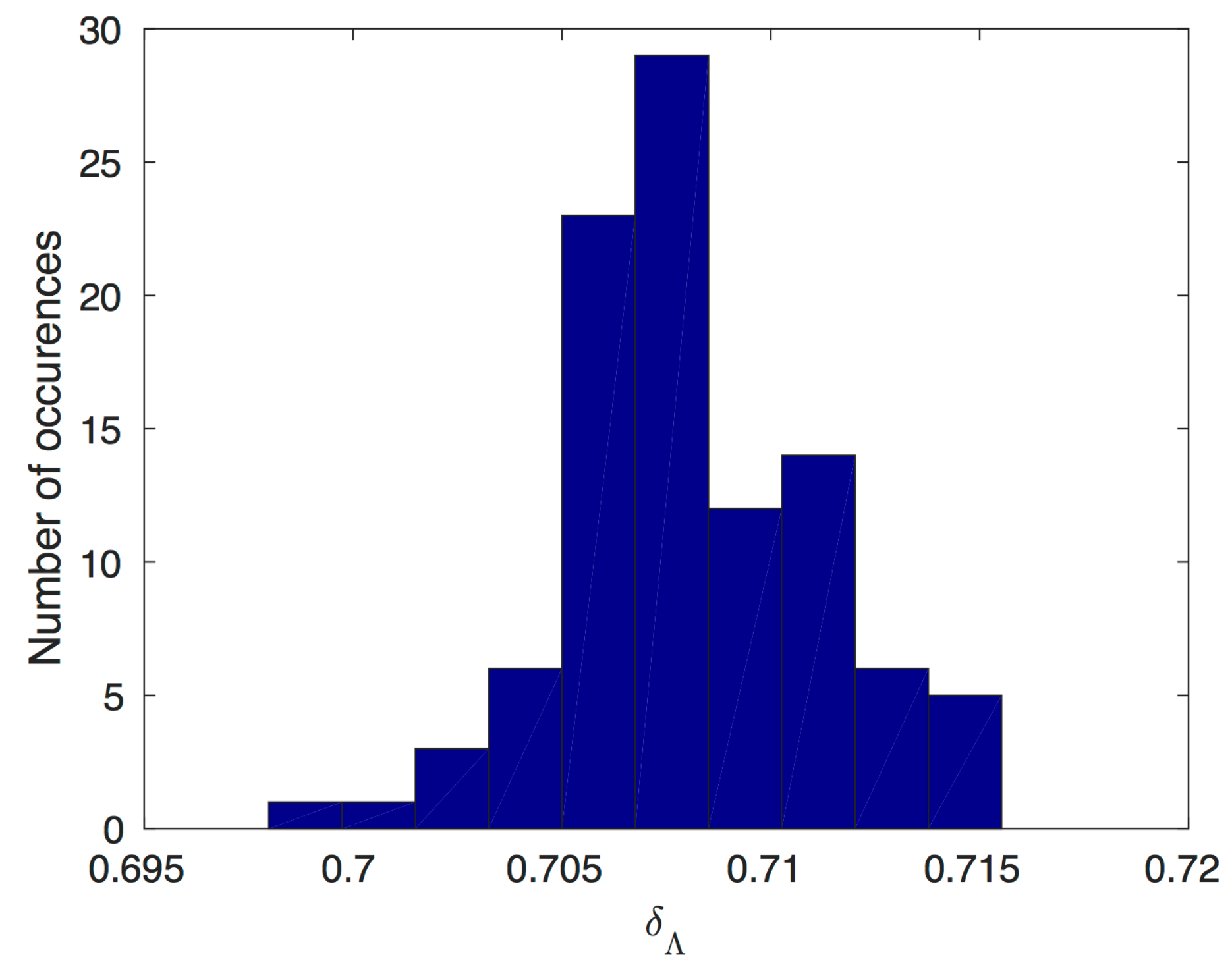
# Restricted Isometry Property (RIP)

- indicates whether every group of  $k$  columns of  $\mathbf{A}$  are nearly orthogonal
- restricted isometry constant  $0 < \delta_k < 1$  for which
$$(1 - \delta_k) \|\mathbf{u}\|_2^2 \leq \|\mathbf{A}_\Lambda \mathbf{u}\|_2^2 \leq (1 + \delta_k) \|\mathbf{u}\|_2^2$$

**nonrealistic**

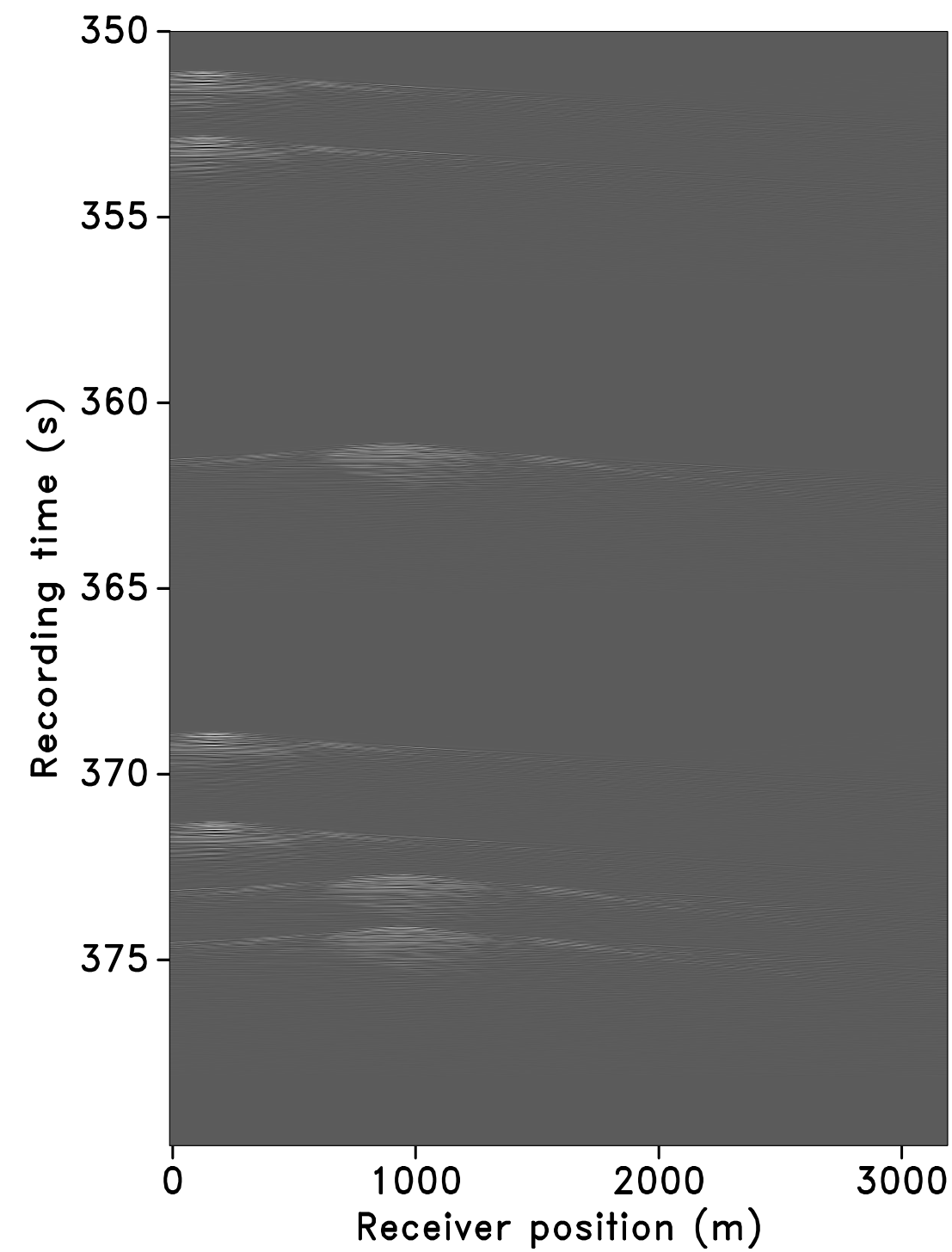


**realistic**



# Time-jittered marine acquisition

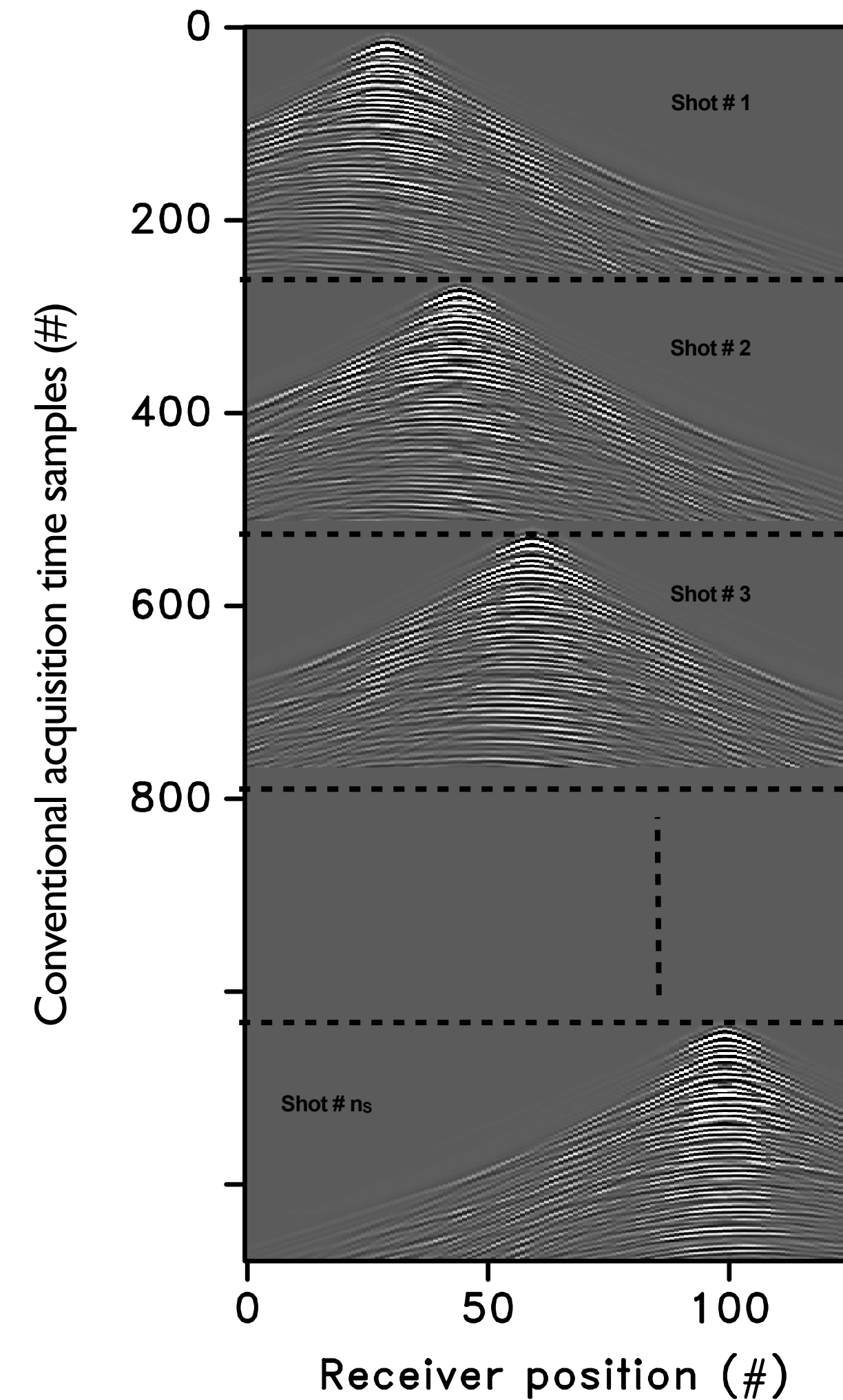
**subsampled** shots **with**  
**overlap** between shot records



source fires at jittered times  
and jittered positions

←  
sum

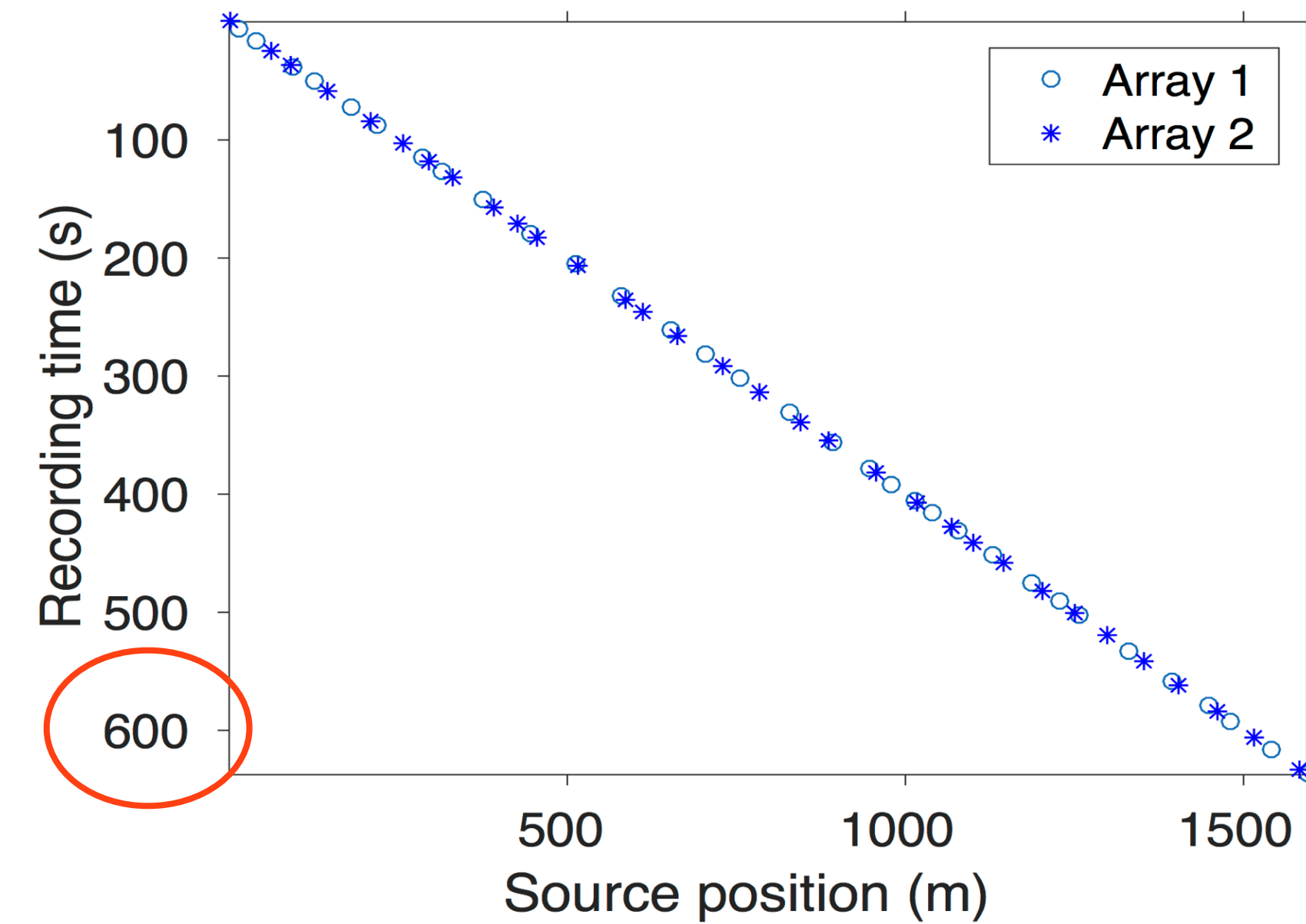
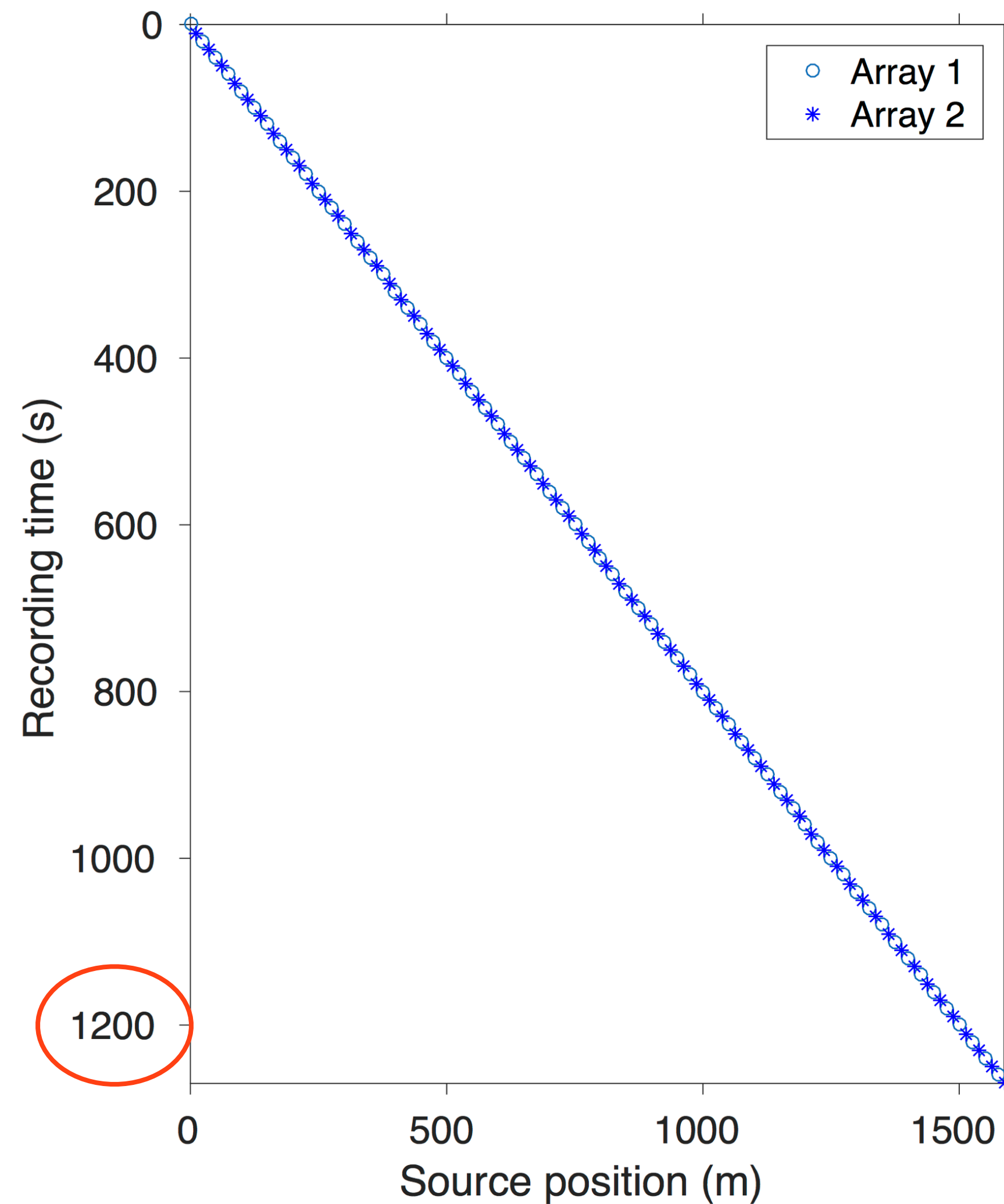
**all** shots **without** overlap  
between shot records





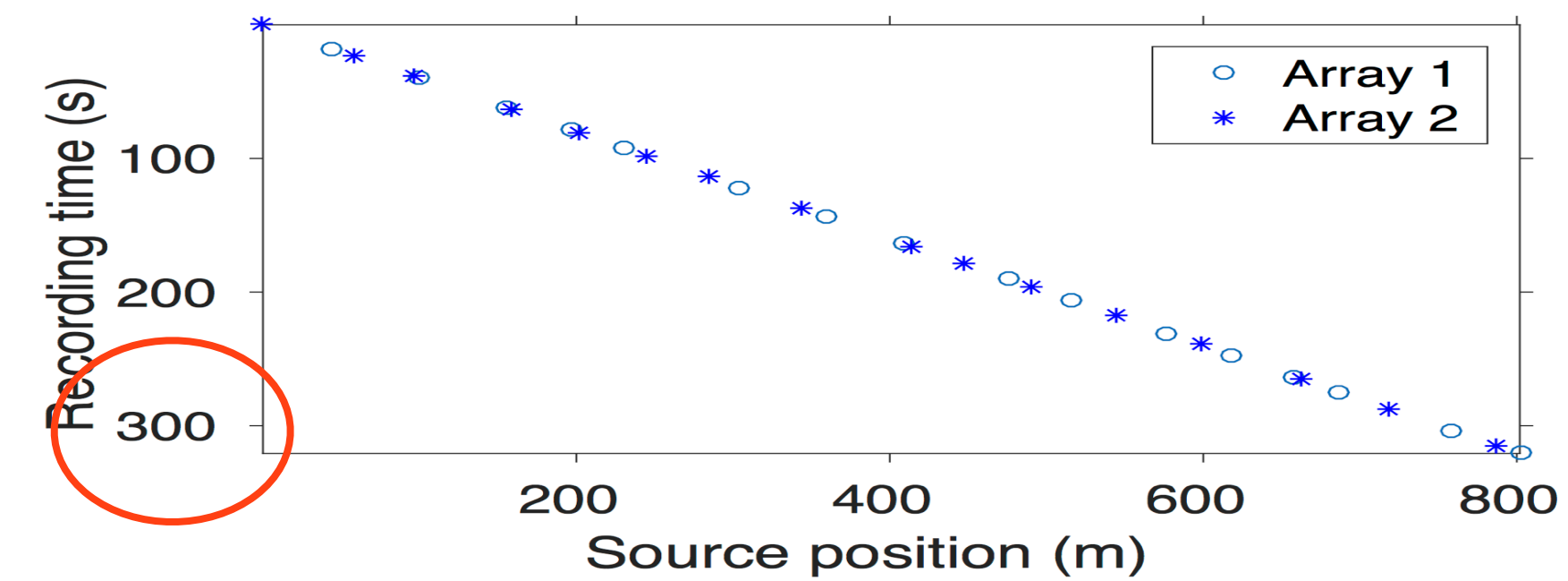
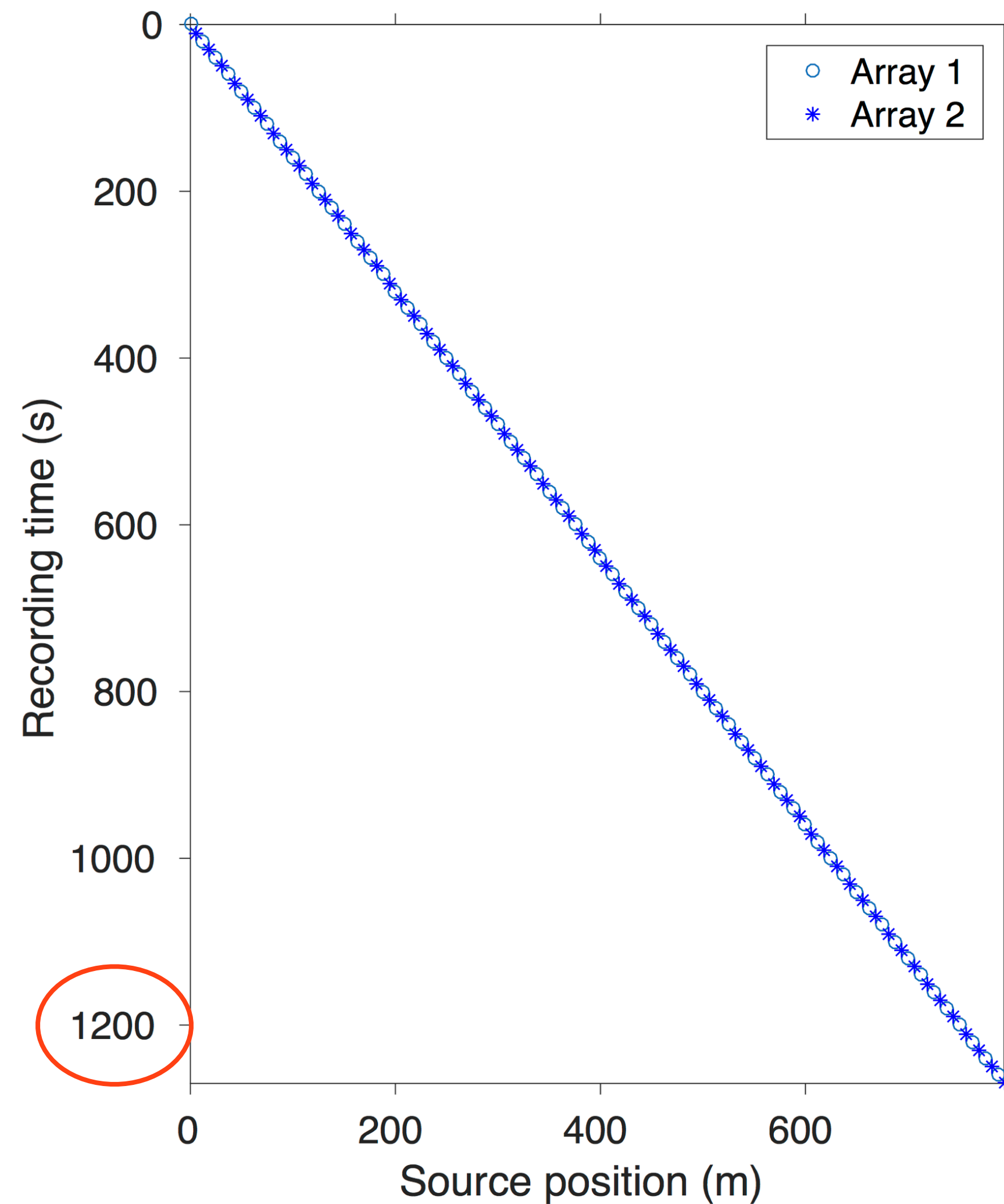
# Conventional vs. time-jittered marine acquisition

– subsampling factor = 2



# Conventional vs. time-jittered marine acquisition

– subsampling factor = 4





# Compressive simultaneous acquisition

subsampling factor

$$\eta = \frac{1}{\text{number of air-gun arrays}} \times \frac{\text{jittered spatial grid interval}}{\text{conventional spatial grid interval}}$$

for spatial sampling = 12.5 m

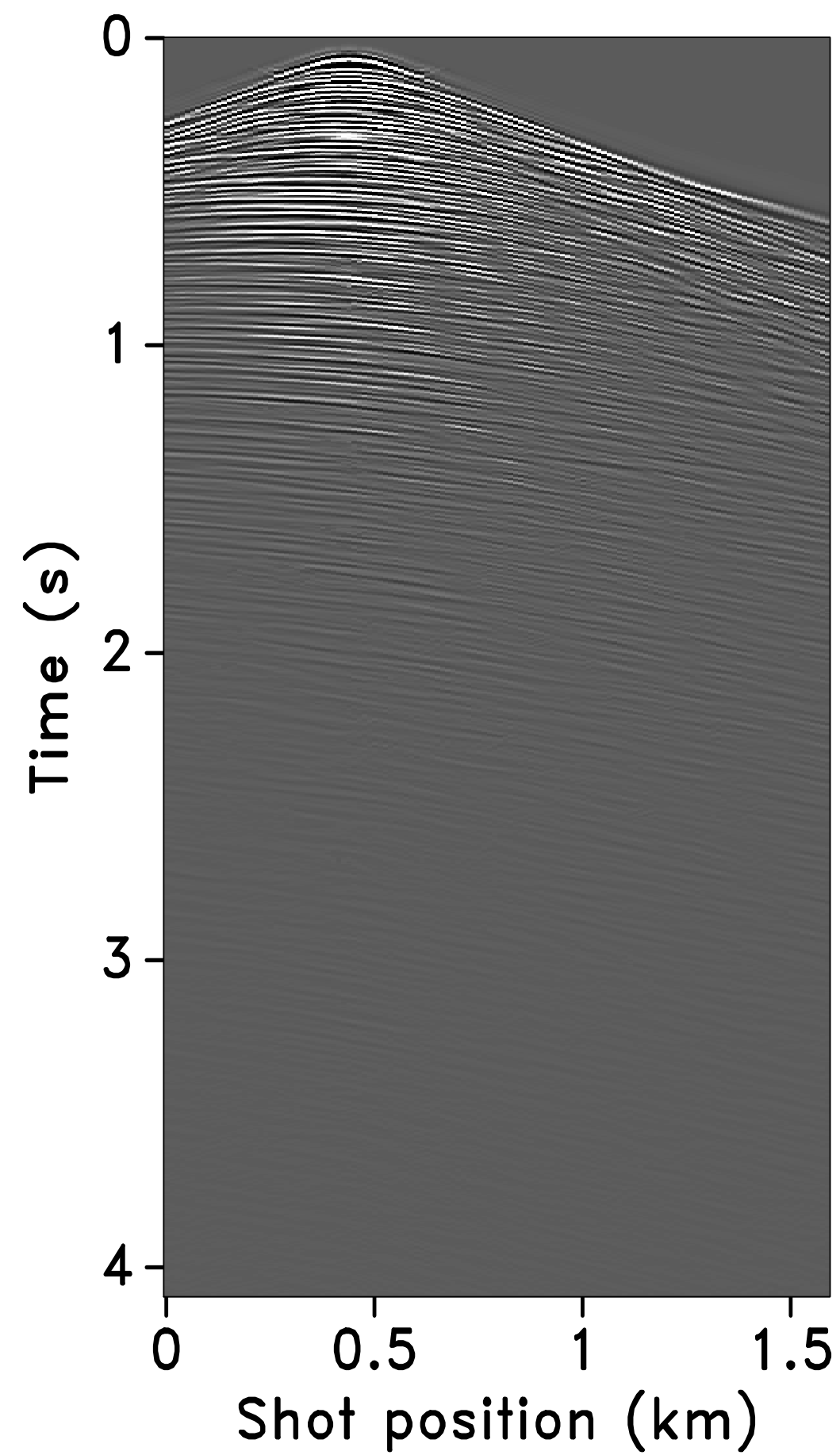
$$\eta = \frac{1}{2} \times \frac{50.0 \text{ m}}{12.5 \text{ m}} = 2$$

for spatial sampling = 6.25 m

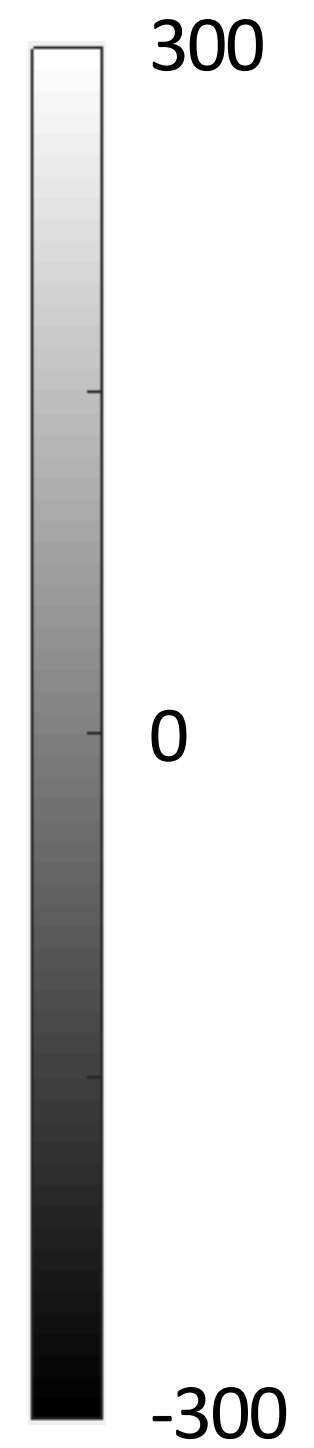
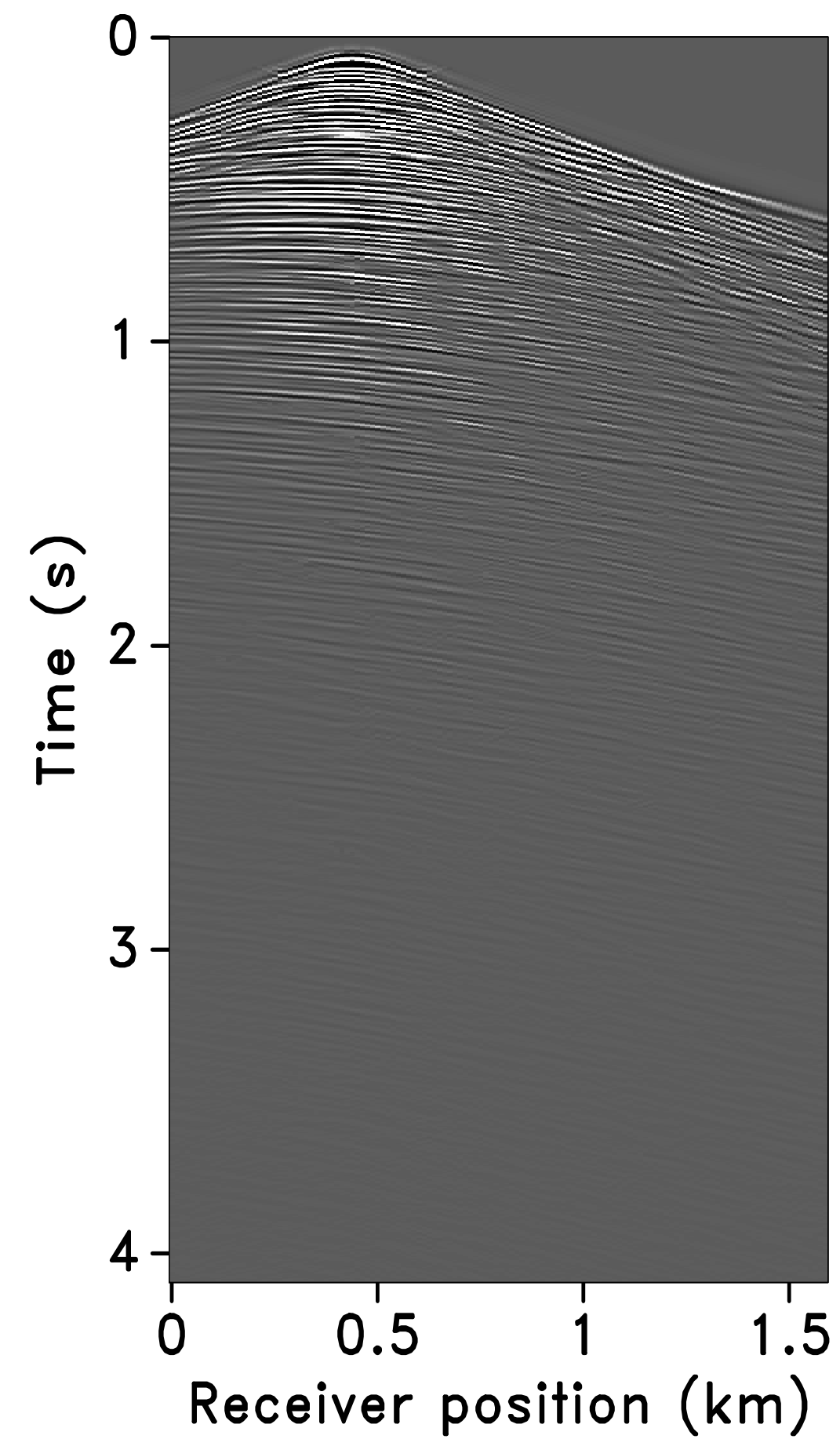
$$\eta = \frac{1}{2} \times \frac{50.0 \text{ m}}{6.25 \text{ m}} = 4$$

# Conventional data

## Receiver gather



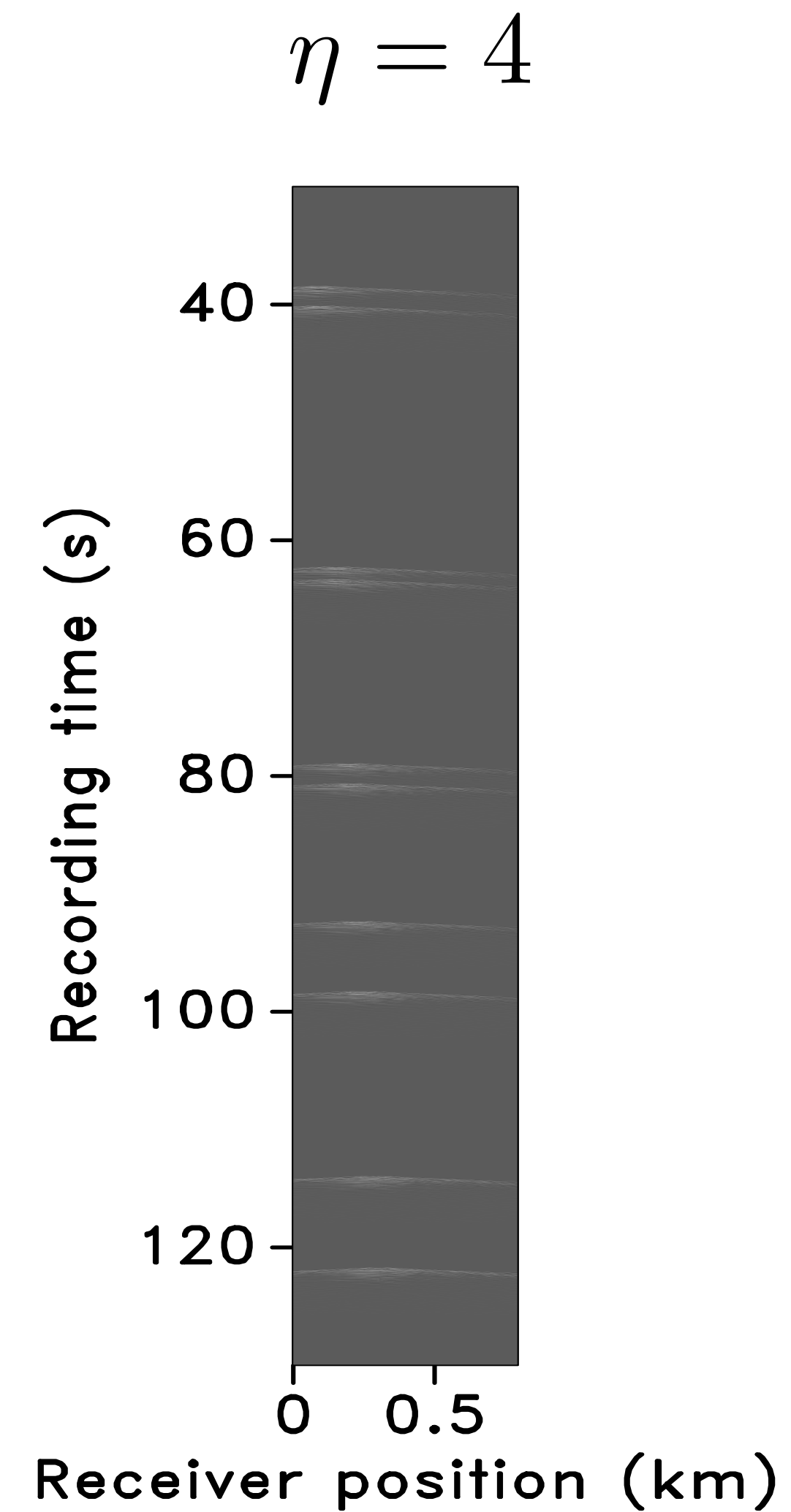
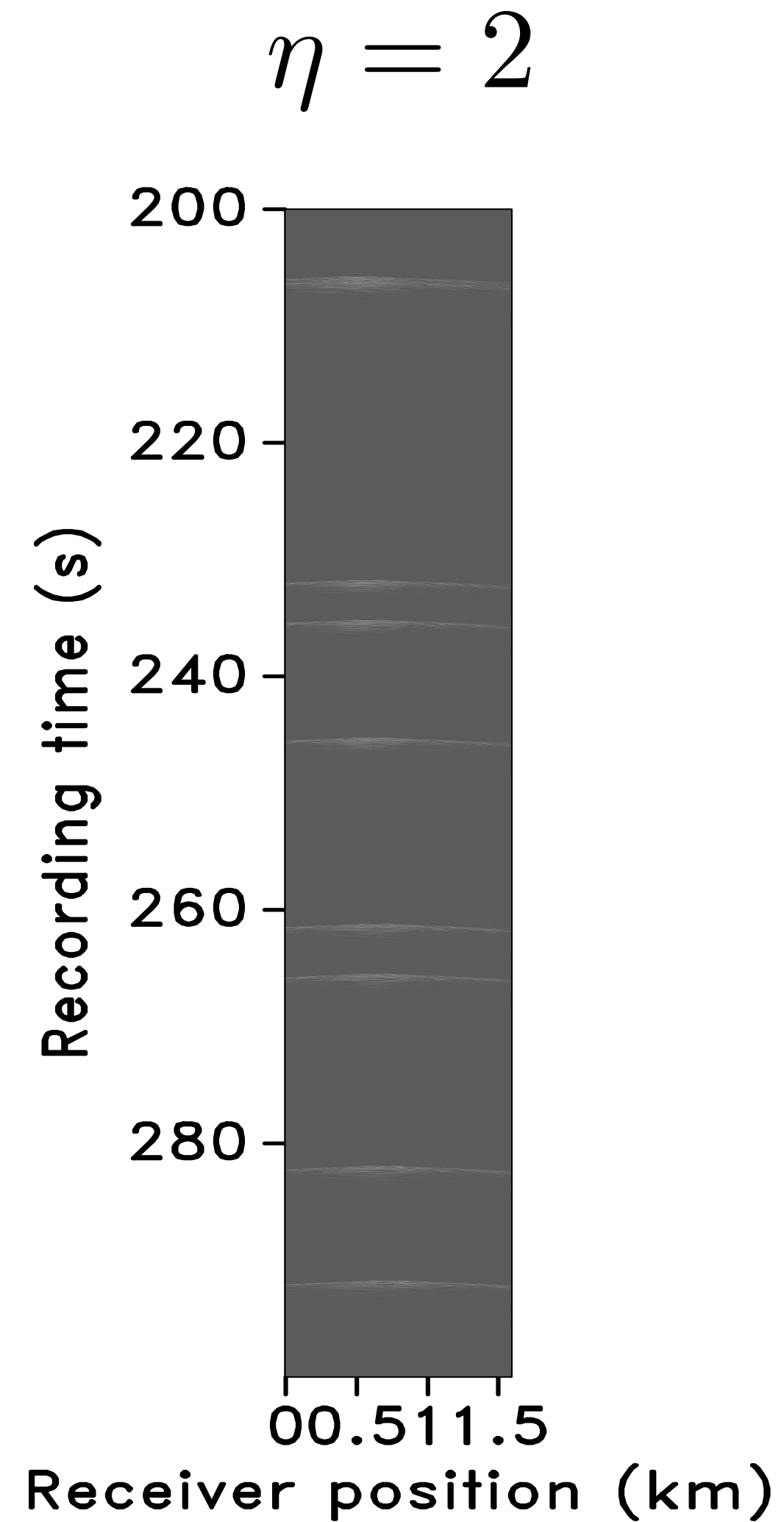
## Shot gather





