

# Machine learning applications to geophysical data analysis

Ben Bougher, August 15th 2016

## Contributions

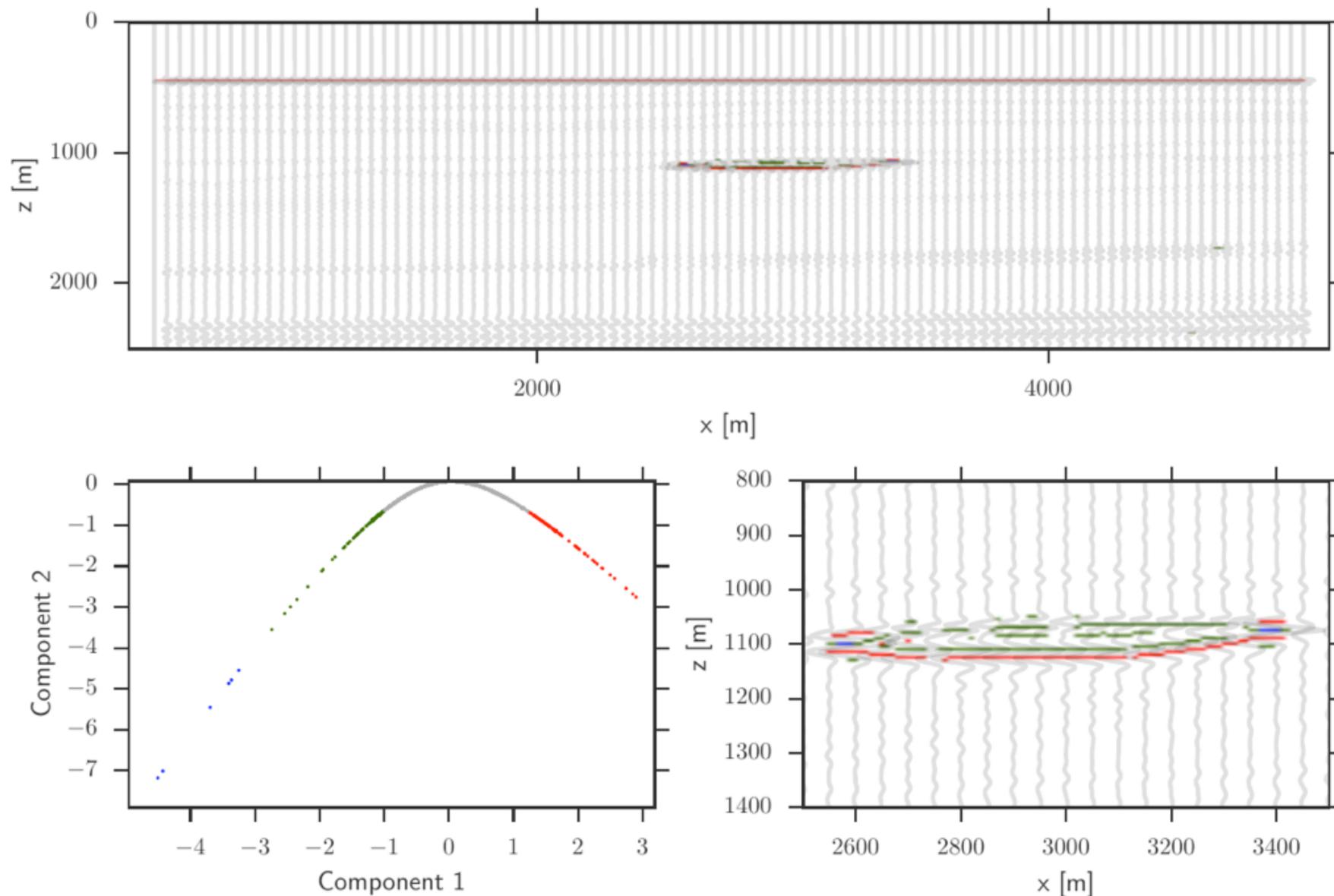
### **Predicting stratigraphic units from well logs using supervised learning**

- Novel use of the scattering transform as a feature representation of well logs.
- CSEG 2015 expanded abstract, honorable mention for best student talk.
- Published article in the CSEG Recorder (Jan 2015).

### **Reflection seismology as an unsupervised learning problem**

- Generalized and automated a hydrocarbon exploration analysis workflow.
- Reservoir discovery as convex optimization.
- Accepted abstract, to be presented @SEG (Houston, 2016)

# Reflection seismology as an unsupervised learning problem



## Motivation:

Inability to discover hydrocarbons directly from seismic data.

## Problem:

Automatically segment potential hydrocarbon reserves from seismic images.

## Approaches:

Physics driven (conventional)  
Data driven (thesis contributions)

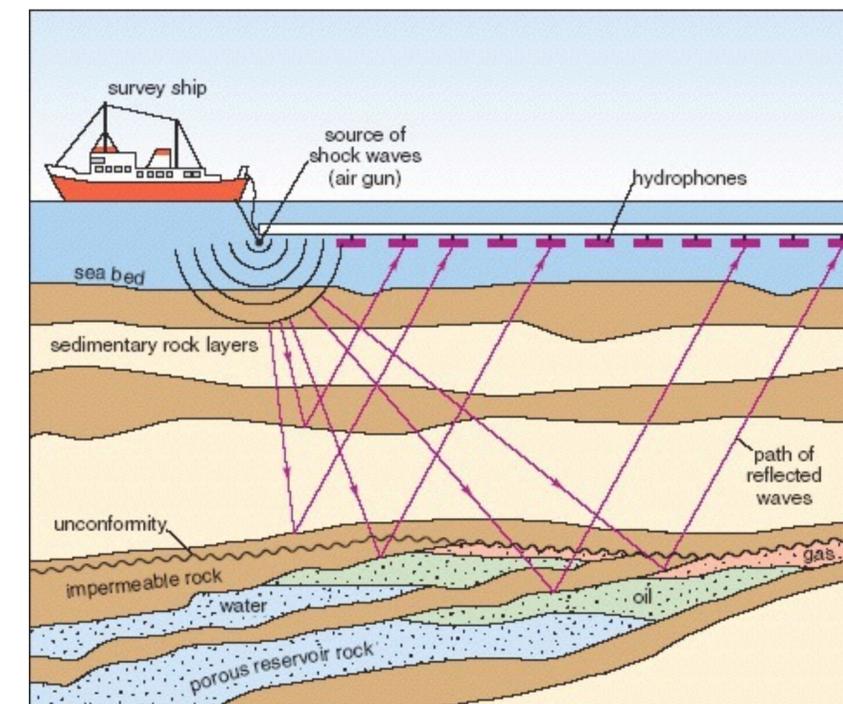
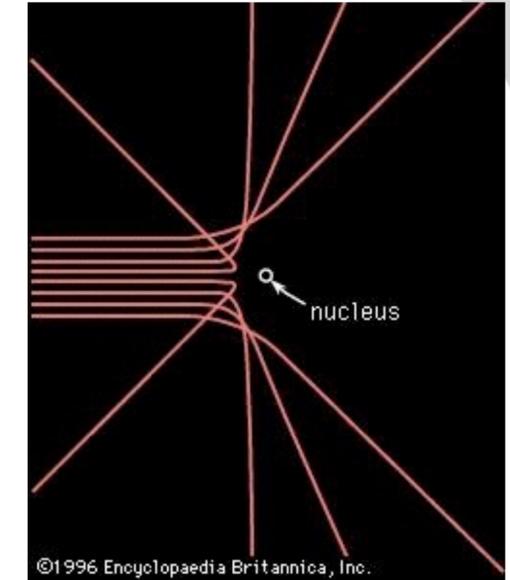
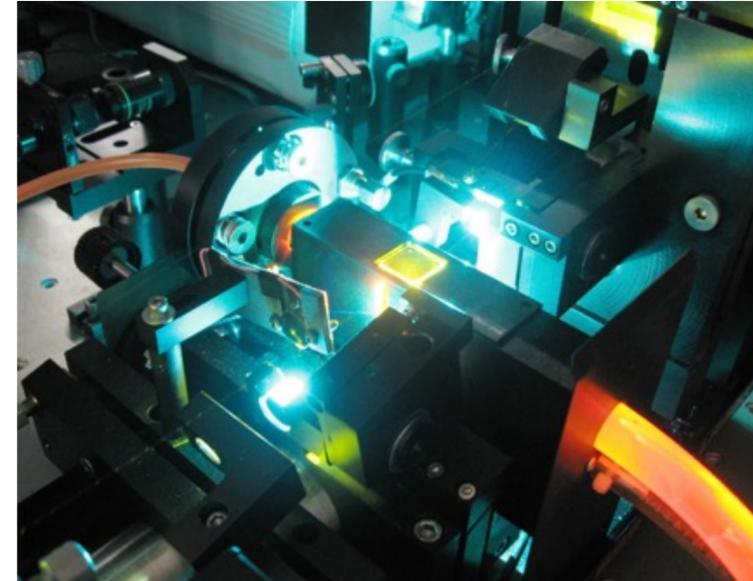
# Scattering physics

Ubiquitous in experimental physics.

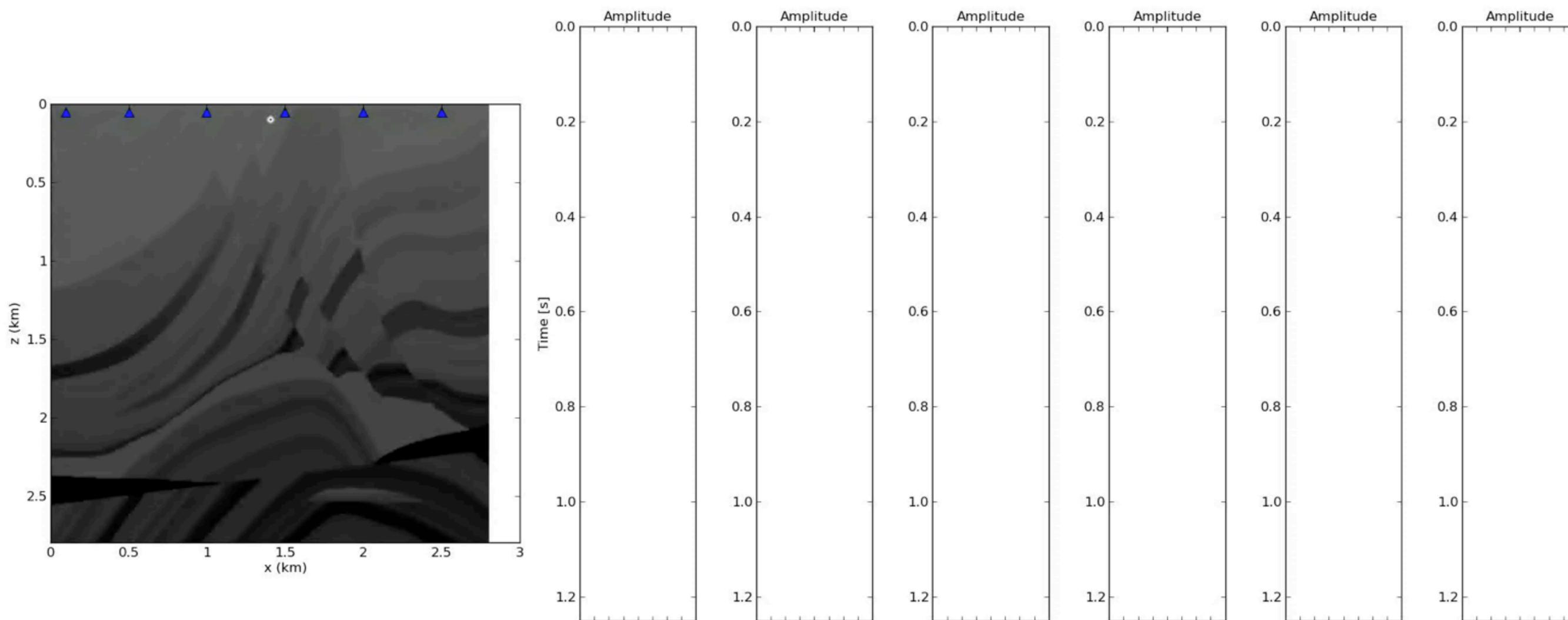
Measure the scattering pattern from a known source incident on a material.

Performed in highly controlled and calibrated laboratories (laser sources, temperature controlled, vacuums, etc...).