# Measurements

– subsampled and overlapping shots

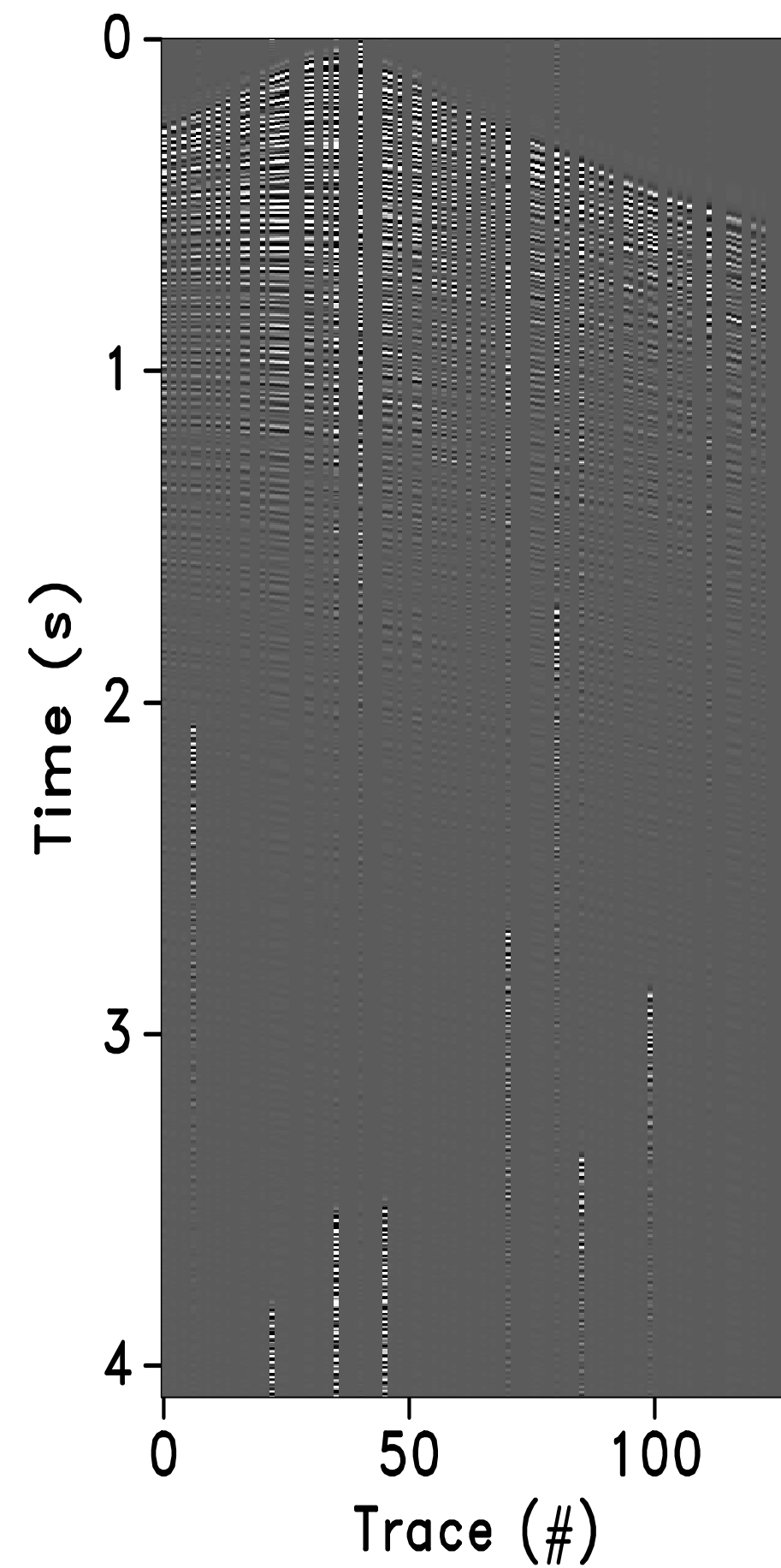


# Adjoint of acquisition operator ( $\mathbf{M}^H \mathbf{b}$ )

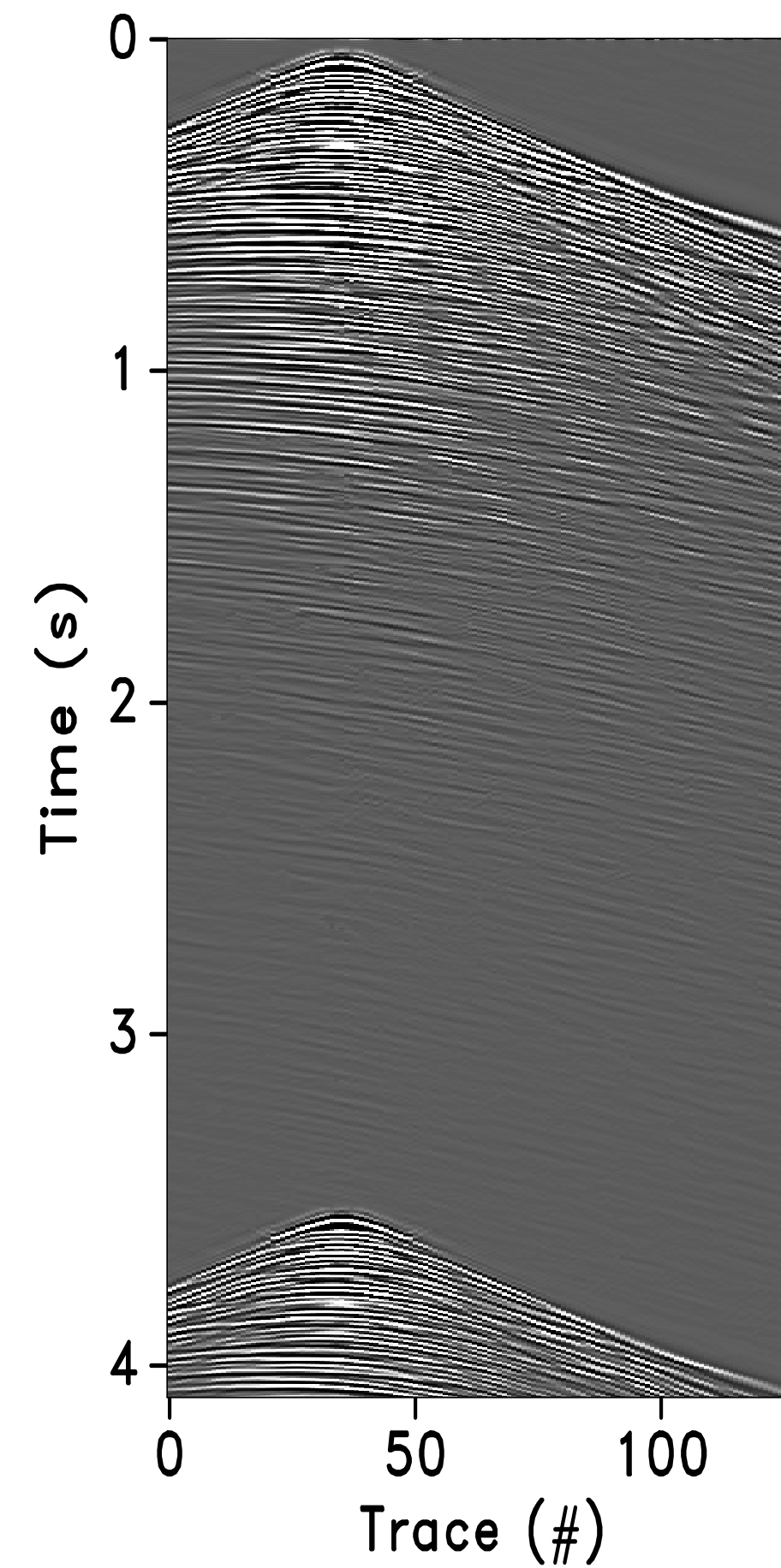
$$\eta = 2$$

$$\eta = 4$$

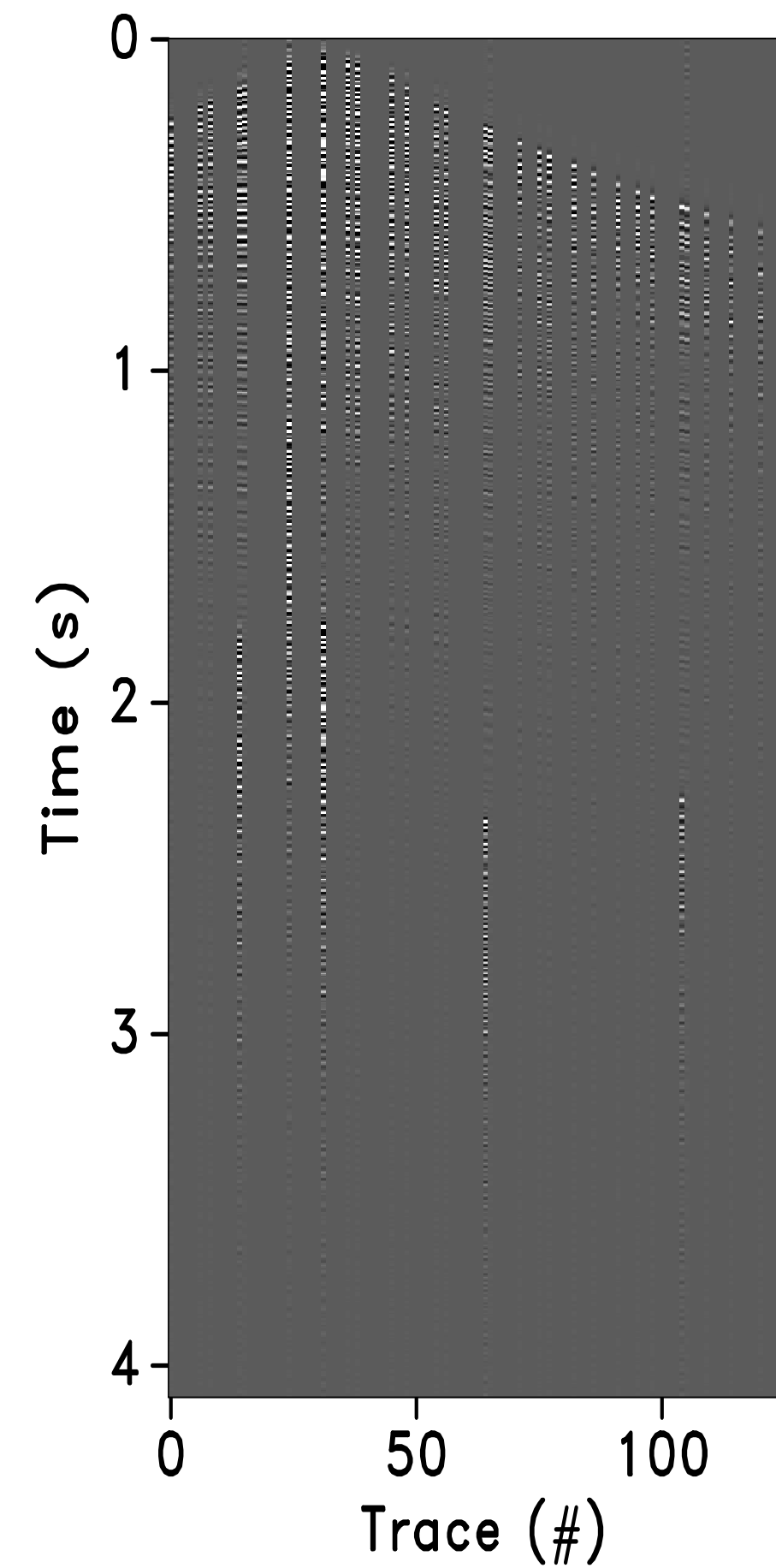
Receiver



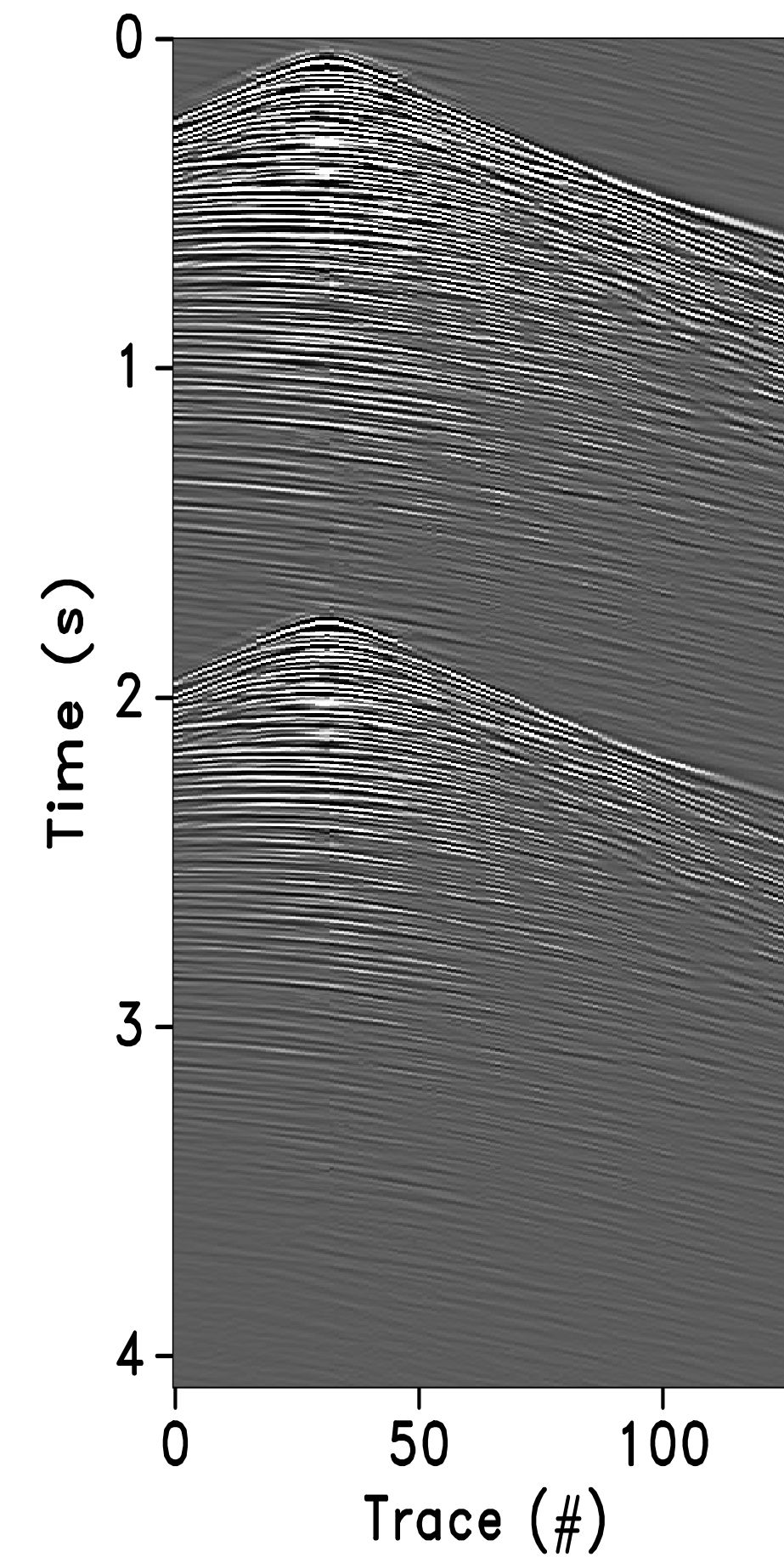
Shot



Receiver



Shot

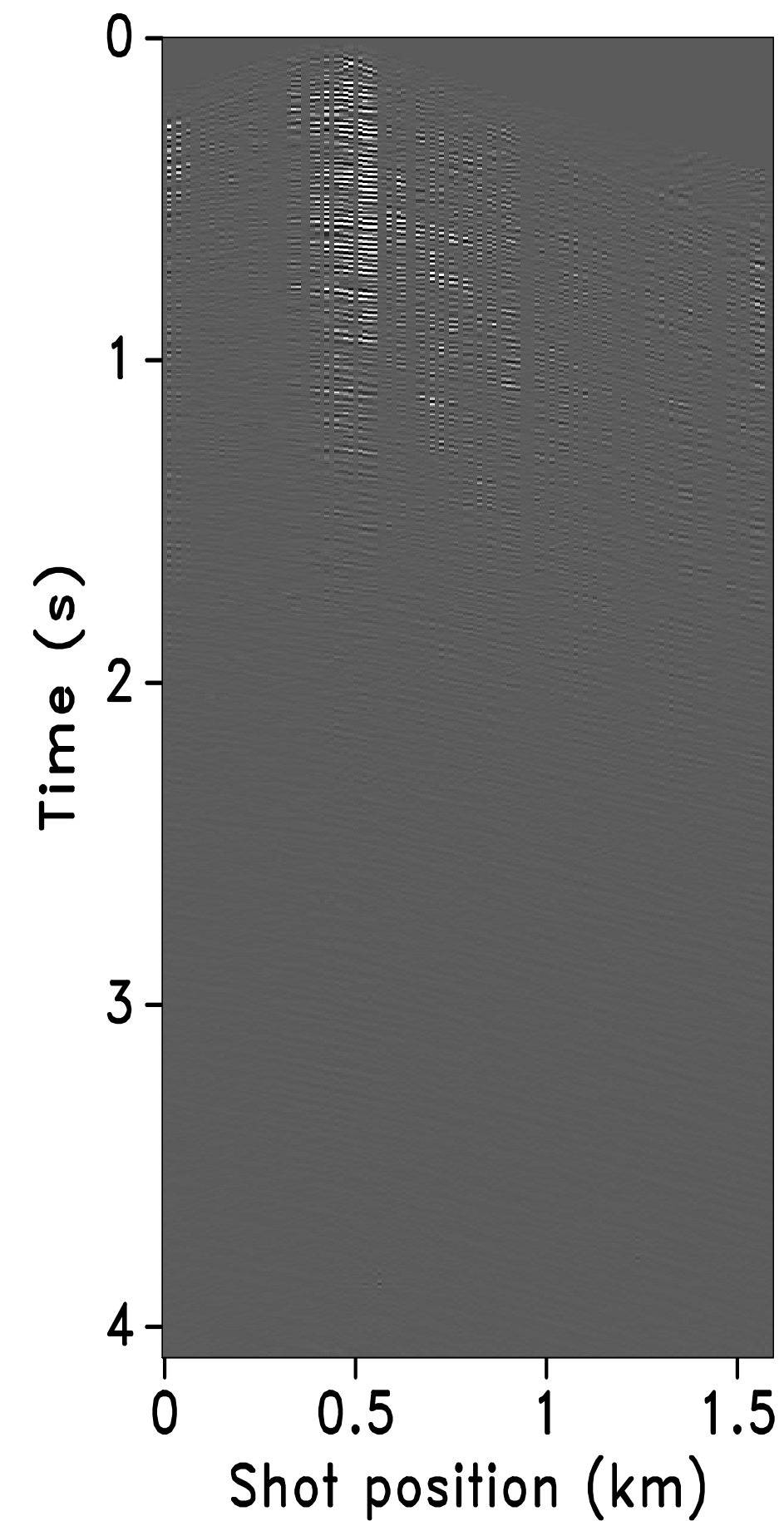
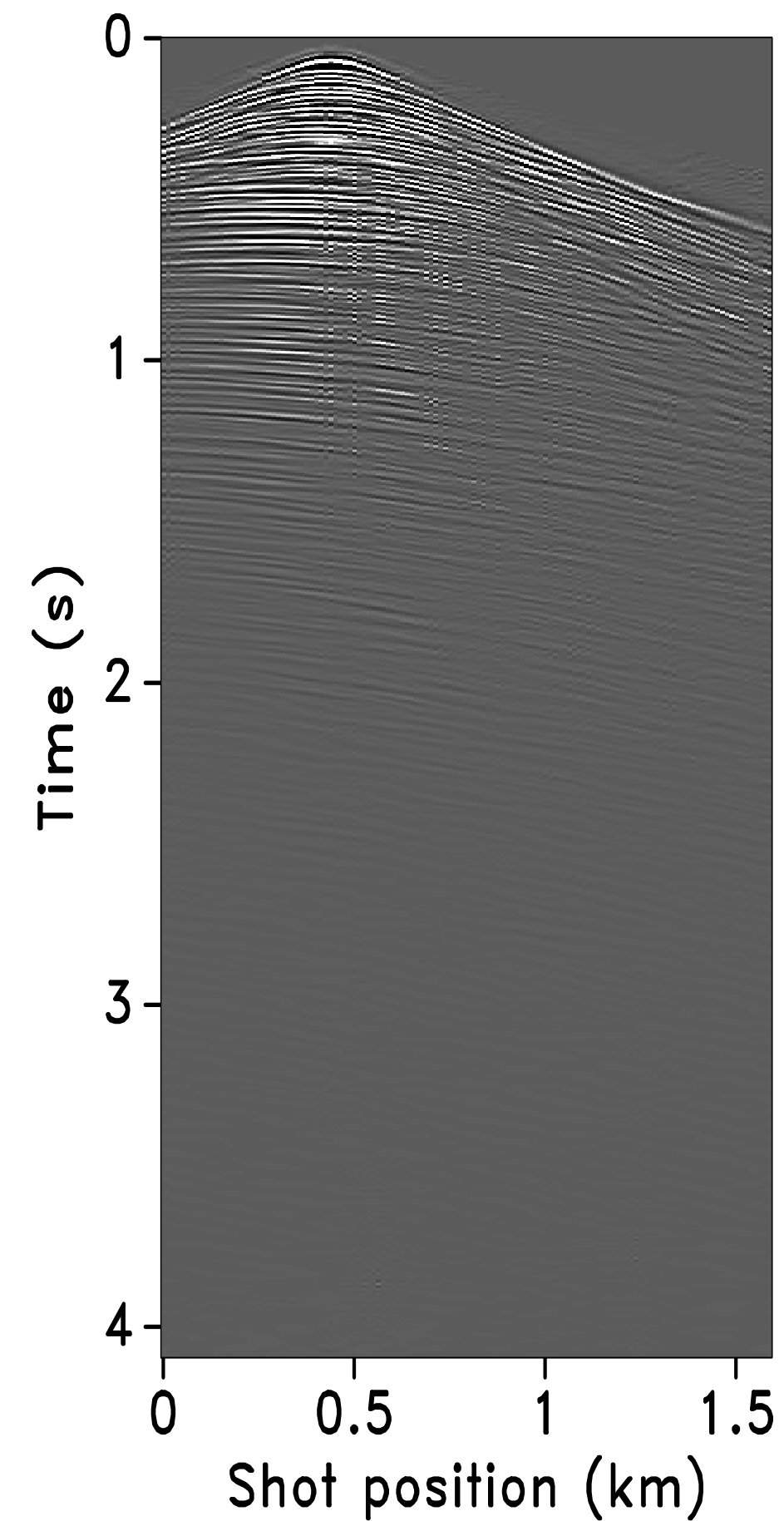




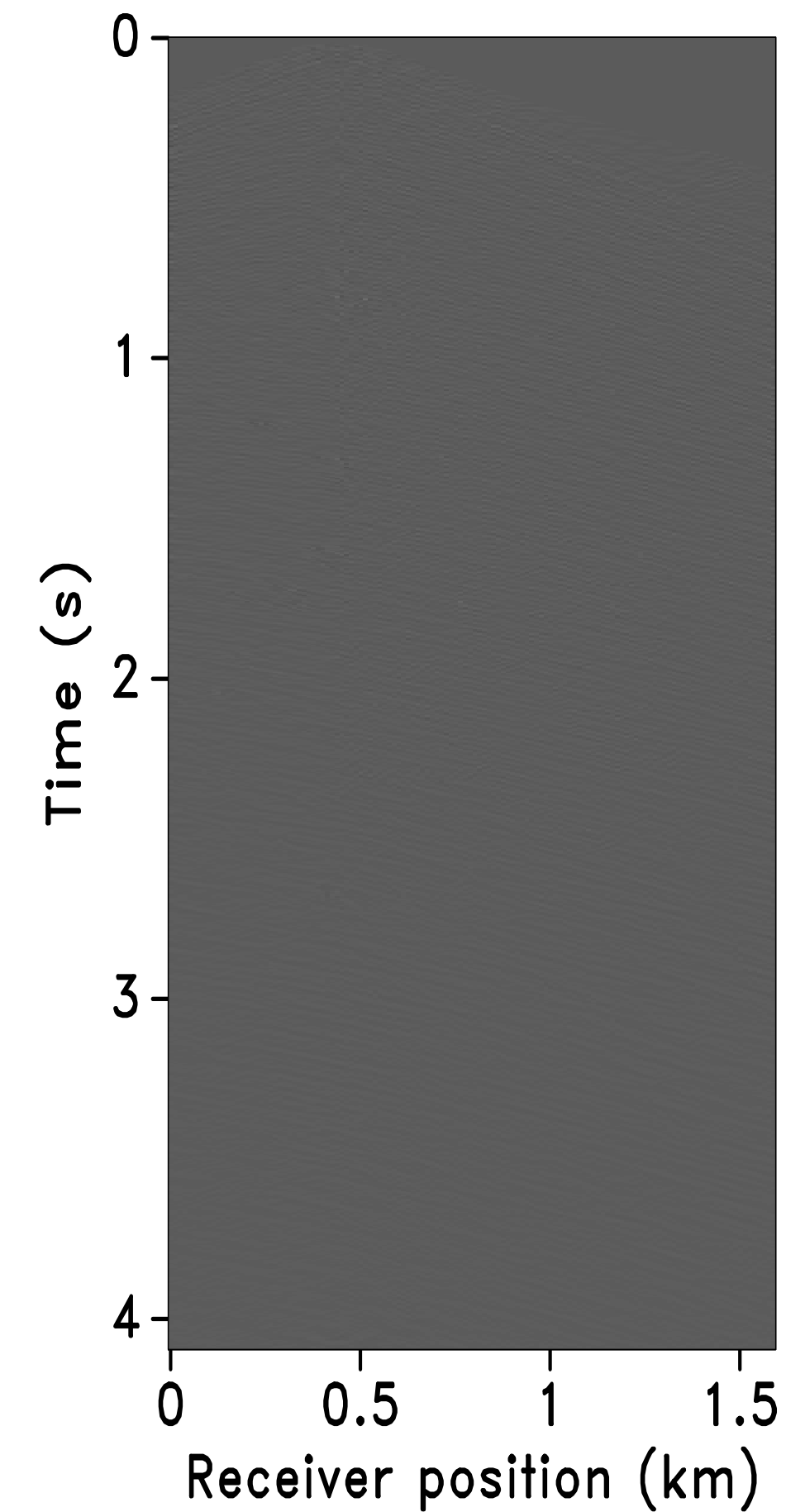
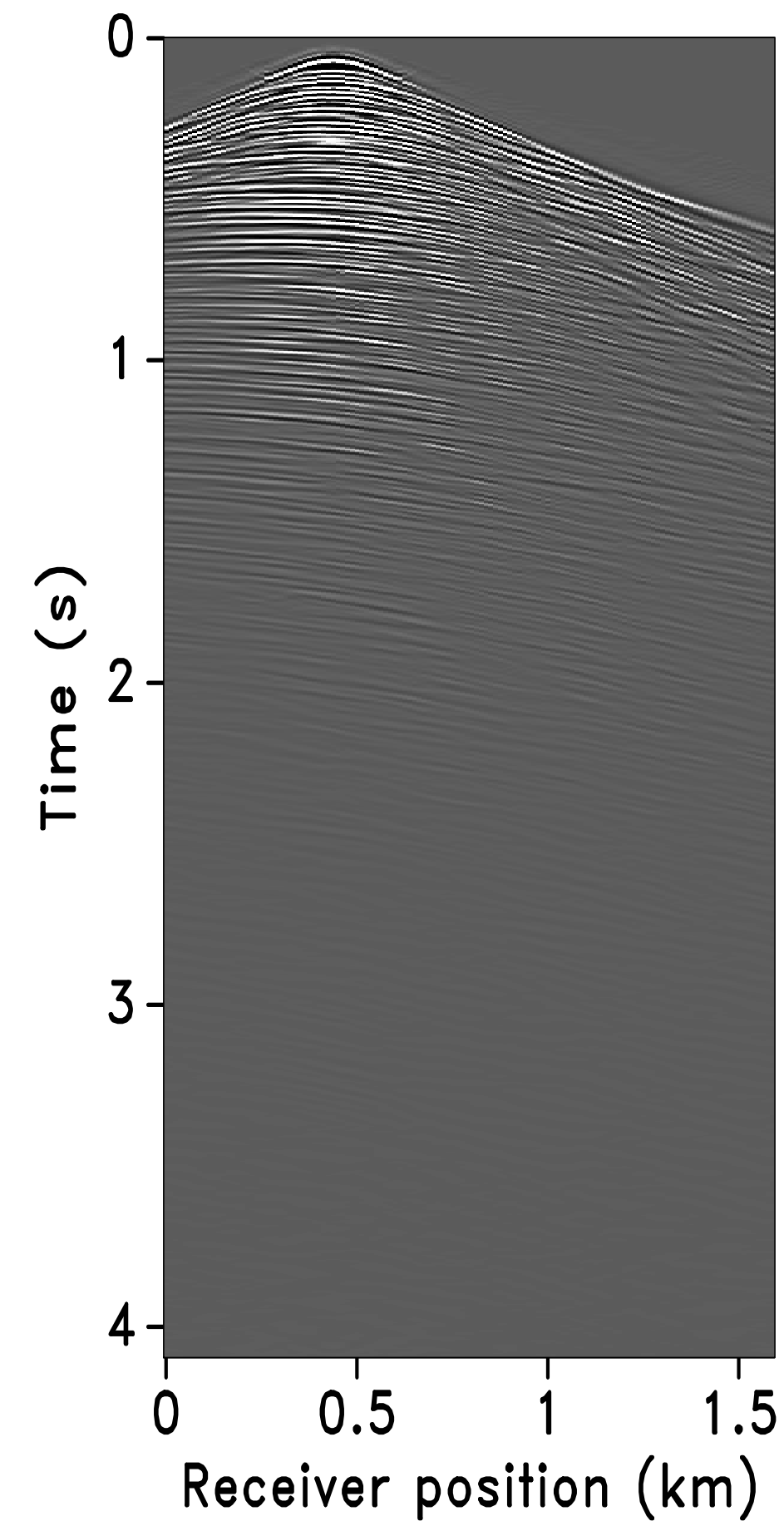
# Sparsity-promoting recovery & residual

– 2D curvelets; subsampling factor = 2

Receiver gather

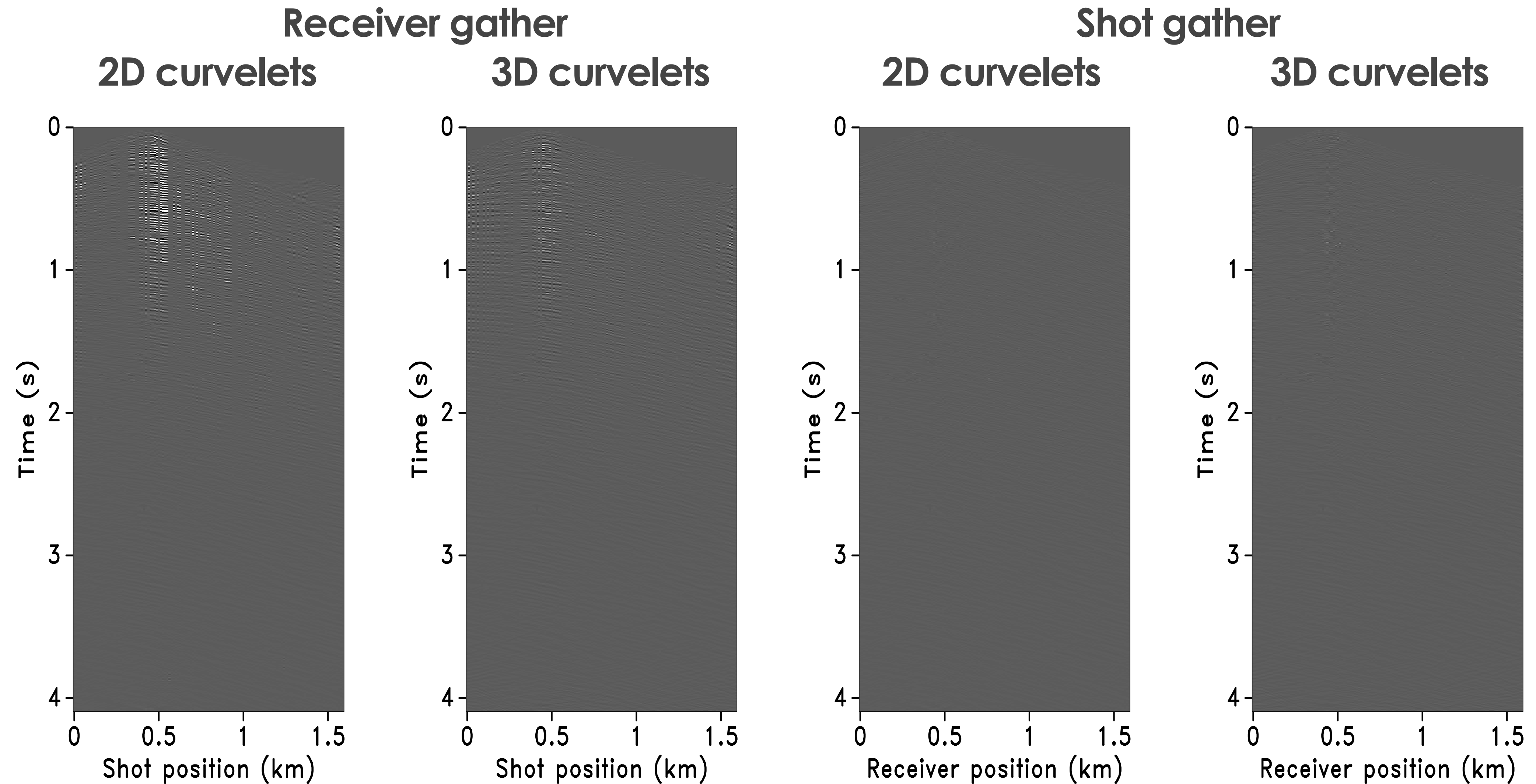


Shot gather



# Residual

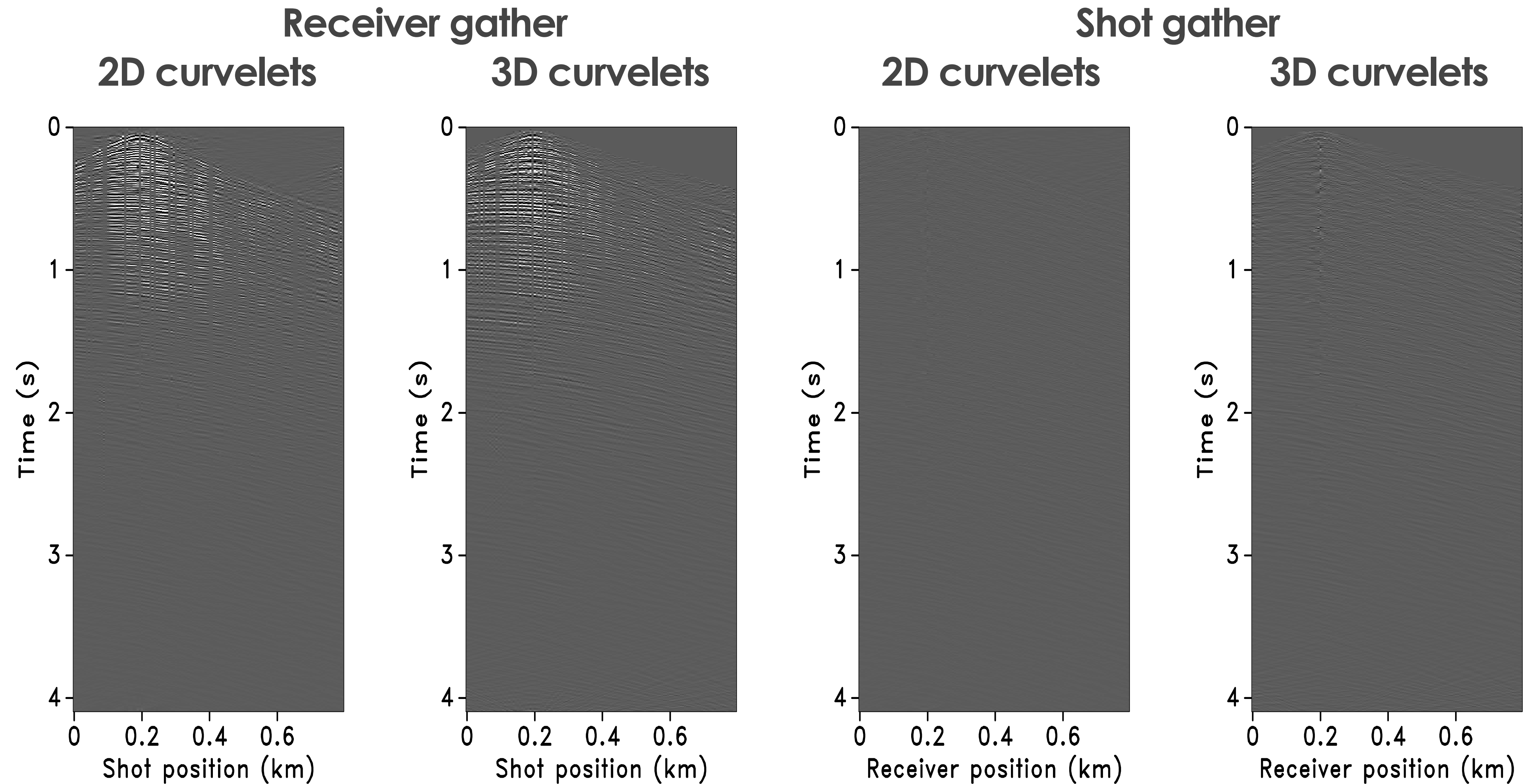
– 2D vs. 3D curvelets; subsampling factor = 2





# Residual

– 2D vs. 3D curvelets; subsampling factor = 4



# Summary (S/N (dB))

$$S/N(\mathbf{f}, \tilde{\mathbf{f}}) = -20 \log_{10} \frac{\|\mathbf{f} - \tilde{\mathbf{f}}\|_2}{\|\mathbf{f}\|_2}$$

	jittered to regular (m), subsampling ( $\eta$ )	recovery with 2D FDCT*	recovery with 3D FDCT*
1 source vessel (2 air-gun arrays)	50 to 12.5, 2	11.5	12.4
	50 to 6.25, 4	4.9	5.7

\* FDCT : Fast Discrete Curvelet Transform



## Economic performance indicators

Improved spatial-sampling ratio (ISSR):

$$\text{ISSR} = \frac{\text{number of shots recovered via sparsity-promoting inversion}}{\text{number of shots in simultaneous-source acquisition}}$$

for  $\eta = 2, 4$ , etc., gain in spatial sampling by the same factor

Survey-time ratio (STR): [Berkhout, 2008]

$$\text{STR} = \frac{\text{time of conventional acquisition}}{\text{time of simultaneous-source acquisition}}$$

for  $\eta = 2, 4$ , etc., reduction in survey time by  $\frac{1}{\eta}$

## Conclusions

Simultaneous-source **time-jittered marine** acquisition is an instance of compressive sensing

- **economic** acquisition with **reduced** environmental **imprint**

**Jittered (sub)sampling** shares the benefits of random sampling while offering control on maximum acquisition gap

3D FDCT slightly **improves** sparse recovery; however, its redundancy (about 24 x) renders large-scale processing extremely **memory intensive**, and hence **impractical**



# Chapter 5

Compressive time-lapse seismic acquisition

- distributed compressive sensing
- static acquisition geometry
- **on-the-grid** marine surveys
- % overlap => **exact** replication of shot positions

# Time-lapse seismic

## Current acquisition paradigm:

- repeat **expensive** dense acquisitions & “independent” processing
- compute differences between baseline & monitor survey(s)
- hampered by practical challenges to ensure repetition

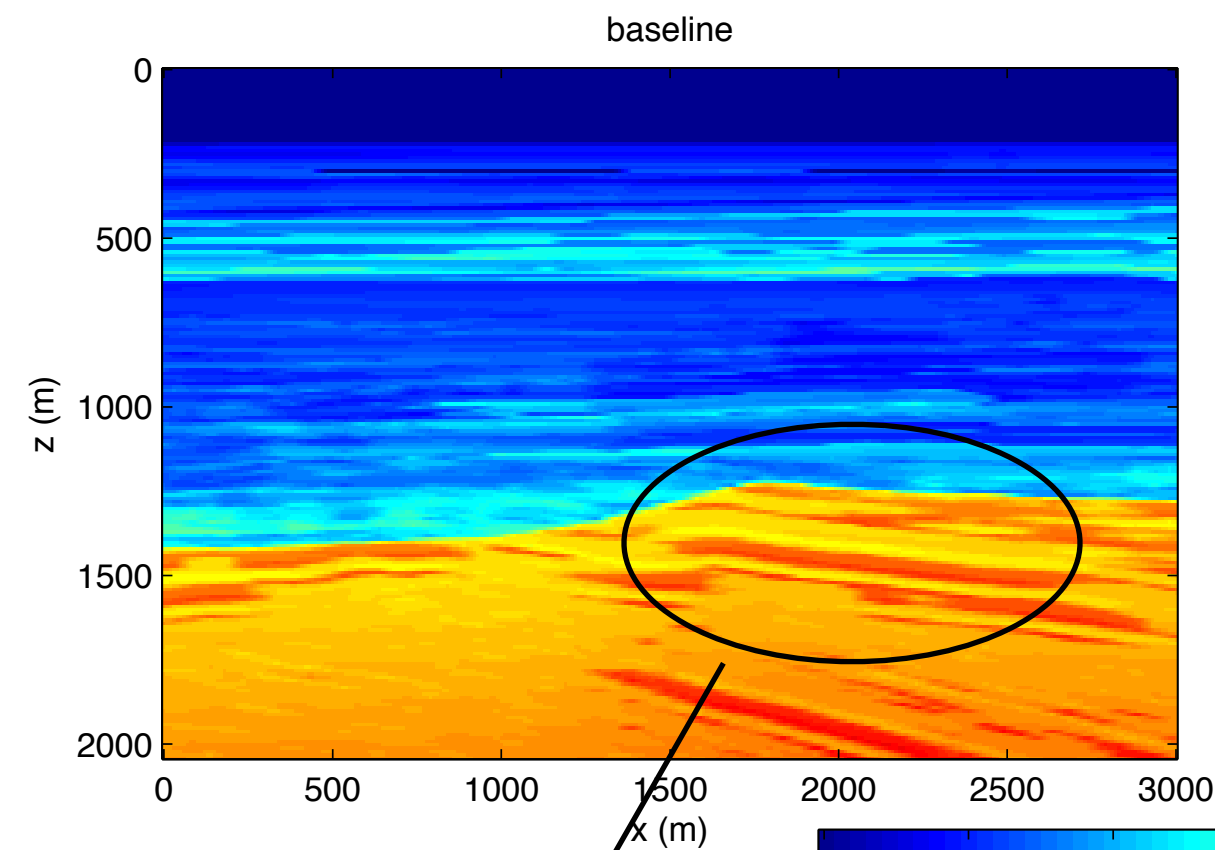
## New compressive sampling paradigm:

- **cheap** subsampled acquisition, e.g., via time-jittered marine subsampling
- offers possibility to relax insistence on replicability
- exploits insights from distributed compressive sensing