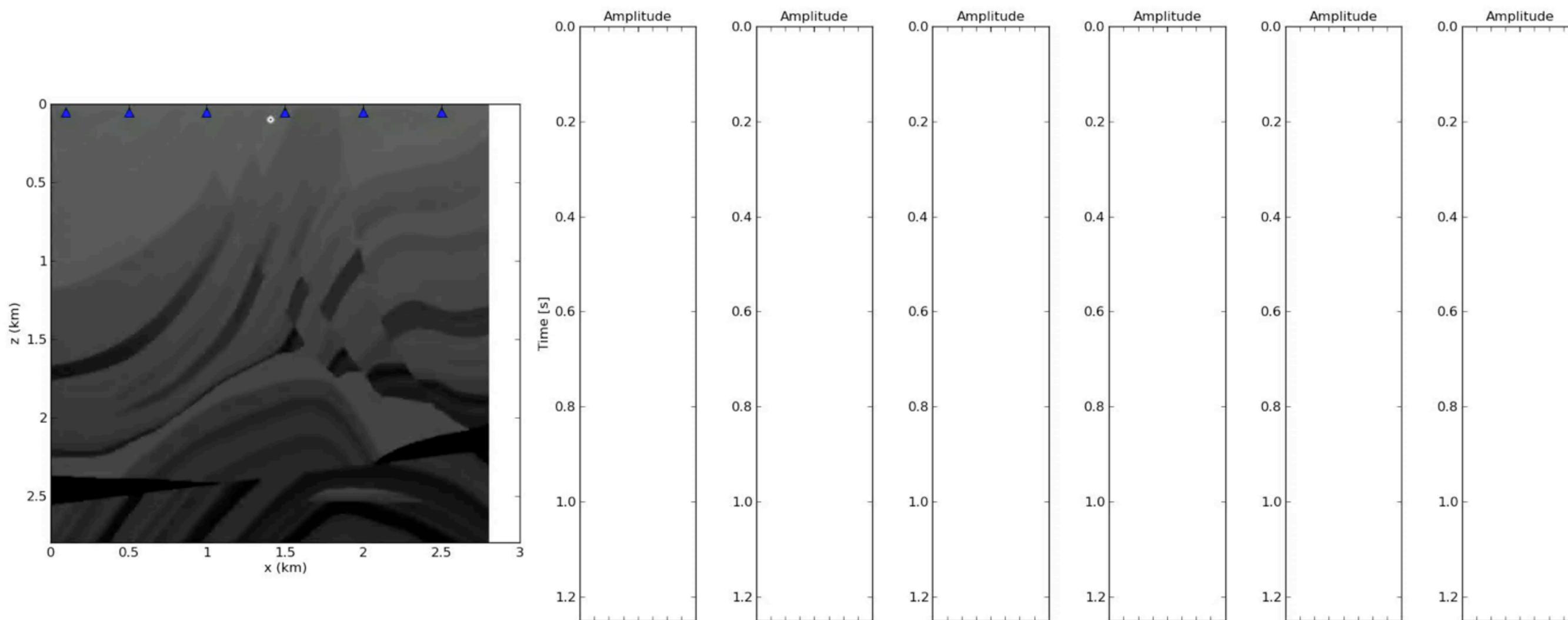
**Reflection seismology is a scattering experiment in an uncontrolled environment.**