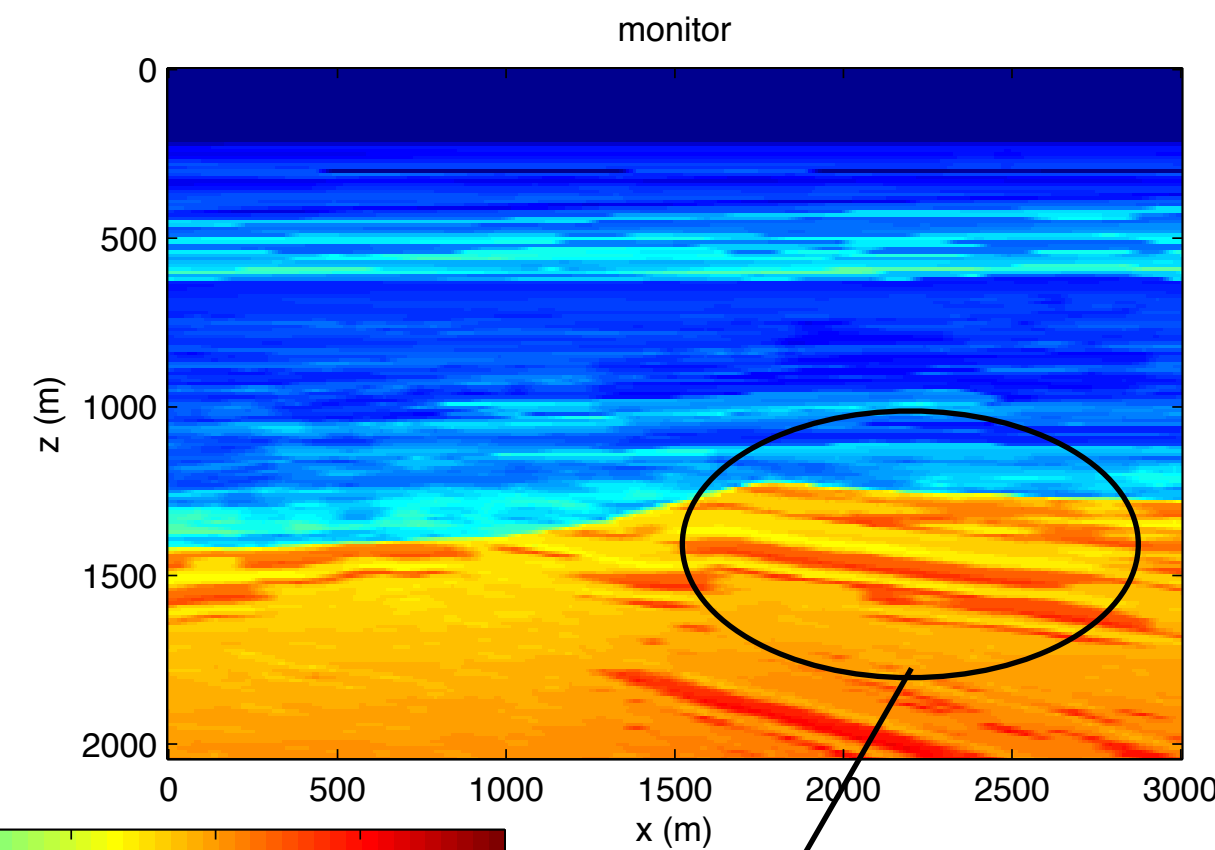


# Time-lapse model

Baseline Model

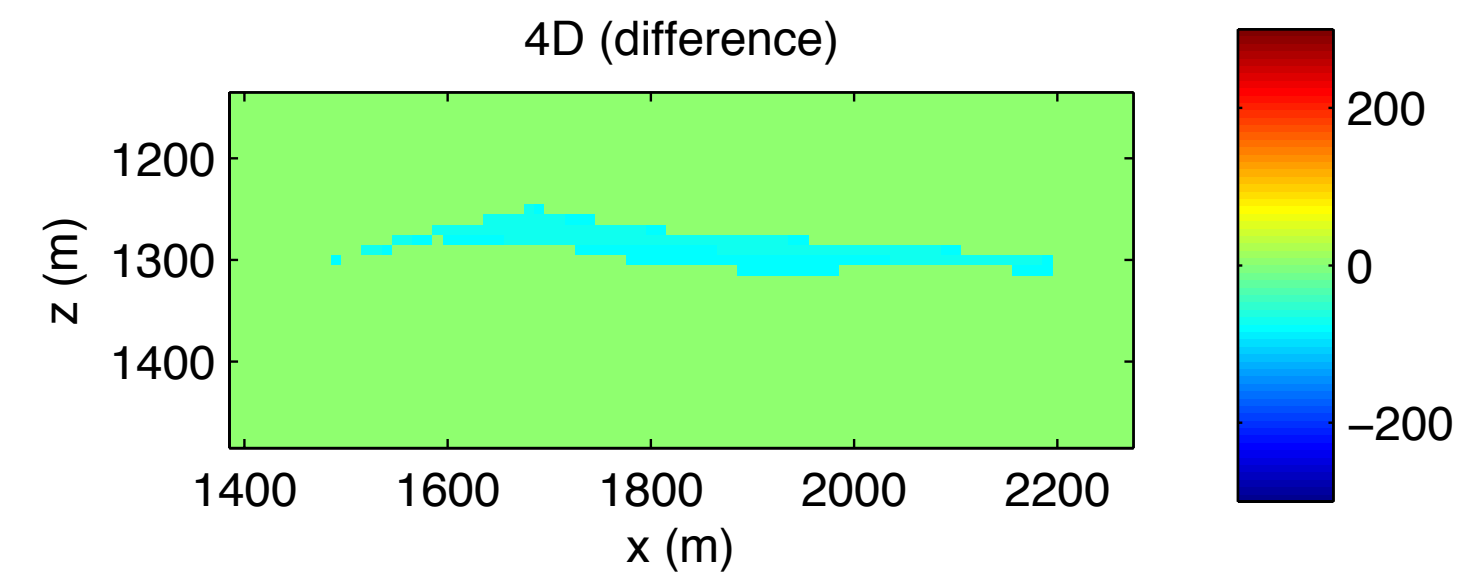
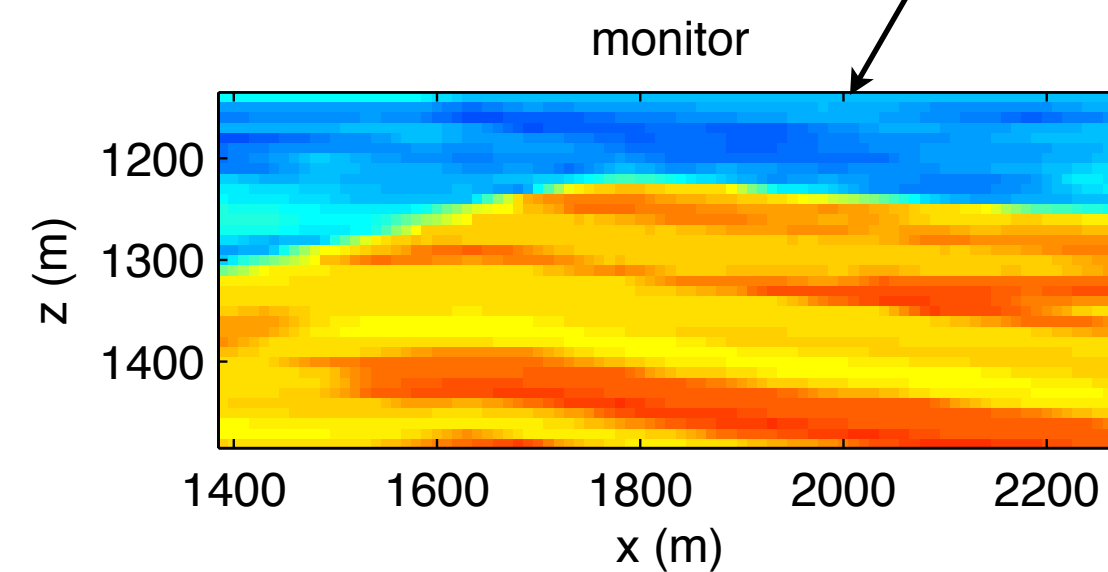
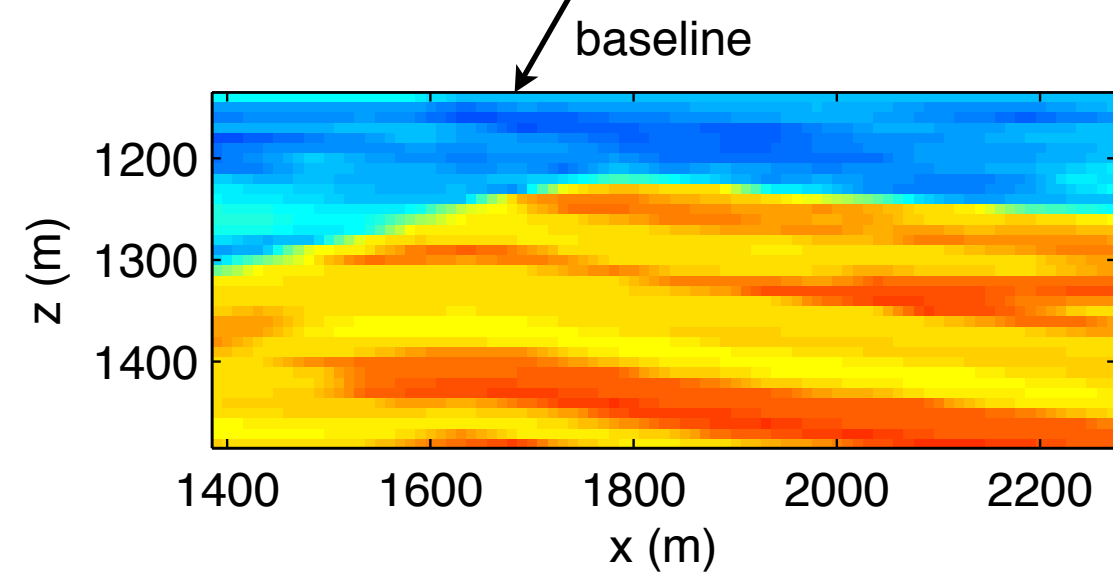


Monitor Model



## Method

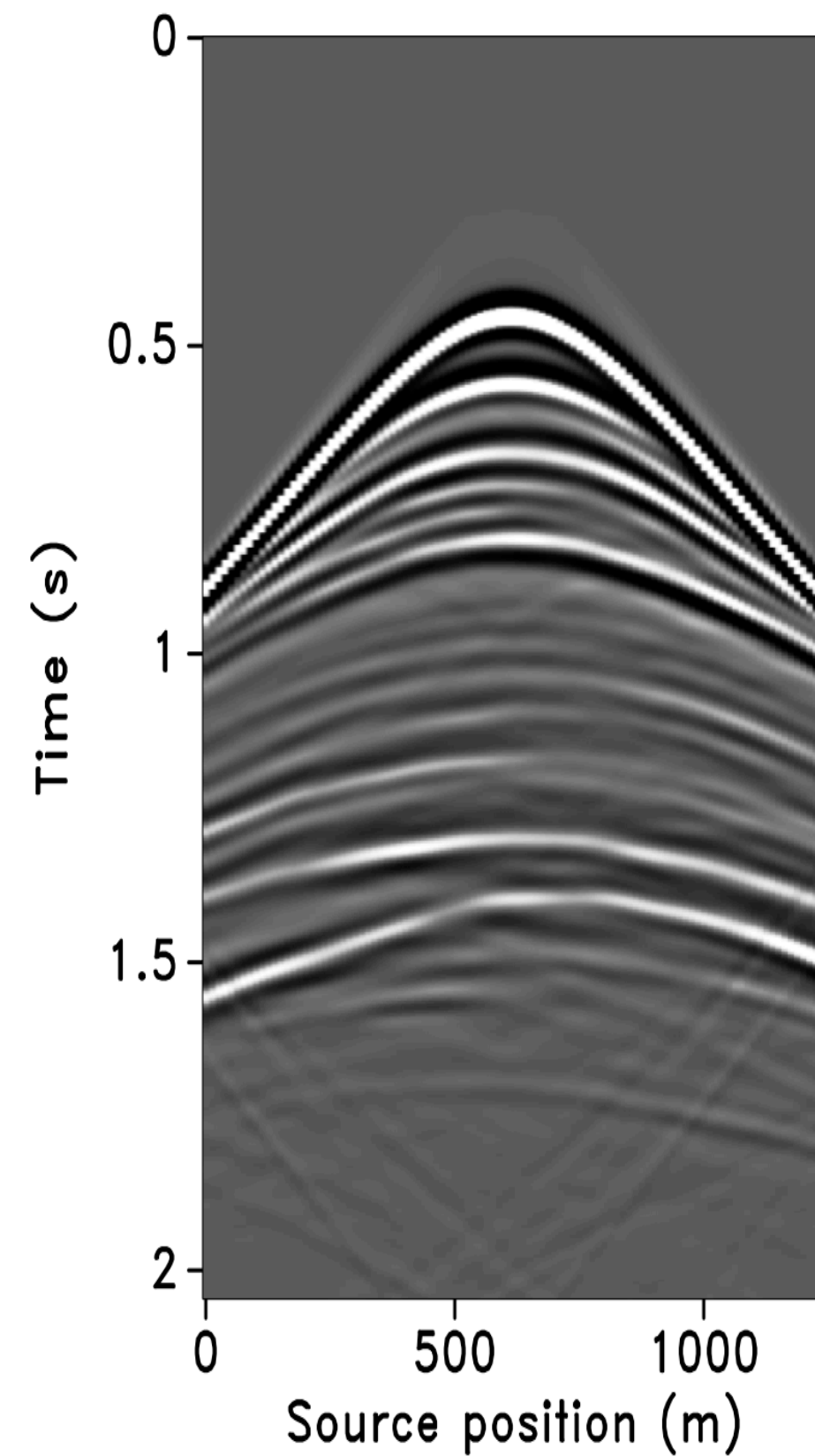
- ▶ Velocity and density model provided by BG Group, taken as baseline
- ▶ High permeability zone identified at a depth of  $\sim 1300$ m
- ▶ Fluid substitution (gas/oil replaced with brine) simulated to derive monitor velocity model
- ▶ Wavefield simulation to generate synthetic time-lapse data
- ▶ scales to 11733300 x 114882048



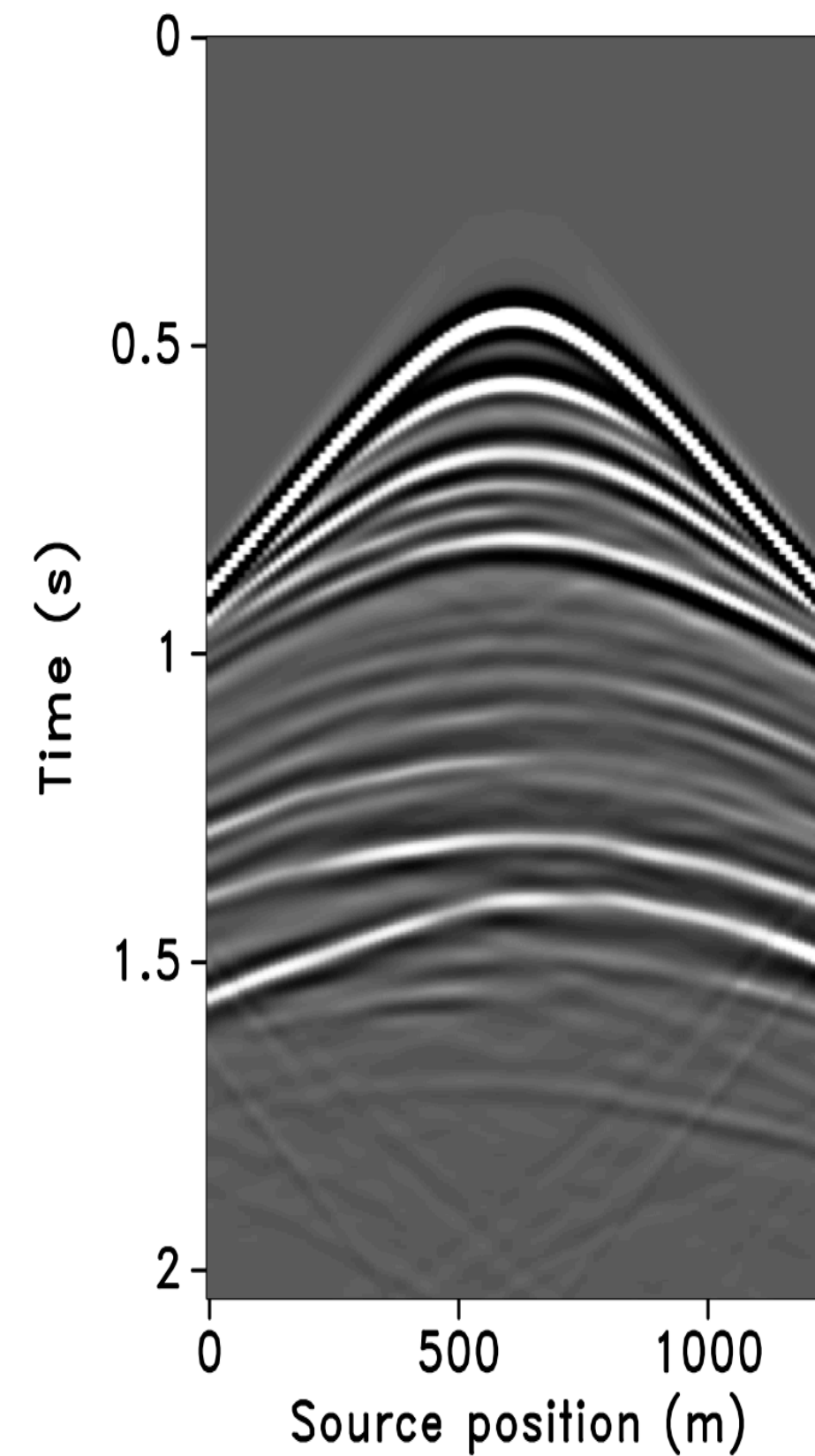
# Simulated time-lapse data

– time-domain finite differences

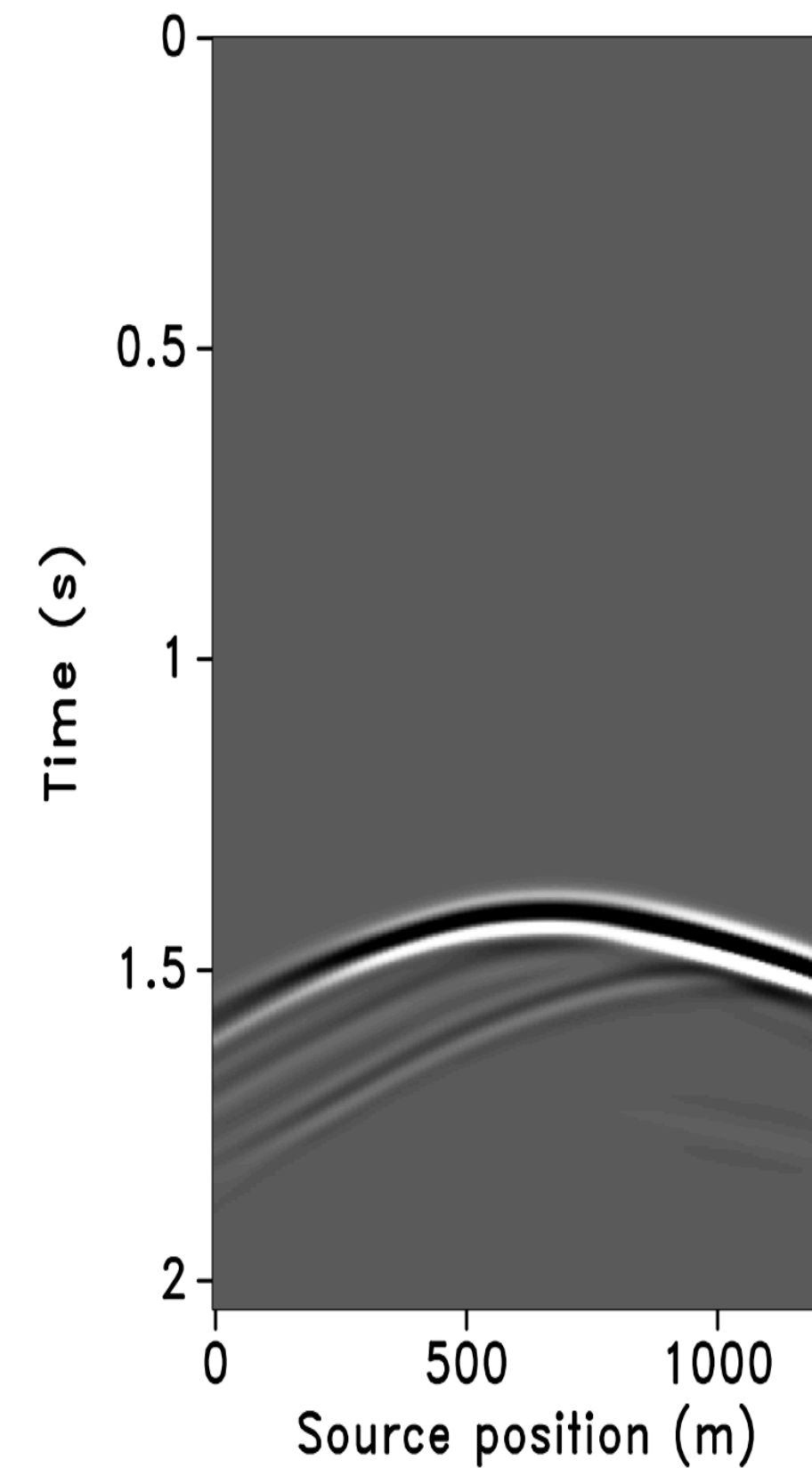
## Baseline



## Monitor

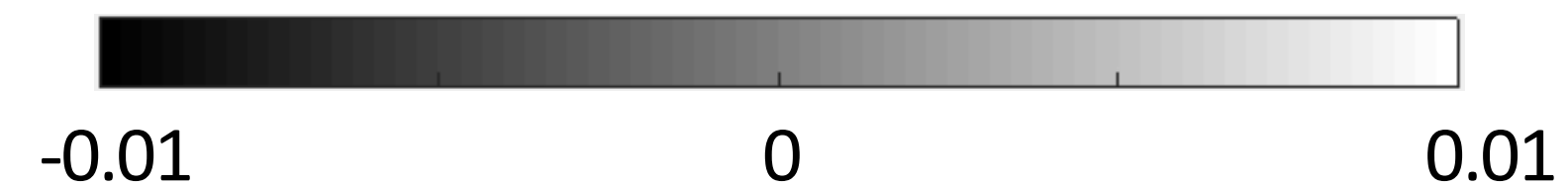
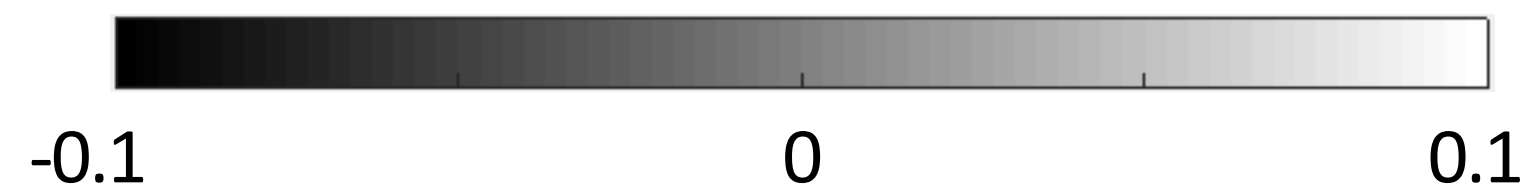


## 4D signal



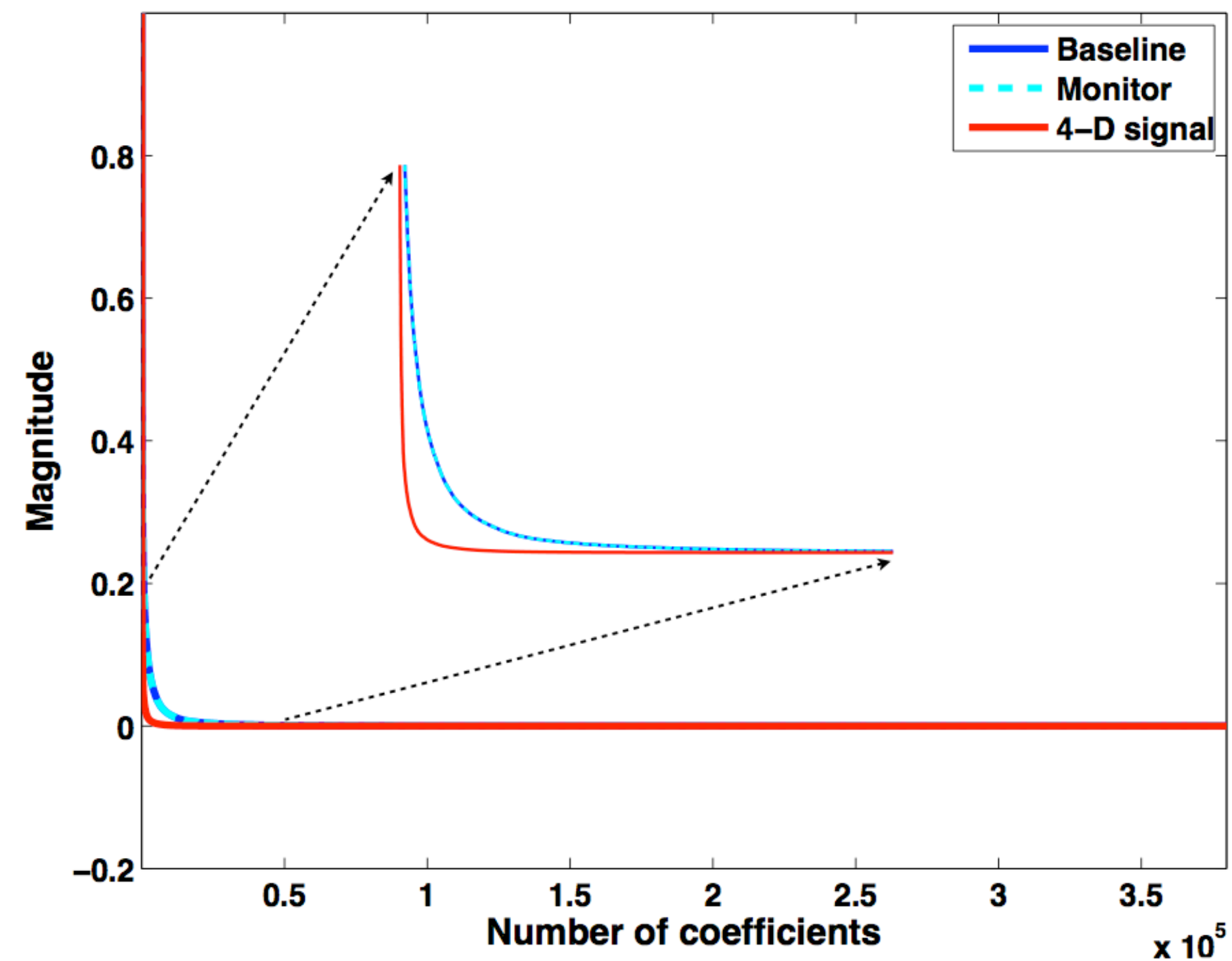
time samples: **512**  
receivers: **100**  
sources: **100**

sampling  
time: **4.0 ms**  
receiver: **12.5 m**  
source: **12.5 m**

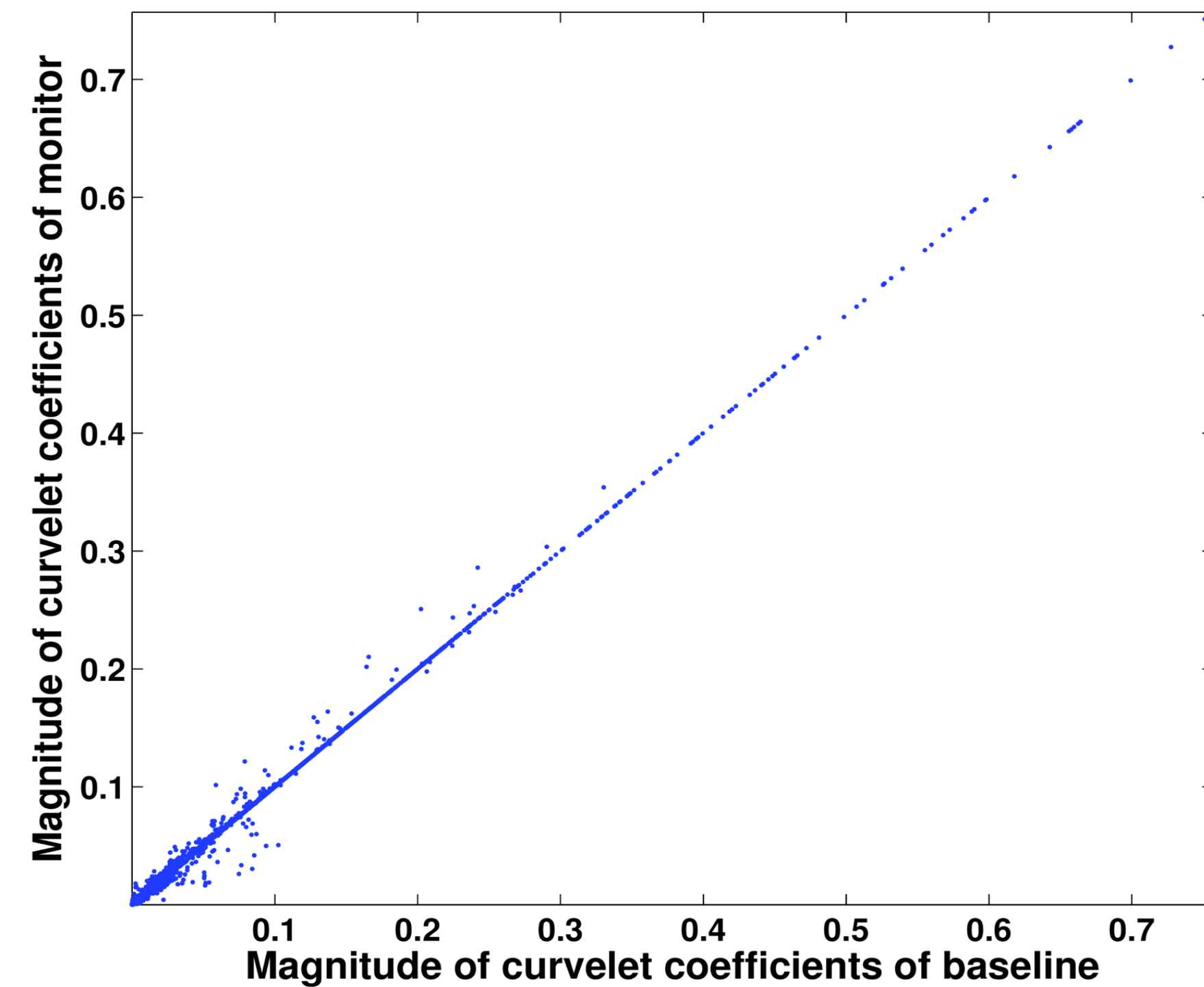




# Sparse structure via curvelets



**significant** correlation between the vintages



# Distributed compressive sensing

– joint recovery model (JRM)

$$\overbrace{\begin{bmatrix} \mathbf{A}_1 & \mathbf{A}_1 & \mathbf{0} \\ \mathbf{A}_2 & \mathbf{0} & \mathbf{A}_2 \end{bmatrix}}^{\mathbf{A}} \overbrace{\begin{bmatrix} \mathbf{z}_0 \\ \mathbf{z}_1 \\ \mathbf{z}_2 \end{bmatrix}}^{\mathbf{z}} = \overbrace{\begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \end{bmatrix}}^{\mathbf{b}} \begin{matrix} \nearrow \text{baseline} \\ \searrow \text{monitor} \end{matrix}$$

vintages

$$\begin{matrix} \downarrow \\ \mathbf{x}_1 = \mathbf{z}_0 + \mathbf{z}_1 \\ \mathbf{x}_2 = \mathbf{z}_0 + \mathbf{z}_2 \end{matrix} \begin{matrix} \nearrow \\ \nearrow \end{matrix} \text{differences}$$

common component

- different vintages share common information
- common component observed by all surveys
- invert for common component & vintages w.r.t. common component with sparse recovery

# Time-lapse seismic

## – with & without replication

In an **ideal** world ( $\mathbf{A}_1 = \mathbf{A}_2$ )

- JRM simplifies to  $(\mathbf{b}_2 - \mathbf{b}_1) = \mathbf{A}_1(\mathbf{x}_2 - \mathbf{x}_1)$
- expect good recovery when difference is sparse
- but relies on “exact” replicability of surveys...

In the **real** world ( $\mathbf{A}_1 \neq \mathbf{A}_2$ )

- no absolute control on surveys
- deviations in shot/receiver positions
- noise...



# Synthetic seismic case study

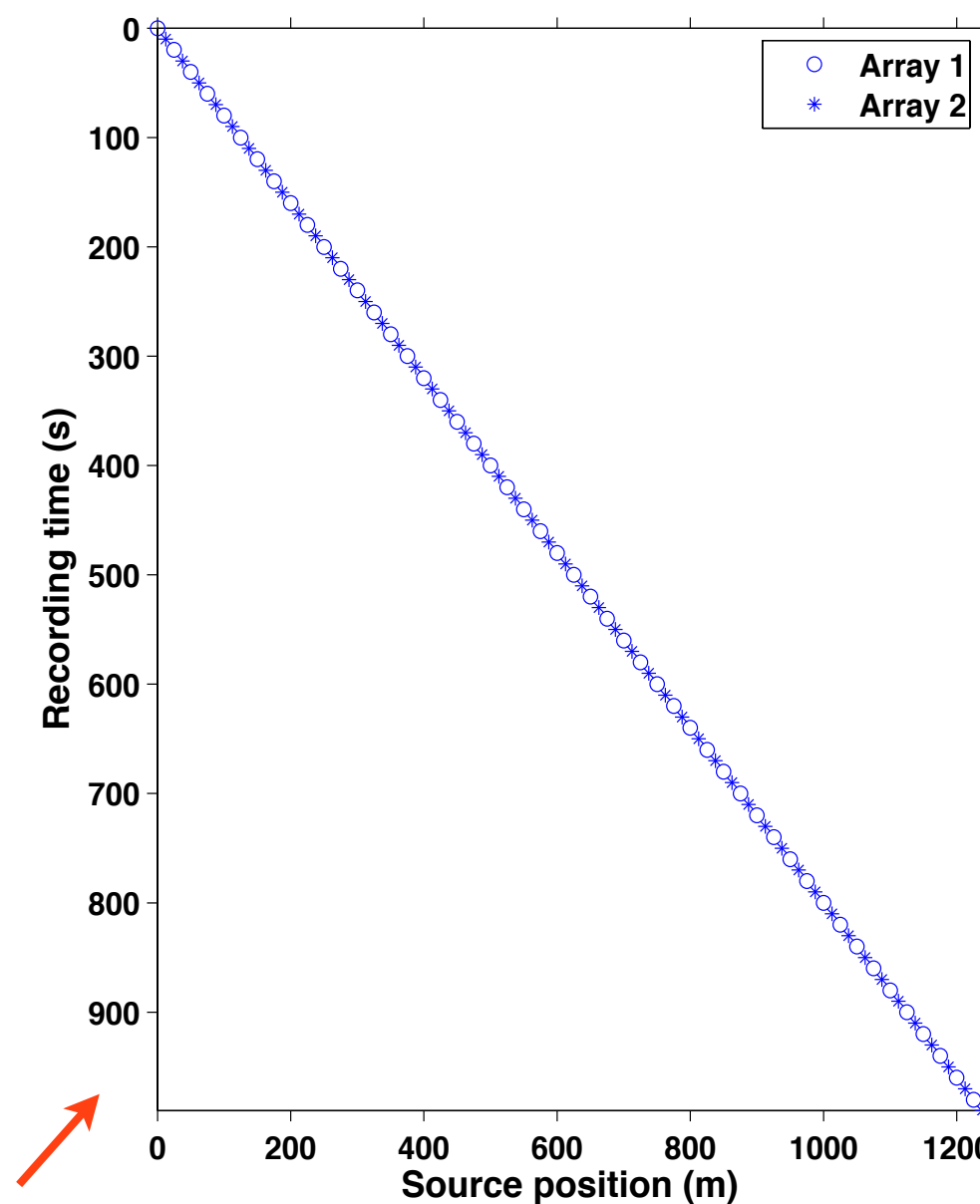
Time-jittered marine acquisition **on the grid**

- % overlap => **exact** replication of shot positions

# Conventional vs. time-jittered sources

– subsampling factor = 2 (2 source arrays)

conventional



## conventional shot gathers

number of shots = **100** (per array)

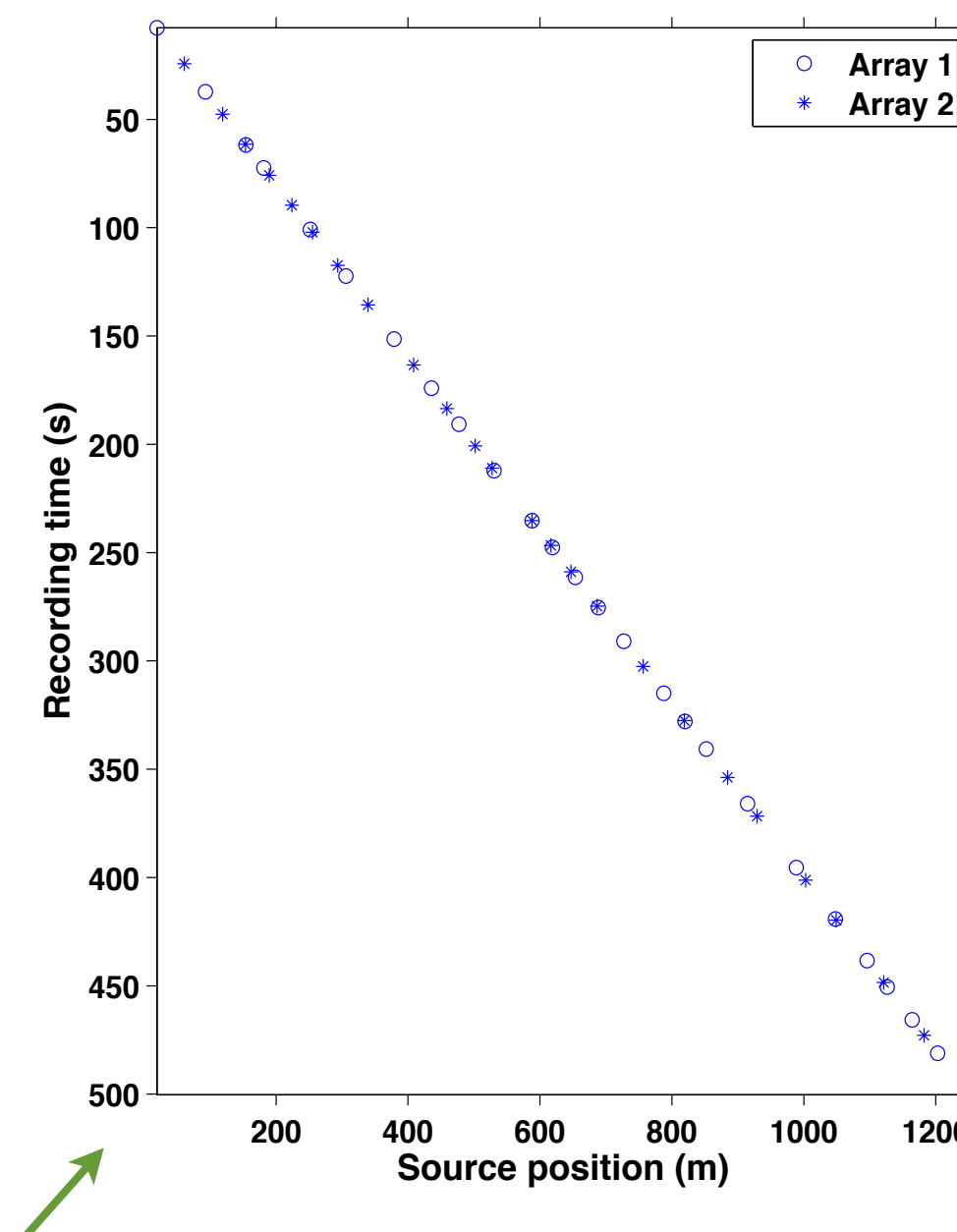
shot record length: 10.0 s

spatial sampling: **12.5 m**

vessel speed: **1.25 m/s**

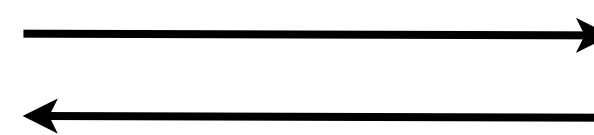
recording time =  $100 \times 10.0 = \mathbf{1000.0\ s}$

jittered acquisition 1  
(baseline)



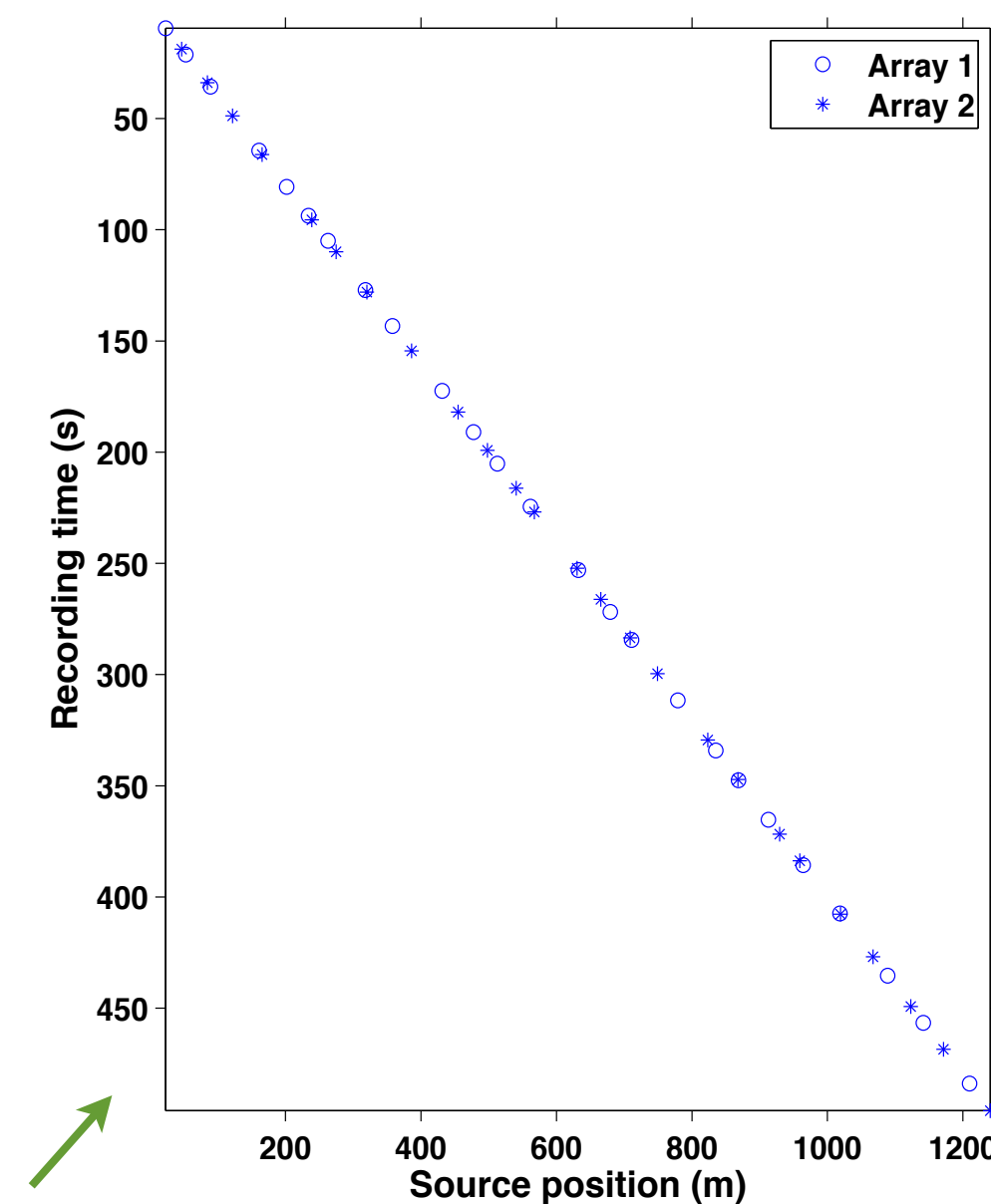
## [MIXING & SUBSAMPLING]

spatial subsampling factor = 2



increase in spatial sampling factor = 2  
[SOURCE SEPARATION & INTERPOLATION]

jittered acquisition 2  
(monitor)