# Seismic experiment

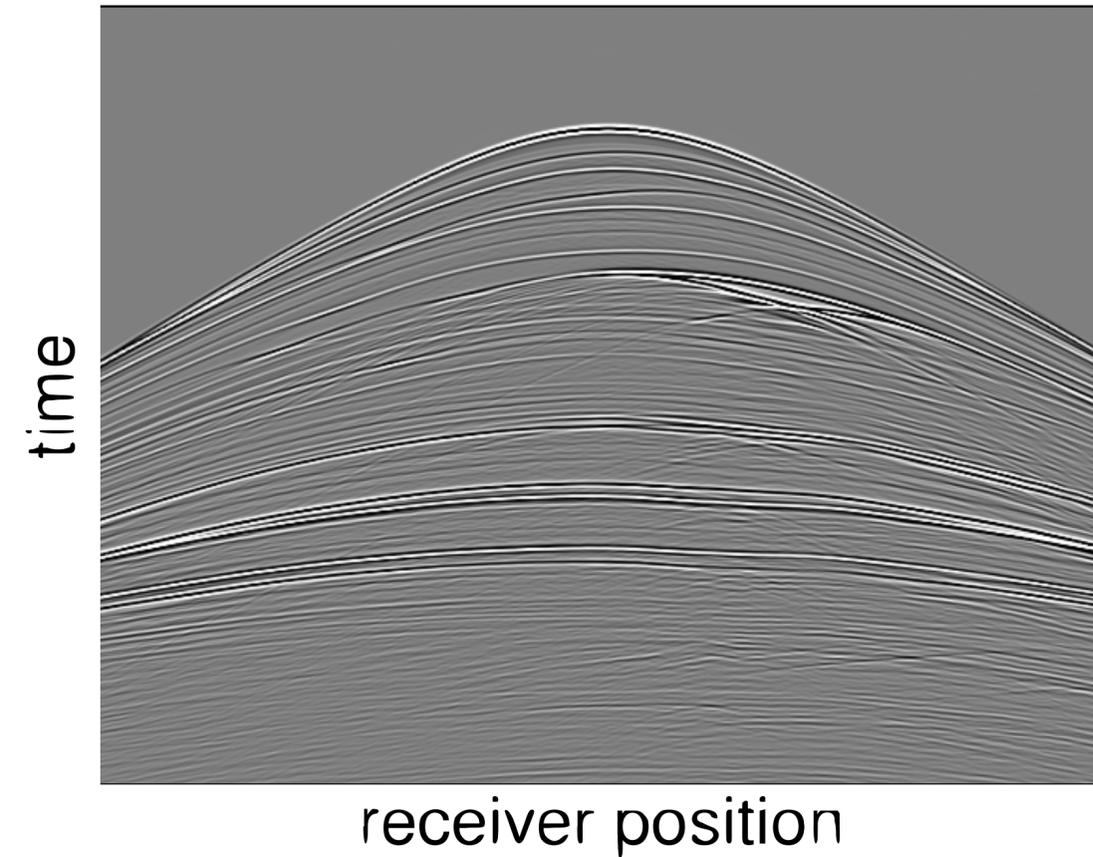


# Seismic experiment

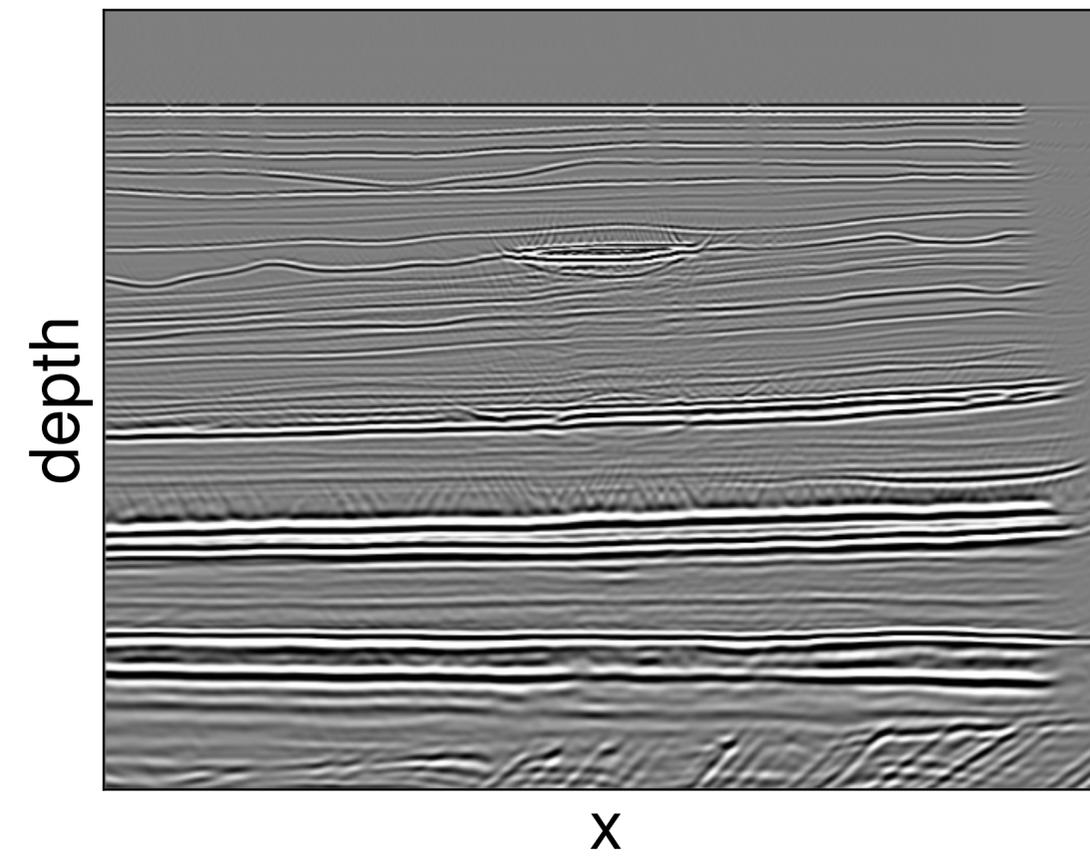


# Migration

Shot Record

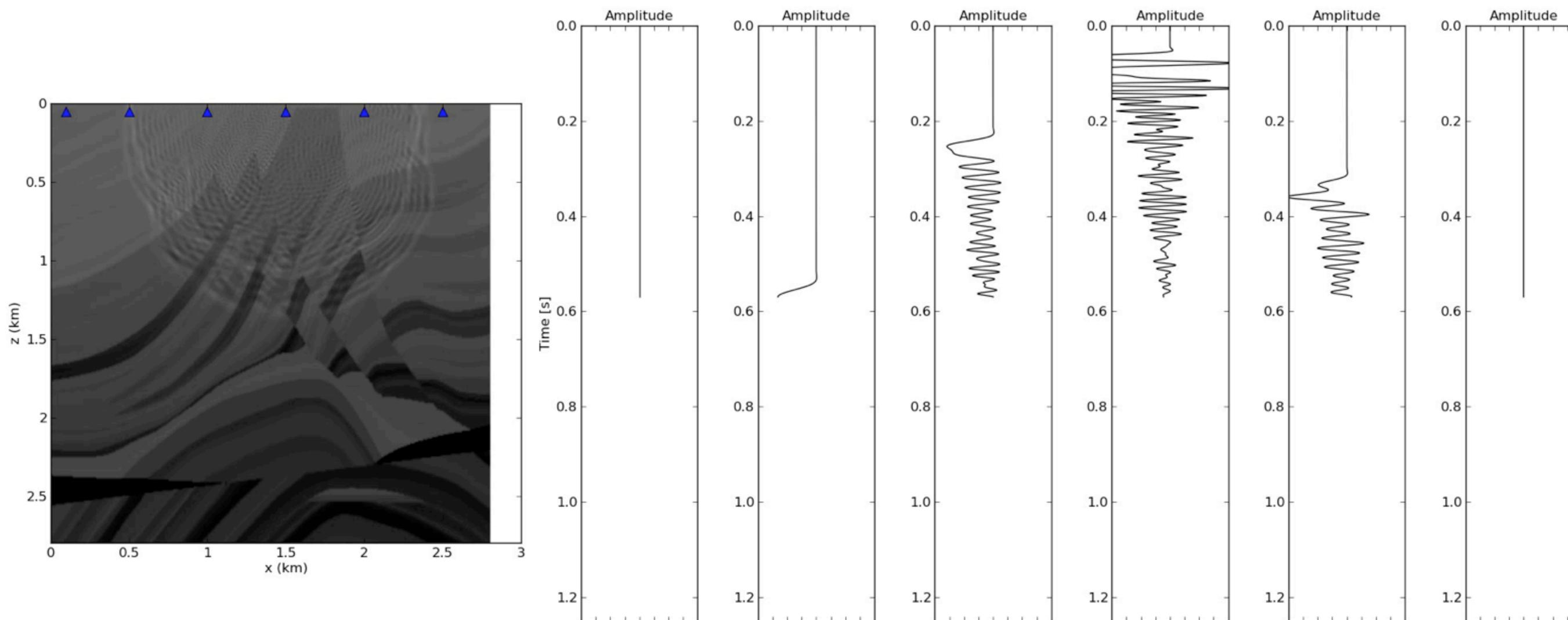


Migrated Image

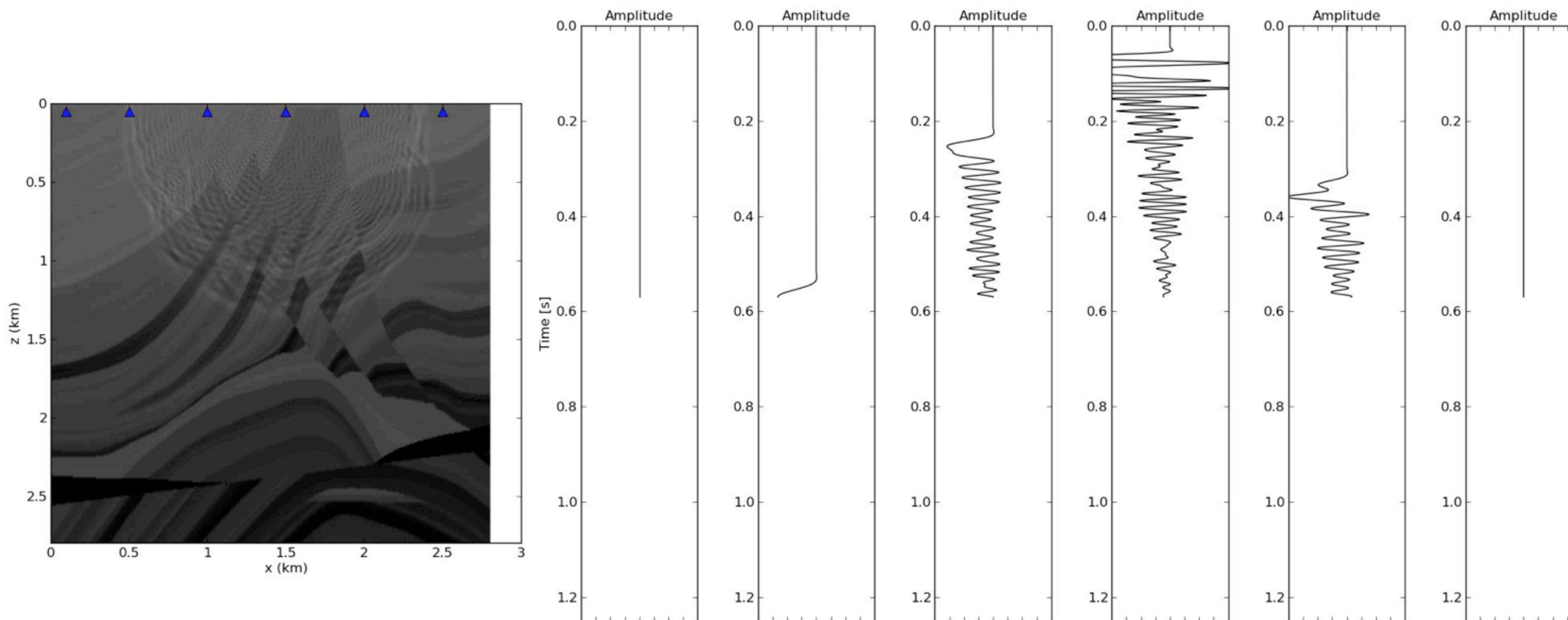


Migration maps **shot records** of **reflections** recorded at the surface into **images** of the subsurface.

# Migration



# Migration



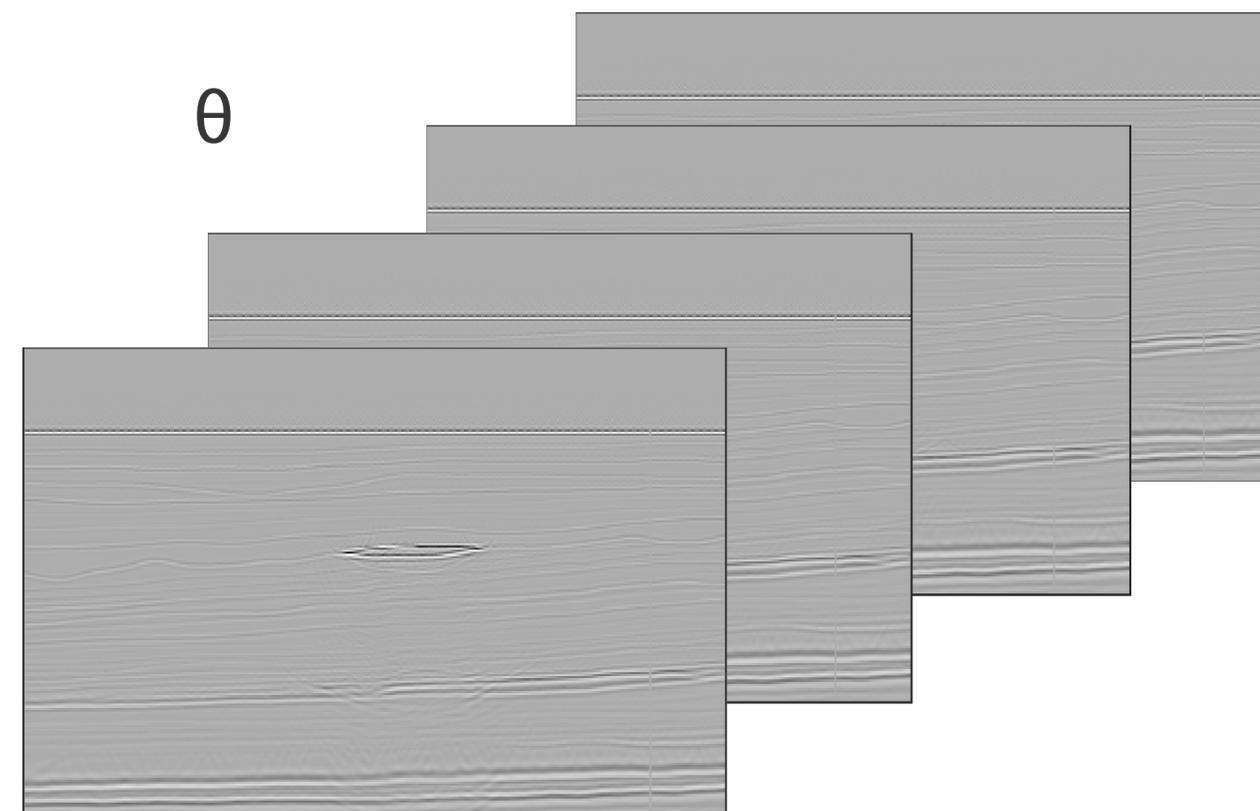
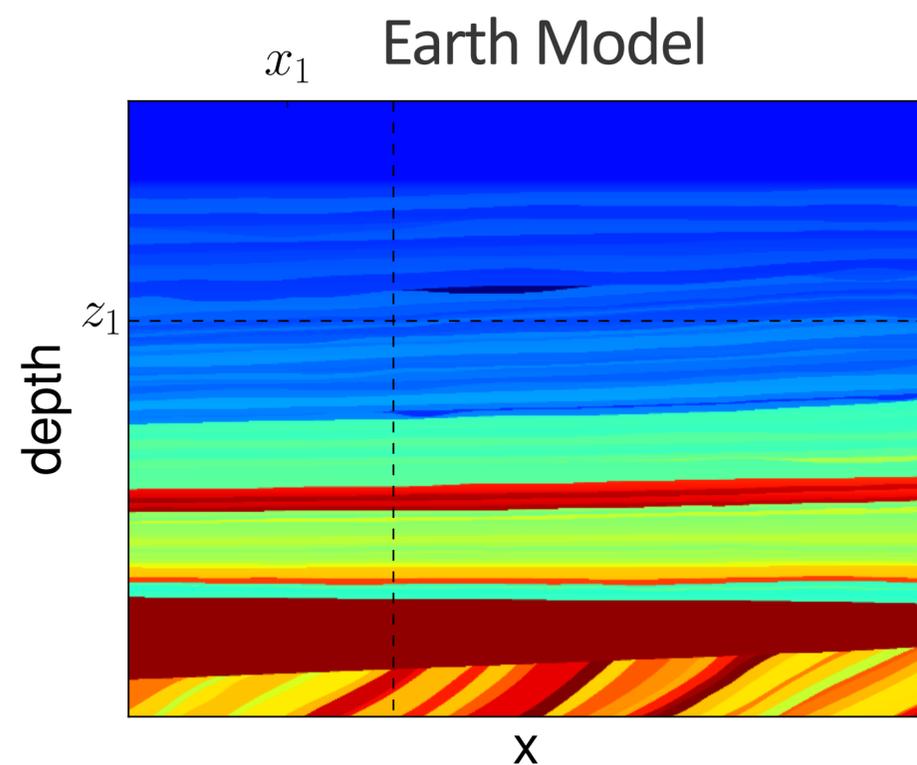
# Angle domain common image gathers

## Problem:

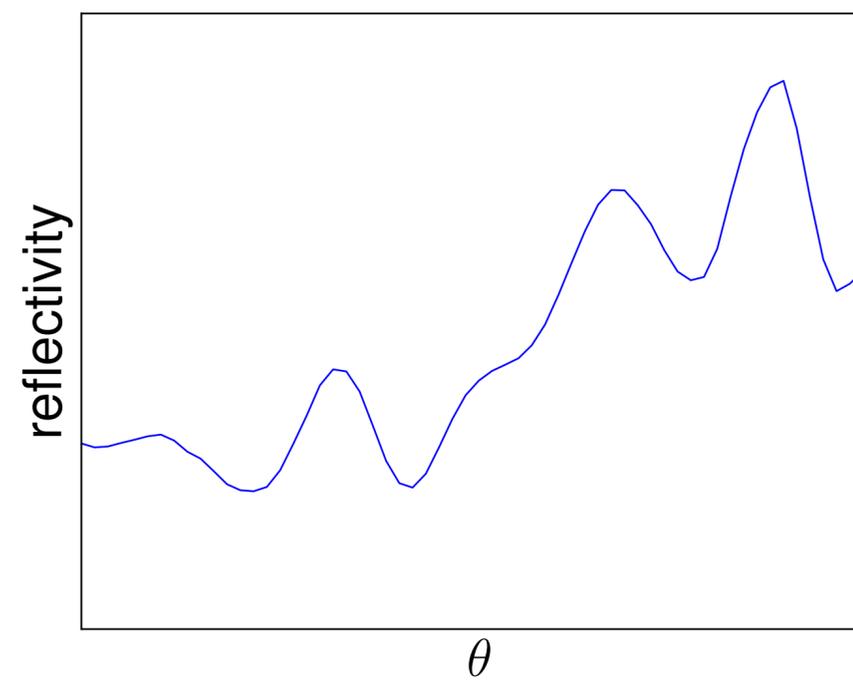
Need angle dependent reflectivity responses

## Solution:

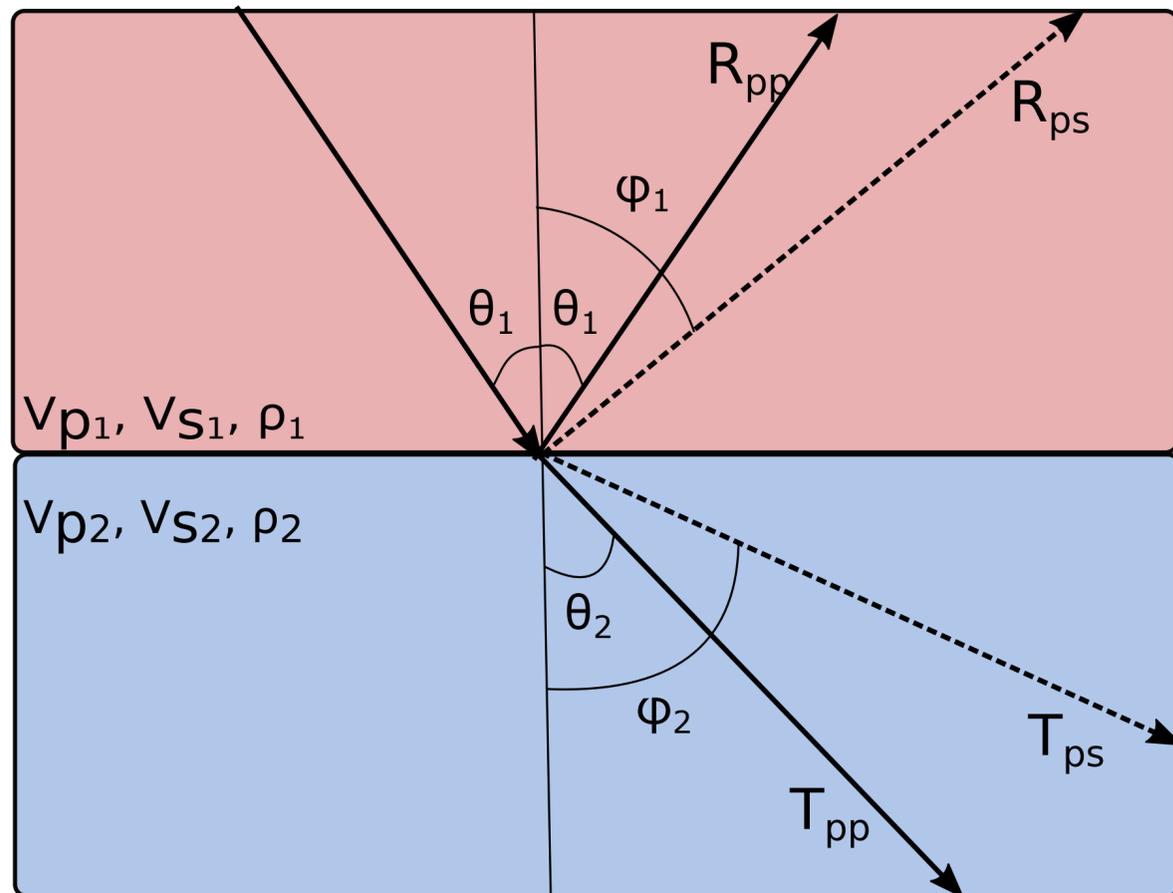
Angle domain common image gather migration



$R(\theta)$  at  $(x_1, z_1)$



# Scattering theory (Zoeppritz)



## Problem:

Relate angle dependent reflectivity to rock physics.