## simultaneous shot gathers

number of shots =  $100/2 = \mathbf{50}$  (25 per array)

spatial sampling: **50.0 m (jittered)**

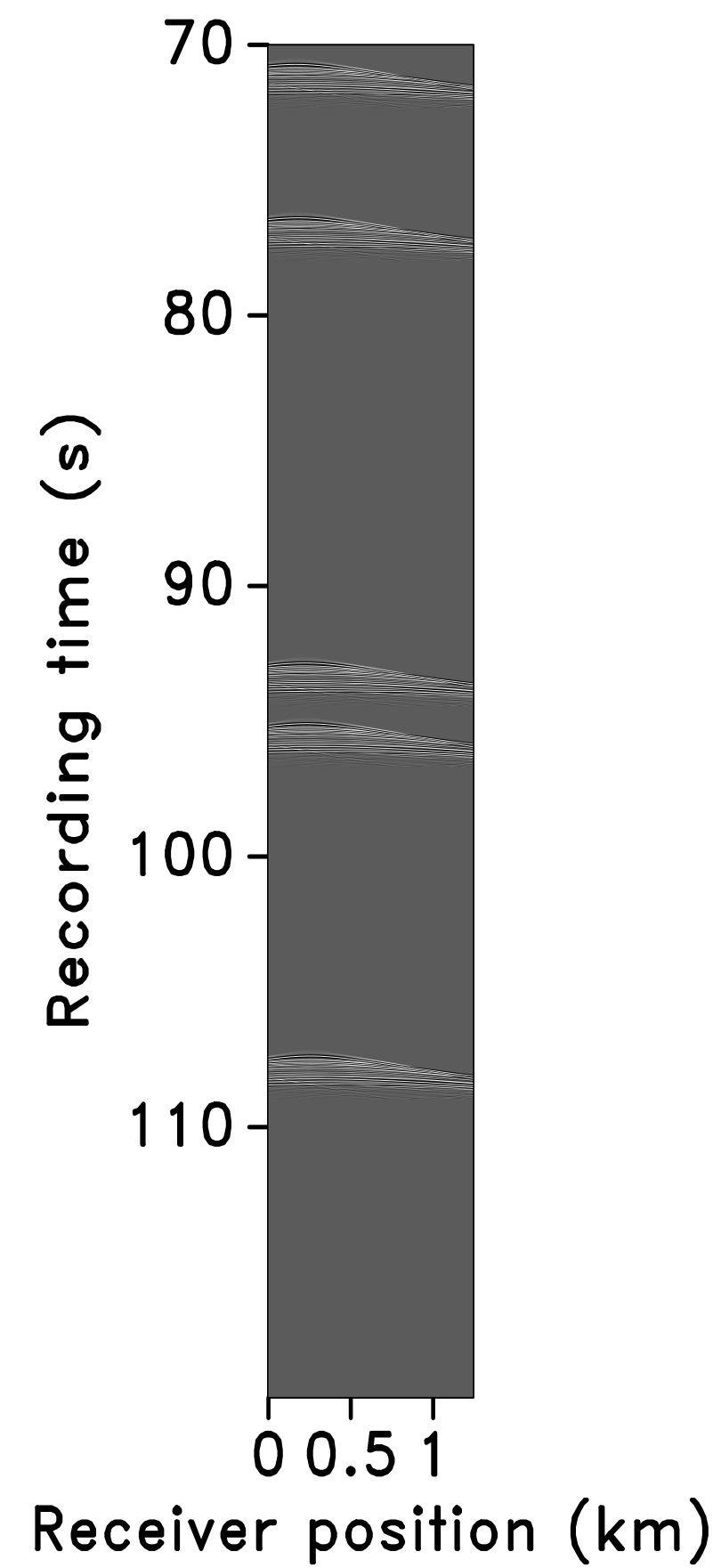
vessel speed: **2.50 m/s**

recording time  $\approx 1000.0\ s/2 = \mathbf{500.0\ s}$

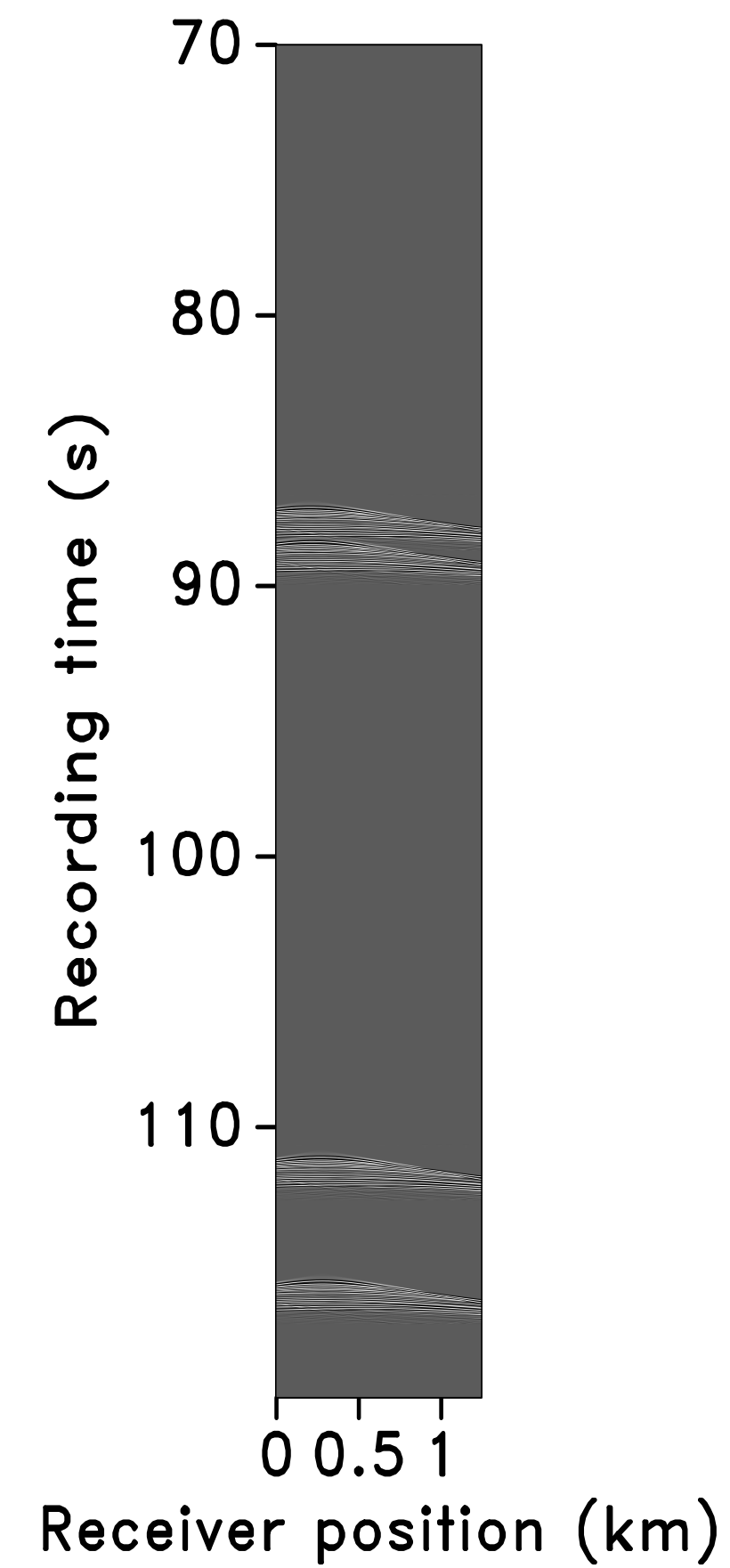
# Measurements

– subsampled and overlapping shots

## Baseline



## Monitor



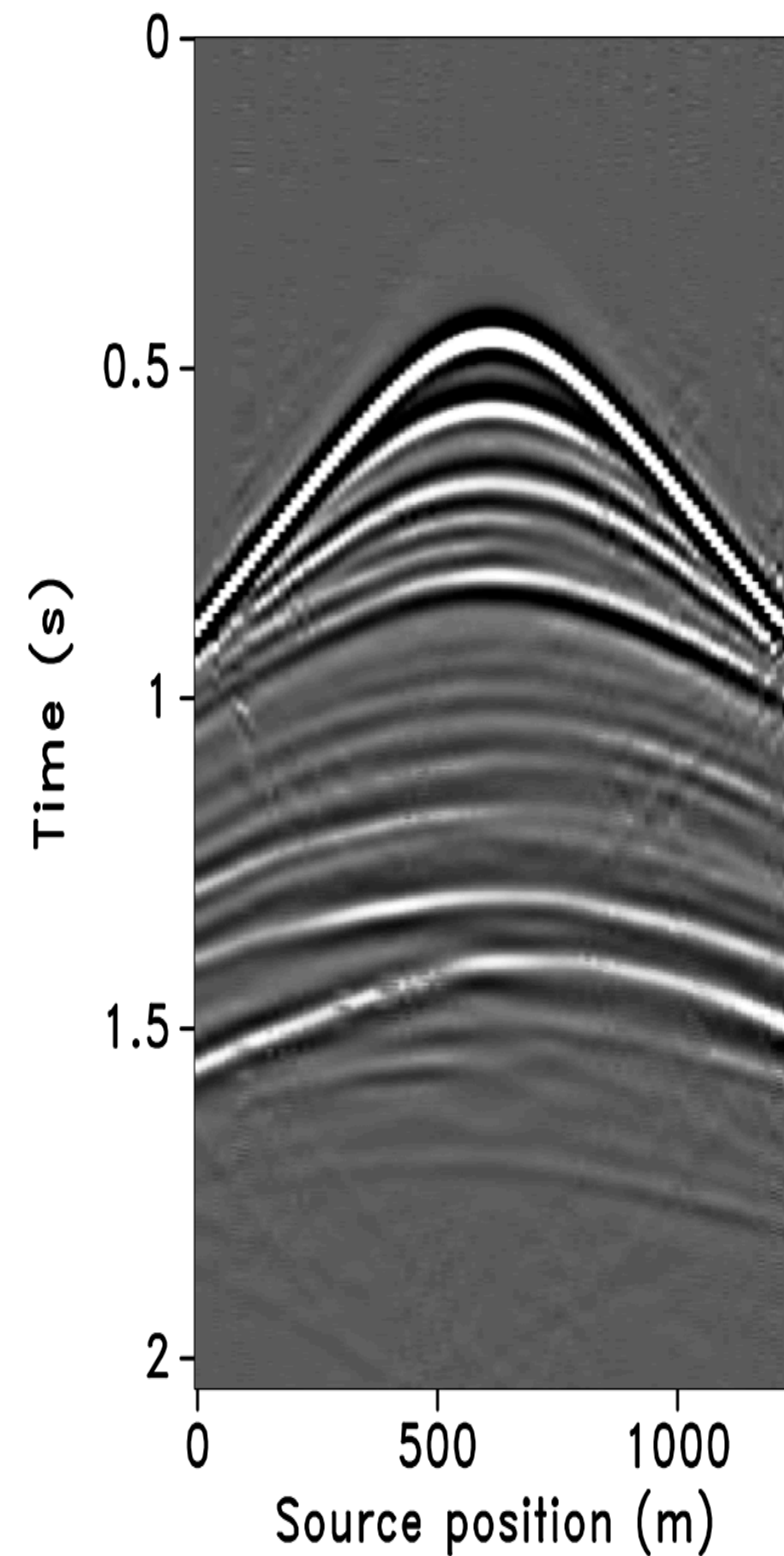


# Monitor recovery

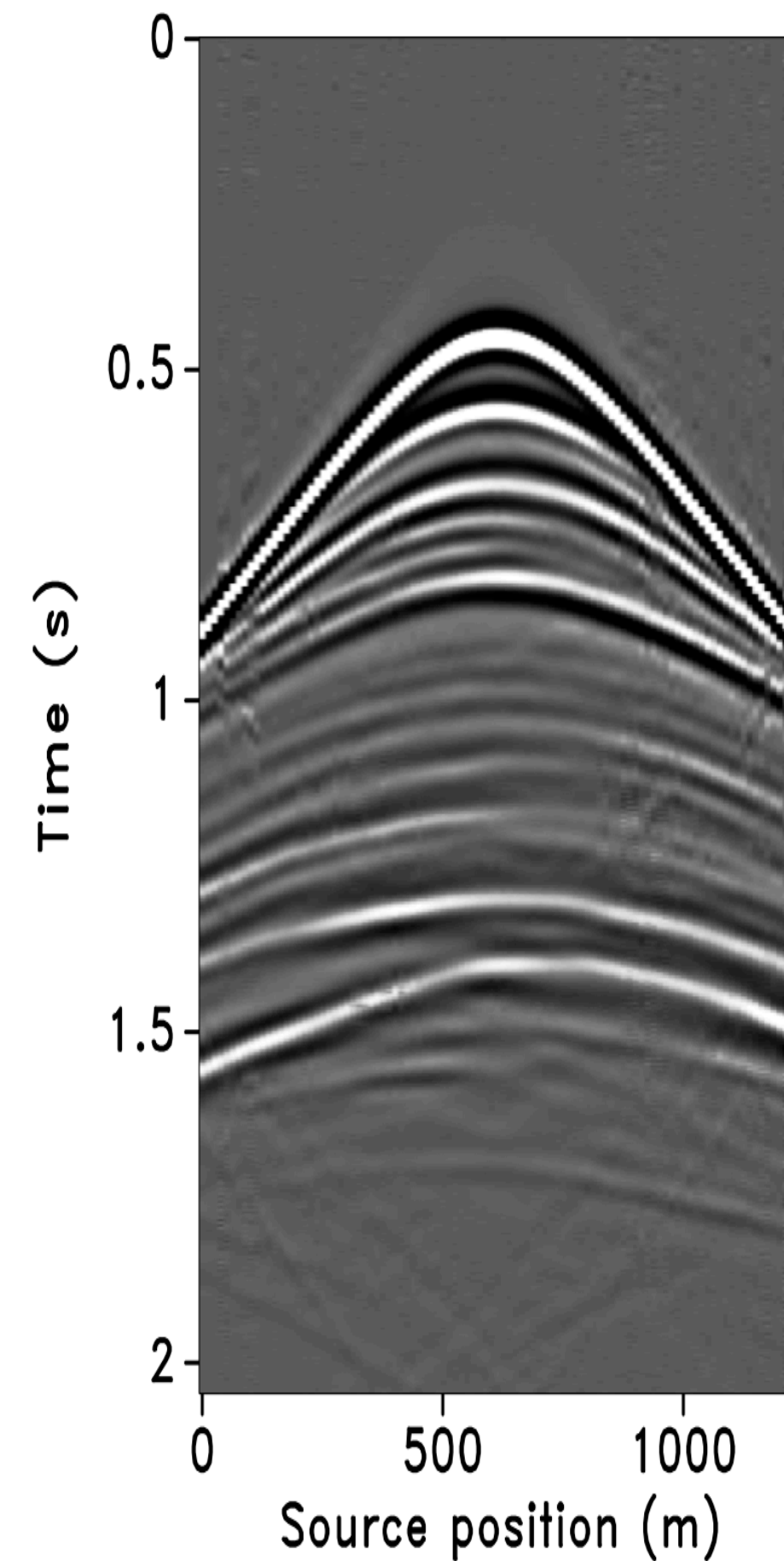
- Independent recovery

“on-the-grid” sampling  
% overlap  $\Rightarrow$  “exact” replication of shot positions

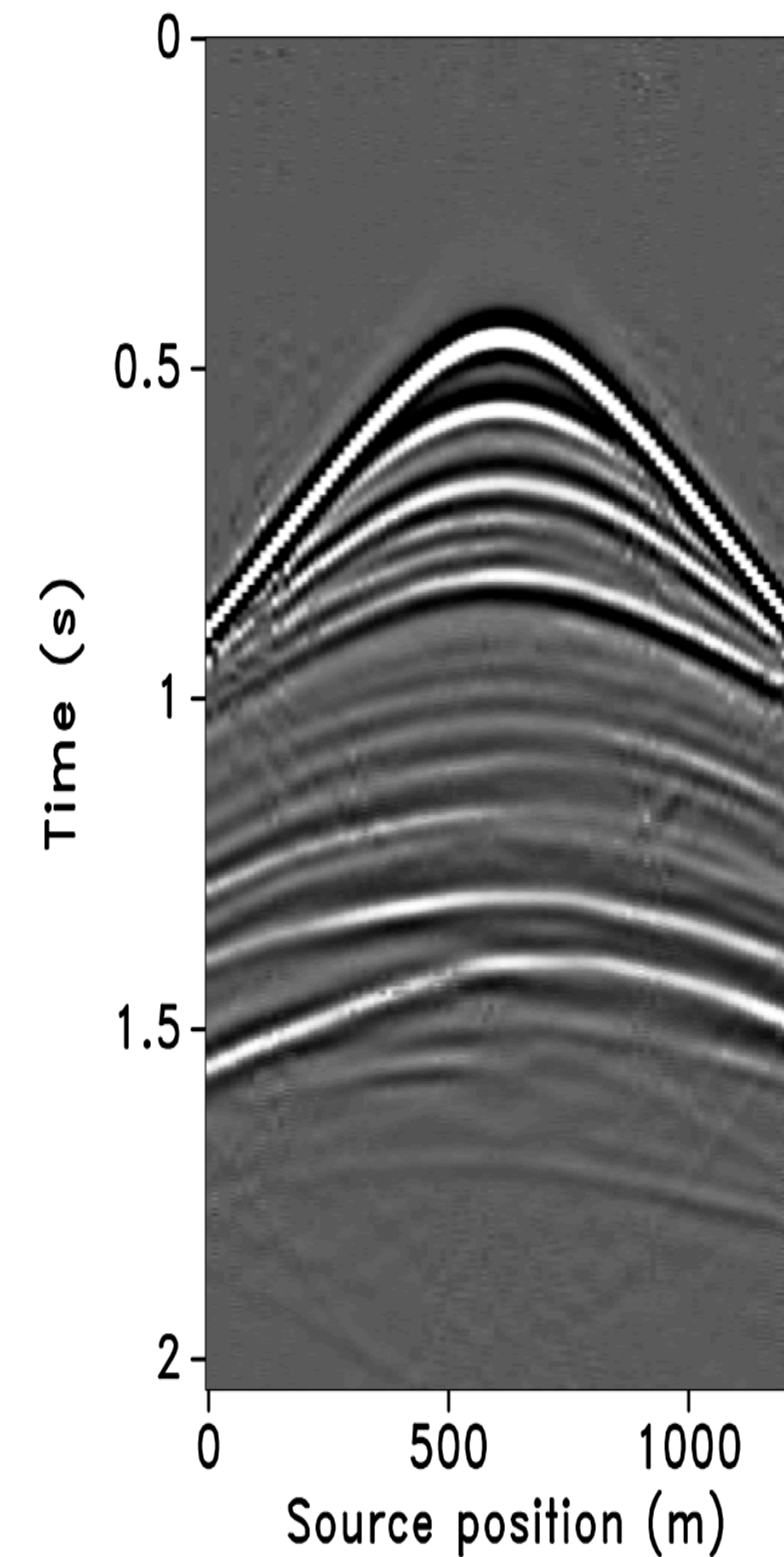
100% overlap  
[11.6 dB]



50% overlap  
[11.0 dB]



25% overlap  
[10.3 dB]



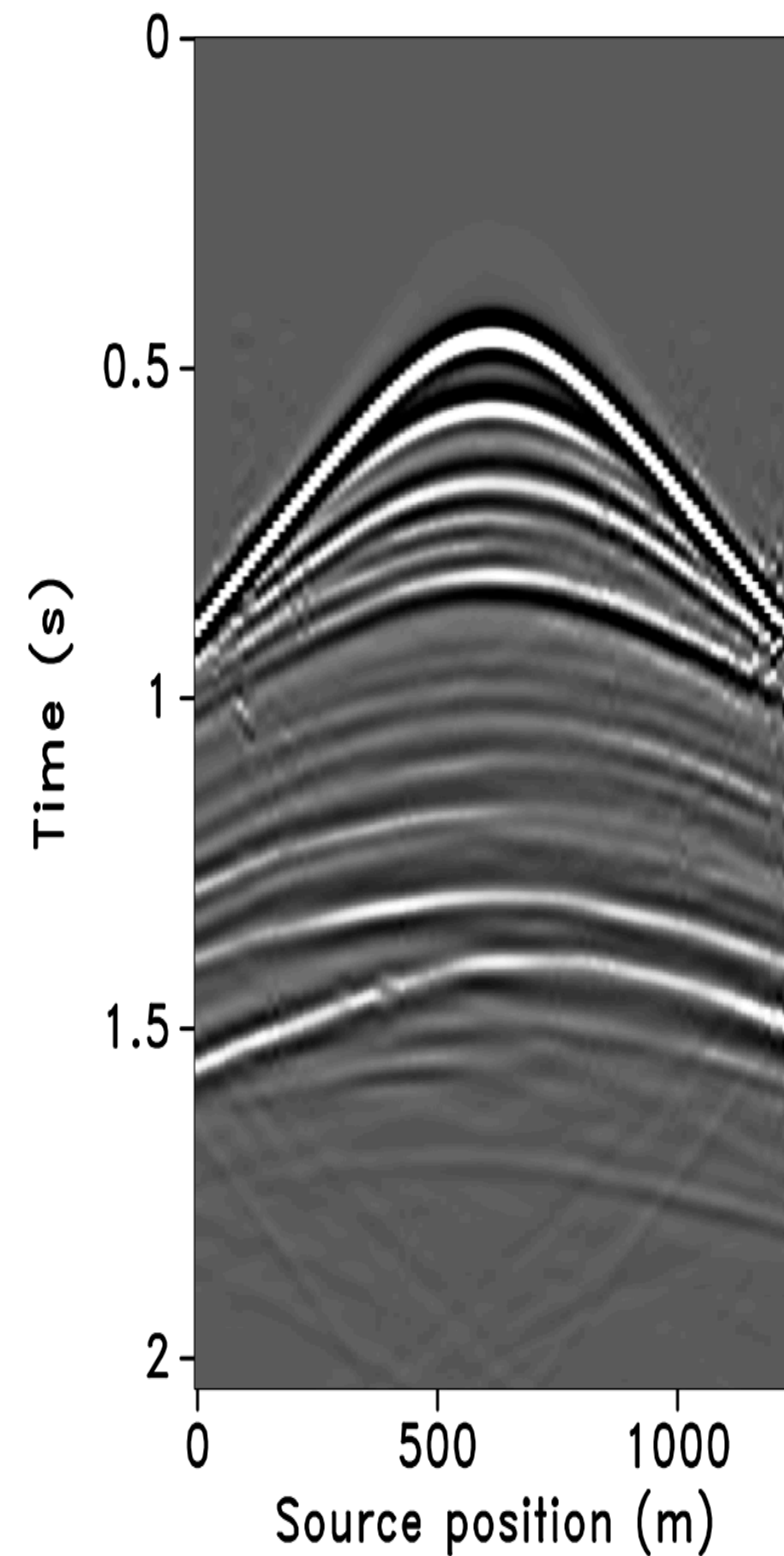


# Monitor recovery

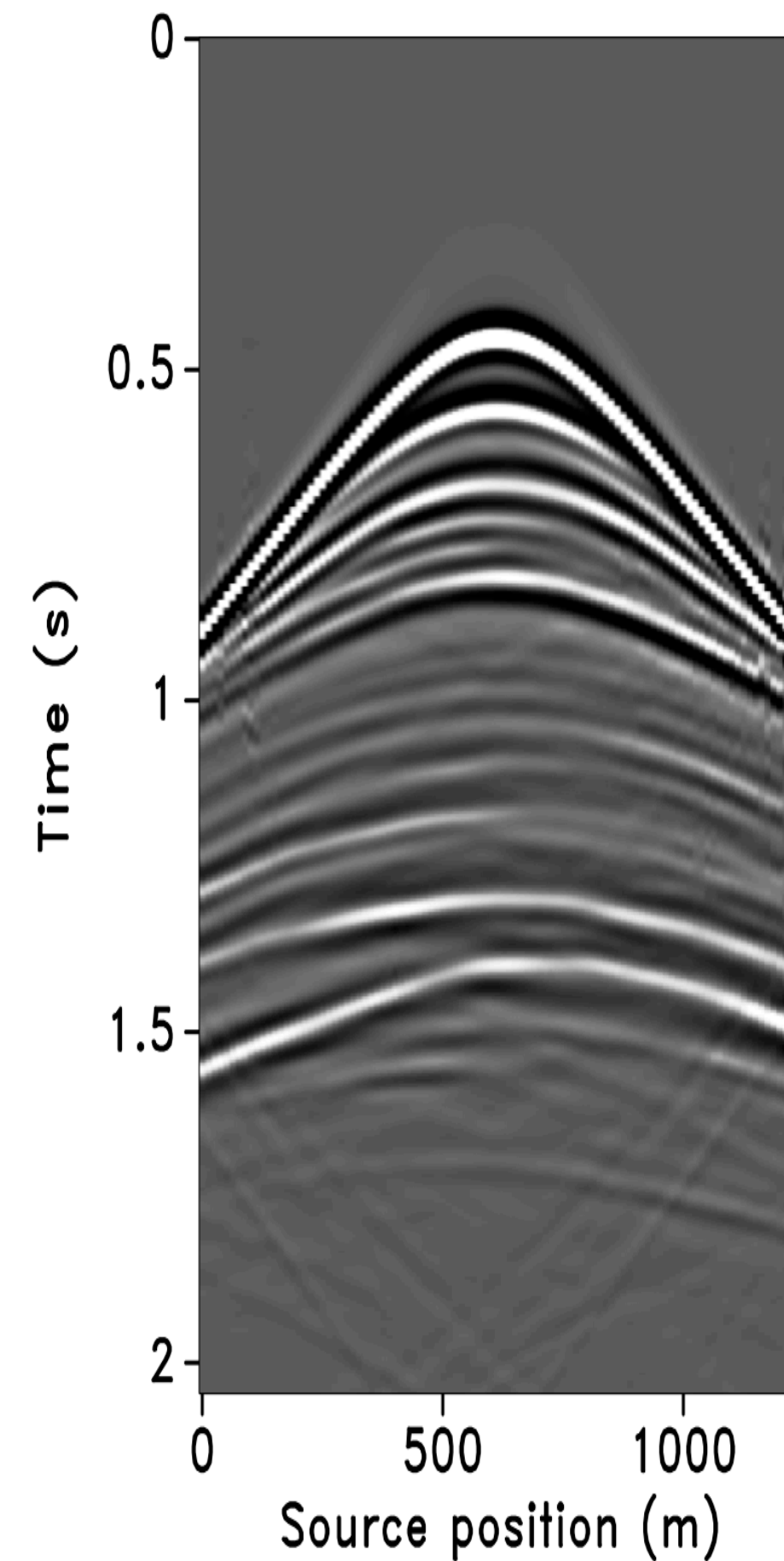
- Joint recovery

“on-the-grid” sampling  
% overlap  $\Rightarrow$  “exact” replication of shot positions

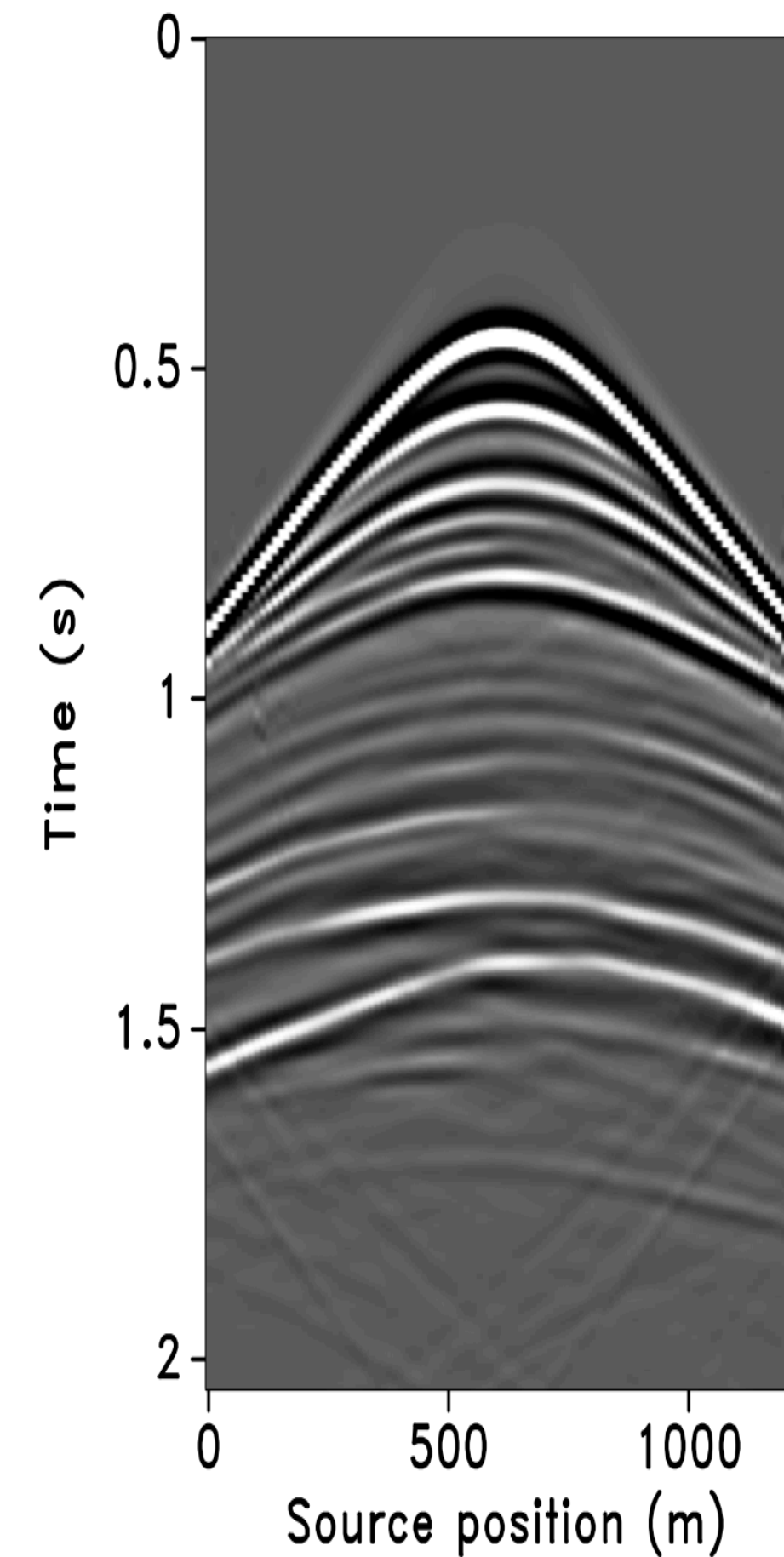
100% overlap  
[11.6 dB]



50% overlap  
[15.7 dB]



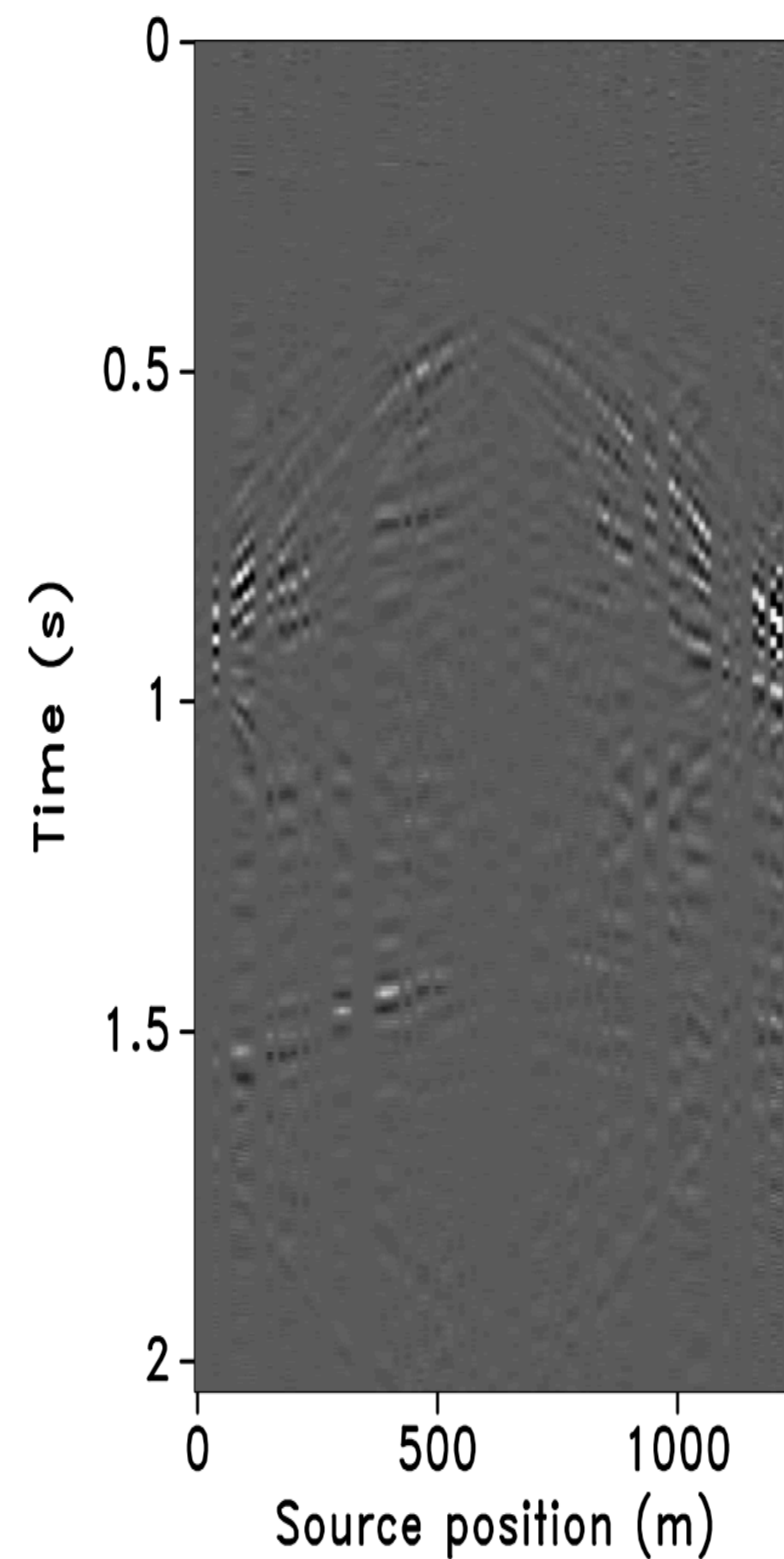
25% overlap  
[18.6 dB]



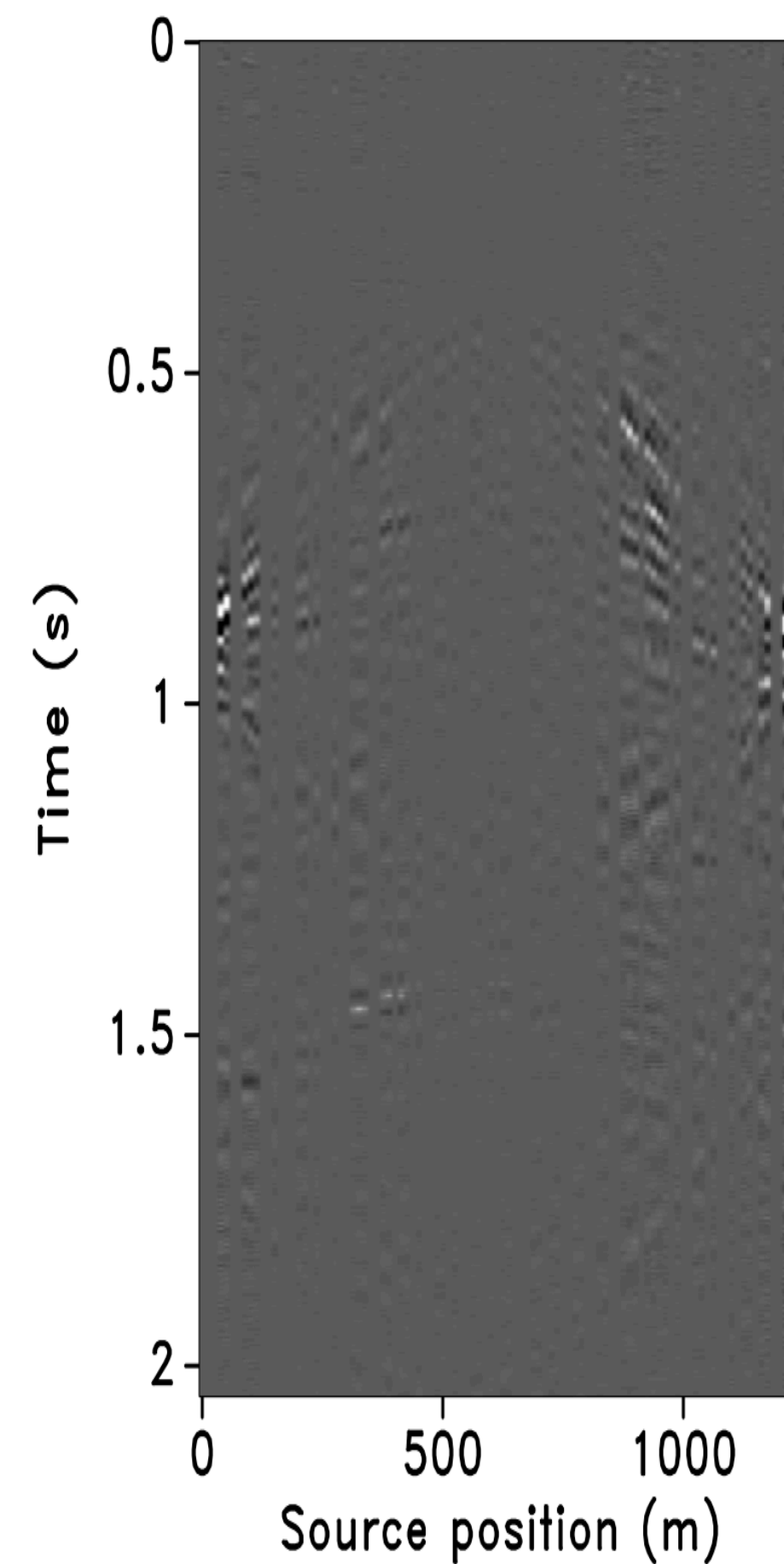
# Monitor residual

- Independent residual

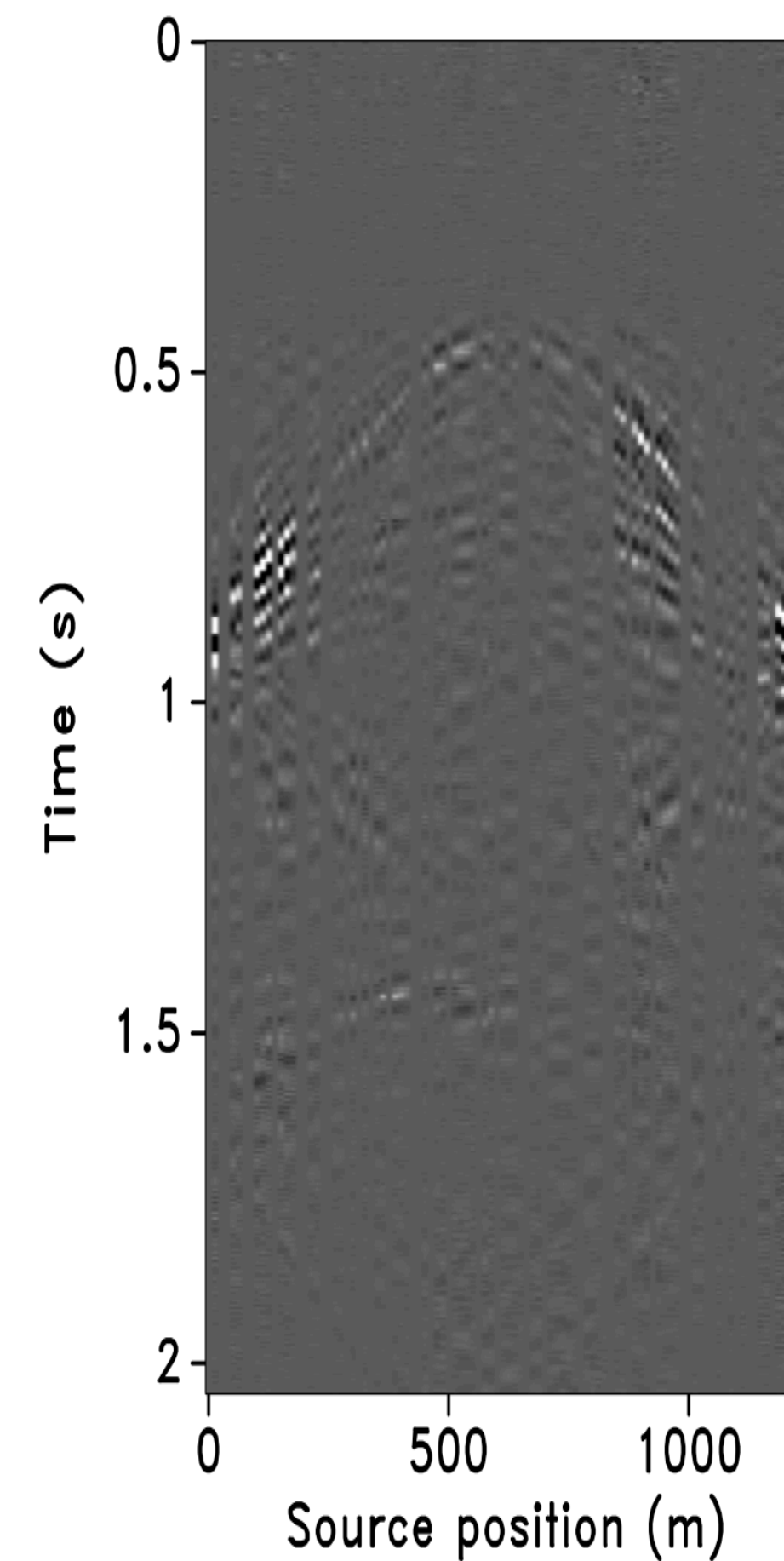
100% overlap  
[11.6 dB]



50% overlap  
[11.0 dB]



25% overlap  
[10.3 dB]

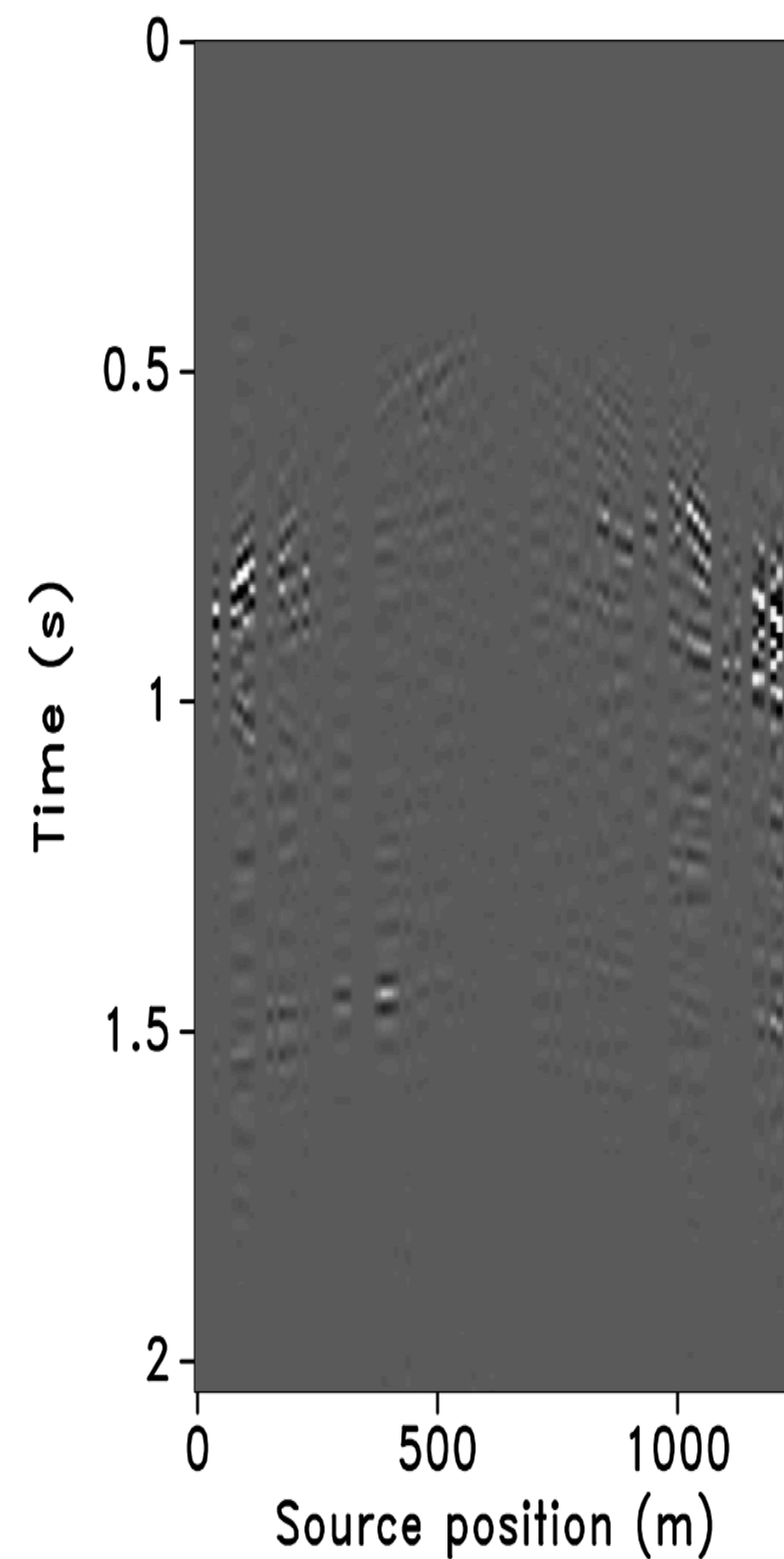




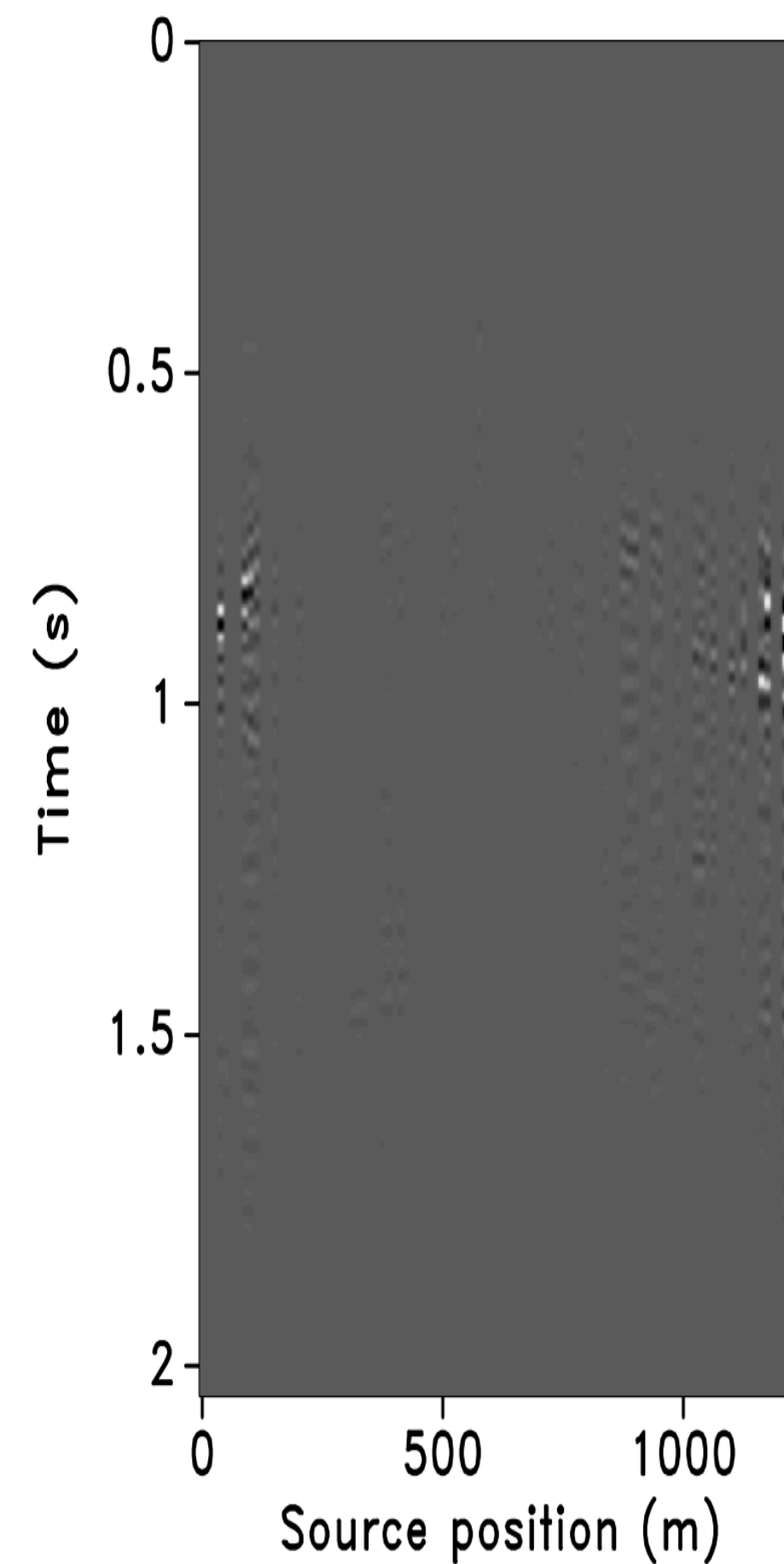
# Monitor residual

## – Joint residual

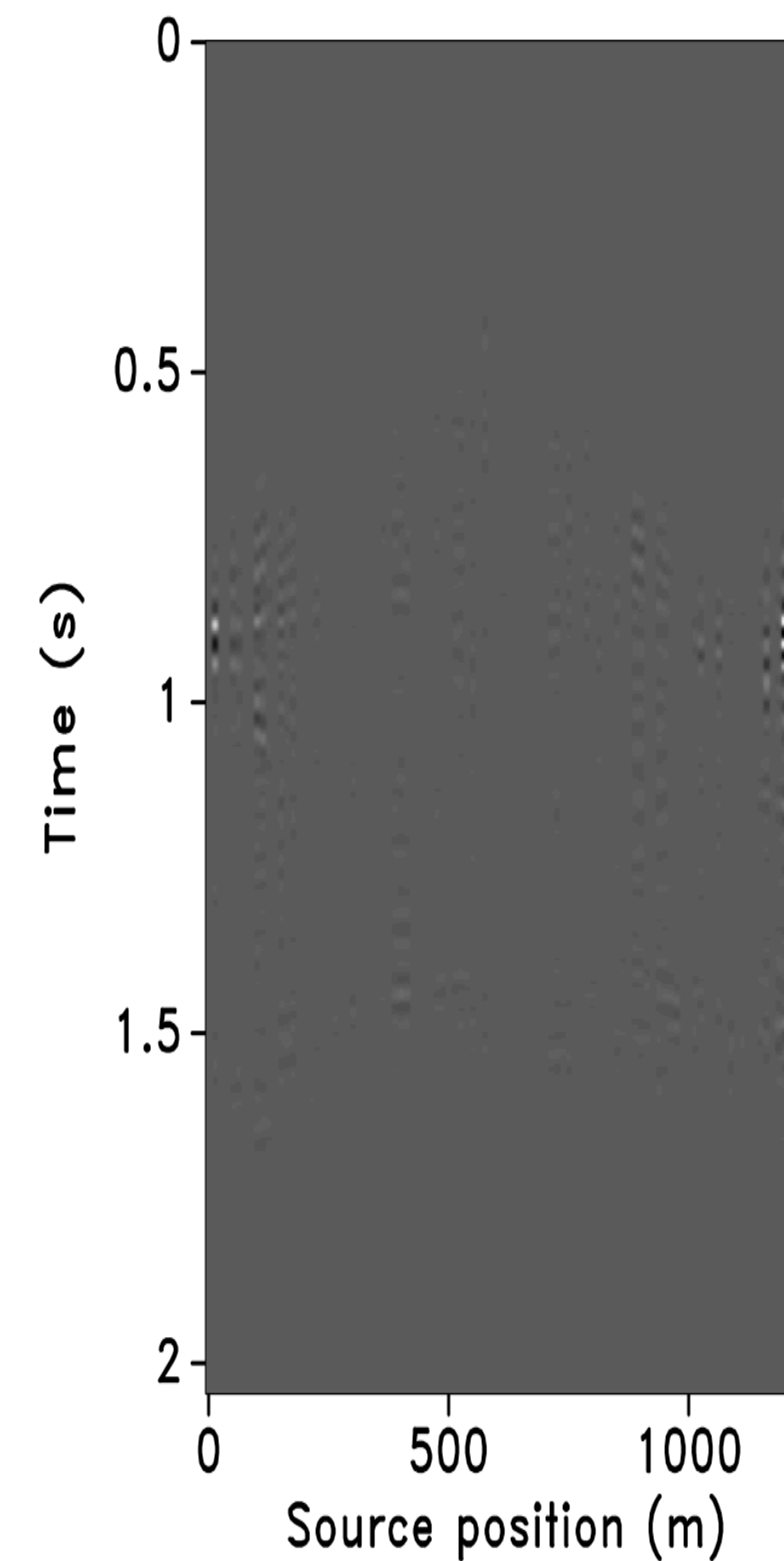
100% overlap  
[11.6 dB]