**Assumption:** Ray theory approximation.

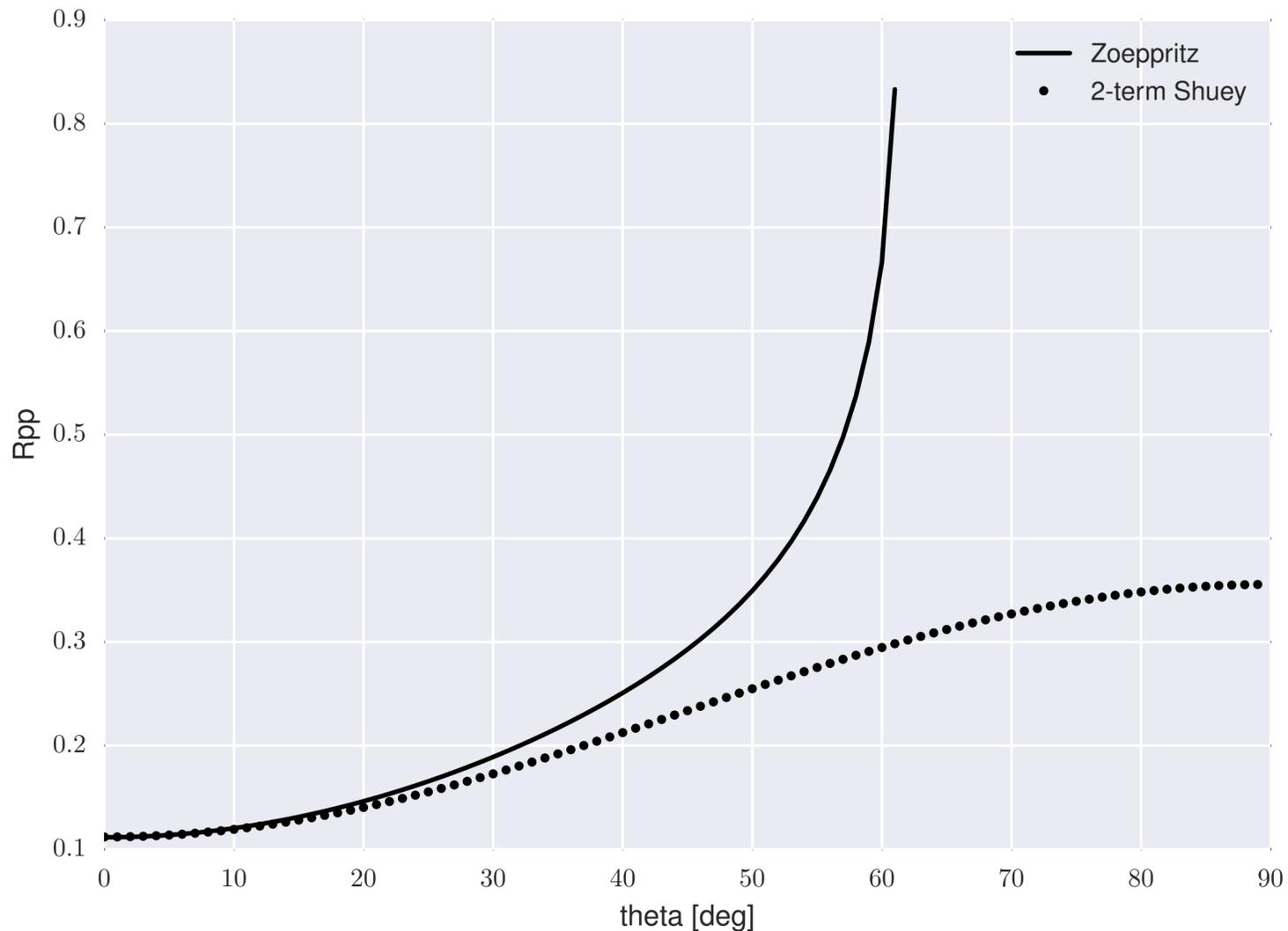
**Solution:**  $R(\theta) \propto V_P, V_S, \rho$

**Problem:** Non-linear, not useful for inversion.

$$\begin{bmatrix} R_{PP} \\ R_{PS} \\ T_{PP} \\ T_{PS} \end{bmatrix} = \begin{bmatrix} -\sin \theta_1 & -\cos \phi_1 & \sin \theta_2 & \cos \phi_2 \\ \cos \theta_1 & -\sin \phi_1 & \cos \theta_2 & -\sin \phi_2 \\ \sin 2\theta & \frac{V_{P1}}{V_{S1}} \cos 2\phi_1 & \frac{\rho_2 V_{S2}^2 V_{P1}}{\rho_1 V_{S1}^2 V_{P2}} \cos 2\theta_1 & \frac{\rho_2 V_{S2} V_{P1}}{\rho_1 V_{S1}^2} \cos 2\phi_2 \\ -\cos \phi_2 & \frac{V_{S1}}{V_{P1}} \sin 2\phi_1 & \frac{\rho_2 V_{P2}}{\rho_1 V_{P1}} & \frac{\rho_2 V_{S2}}{\rho_1 V_{P1}} \sin 2\phi_2 \end{bmatrix}^{-1} \begin{bmatrix} \sin \theta_1 \\ \cos \theta_1 \\ \sin 2\theta_1 \\ \cos 2\phi_1 \end{bmatrix}$$

# Scattering theory (Shuey)

$R(\theta)$  at  $(x_1, z_1)$



## Shuey approximation

$$R_{pp}(\theta) = i(\Delta V_P, \Delta \rho) + g(\Delta V_P, \Delta V_S, \Delta \rho) \sin^2 \theta$$

### Limitations:

Small perturbations over a background trend  
valid < 30 degrees

### Benefits:

linear for  $i$  and  $g$   
invert using simple least squares

# Shuey term inversion as a projection

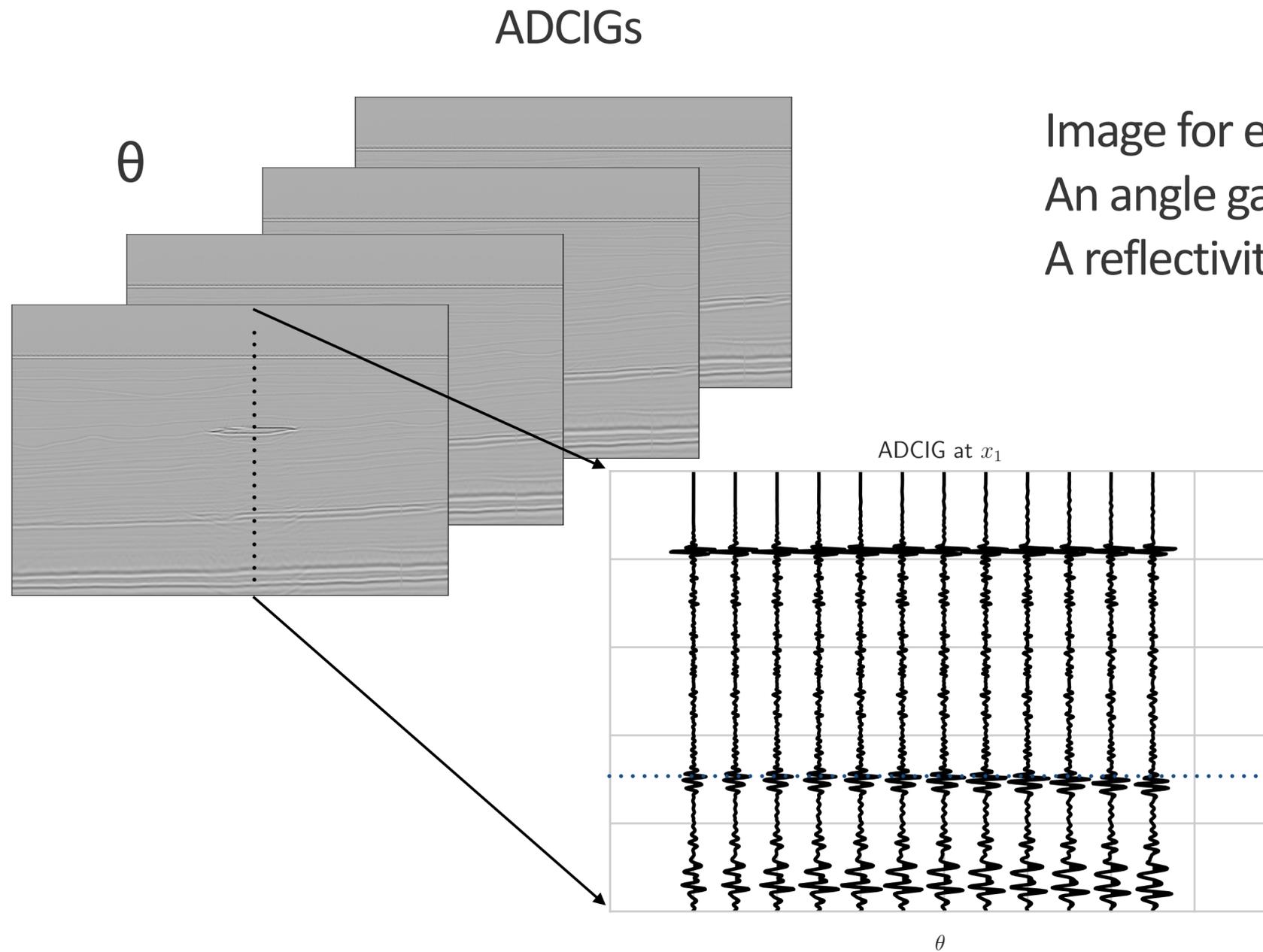
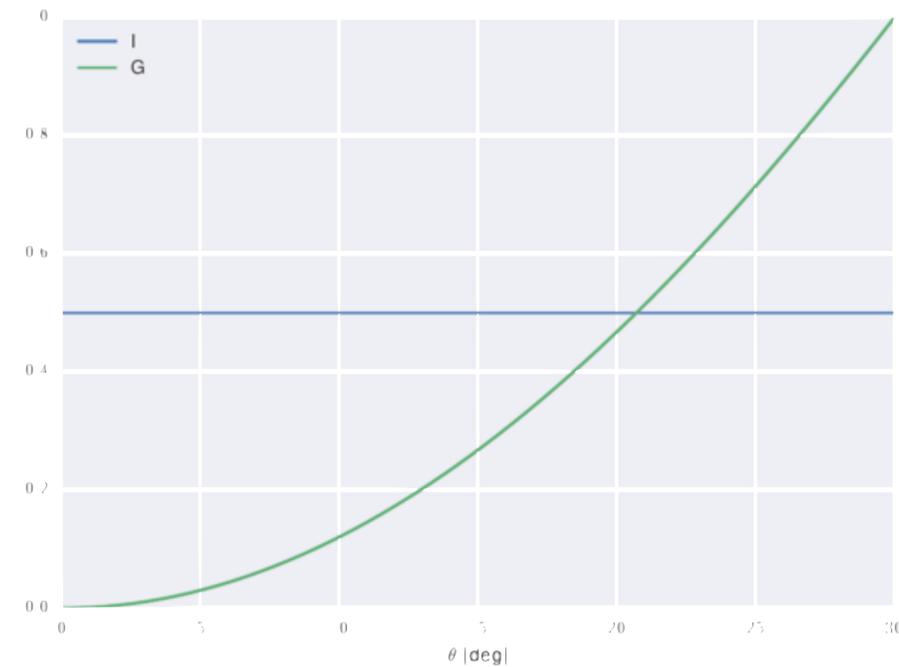
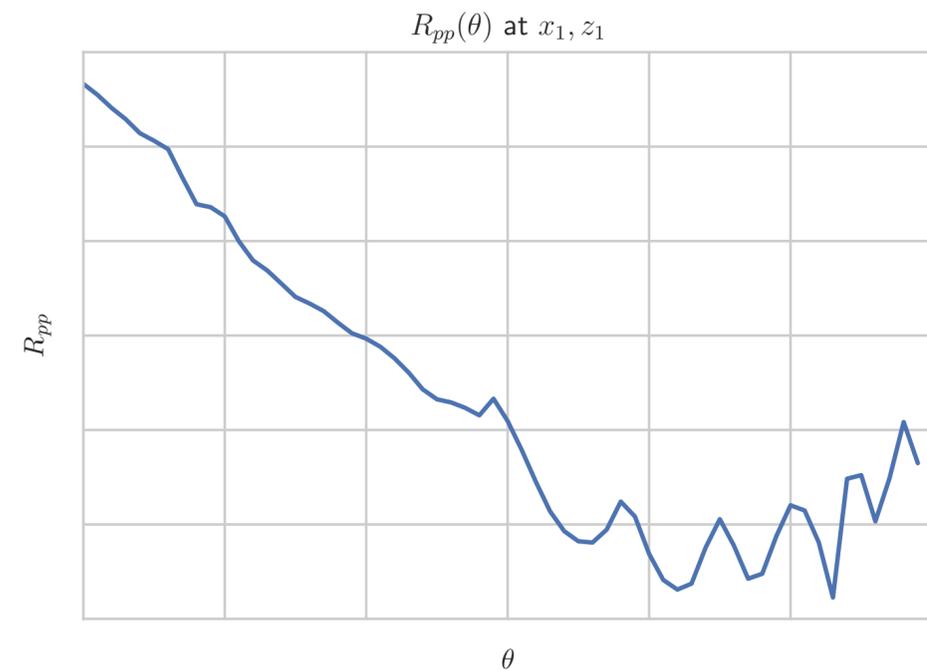


Image for every scattering angle.  
An angle gather for every slice.  
A reflectivity curve for every point.

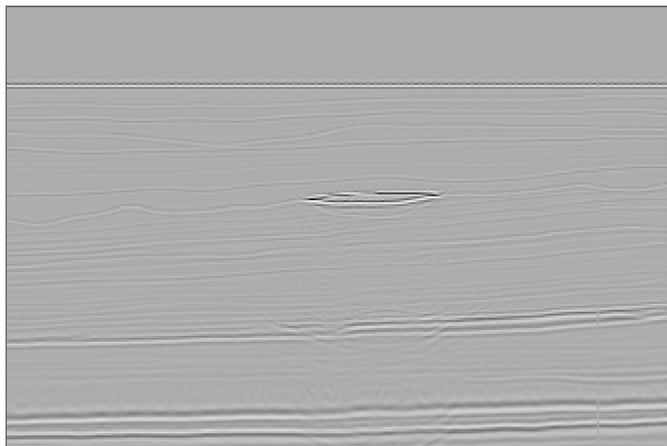
# Shuey term inversion as a projection



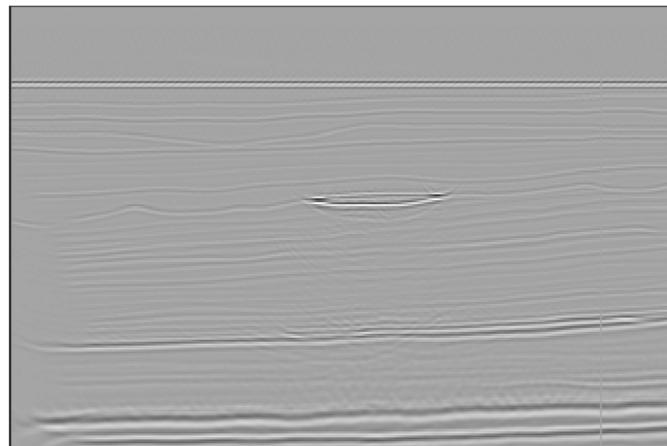
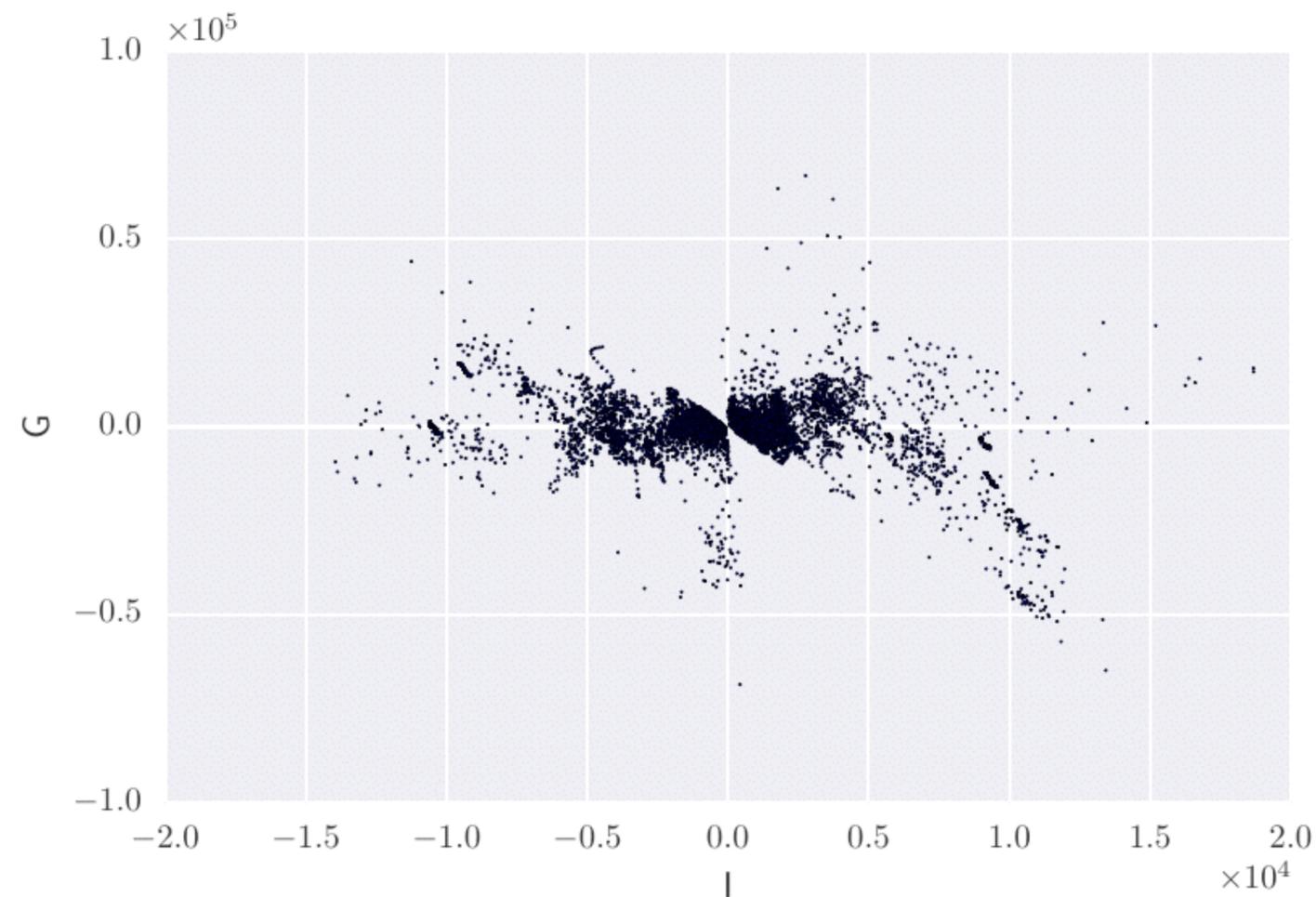
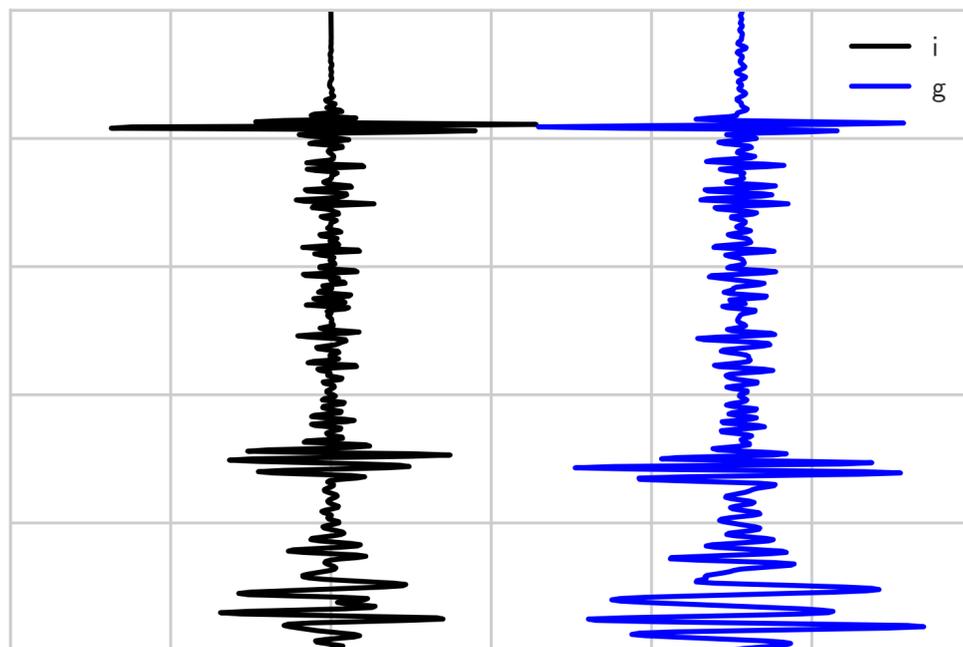
Fit the reflectivity curve using a linear combination of the Shuey vectors.  
Each reflectivity curve is projected down to two coefficients.

# Shuey term inversion as a projection

i



g

i,g at  $x_1$ 

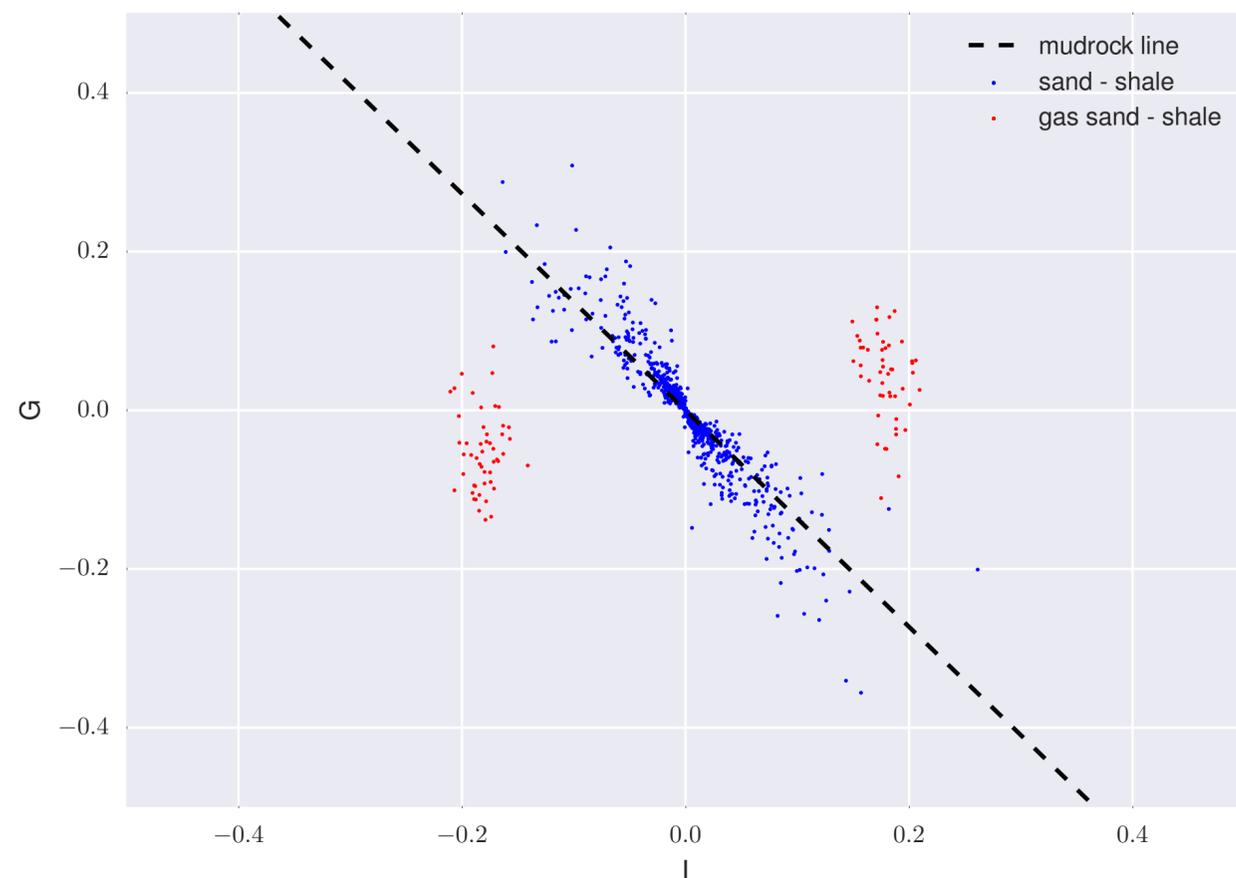
Reduced the dimensionality of the angle gathers to two coefficients.  
Projection coefficients can be plotted to analyze the multivariate relationships.