50% overlap  
[15.7 dB]



25% overlap  
[18.6 dB]



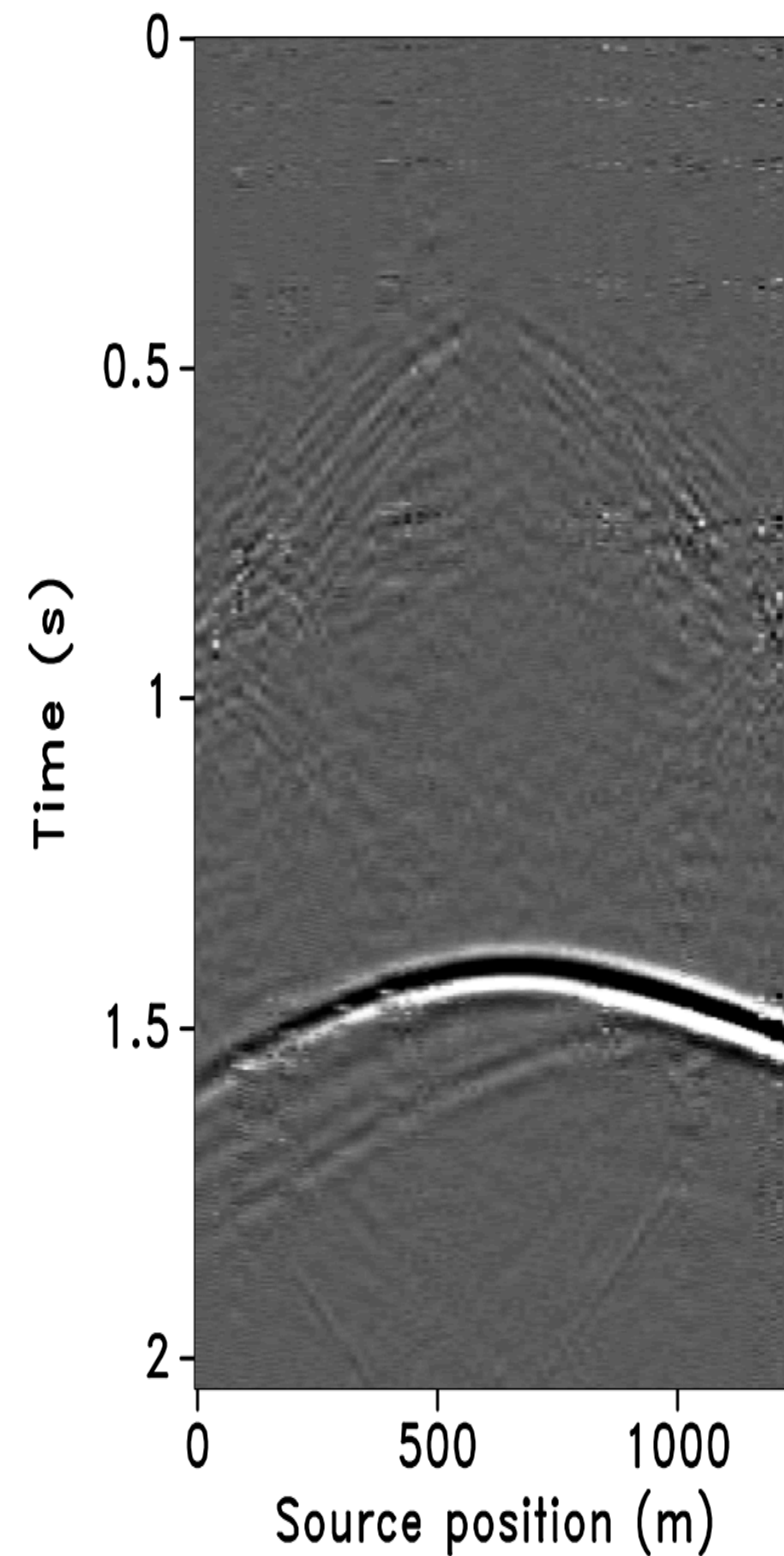


# 4D recovery

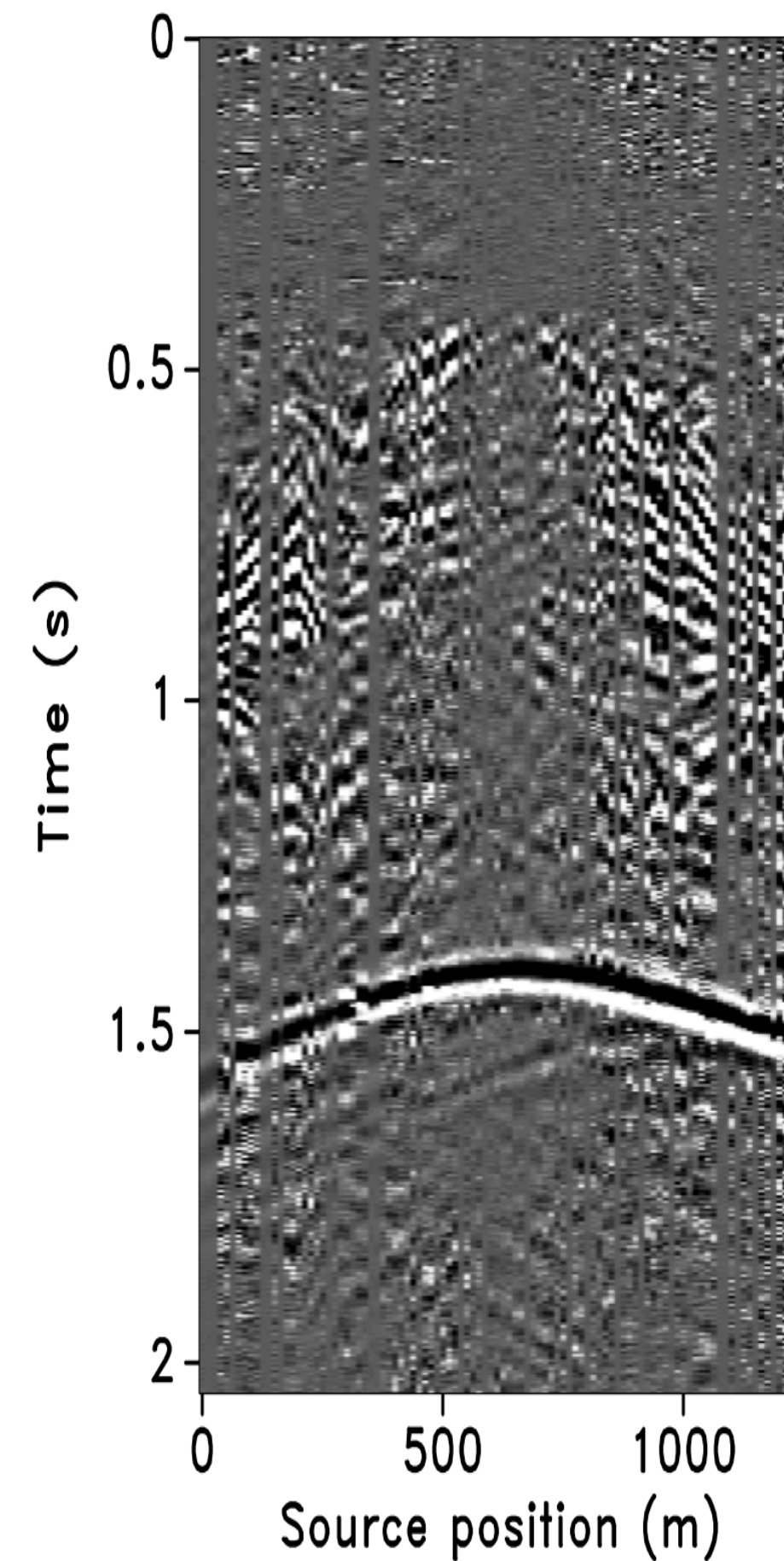
## – Independent recovery

[colormap scale: 10 X]

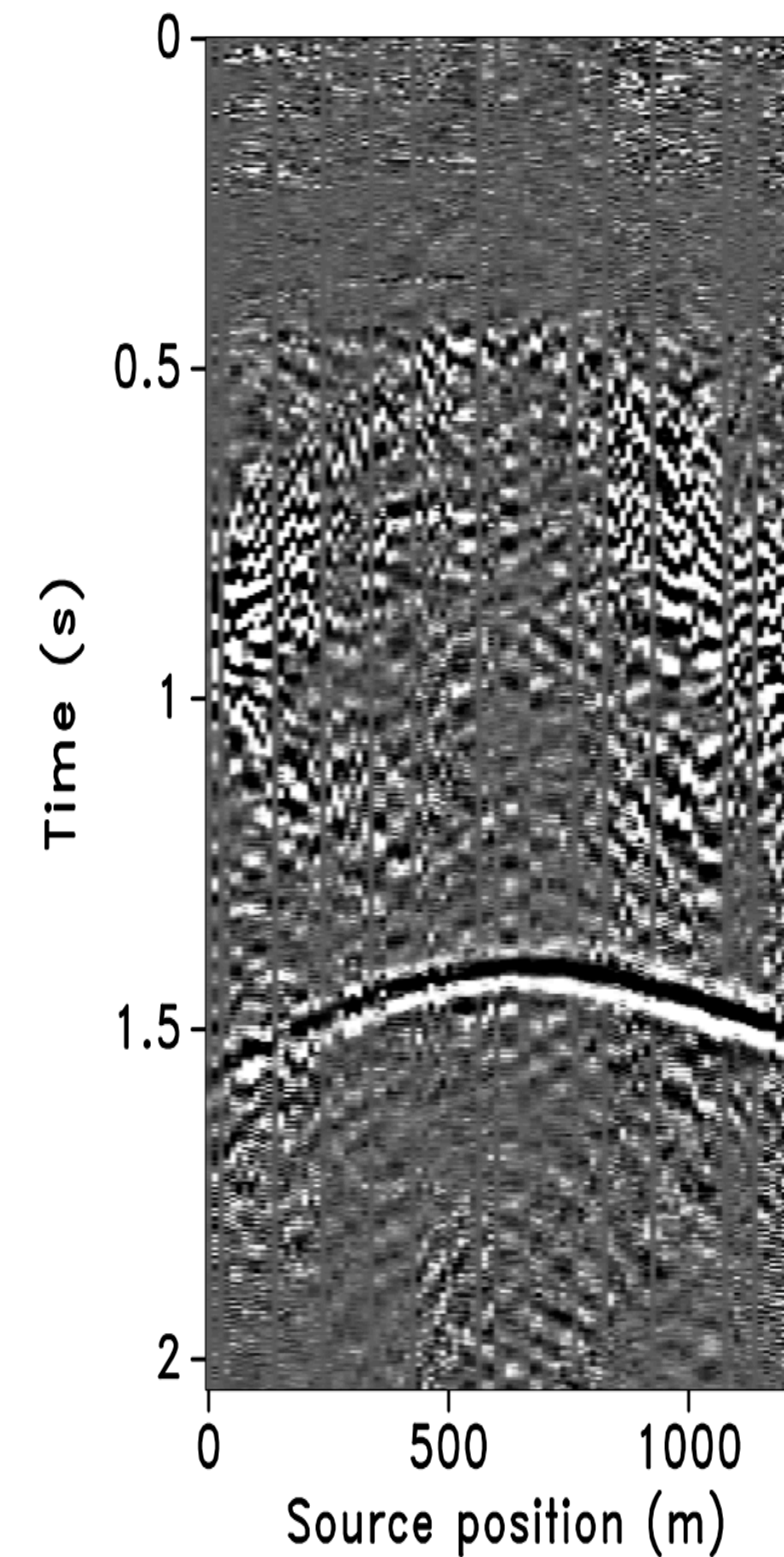
100% overlap  
[10.2 dB]



50% overlap  
[-16.0 dB]



25% overlap  
[-18.5 dB]



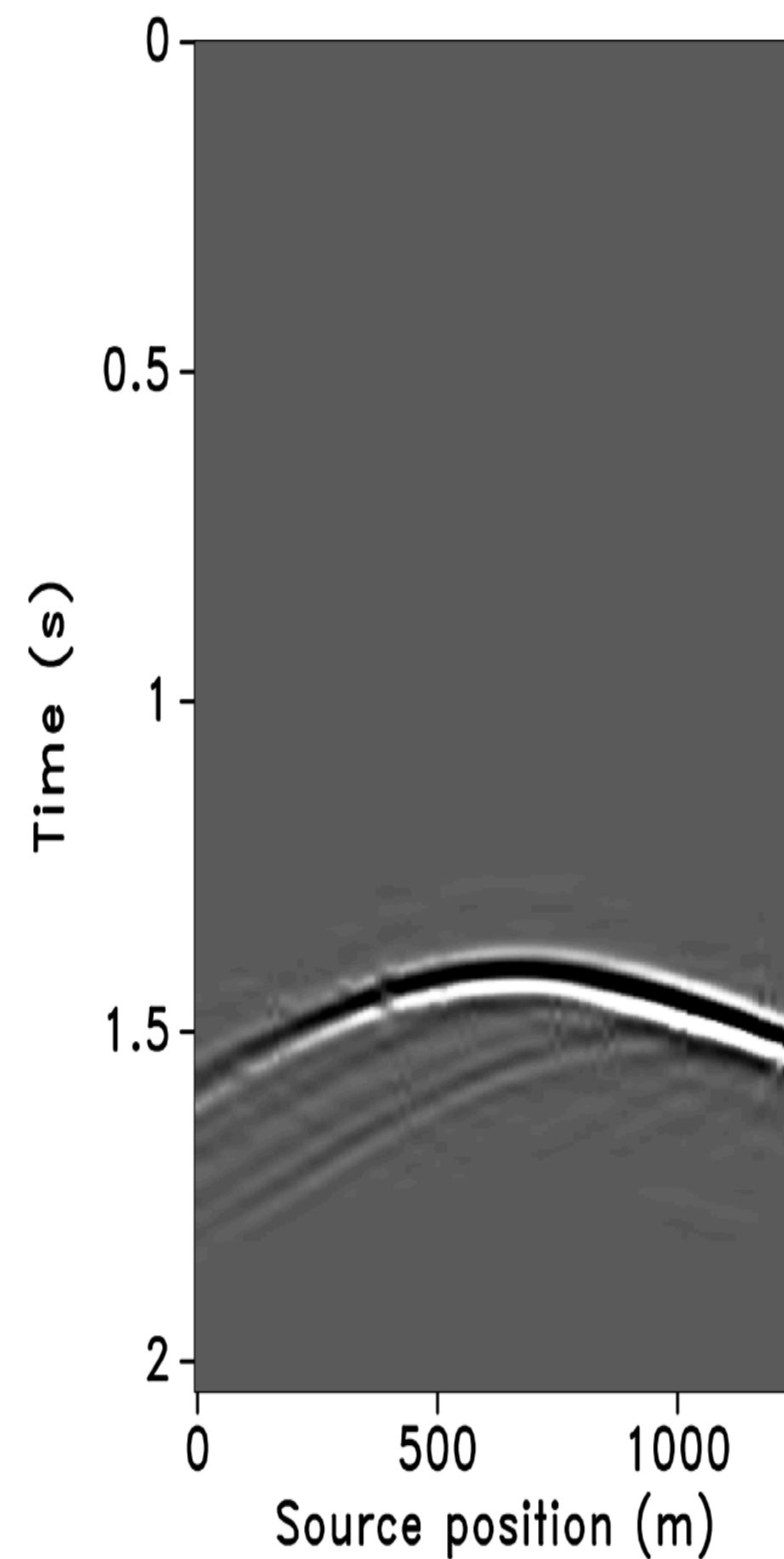


# 4D recovery

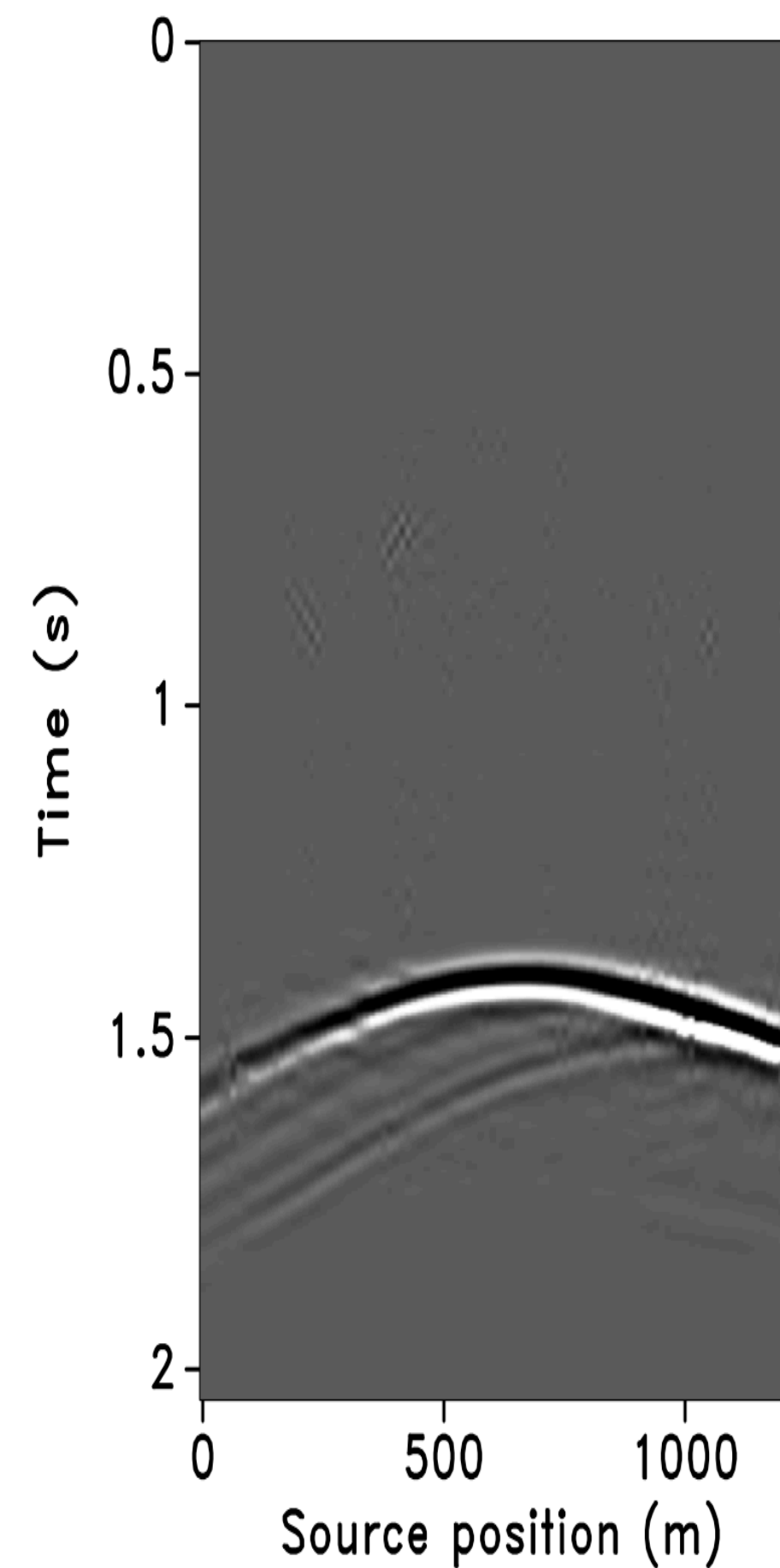
## – Joint recovery

[colormap scale: 10 X]

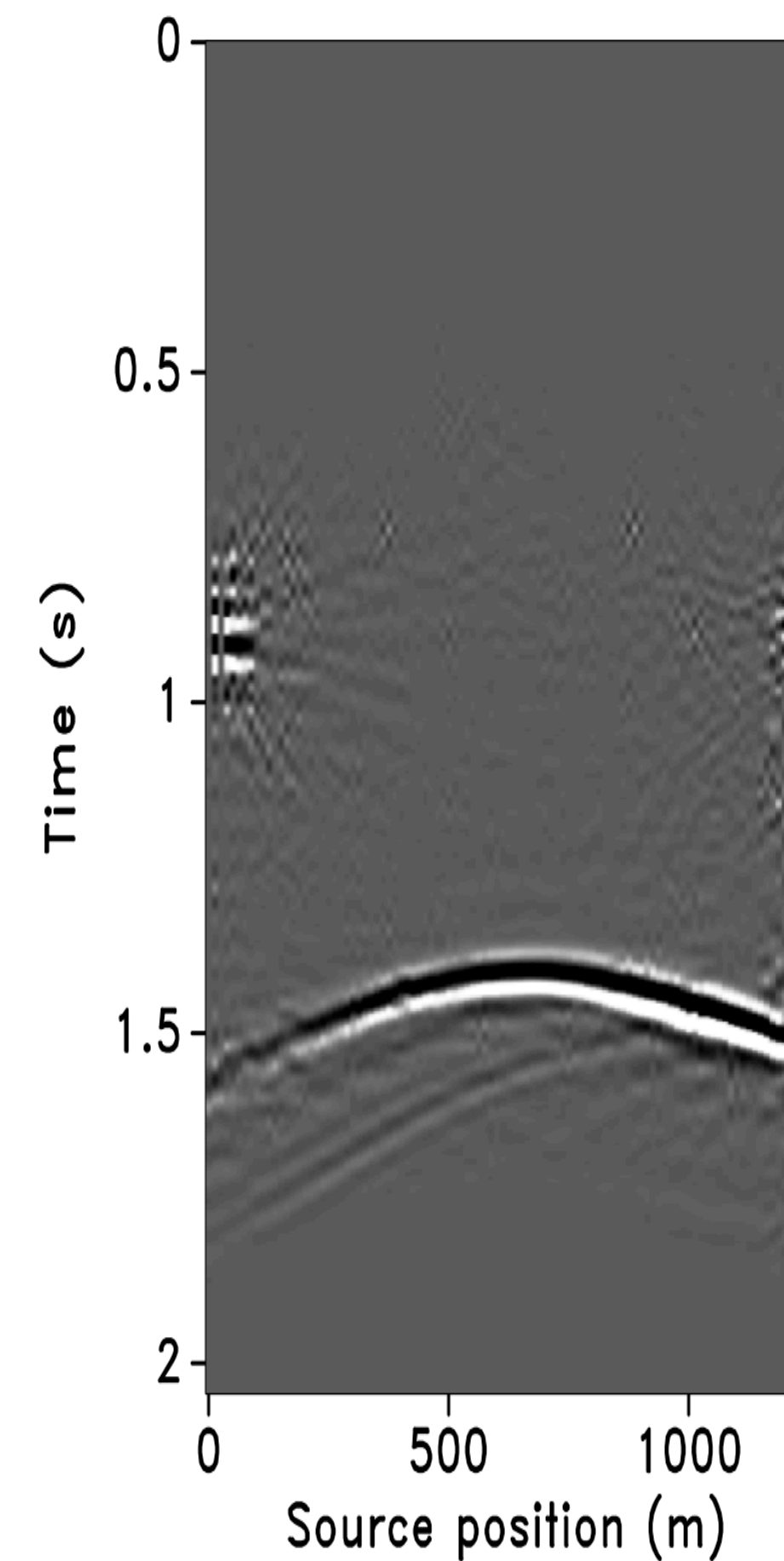
100% overlap  
[12.8 dB]



50% overlap  
[5.0 dB]



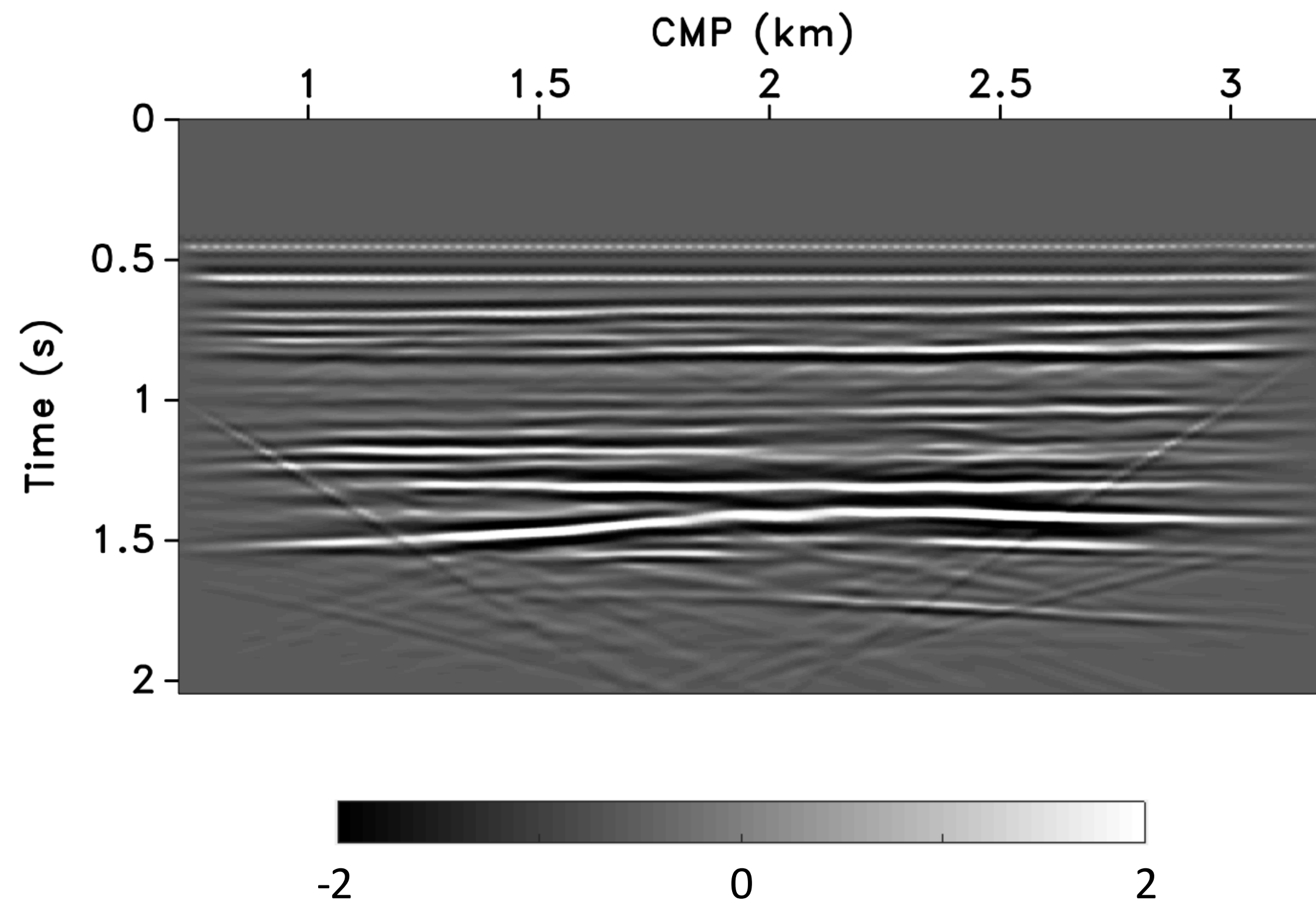
25% overlap  
[2.0 dB]



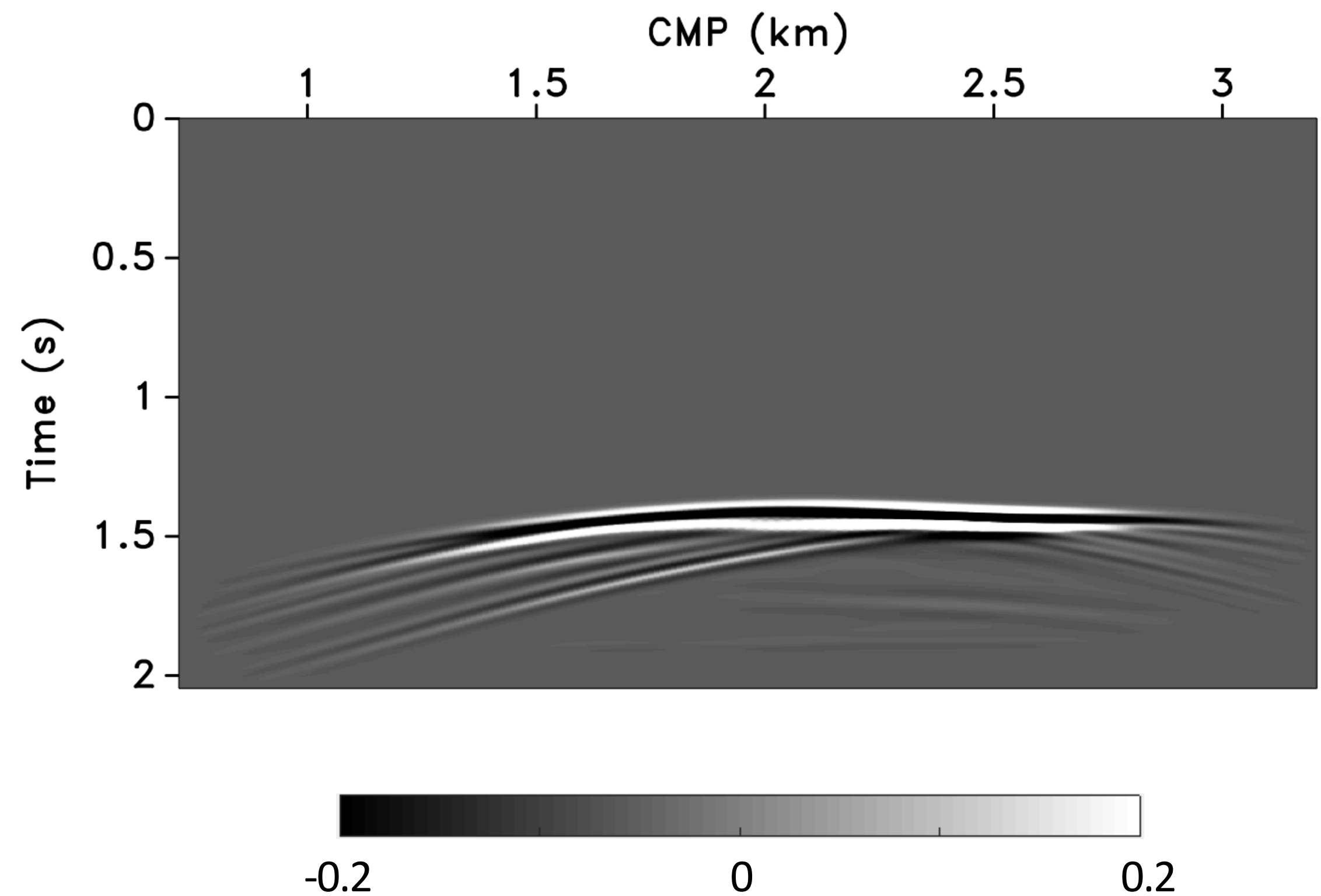


# Stacked sections

Baseline

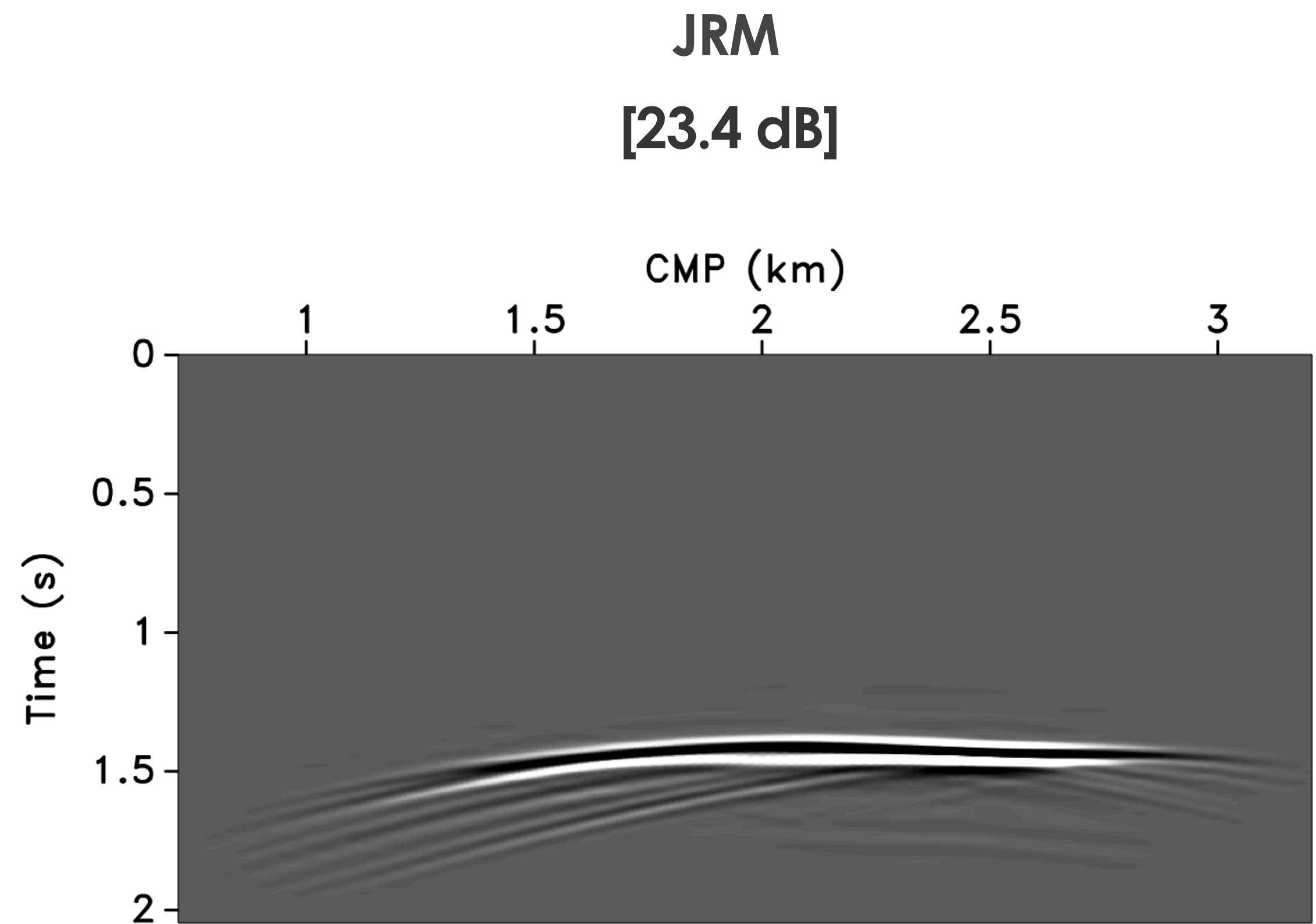
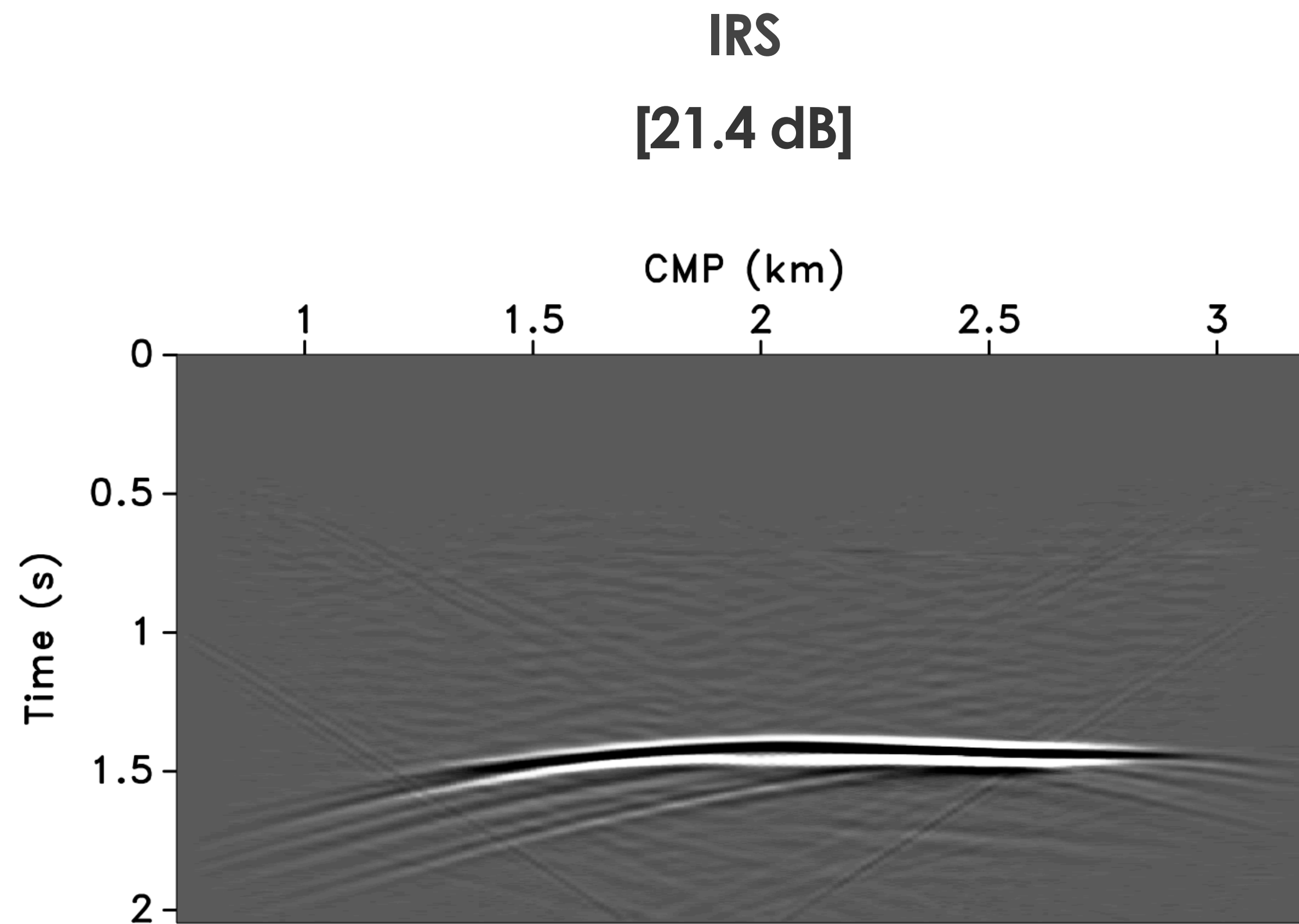