## Relation to hydrocarbons

Brine-saturated sands and shales follow a mudrock line:

$$g = \frac{i}{1+k} \left[ 1 - 4 \frac{\langle V_S \rangle}{\langle V_P \rangle} \left( \frac{2}{m} + k \frac{\langle V_S \rangle}{\langle V_P \rangle} \right) \right]$$

Hydrocarbon saturated sands deviate from this trend.

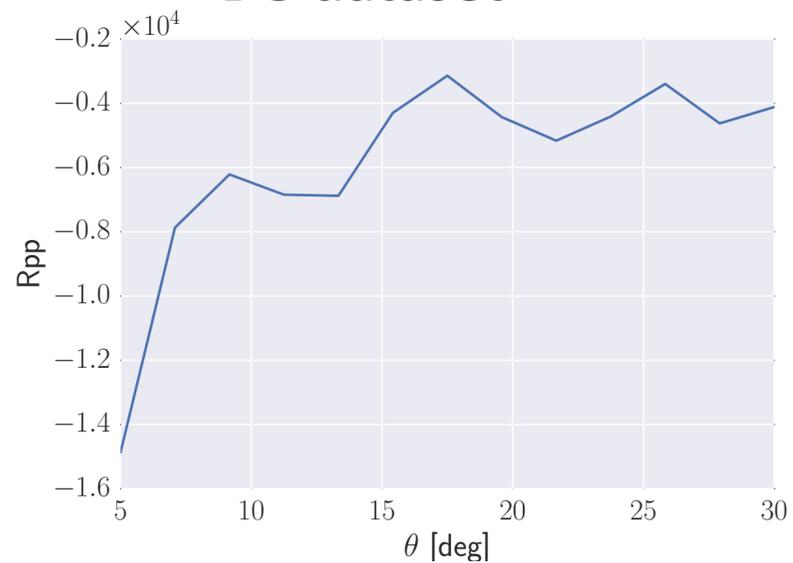


**Hydrocarbon reserves are found from outliers of a crossplot!**

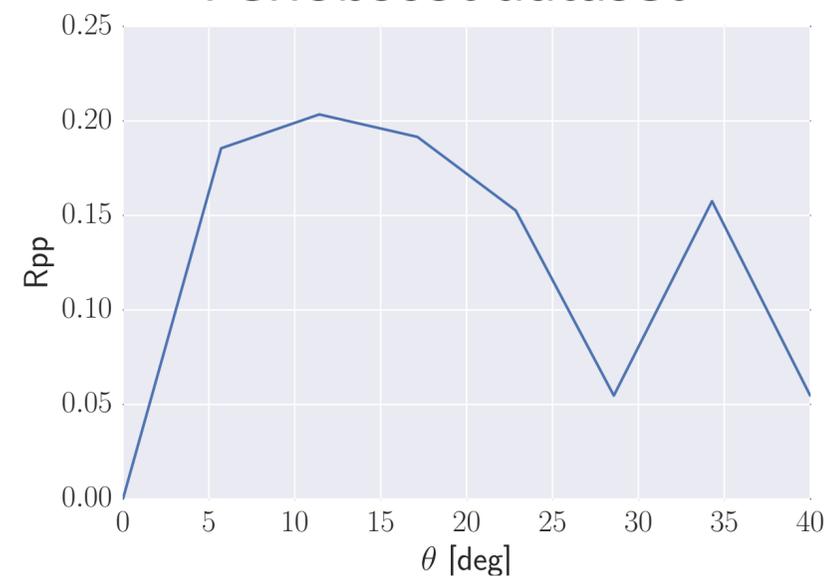
\*m, c, k are geological parameters determined empirically from well logs/laboratory measurements

# Reality bites

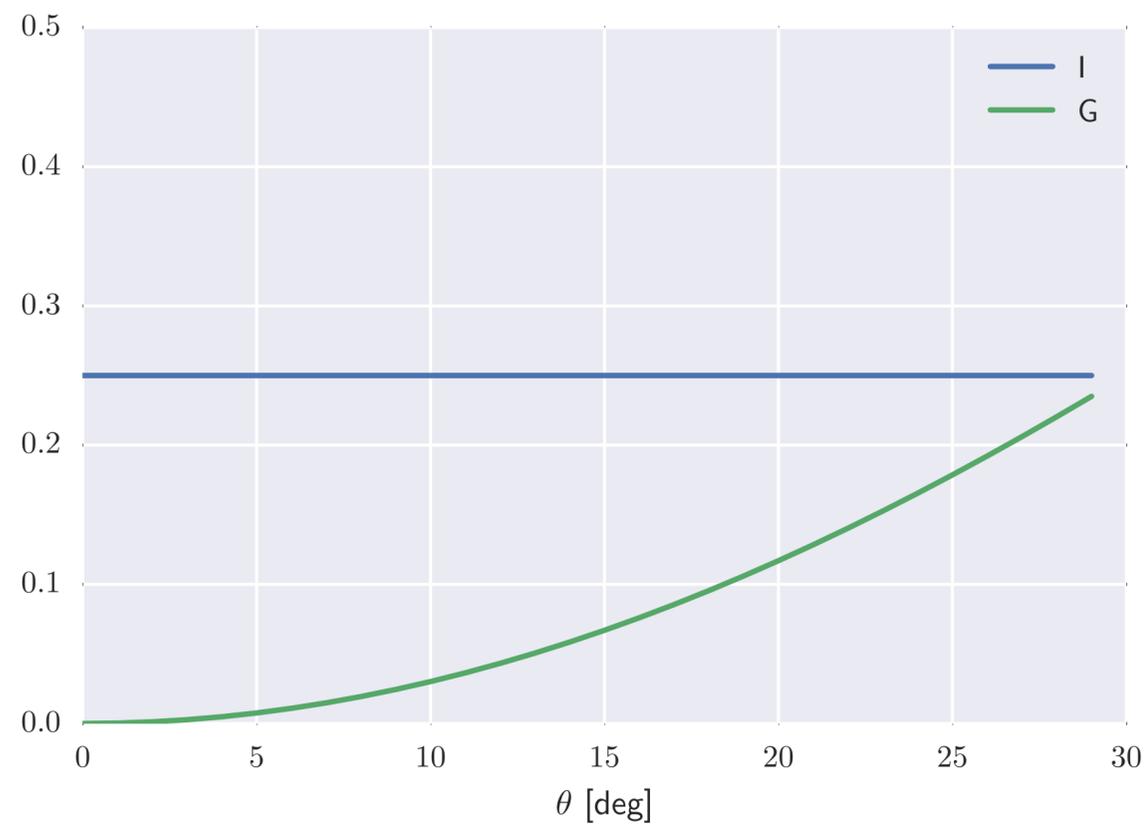
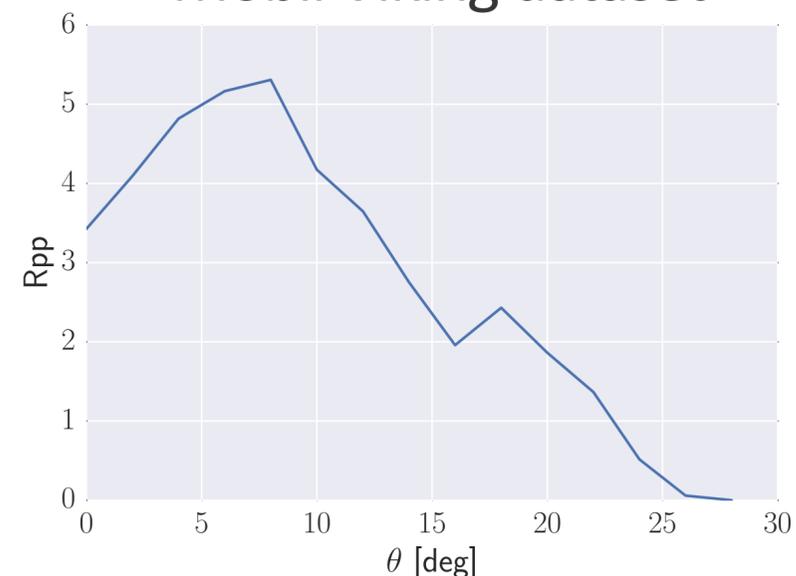
## BG dataset



## Penobscot dataset



## Mobil Viking dataset



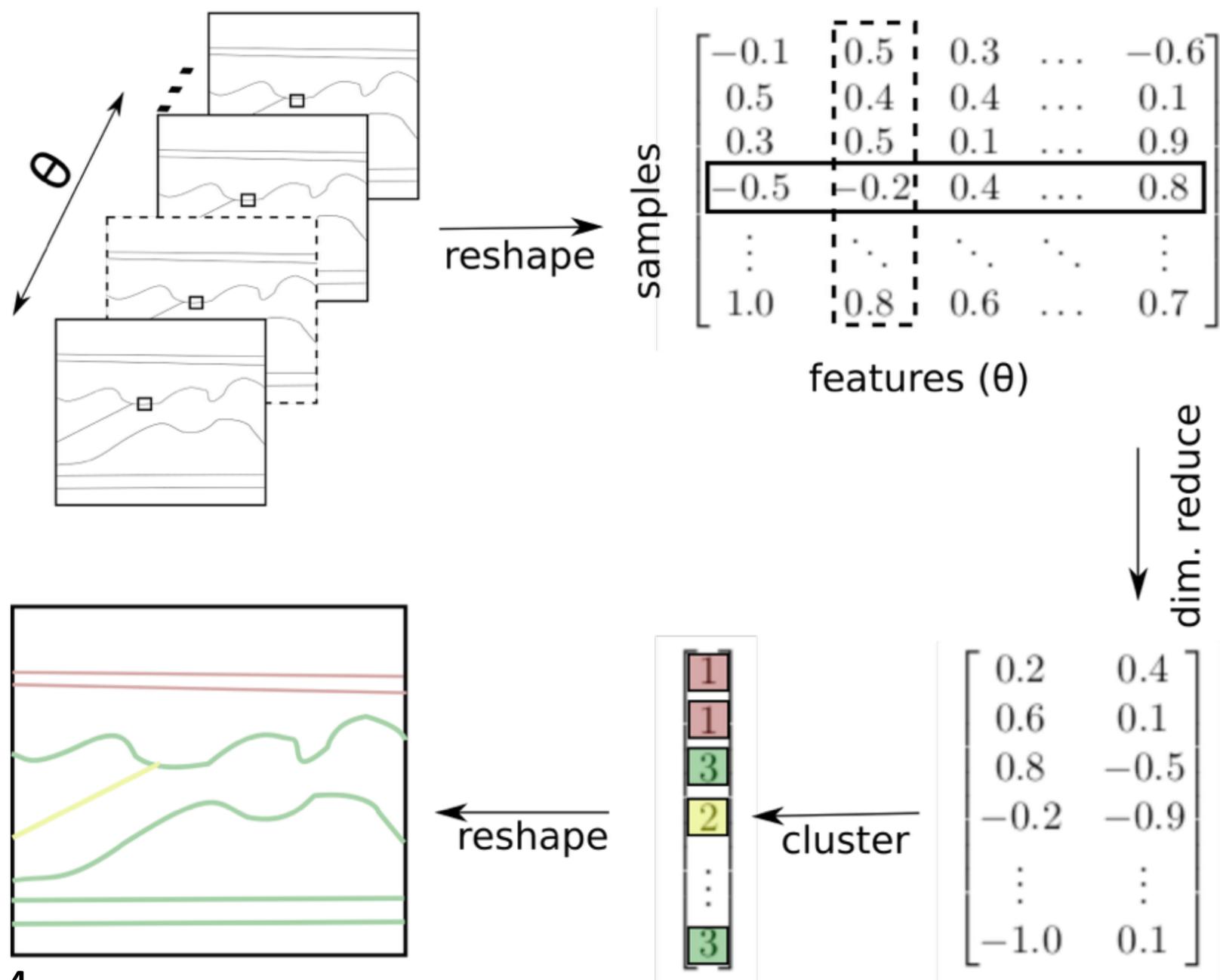
### Problem:

Shuey components can't explain the features in real data.