4D signal



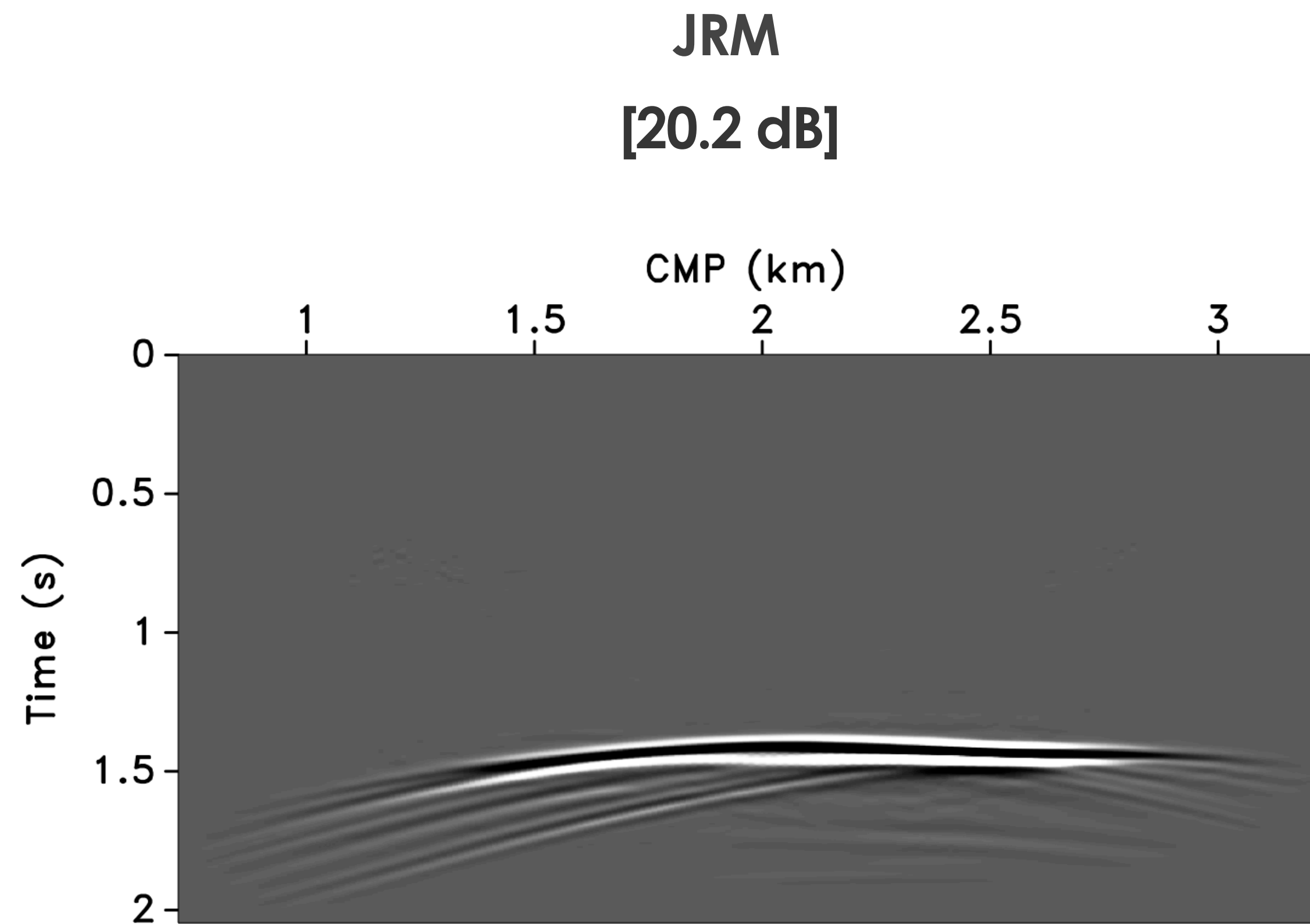
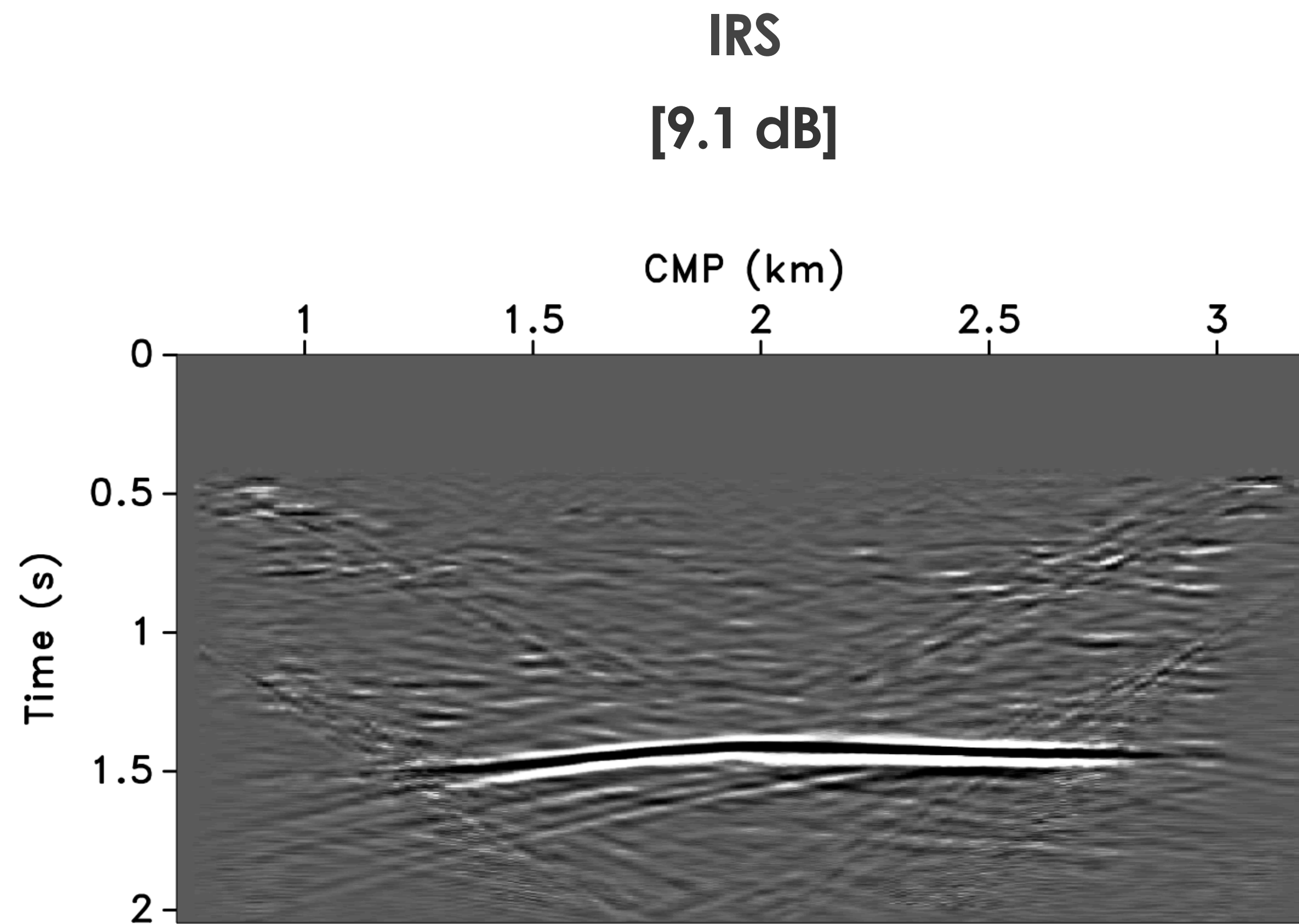
# Stacked sections

- **100% overlap** in acquisition matrices



# Stacked sections

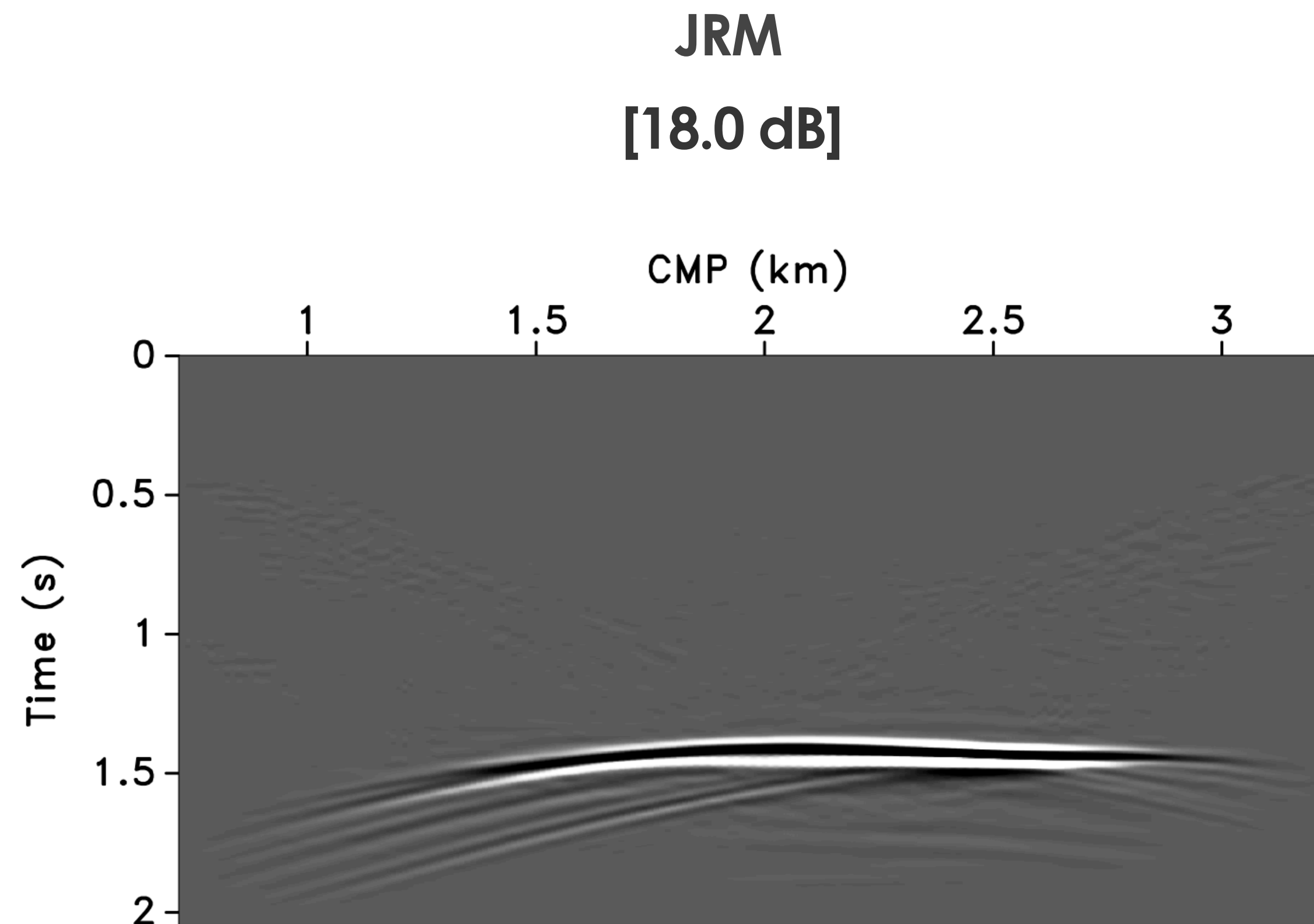
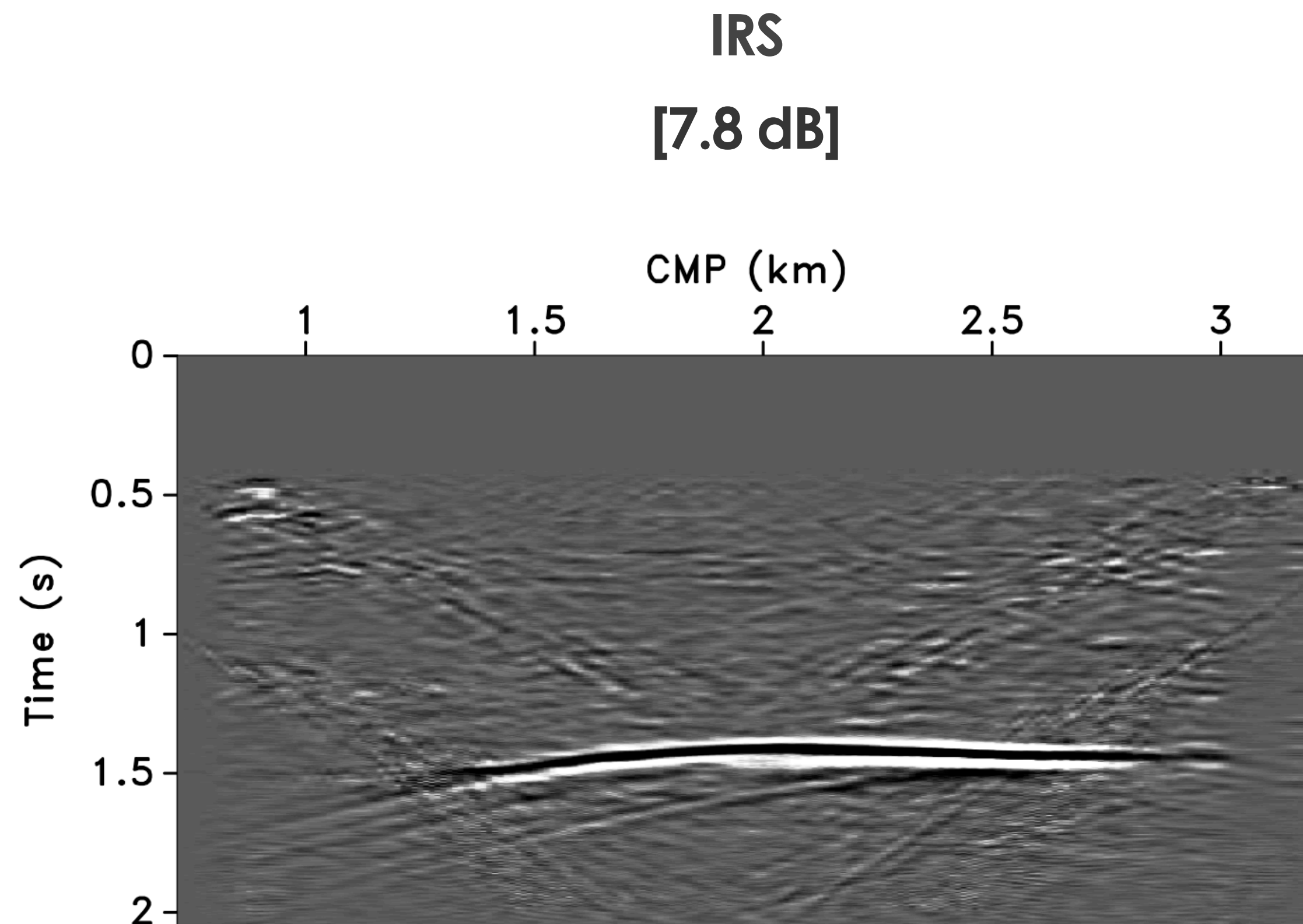
- **50% overlap** in acquisition matrices





# Stacked sections

- **25% overlap** in acquisition matrices



# SNR (dB) for stacked sections

– average of 100 experiments

overlap	baseline		monitor		4D signal	
	IRS	JRM	IRS	JRM	IRS	JRM
100%	$23.1 \pm 1.2$	$24.8 \pm 1.2$	$23.1 \pm 1.3$	$24.8 \pm 1.2$	$21.4 \pm 1.8$	<b><math>23.4 \pm 2.1</math></b>
50%	$23.1 \pm 1.2$	$32.8 \pm 1.6$	$23.4 \pm 1.2$	$32.8 \pm 1.6$	$9.1 \pm 1.2$	$20.2 \pm 1.3$
25%	$23.1 \pm 1.2$	<b><math>35.3 \pm 1.5</math></b>	$22.0 \pm 1.1$	<b><math>35.0 \pm 1.5</math></b>	$7.8 \pm 1.3$	<b><math>18.0 \pm 1.1</math></b>

## Conclusions

Seismic synthetics show that we do **not** necessarily have to insist on full replication of surveys depending on the recovery of the vintages

**Processing** time-lapse data **jointly** leads to improved recovery of the vintages with little variability in the time-lapse difference

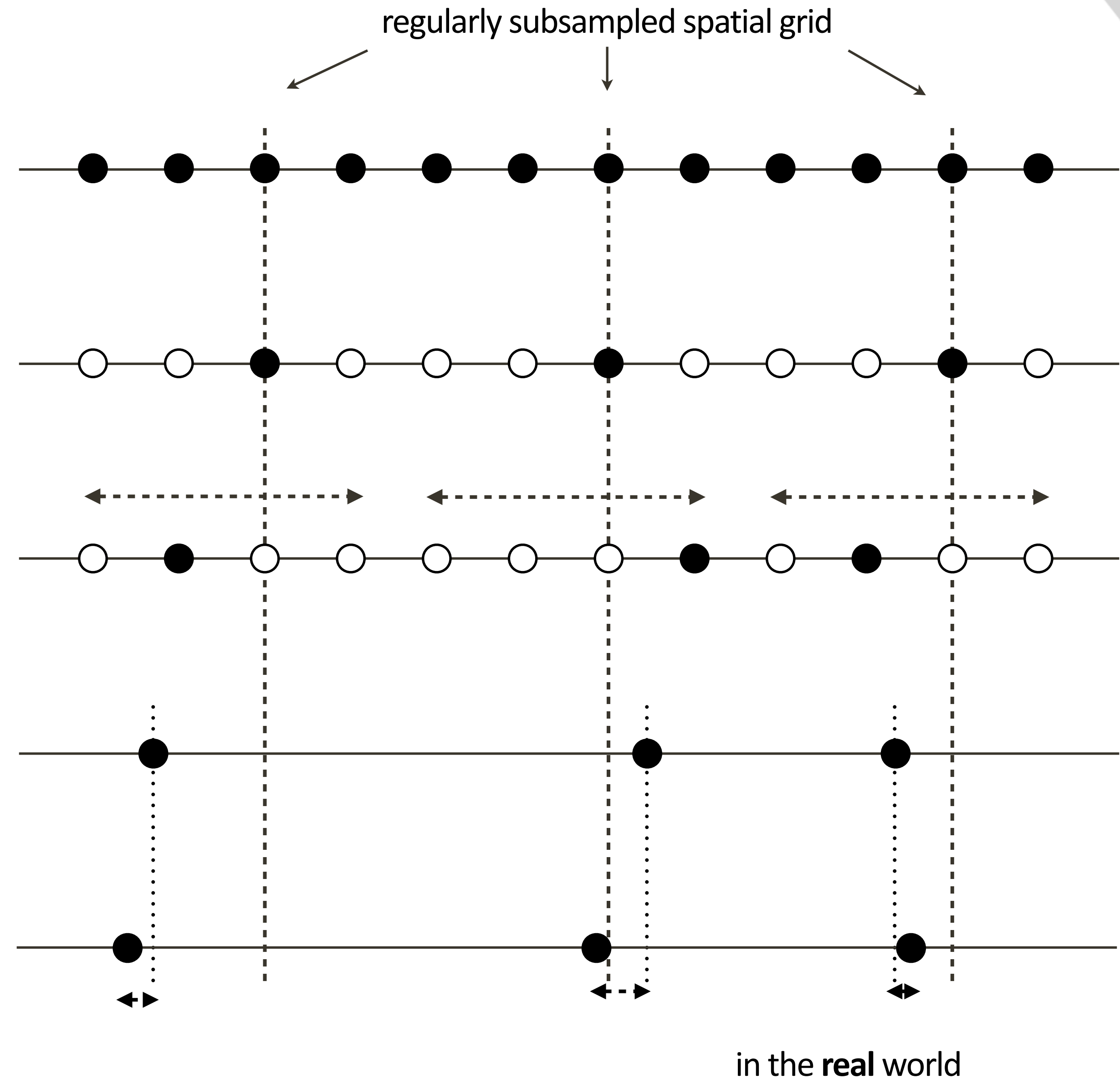
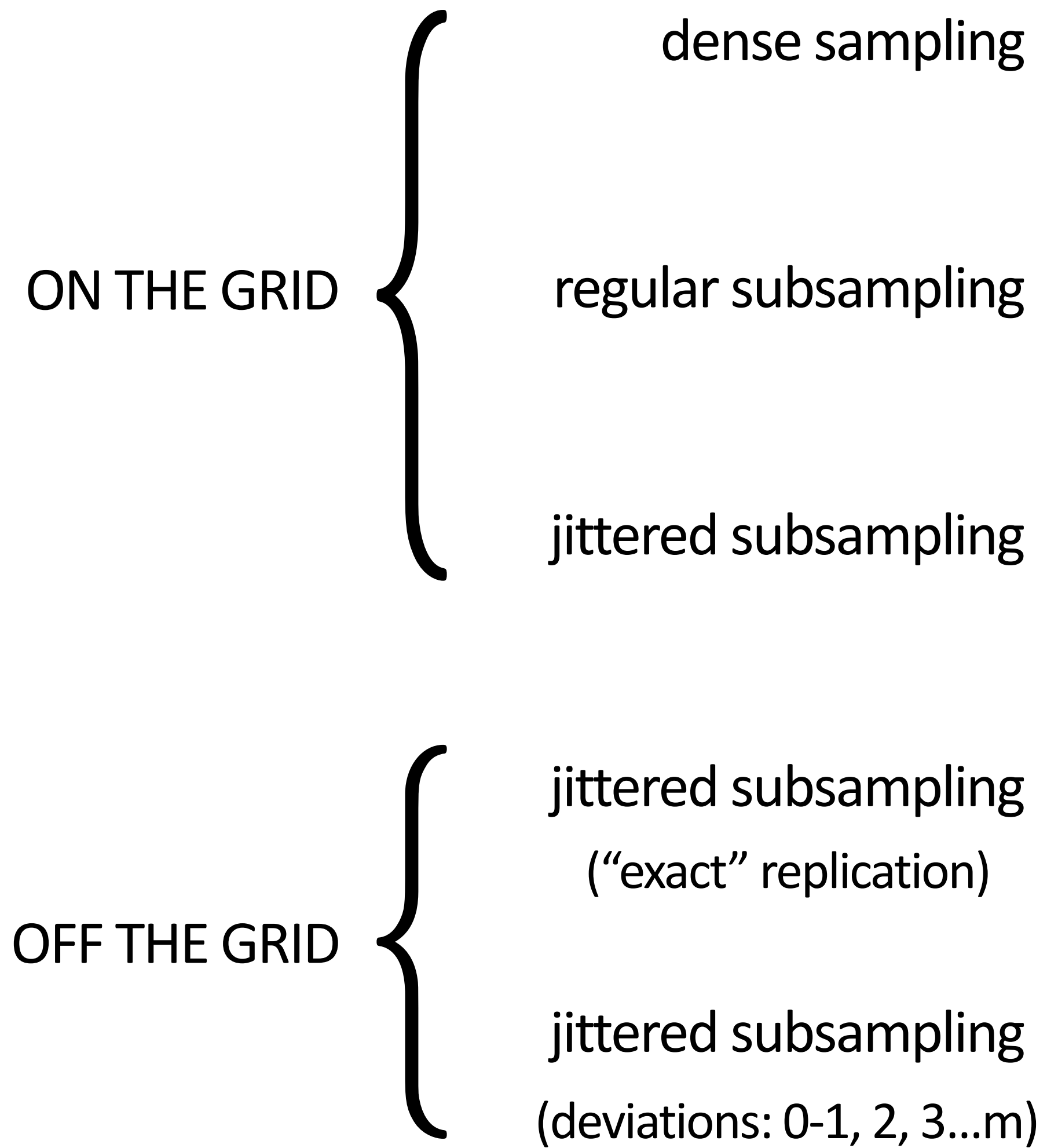
Recall: we are still **on the grid** => exactly replicated (subsampled) shot locations ..... **not realistic!**



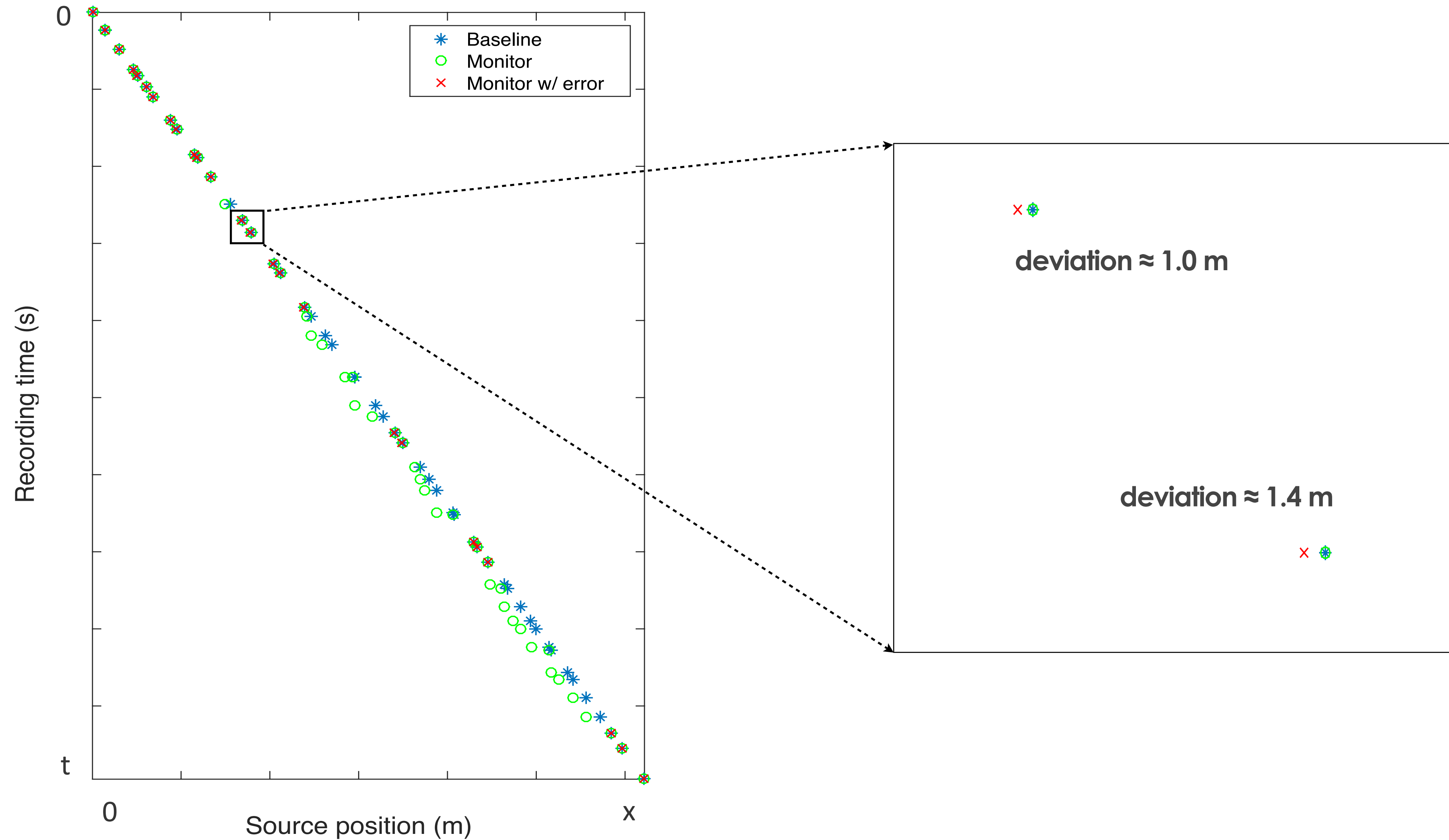
# Chapter 6

- Compressive time-lapse marine acquisition
- static acquisition geometry
  - **off-the-grid** (or irregular) marine surveys
  - with & without **deviations** in shot positions

# Sampling schemes

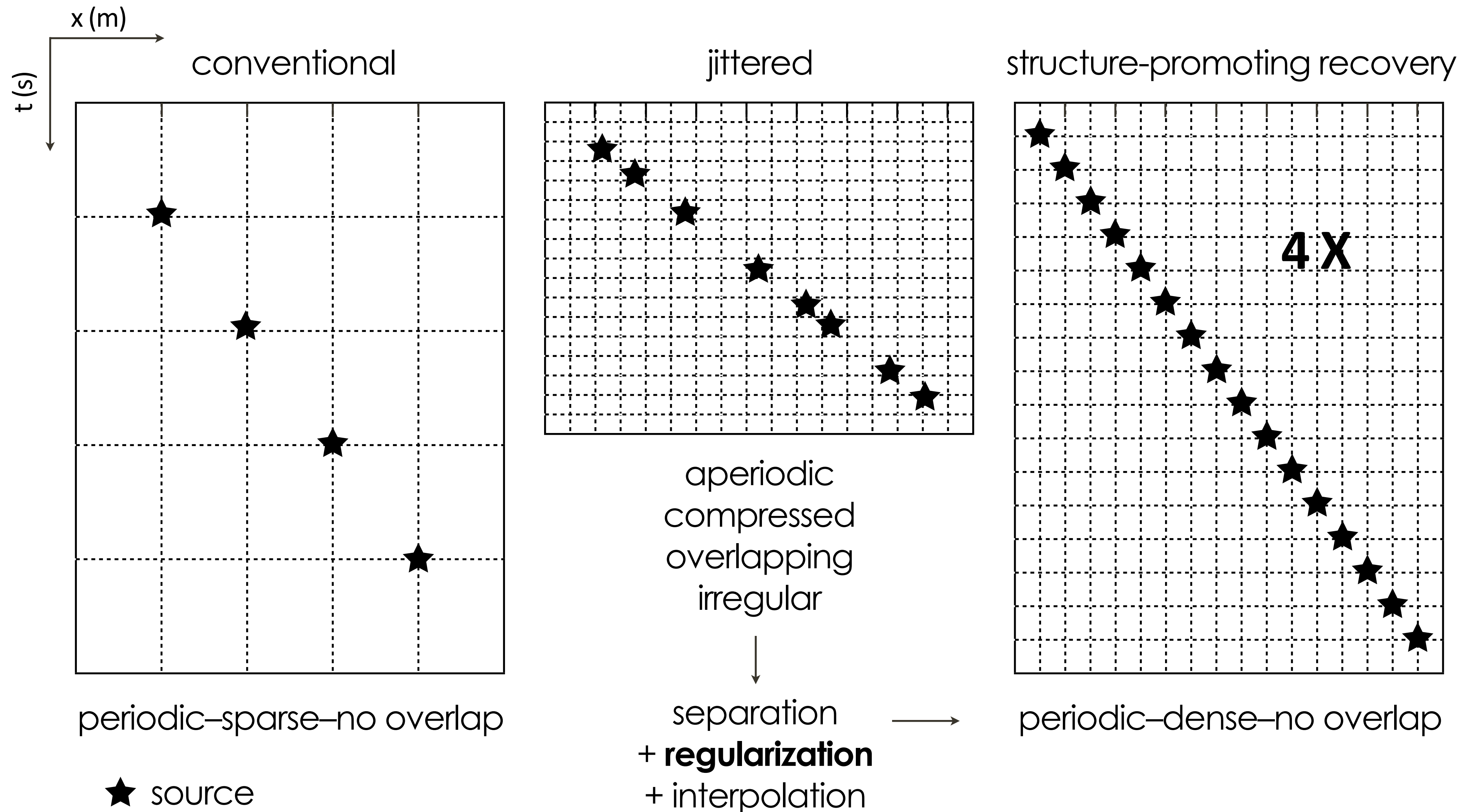


# 4D time-jittered marine acquisition





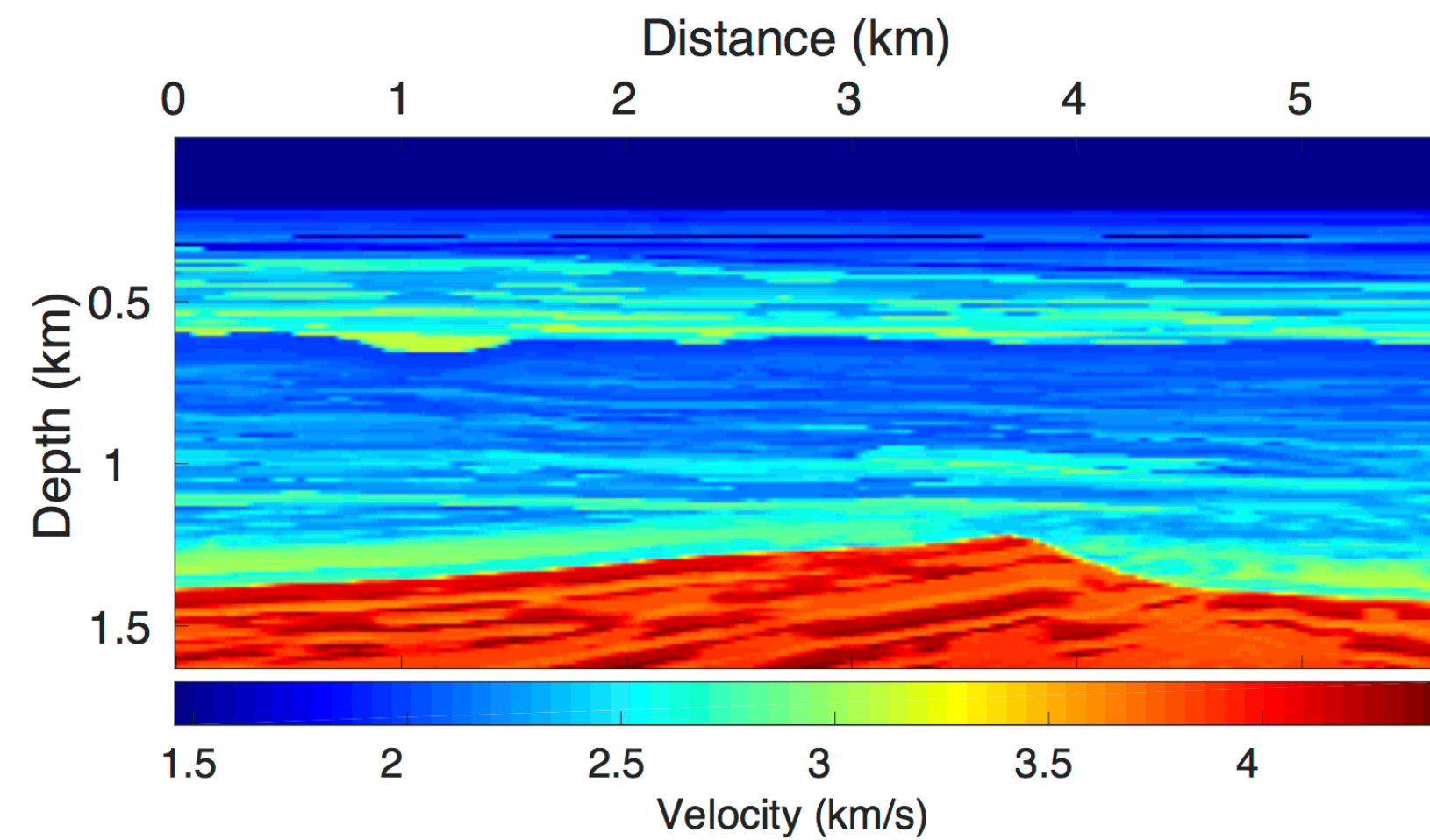
# Conventional vs. compressive acquisition



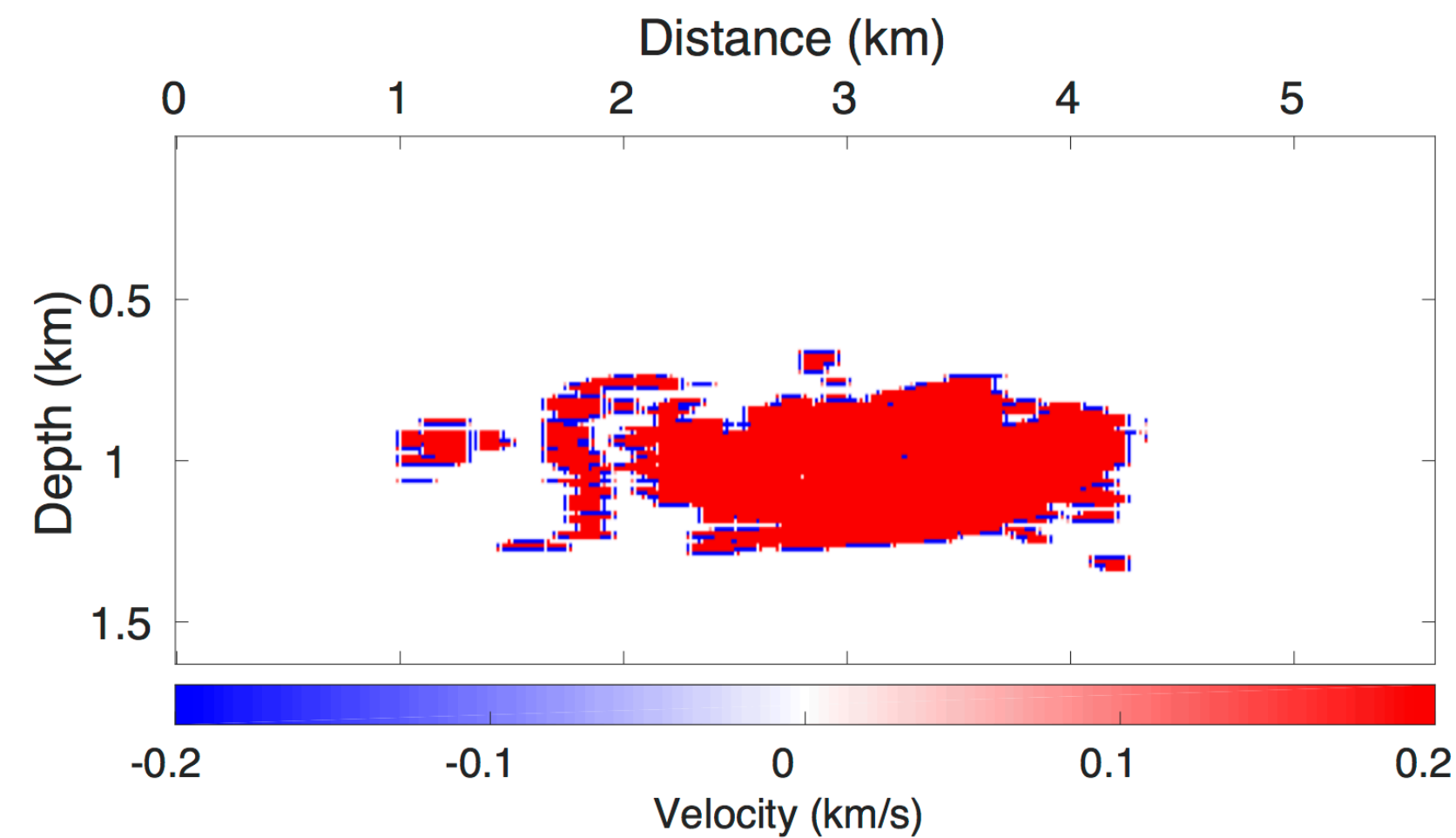
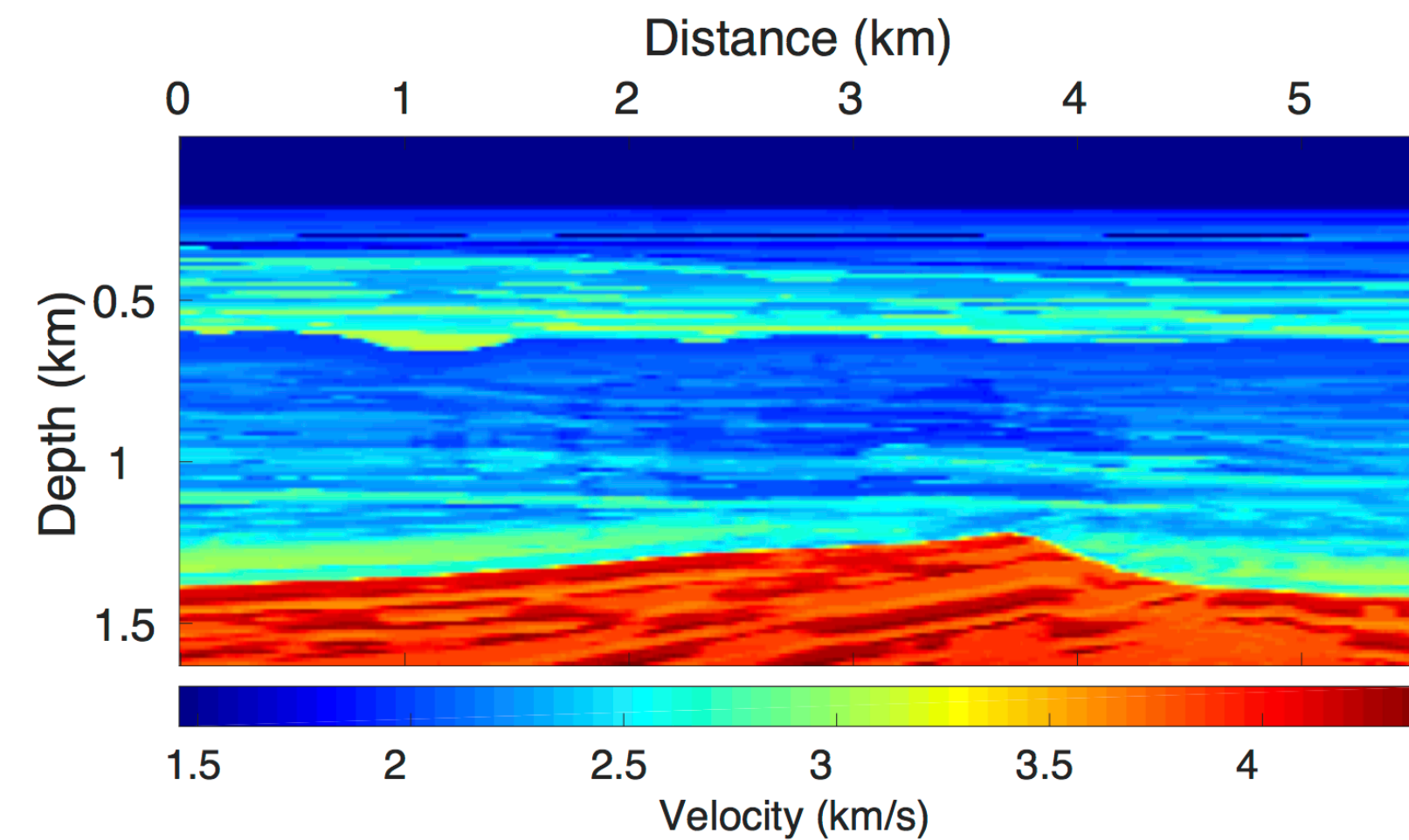
# BG Compass model

– contains gas cloud

Baseline



Monitor

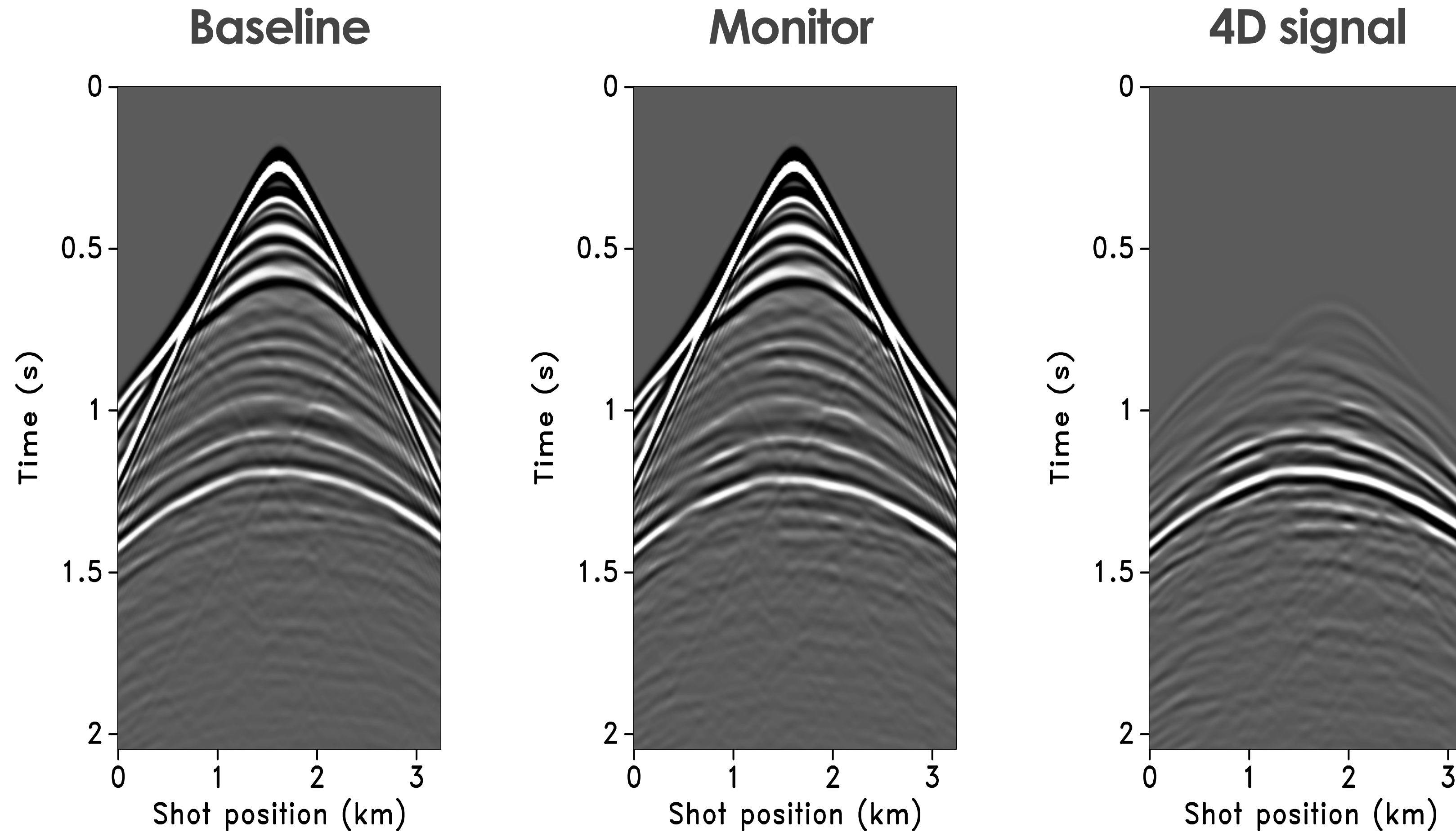


Time-lapse difference



# Simulated time-lapse data

– time-domain finite differences



time samples: **512**  
receivers: **260**  
sources: **260**

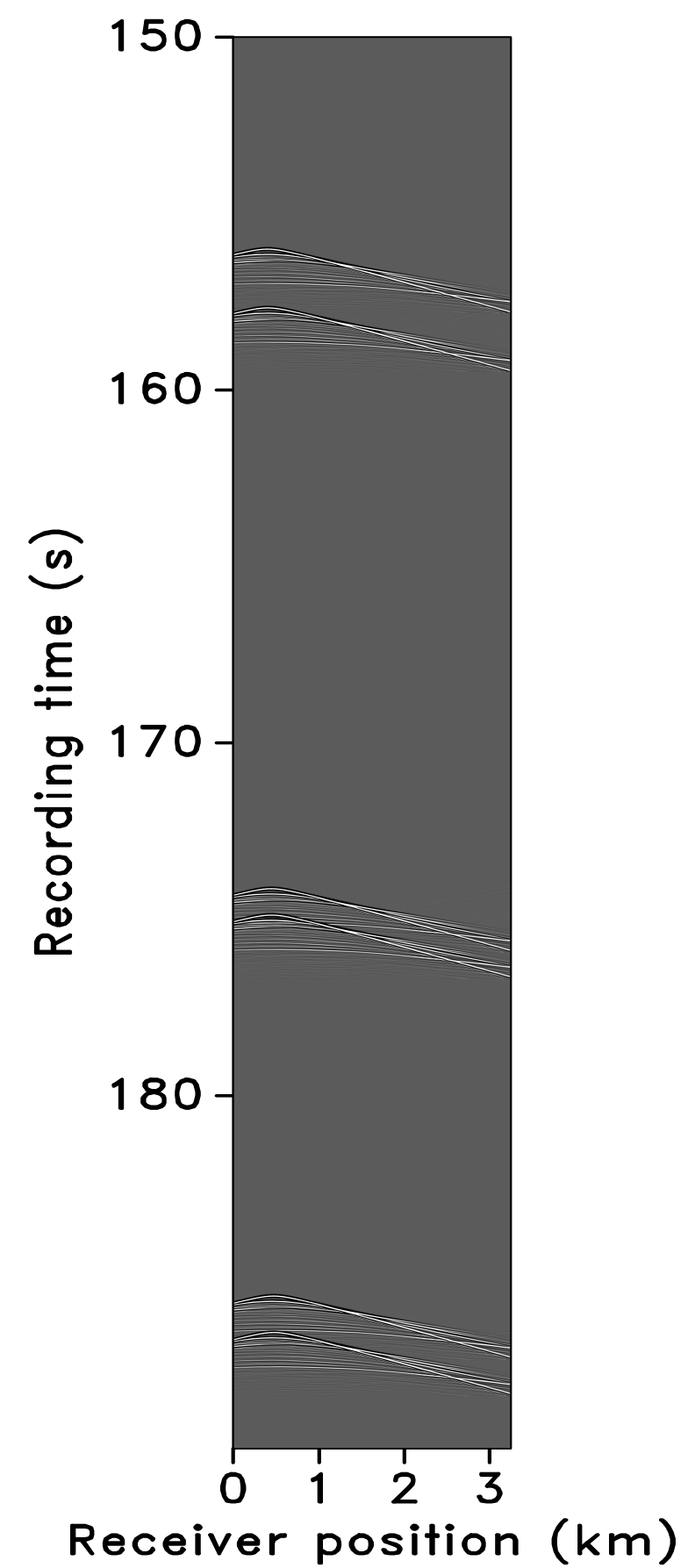
sampling  
time: **4.0 ms**  
receiver: **12.5 m**  
source: **12.5 m**



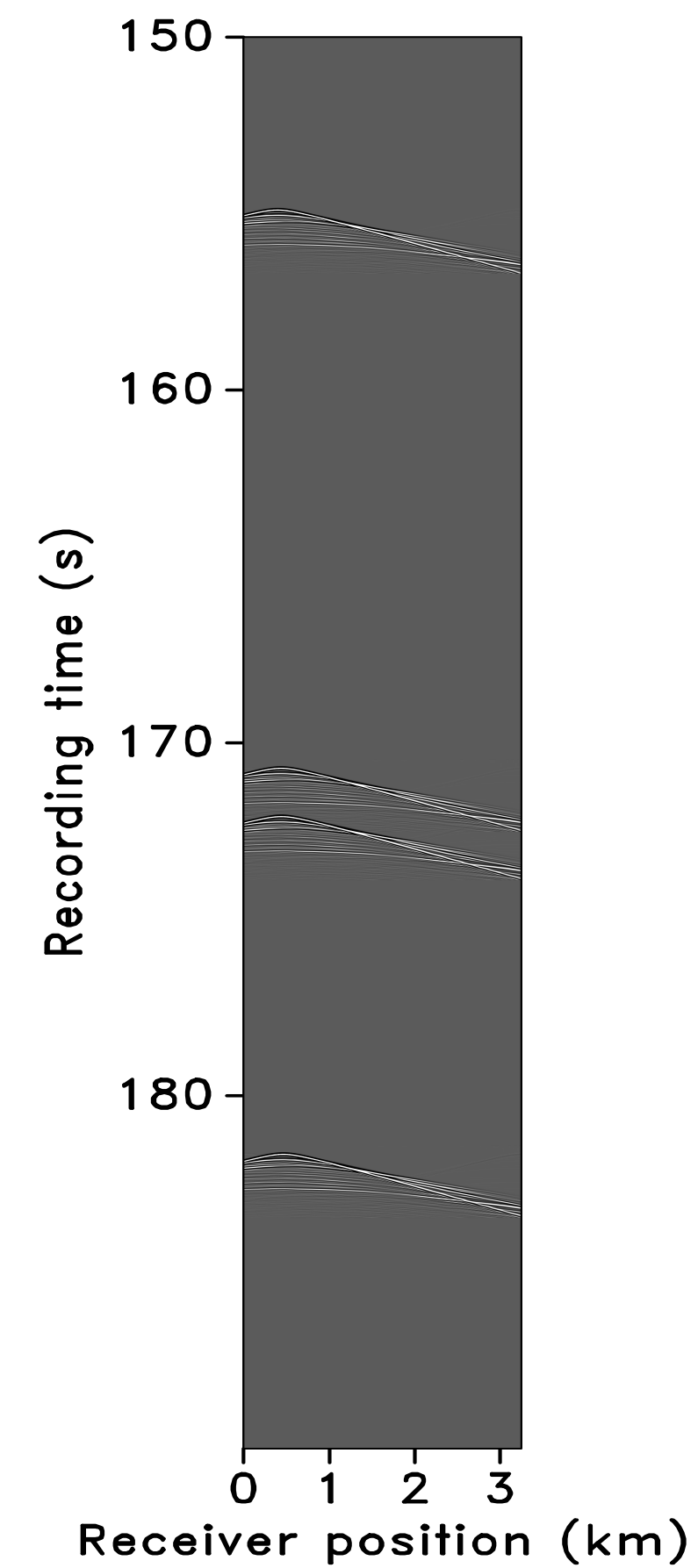
# Measurements

– subsampled, overlapping and **irregular** shots

## Baseline

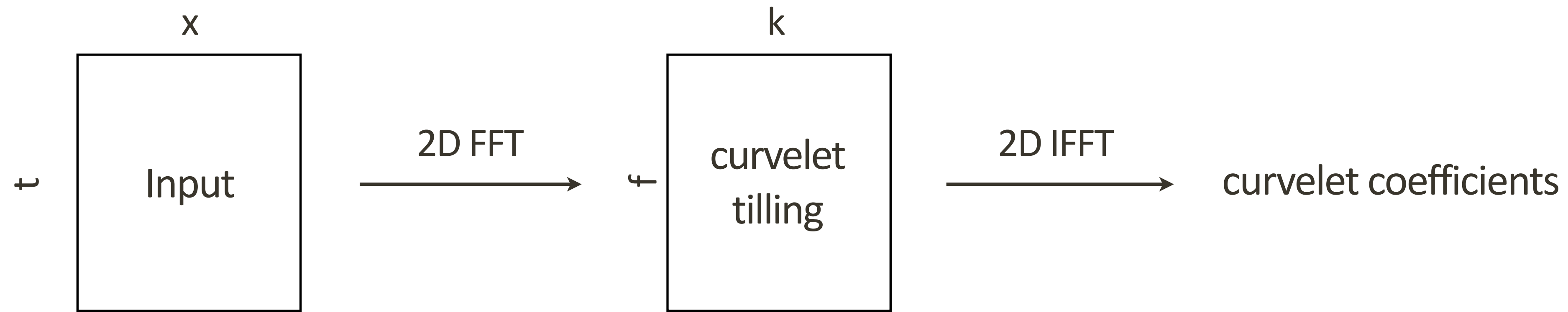


## Monitor

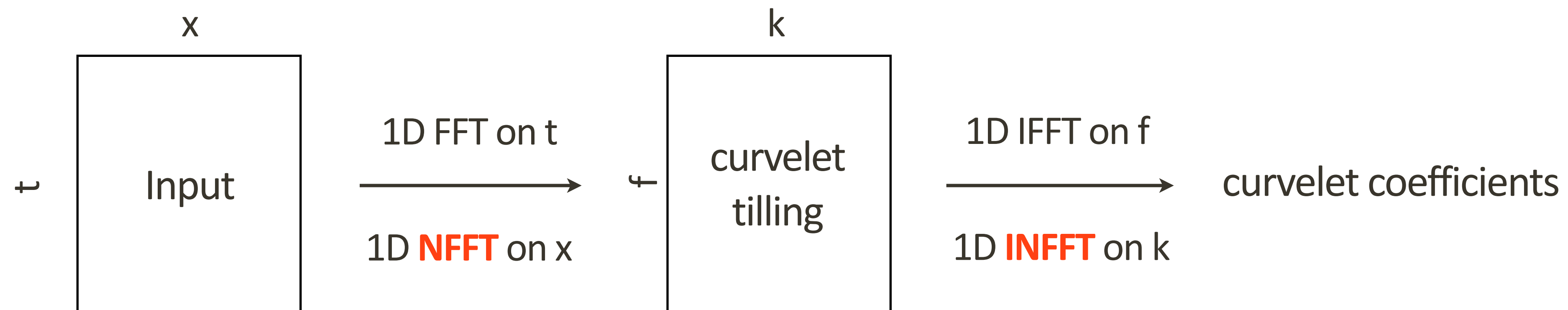


# FDCT vs. NFDCT

## Fast Discrete Curvelet Transform (FDCT)

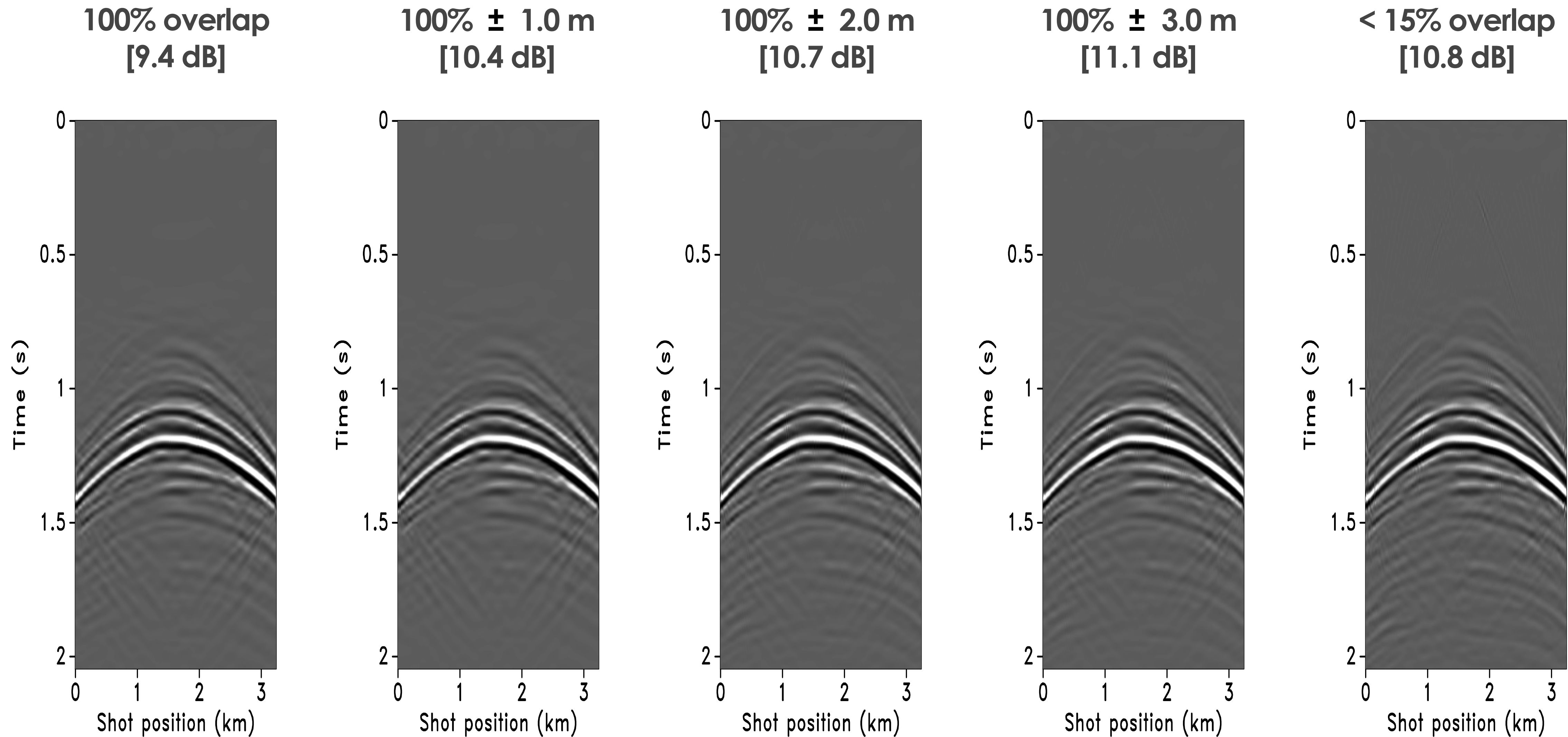


## Nonequispaced Fast Discrete Curvelet Transform (NFDCT)



# 4D recovery

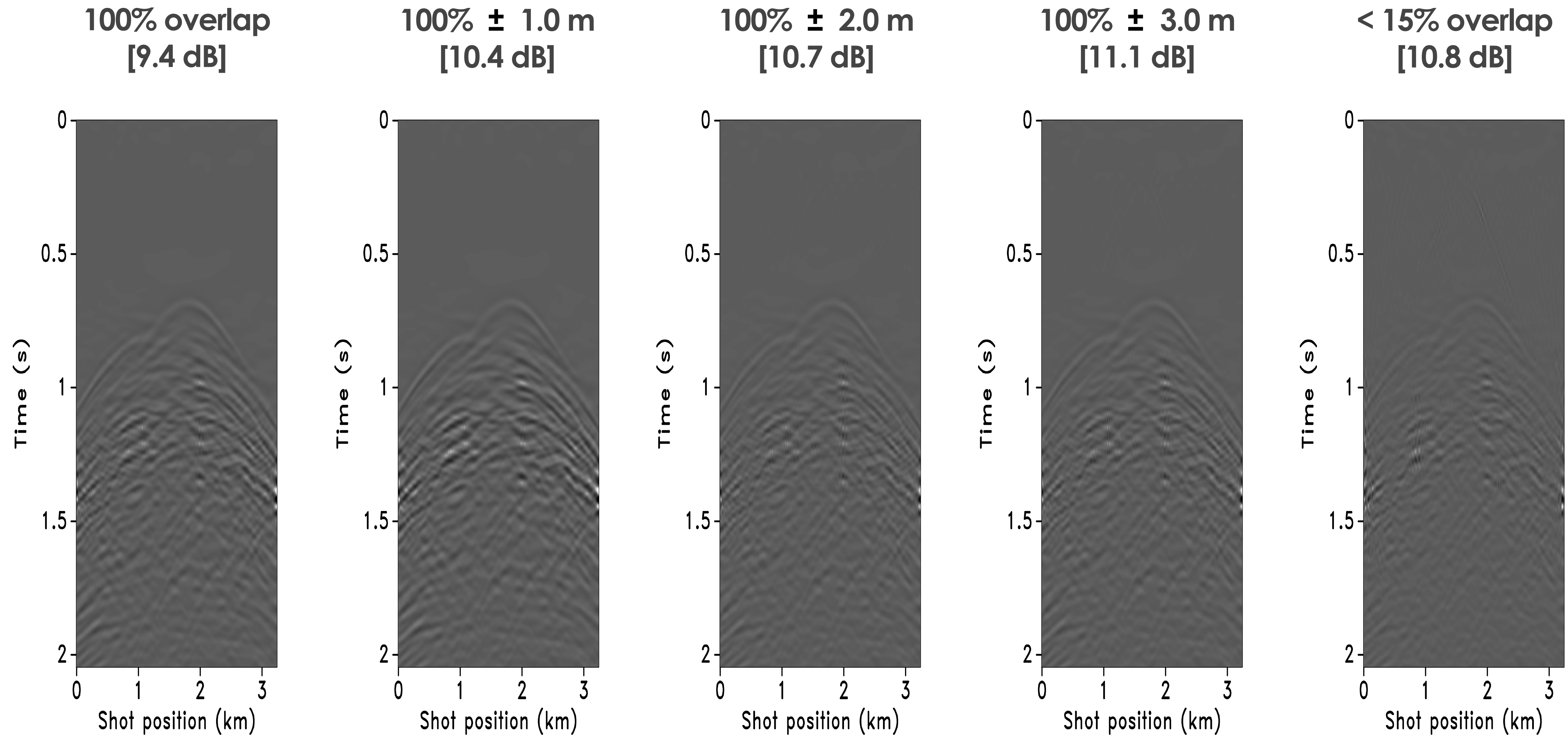
- **Joint recovery**; subsampling factor = 2





# 4D residual

- **Joint recovery**; subsampling factor = 2



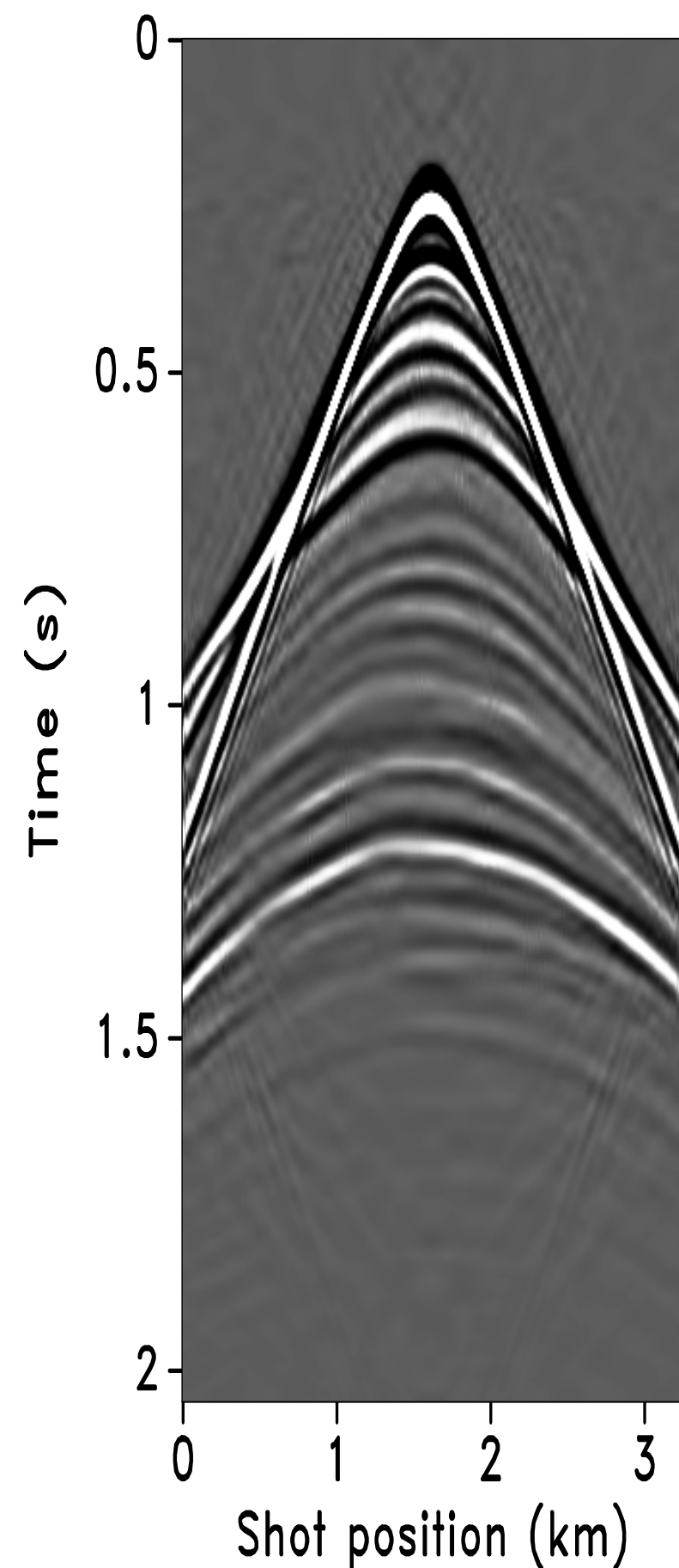
position deviations **improve** recovery of the vintages



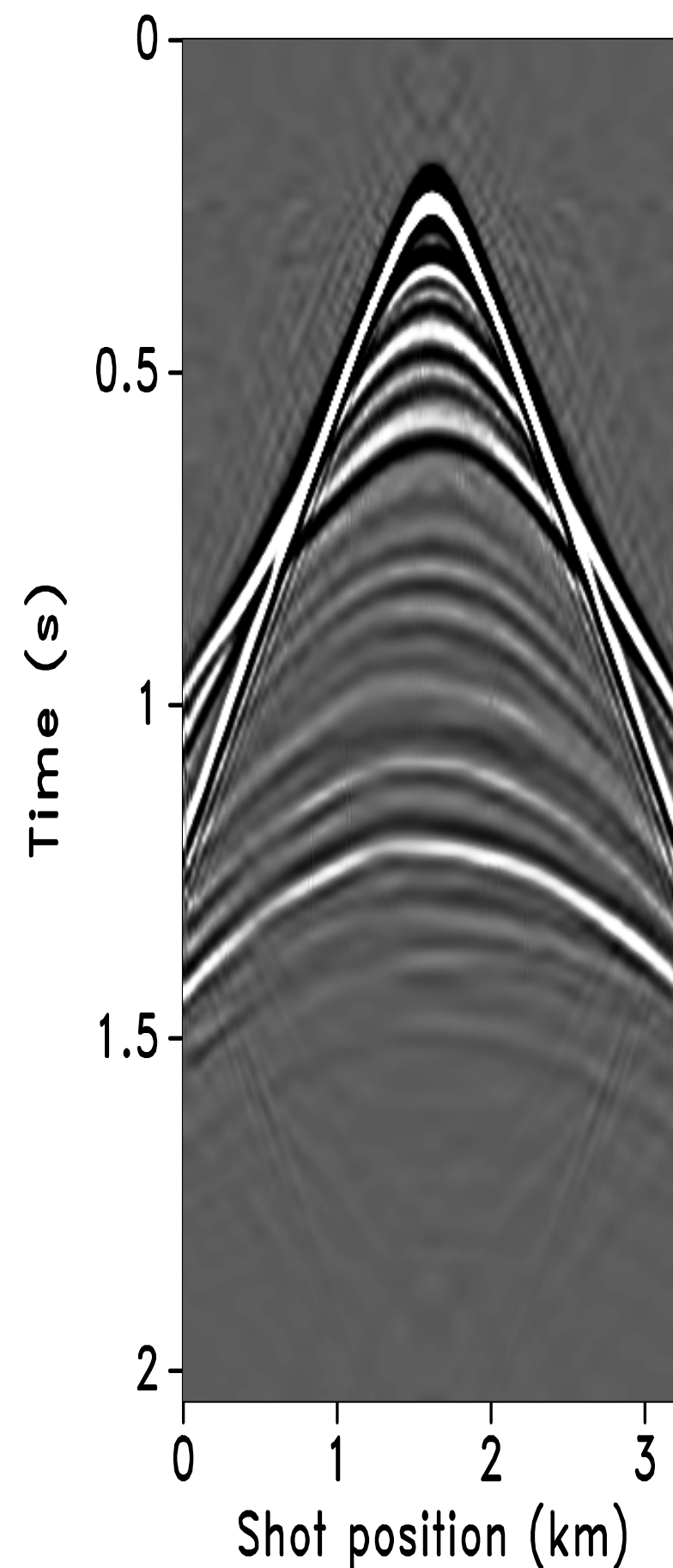
# Monitor recovery

- **Joint recovery**; subsampling factor = 2

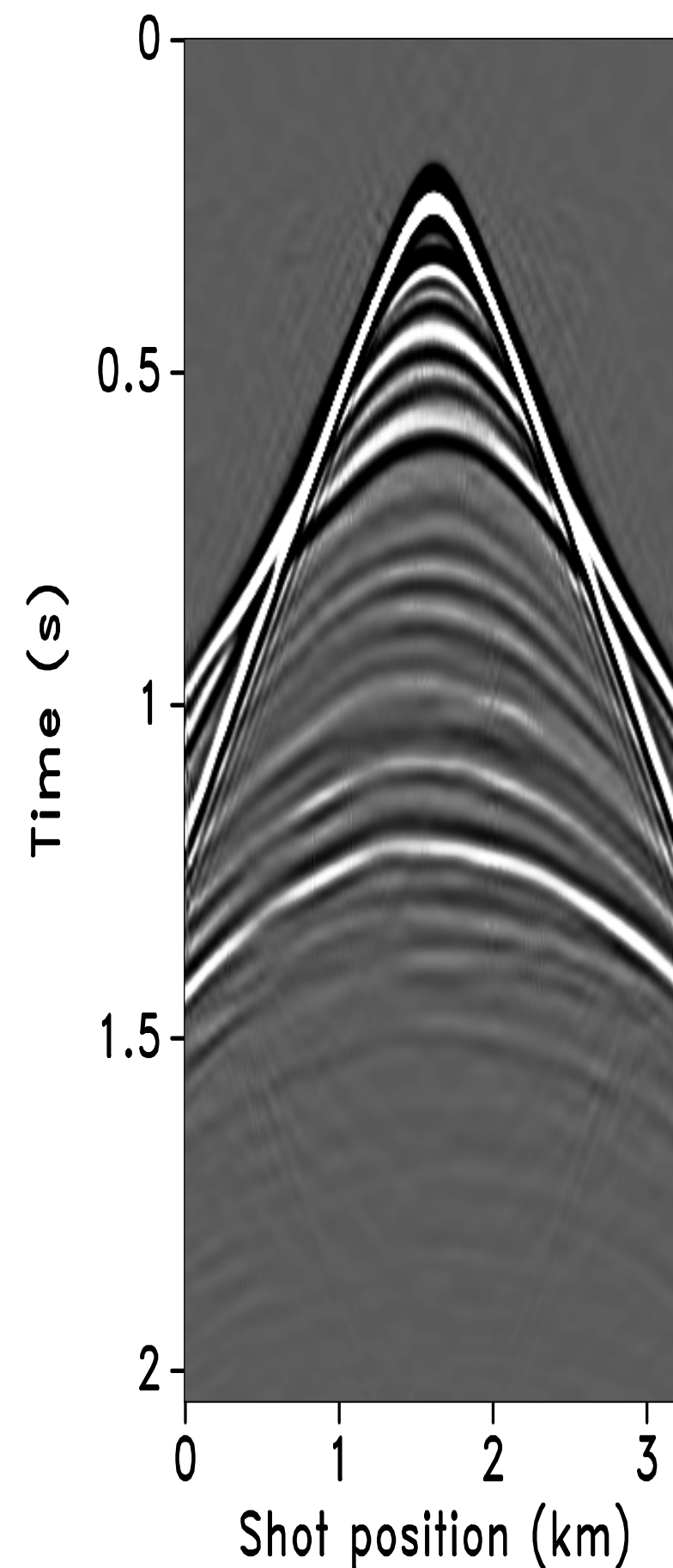
100% overlap  
[19.0 dB]



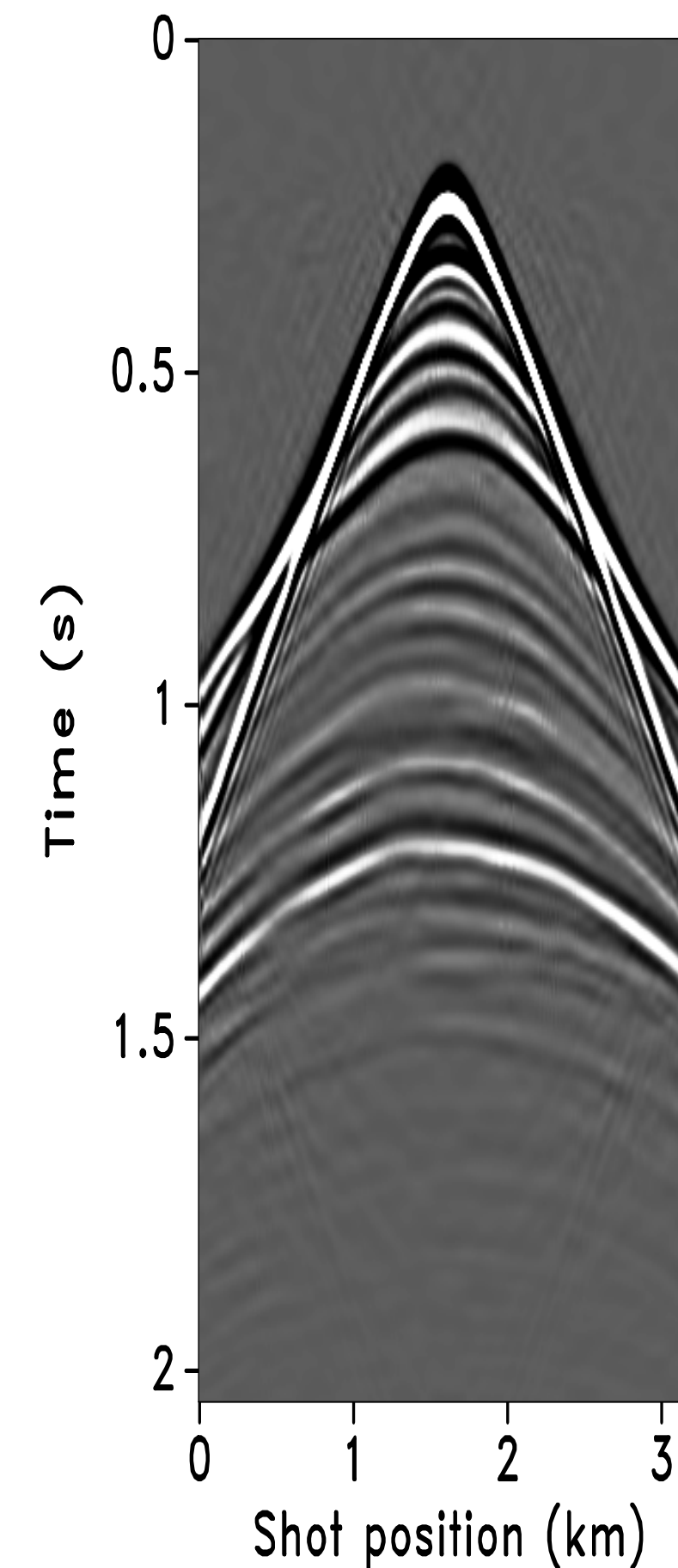
100%  $\pm$  1.0 m  
[19.6 dB]



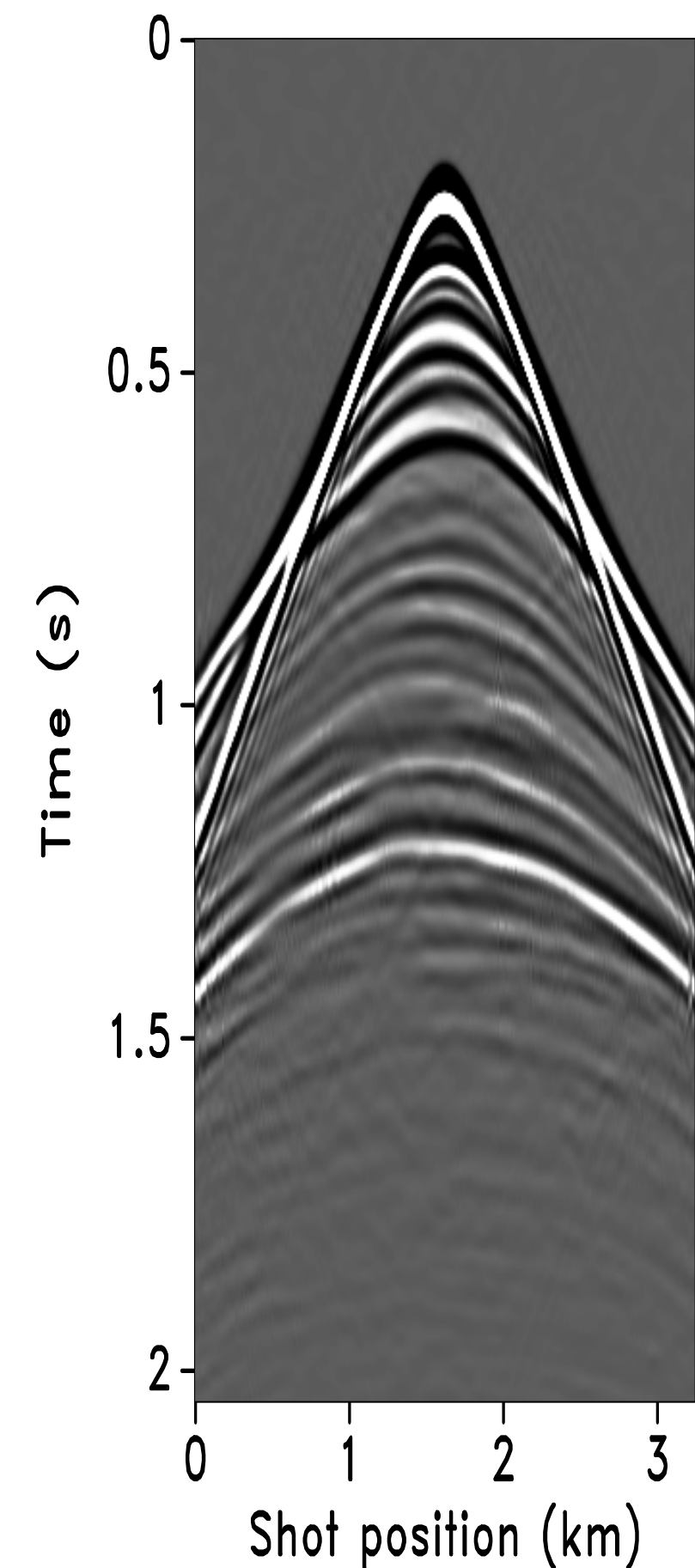
100%  $\pm$  2.0 m  
[20.2 dB]



100%  $\pm$  3.0 m  
[20.8 dB]



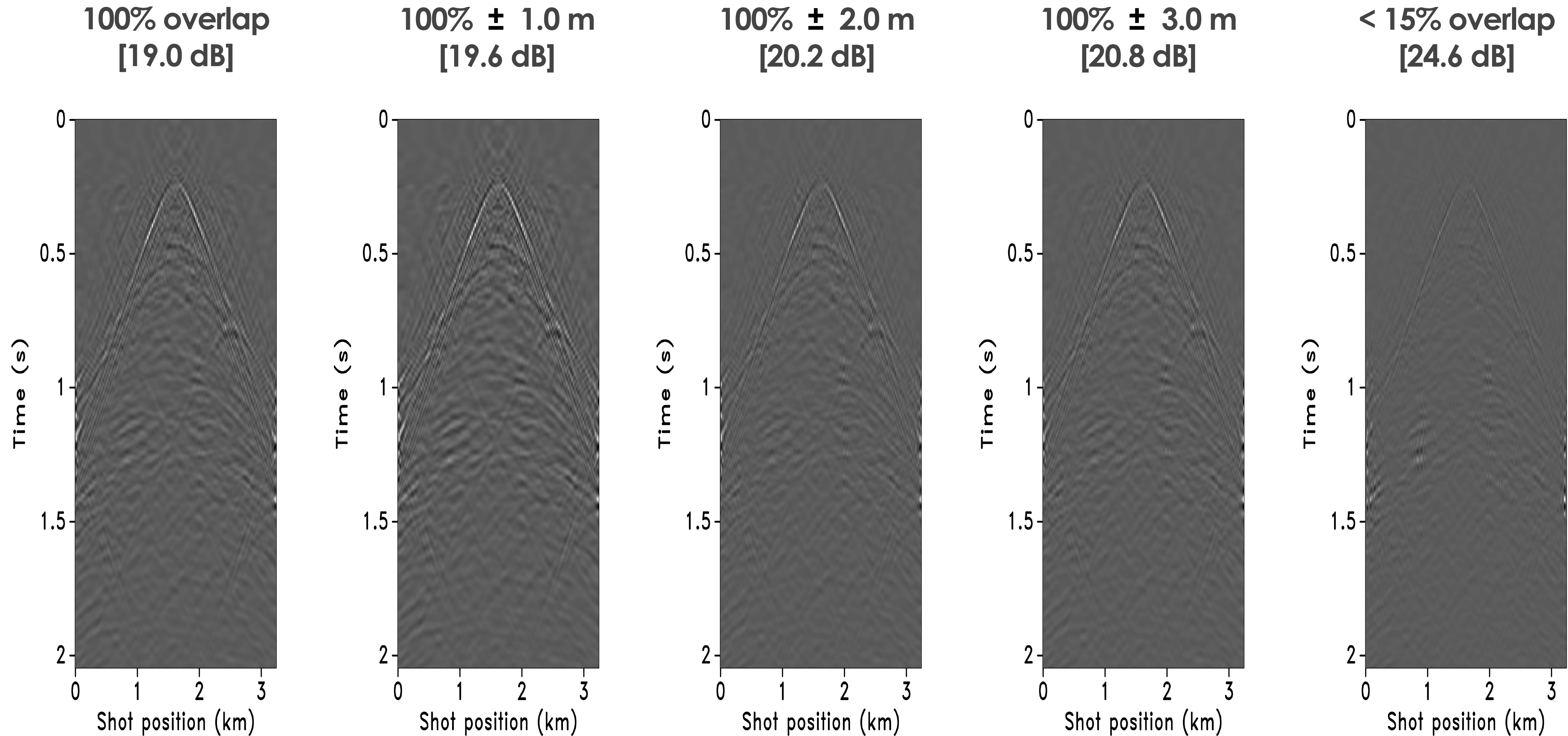
< 15% overlap  
[24.6 dB]





# Monitor residual

- **Joint recovery**; subsampling factor = 2



# SNR (dB) for data recovered via JRM

– average of 10 experiments; **subsampling factor = 2**

overlap $\pm$ deviation	Baseline	Monitor	4D signal
100%	$19.1 \pm 0.9$	$19.0 \pm 0.9$	$9.4 \pm 1.8$
$100\% \pm 1.0$ m	$19.7 \pm 0.7$	$19.6 \pm 0.7$	$10.4 \pm 1.3$
$100\% \pm 2.0$ m	$20.3 \pm 1.5$	$20.2 \pm 1.5$	$10.7 \pm 1.9$
$100\% \pm 3.0$ m	$21.0 \pm 1.5$	$20.8 \pm 1.5$	$11.1 \pm 1.8$
$< 15\%$ *	<b><math>24.8 \pm 1.8</math></b>	<b><math>24.6 \pm 1.7</math></b>	$10.8 \pm 0.9$

\* least possible overlap range  $> 0\%$  and  $< 15\%$  (depends on simultaneous acquisition design and subsampling factor)



# SNR (dB) for data recovered via JRM

– average of 10 experiments; **subsampling factor = 4**

overlap $\pm$ deviation	Baseline	Monitor	4D signal
100%	$14.1 \pm 0.7$	$13.9 \pm 0.7$	$6.1 \pm 0.8$
$100\% \pm 1.0$ m	$14.5 \pm 0.8$	$14.3 \pm 0.8$	$5.6 \pm 0.8$
$100\% \pm 2.0$ m	$15.6 \pm 0.7$	$15.5 \pm 0.7$	$6.4 \pm 0.7$
$100\% \pm 3.0$ m	$16.2 \pm 0.7$	$16.0 \pm 0.7$	$6.0 \pm 0.6$
$< 5\%$ *	<b><math>18.0 \pm 0.9</math></b>	<b><math>17.7 \pm 0.8</math></b>	$5.2 \pm 0.5$

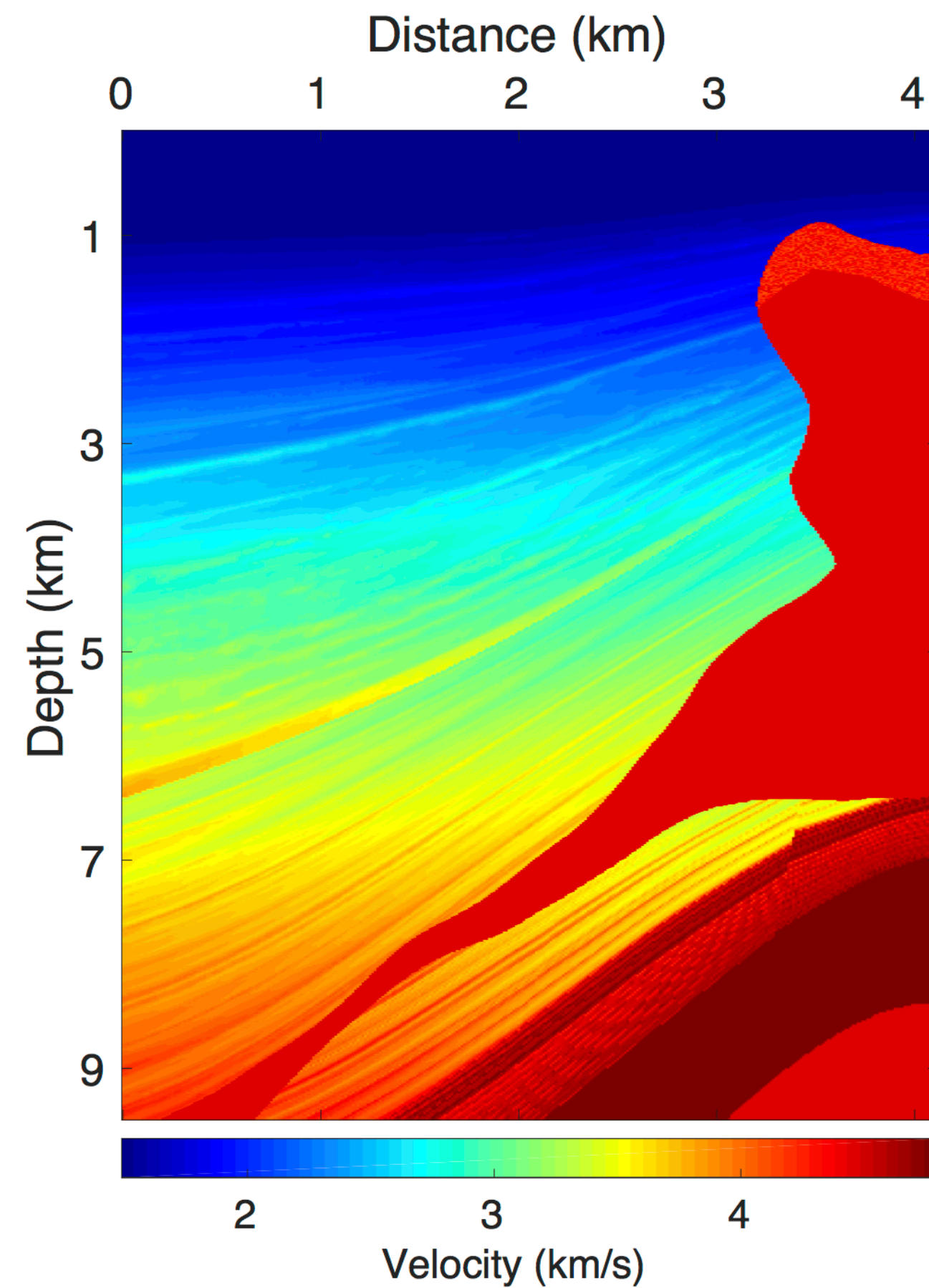
\* least possible overlap range  $> 0\%$  and  $< 5\%$  (depends on simultaneous acquisition design and subsampling factor)