### Solution:

Use unsupervised machine learning to find better projections.

# Unsupervised learning problem



$$X \in \mathbb{R}^{n \times d}$$

$n$  is number of samples in the image,  
 $d$  is the number of angles

## Principle component analysis (PCA)

Eigendecomposition of the covariance matrix:

$$C = X^T X = \frac{1}{n} \sum_i^n \mathbf{x}_i \mathbf{x}_i^T$$

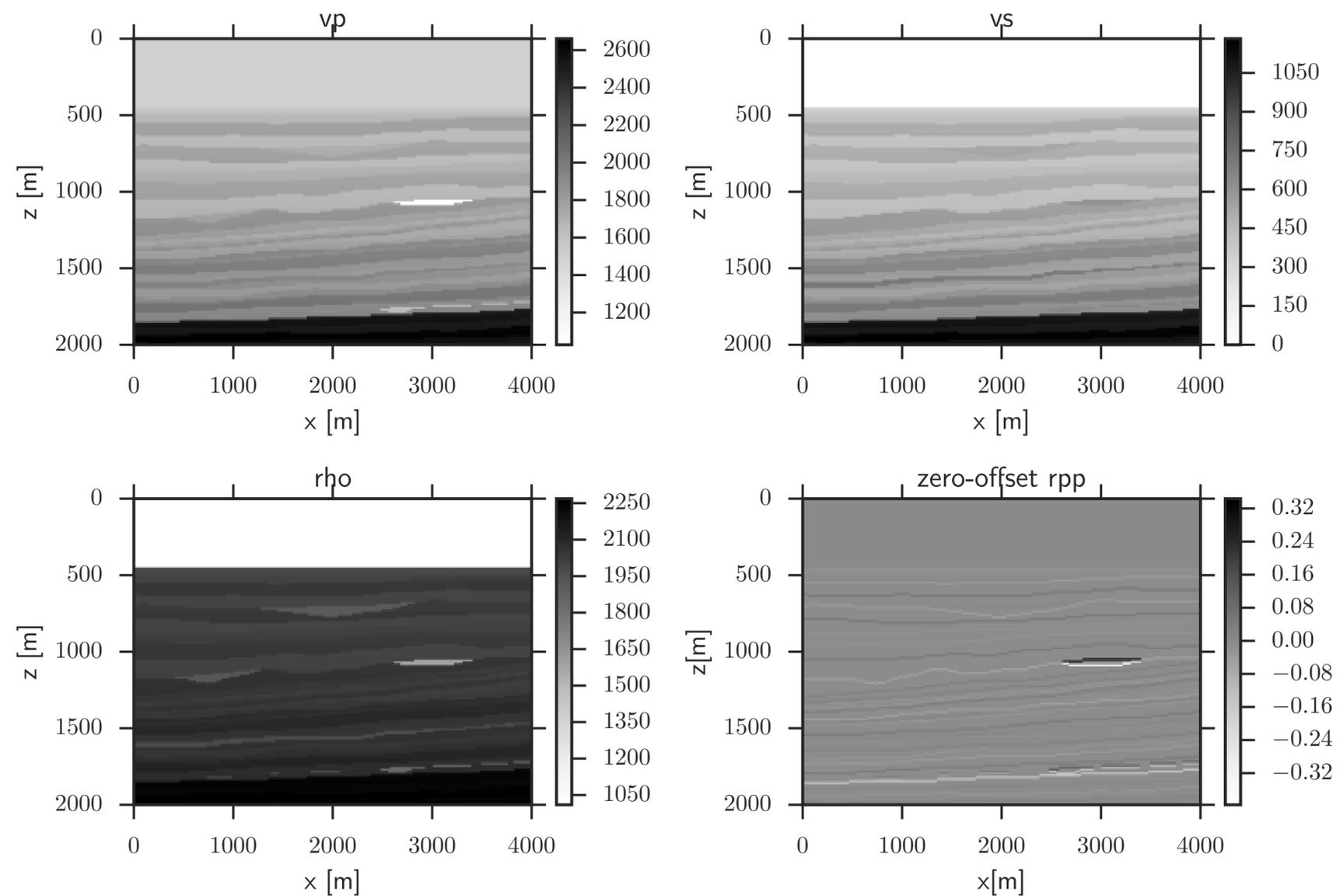
Project onto the eigenvectors with the two largest eigenvalues.

Maximizes the variance (a measure of information).

# DEMO

<http://ec2-54-224-182-64.compute-1.amazonaws.com/#/pca>

# Marmousi II Earth model

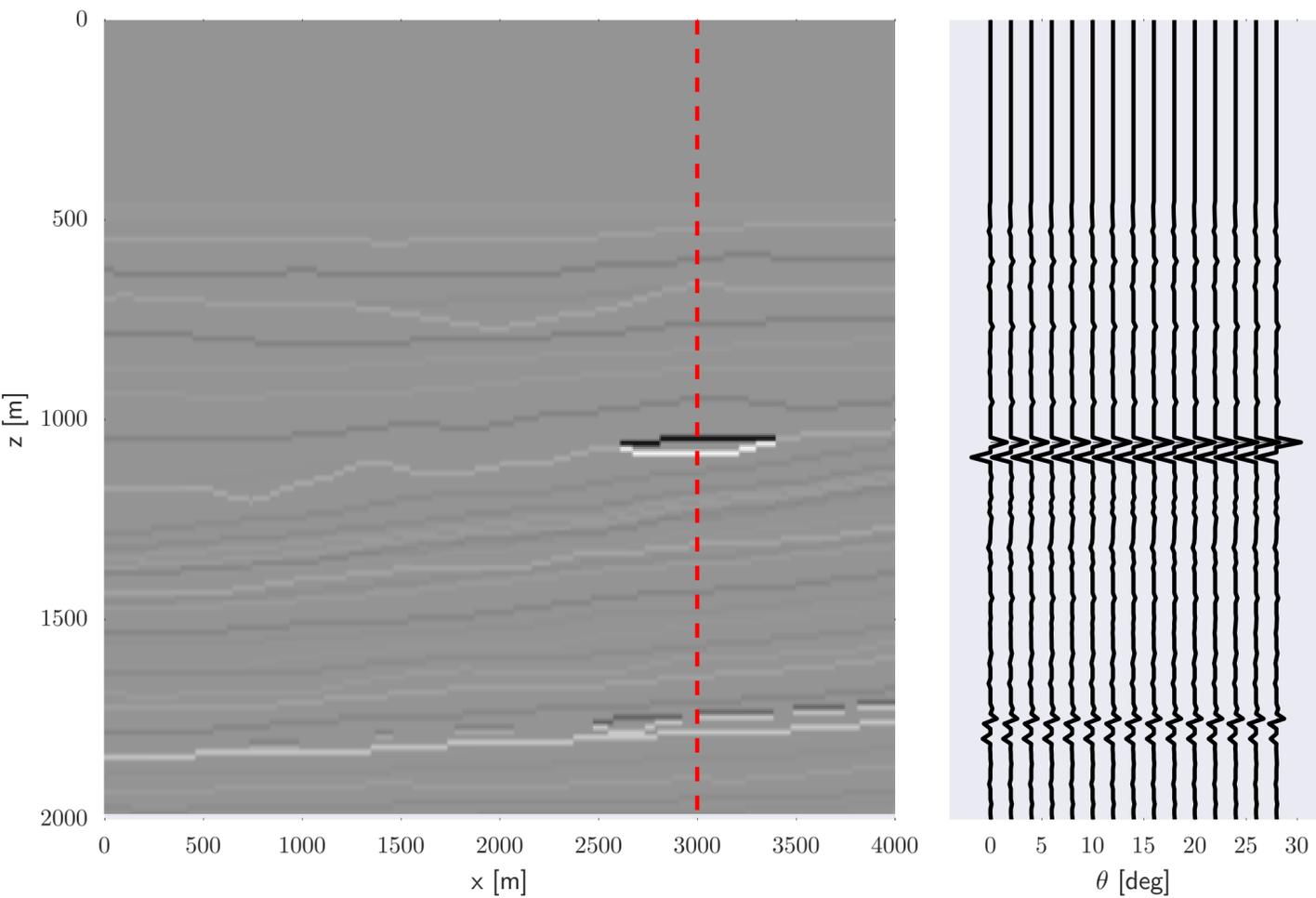


Specifically made for testing  
amplitude vs. offset analysis

Contains gas-saturated sand  
embedded in shales and  
brine-sands.

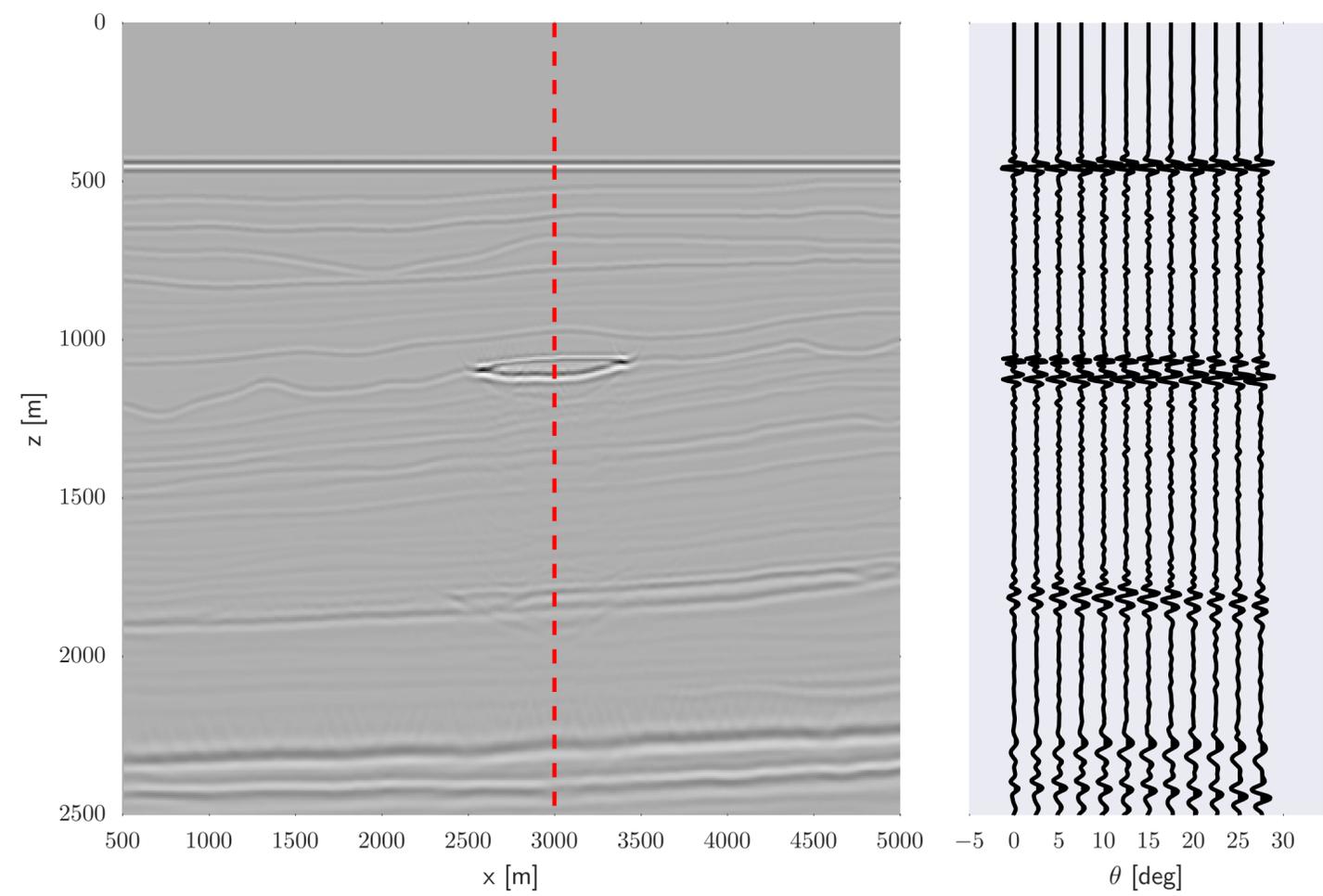
# Seismic modeling

## True reflectivity



Physically consistent with  
the Zoeppritz equations

## Migrated seismic



Migrated visco-acoustic  
survey

# DEMO

<http://ec2-54-224-182-64.compute-1.amazonaws.com/#/avo>

## Kernel PCA

### **Problem:**

Find a non-linear projection that provides better discrimination of trends and outliers.