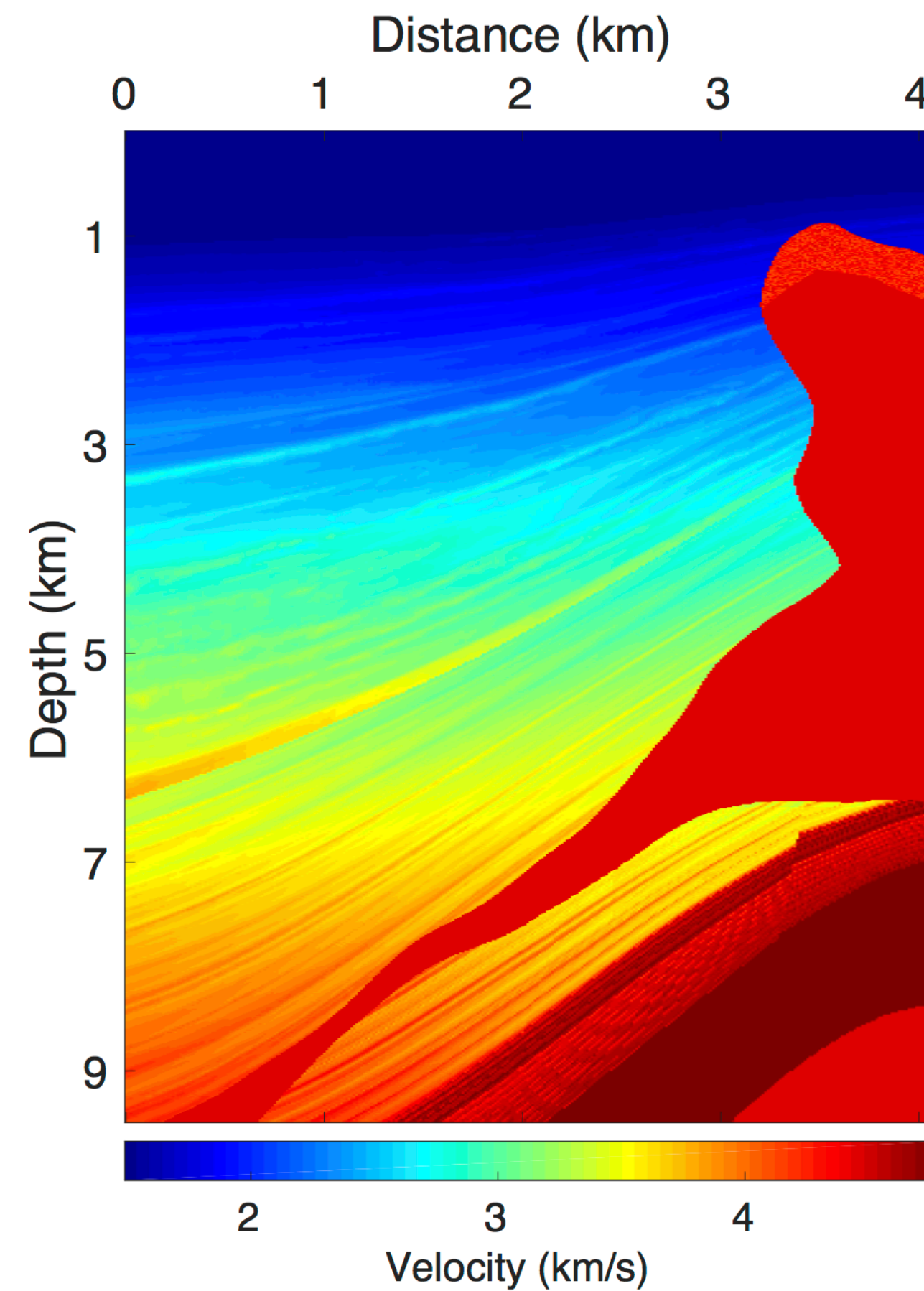
# SEAM Phase 1 model

– time-lapse difference via fluid substitution

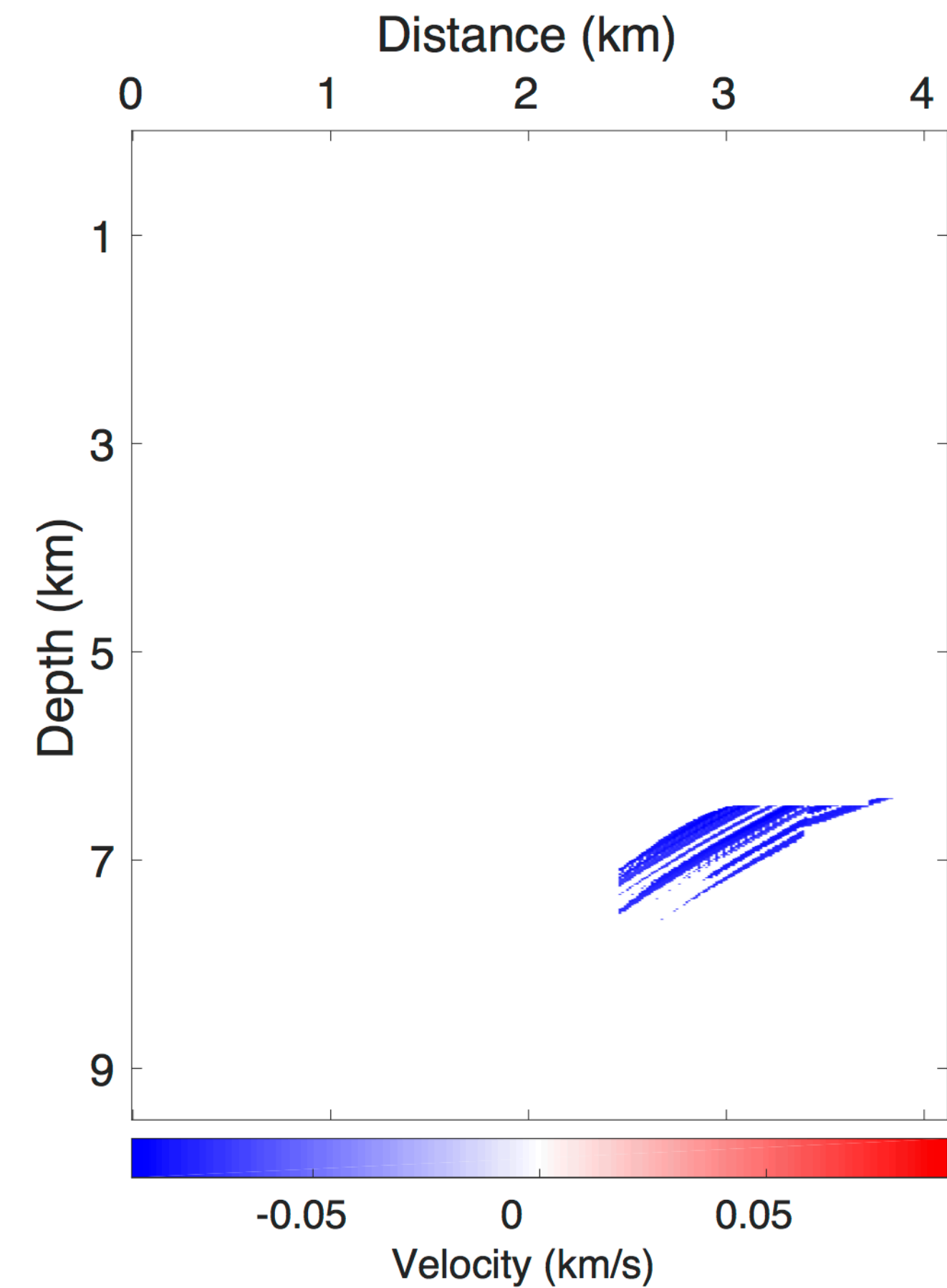
## Baseline



## Monitor



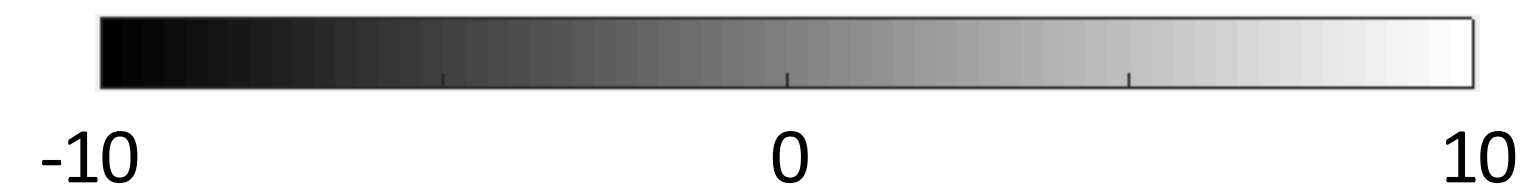
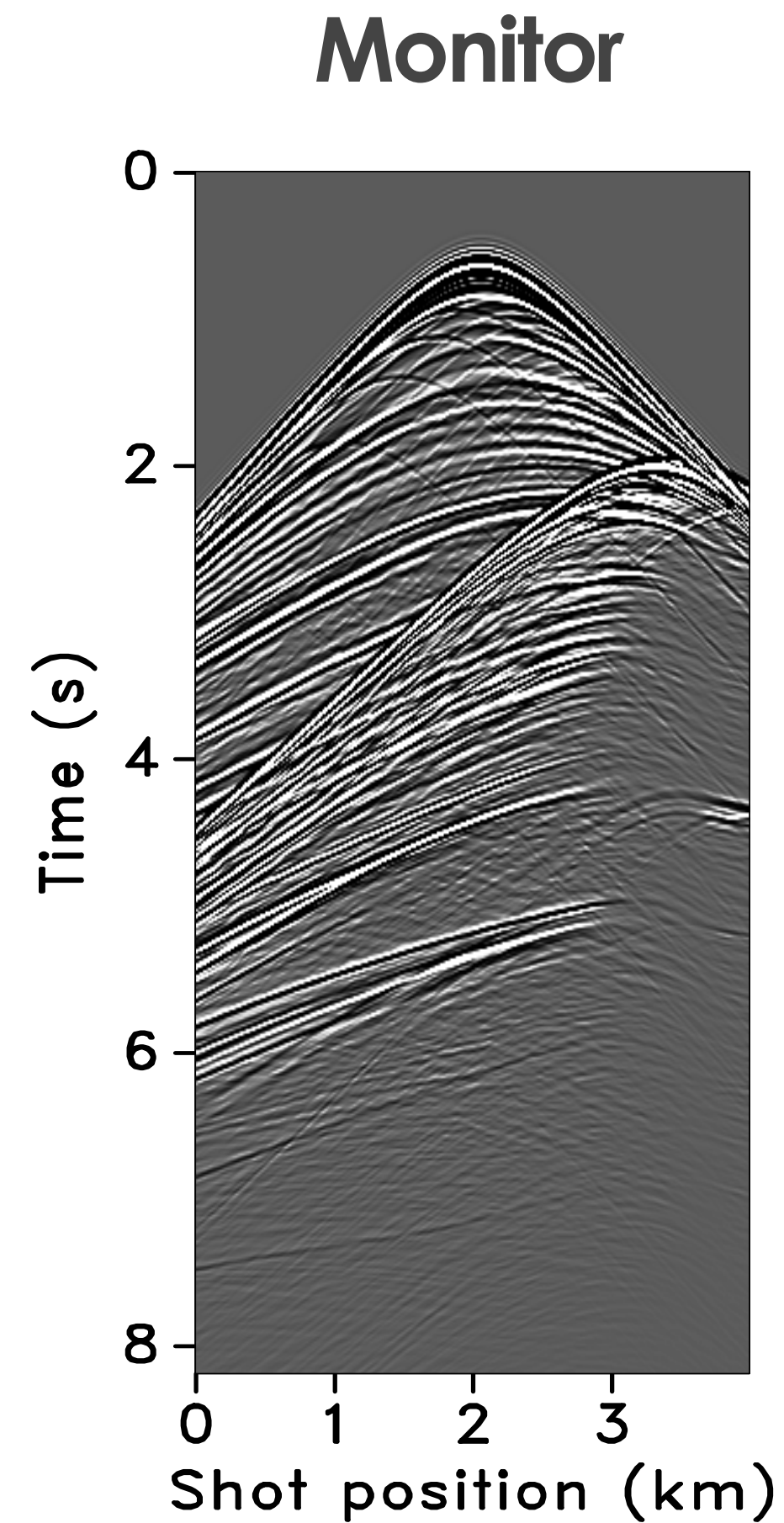
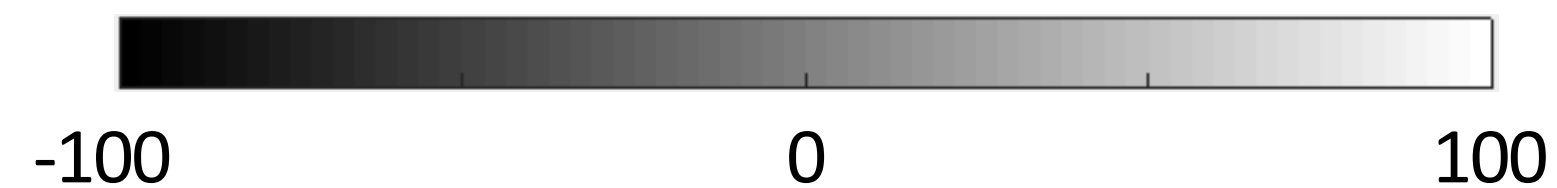
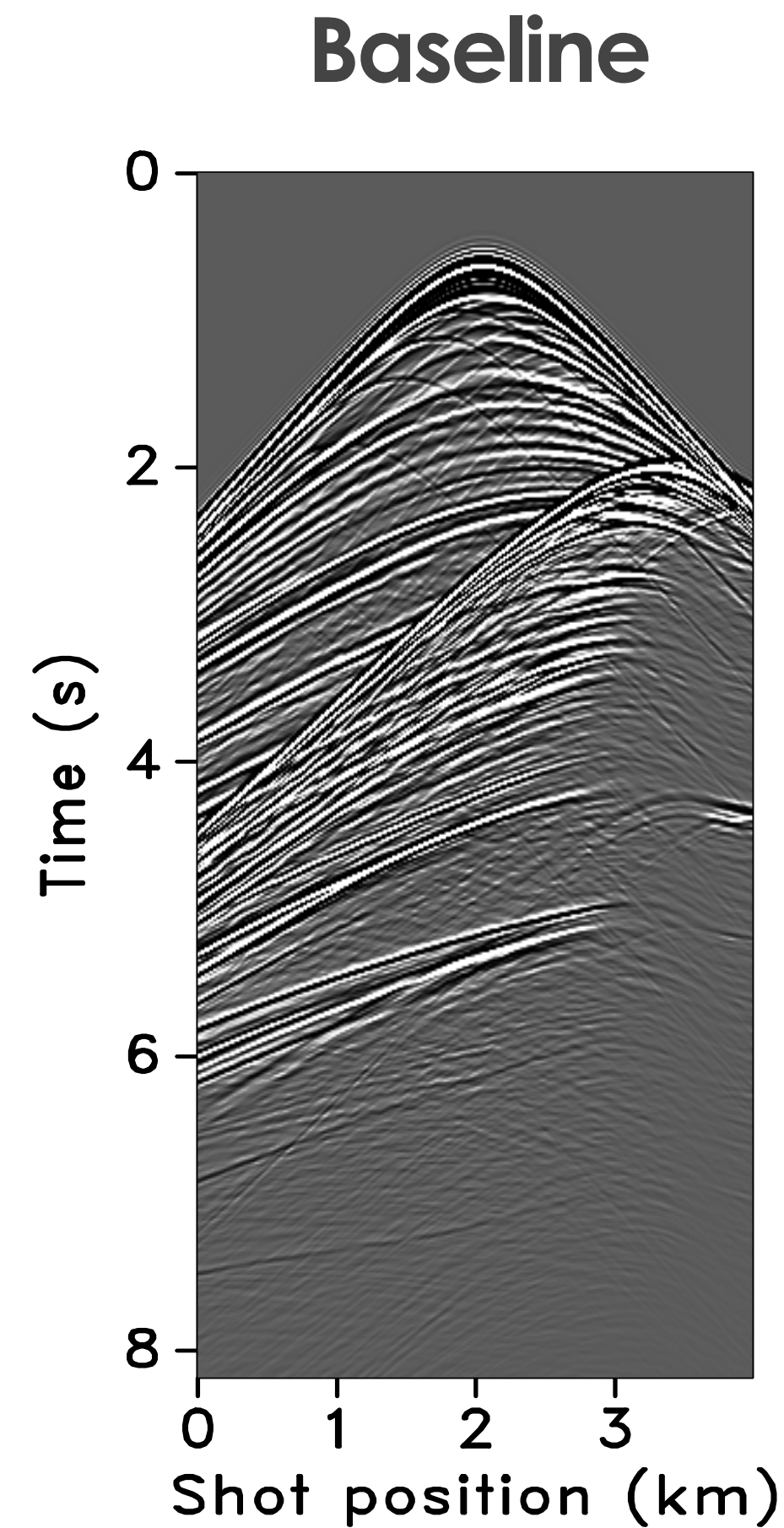
## Time-lapse difference



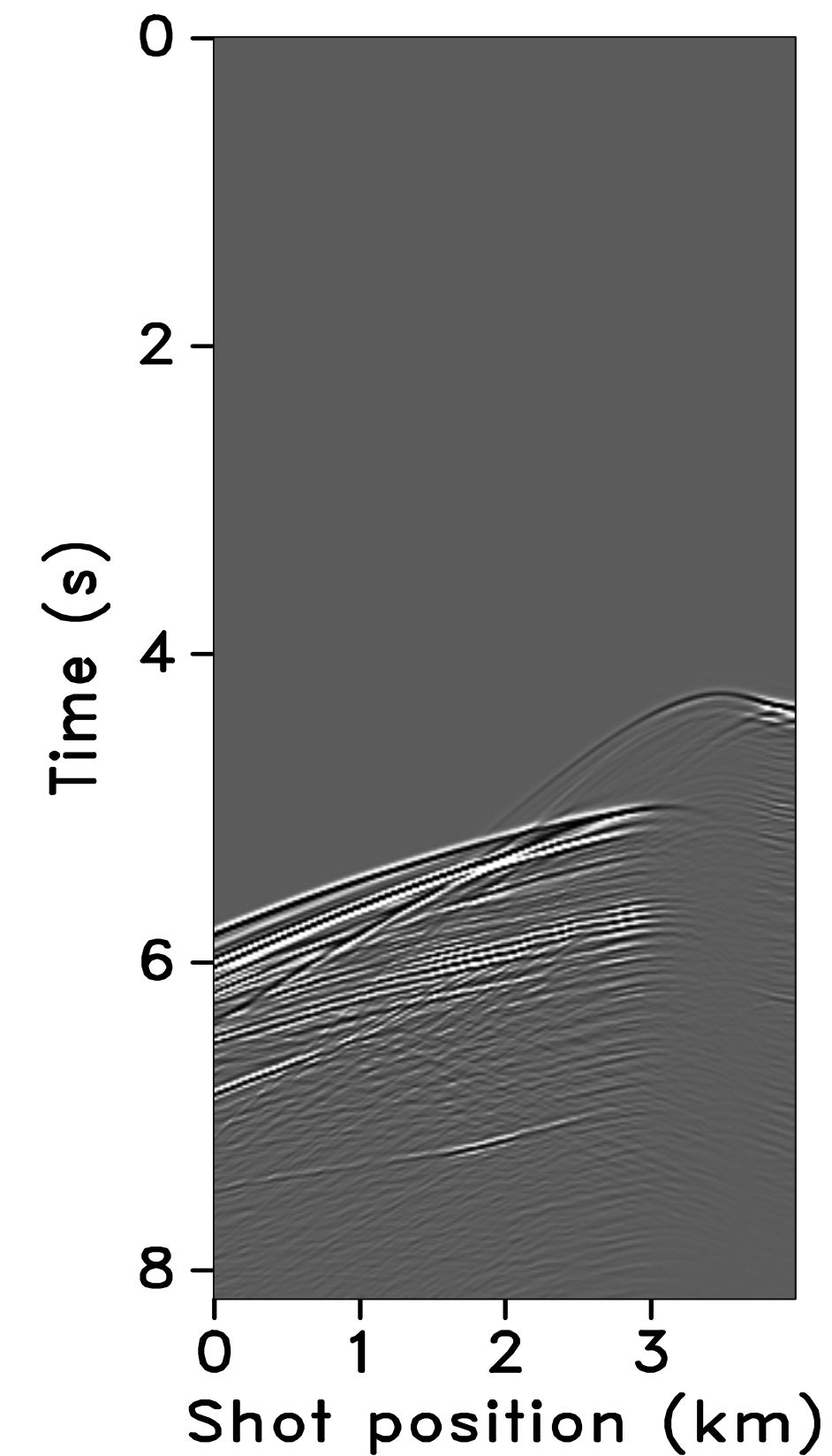


# Simulated time-lapse data

– time-domain finite differences



**4D signal**



time samples: **2048**  
receivers: **330**  
sources: **330**

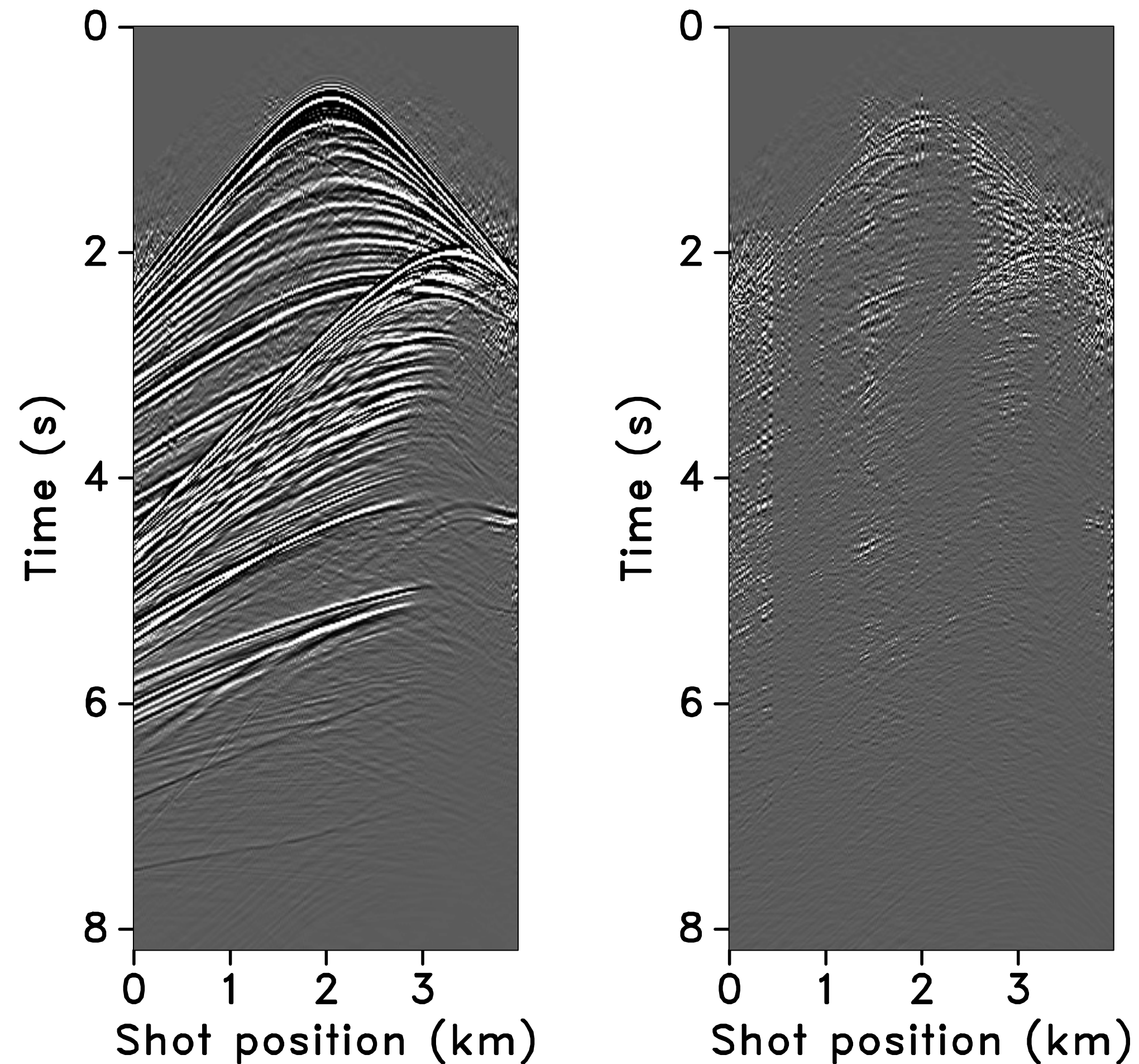
sampling  
time: **4.0 ms**  
receiver: **12.5 m**  
source: **12.5 m**



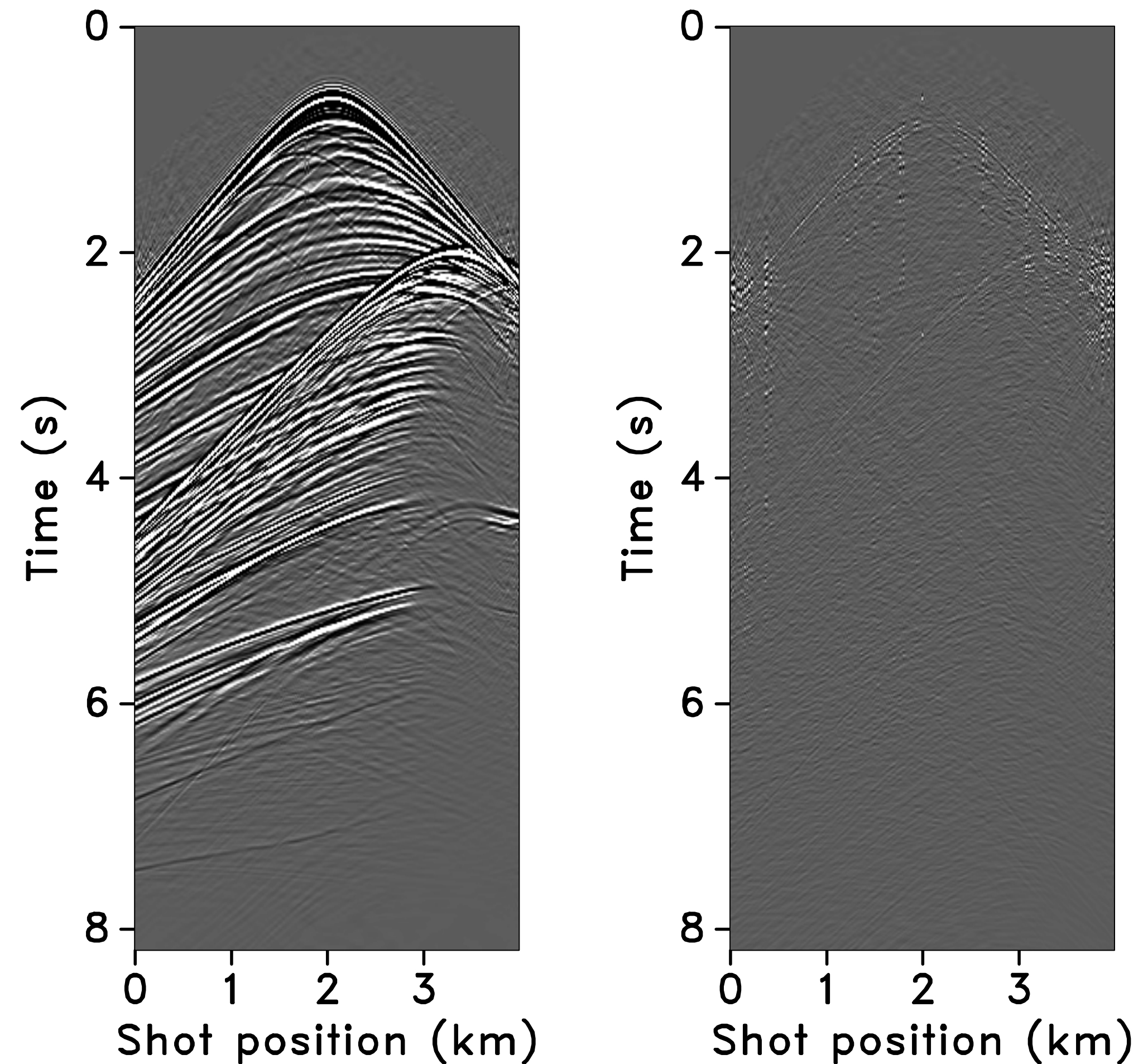
# Monitor recovery & residual

- **Joint recovery**; subsampling factor = 2

100% overlap [19.5 dB]



< 15% overlap [30.2 dB]

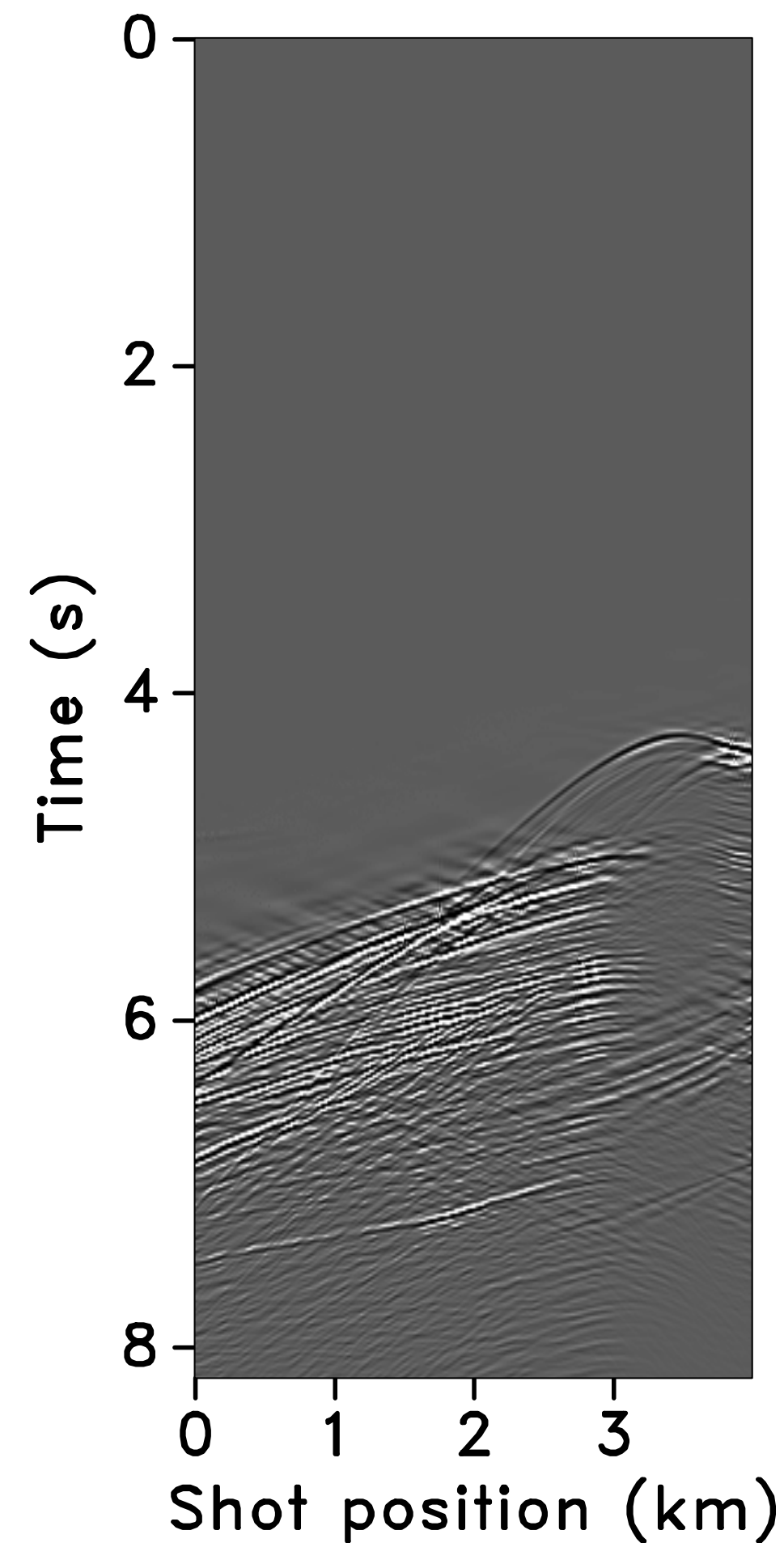
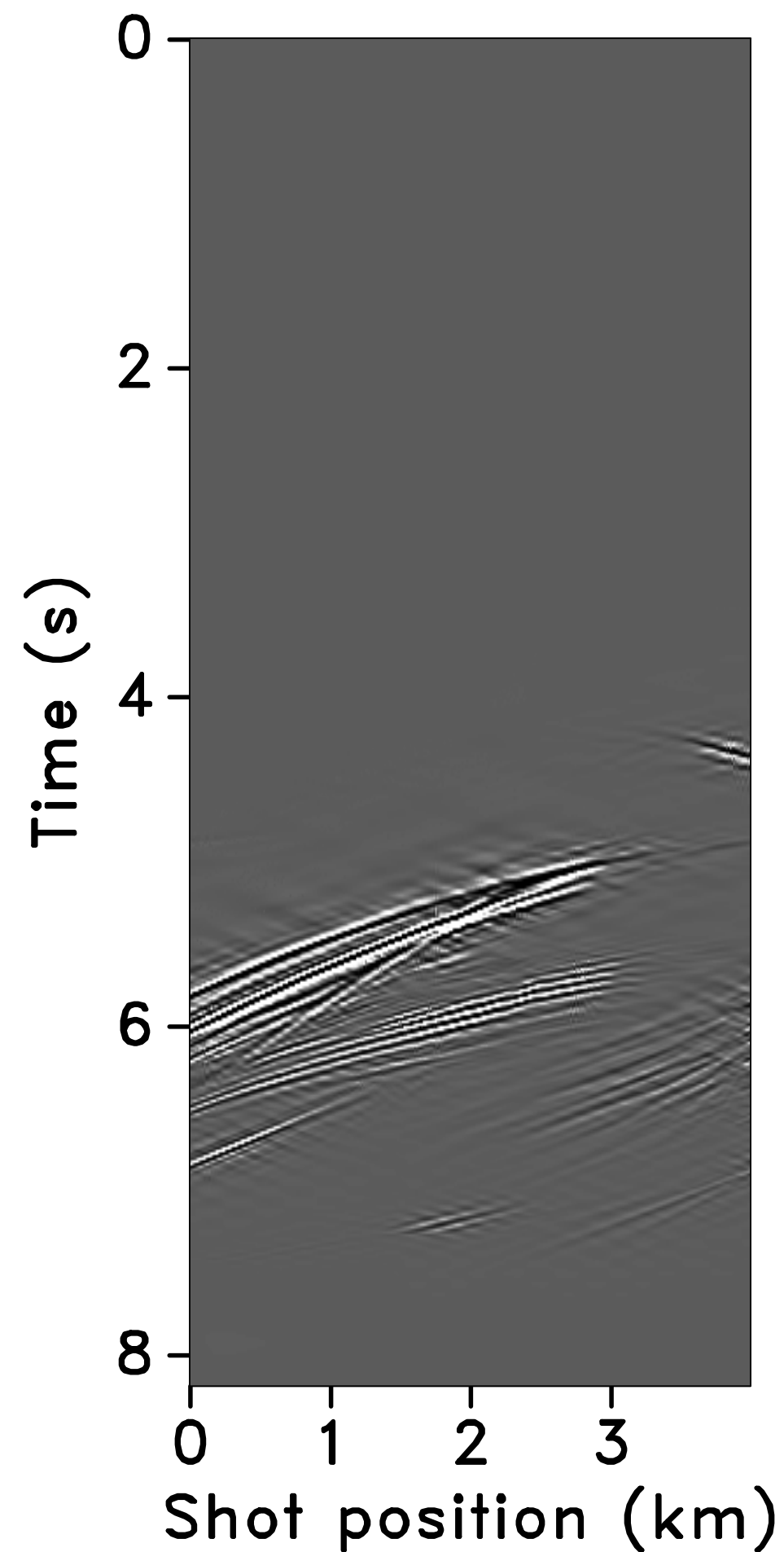




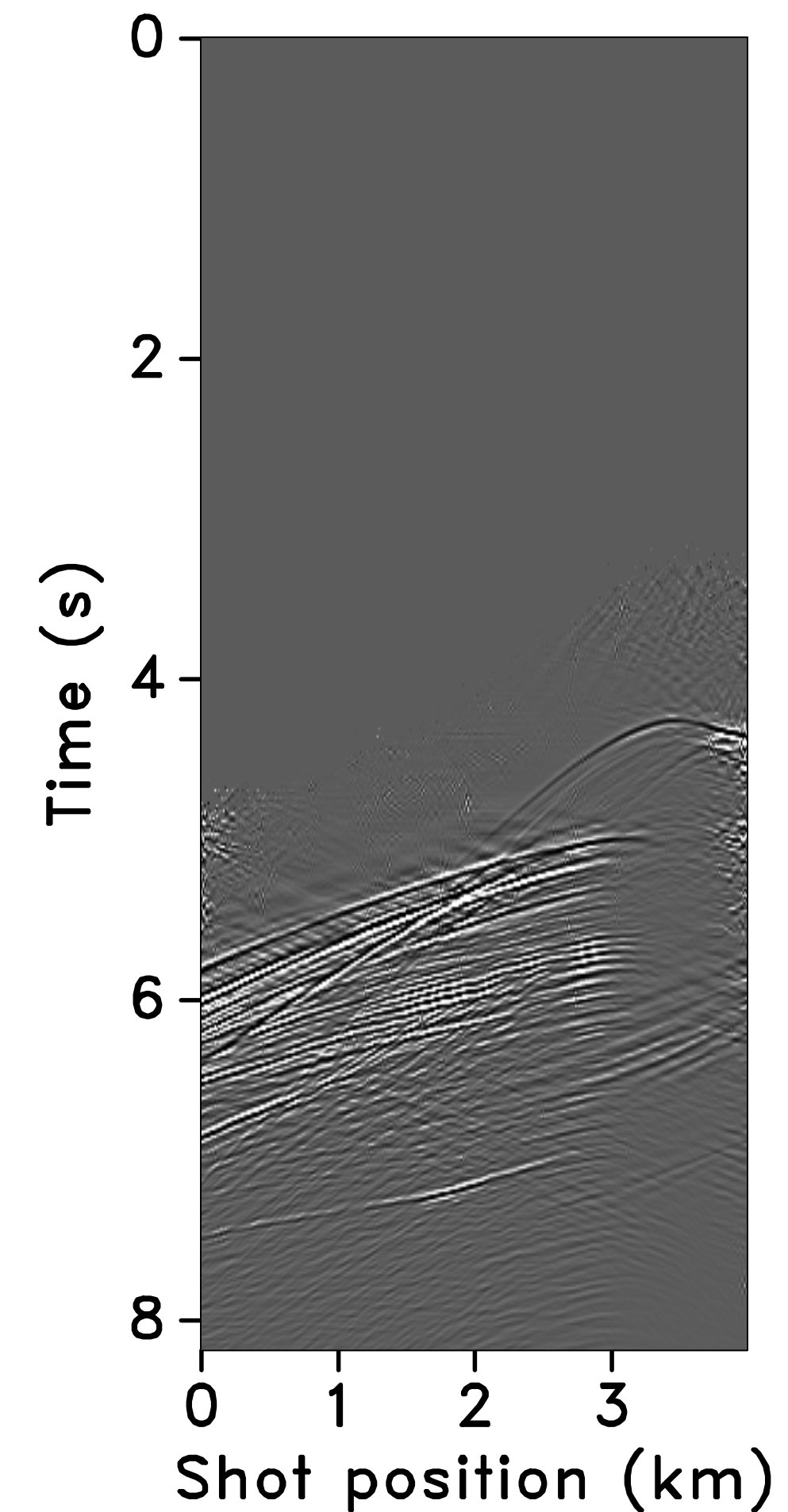
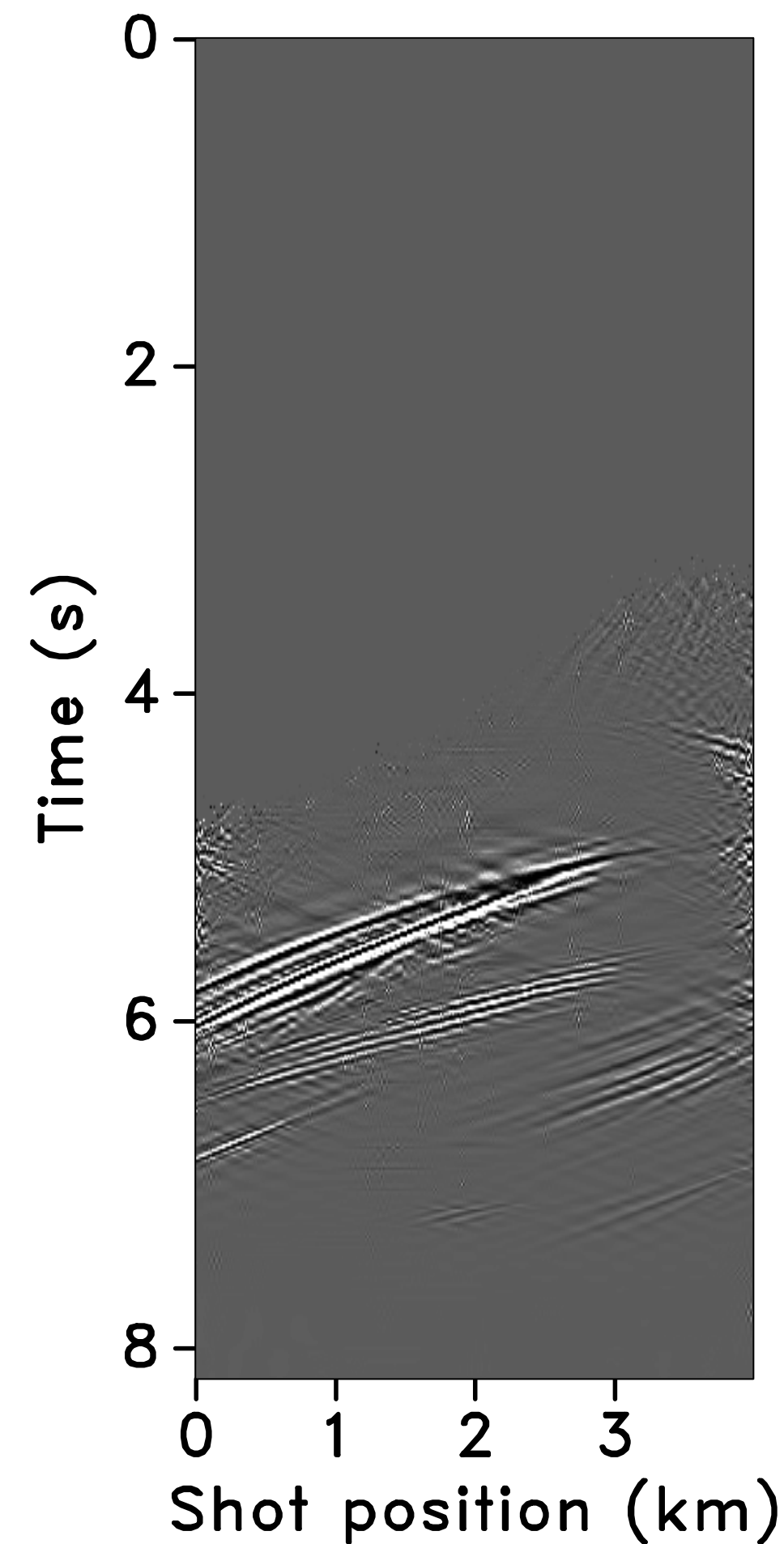
# 4D recovery & residual

- **Joint recovery**; subsampling factor = 2

100% overlap [9.6 dB]



< 15% overlap [6.8 dB]



# Conclusions

In the given context of randomized subsampling, position deviations

- have **little variability** on recovery of the time-lapse **difference**
- **improve** recovery of the **vintages**

Should we repeat compressive randomized time-lapse surveys?

- **Irregular sampling is inevitable in the real world** => “exact” replicability of surveys is naturally not possible
- Better to focus on knowing the shot positions post acquisition

**Embrace** natural **randomness** in the field or better purposefully randomize acquisitions to maximize collection of information



## Main contributions

Design of **pragmatic** simultaneous-source **time-jittered marine** acquisition

Adaptation of **NFDCT** for simultaneous-source acquisition and source separation

Design of **pragmatic** simultaneous-source **time-jittered time-lapse marine** acquisition with different overlaps between baseline & monitor surveys

## Main conclusions

CS ideas can be **successfully** adapted to seismic data acquisition

CS offers new **design** perspectives for seismic data acquisition schemes

Three **key** components:

- find representations that reveal structure, e.g., transform-domain sparsity
- sample to break structure, e.g., randomized acquisitions
- recover by structure promotion, e.g., sparsity via one-norm minimization

**Simultaneous-source acquisition** is an instance of compressive sensing

- **economic** acquisitions with **reduced** environmental **imprint**



# Main conclusions

## Time-lapse seismic

- **processing** time-lapse data **jointly** leads to improved recovery of the vintages with little variability in the time-lapse difference
- **irregular** sampling is **inevitable** in the real world => better to focus on knowing the shot positions post acquisition

**Embrace** natural **randomness** in the field or better purposefully randomize acquisitions to maximize collection of information

# Summary of publications

## Journal papers

**Low-cost time-lapse seismic with distributed compressive sensing --- Impact on repeatability**, Haneet Wason, Felix Oghenekohwo, and Felix J. Herrmann, *Geophysics*, 82, P15--P30.

**Low-cost time-lapse seismic with distributed compressive sensing --- Exploiting common information among the vintages**, Felix Oghenekohwo, Haneet Wason, Ernie Esser, and Felix J. Herrmann, *Geophysics*, 82, P1--P13.

**Source separation for simultaneous towed-streamer marine acquisition --- A compressed sensing approach**, Rajiv Kumar\*, Haneet Wason\*, and Felix J. Herrmann, *Geophysics*, 80, WD73--WD88. \*Equal contribution.

**Randomized marine acquisition with compressive sampling matrices**, Hassan Mansour, Haneet Wason, Tim T.Y. Lin, and Felix J. Herrmann, *Geophysical Prospecting*, 60, 648--662.

**Compressive sensing in seismic exploration: An outlook on a new paradigm**, Felix J. Herrmann, Haneet Wason, and Tim T.Y. Lin, *CSEG Recorder*, 36, Part I [April Edition], 19--33; Part II [June Edition], 34--39.



# Summary of publications

## Conference proceedings

**Compressed sensing in 4D marine --- Recovery of dense time-lapse data from subsampled data without repetition**, Haneet Wason, Felix Oghenekohwo, and Felix. J. Herrmann, EAGE Conference & Exhibition 2015.

**SVD-free matrix completion in randomized marine acquisition**, Oscar Lopez, Haneet Wason, Curt Da Silva, Rajiv Kumar, and Felix. J. Herrmann, SEG Annual Meeting Workshop 2015.

**Randomization and repeatability in time-lapse marine acquisition**, Haneet Wason, Felix Oghenekohwo, and Felix. J. Herrmann, SEG Annual Meeting 2014.

**Source-separation via SVD-free rank minimization in the hierarchical semi-separable representation**, Haneet Wason, Rajiv Kumar, and Felix. J. Herrmann, SEG Annual Meeting 2014.

**Time-jittered ocean bottom seismic acquisition**, Haneet Wason, and Felix. J. Herrmann, SEG Annual Meeting 2013.

**Only dither: efficient simultaneous marine acquisition**, Haneet Wason, and Felix. J. Herrmann, EAGE Conference & Exhibition 2012.

**Sparsity-promoting recovery from simultaneous data: A compressive sensing approach**, Haneet Wason, and Felix. J. Herrmann, SEG Annual Meeting 2011.

## Future research directions

Develop a computationally faster and memory efficient implementation of 2D & 3D curvelet transforms

Improve recovery of weak late-arriving events with weighted one-norm minimization

Develop robust algorithms to use simultaneous-source data directly in imaging and inversion

Improve sparse time-lapse data recoveries with  $\gamma$ -weighted one-norm formulation for DCS:

$$\tilde{\mathbf{z}} = \arg \min_{\mathbf{z}} \gamma_0 \|\mathbf{z}_0\|_1 + \gamma_1 \|\mathbf{z}_1\|_1 + \gamma_2 \|\mathbf{z}_2\|_1 \quad \text{subject to} \quad \mathbf{y} = \mathbf{A}\mathbf{z}$$



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# Thank you!

To my advisor, committee, and everyone at SLIM.