### **Solution:**

Use the “kernel-trick” to compute PCA in a high-dimensional non-linear feature space

## Kernel trick

PCA can be calculated from the Gramian inner product matrix:

$$XX^T = \begin{pmatrix} \langle \mathbf{x}_1, \mathbf{x}_1 \rangle & \langle \mathbf{x}_1, \mathbf{x}_2 \rangle & \dots & \langle \mathbf{x}_1, \mathbf{x}_n \rangle \\ \langle \mathbf{x}_2, \mathbf{x}_1 \rangle & \langle \mathbf{x}_2, \mathbf{x}_2 \rangle & \dots & \langle \mathbf{x}_2, \mathbf{x}_n \rangle \\ \vdots & \vdots & \ddots & \vdots \\ \langle \mathbf{x}_n, \mathbf{x}_1 \rangle & \langle \mathbf{x}_n, \mathbf{x}_2 \rangle & \dots & \langle \mathbf{x}_n, \mathbf{x}_n \rangle \end{pmatrix}$$

Replace  $\langle \mathbf{x}_i, \mathbf{x}_j \rangle$  with a kernel  $\kappa(\mathbf{x}_i, \mathbf{x}_j)$

$$\kappa(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i^T \mathbf{x}_j + b)^c = \langle \phi(\mathbf{x}_i), \phi(\mathbf{x}_j) \rangle$$

Example  $c=2, b=1$

$$\phi(\mathbf{x}) = [1, \sqrt{2}x_1, \sqrt{2}x_2, x_1^2, x_2^2, \sqrt{2}x_1x_2]$$

# DEMO

<http://ec2-54-224-182-64.compute-1.amazonaws.com/#/avo>

## Recap

**Situation:** Exploring seismic data for anomalous responses.

**Problem:** Physical model can not explain real world data.

**Solution:** Learn useful projections directly from the data.

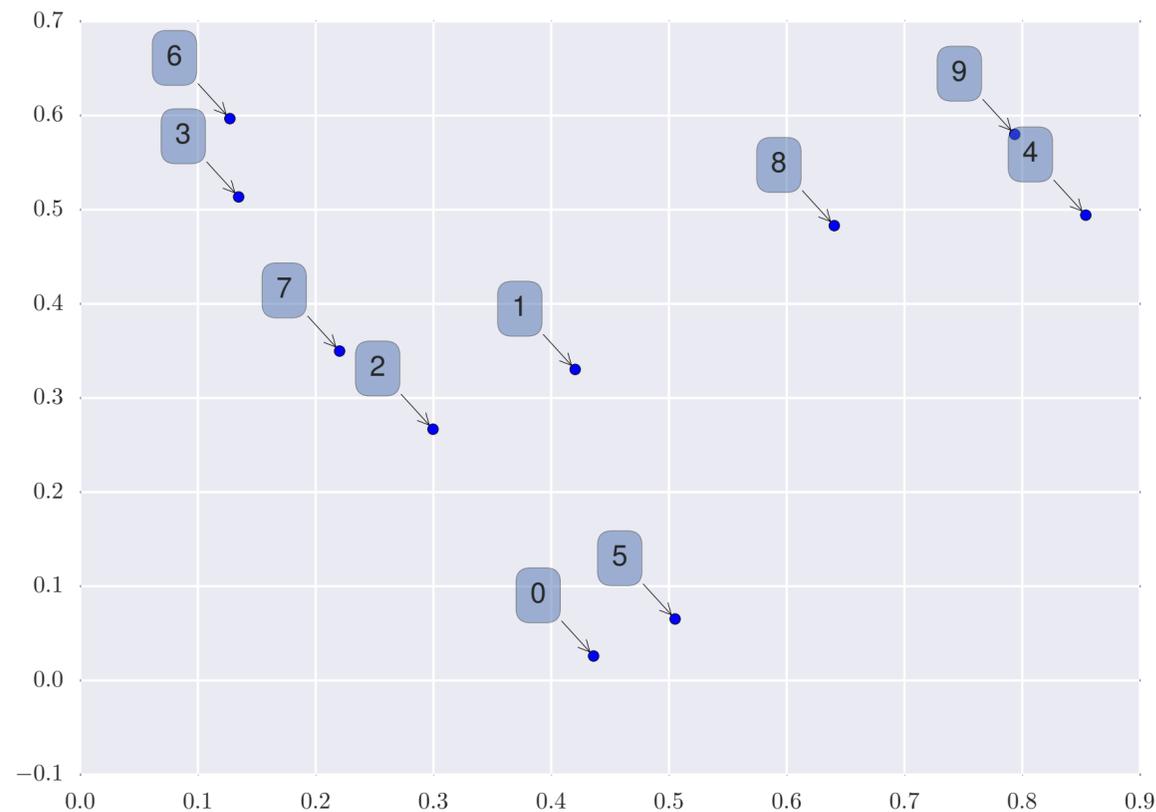
### **Assessment:**

- PCA is equivalent for physically consistent data, but more robust to processing/acquisition artifacts.
- Kernel PCA makes outliers linearly separable from the background.

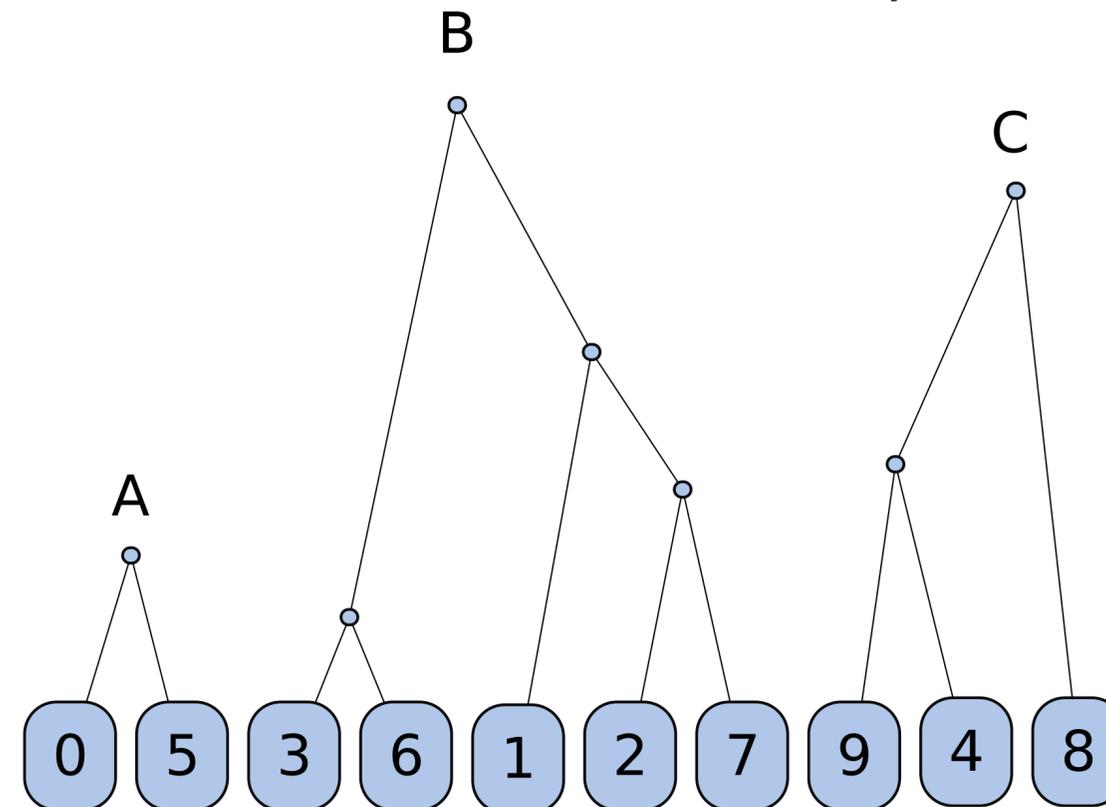
**Next:** Automatic segmentation (clustering)

# Hierarchical clustering

Unclassified data



Classification hierarchy



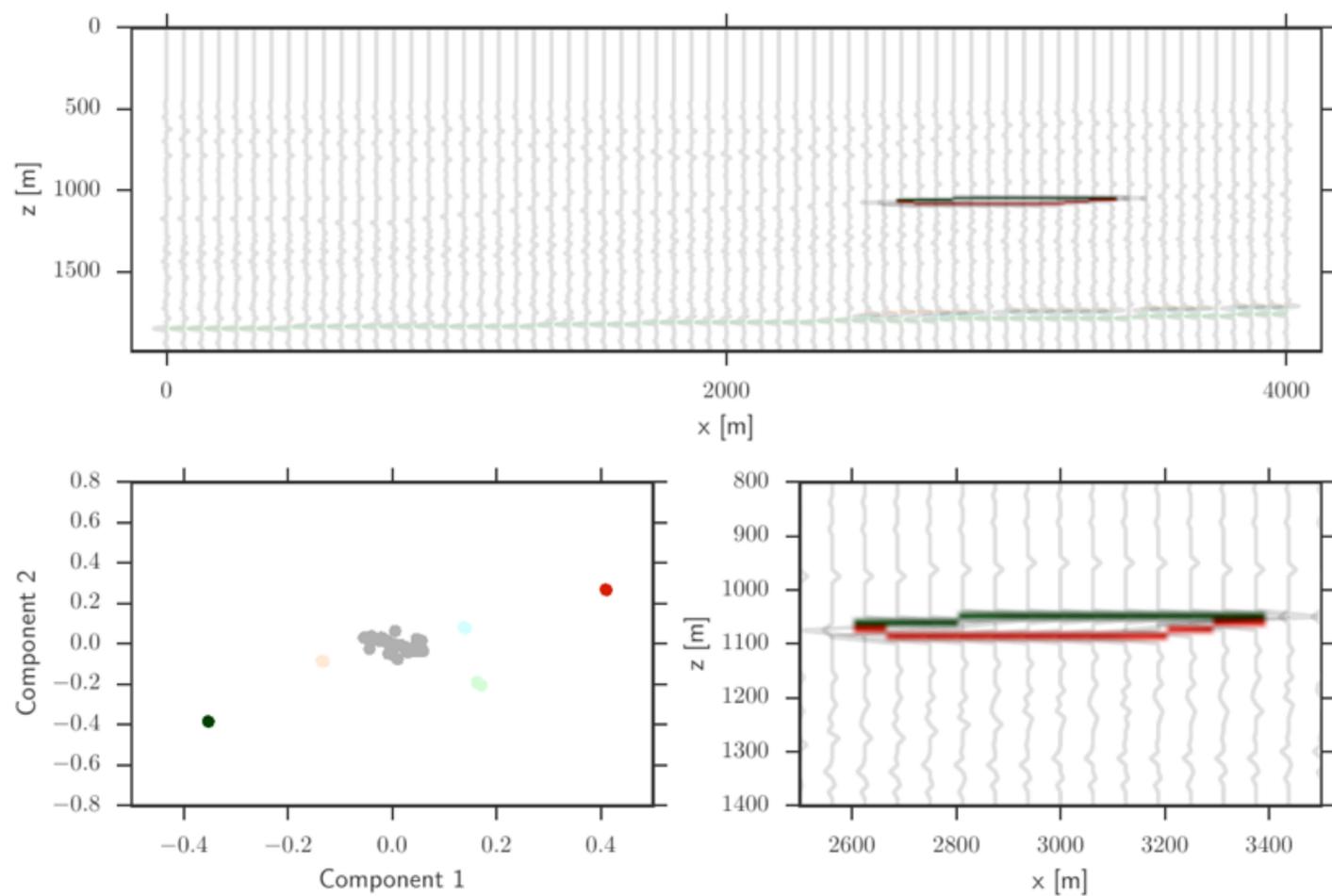
Each point is initially considered a cluster.

Each iteration merges the closest clusters into a larger cluster.

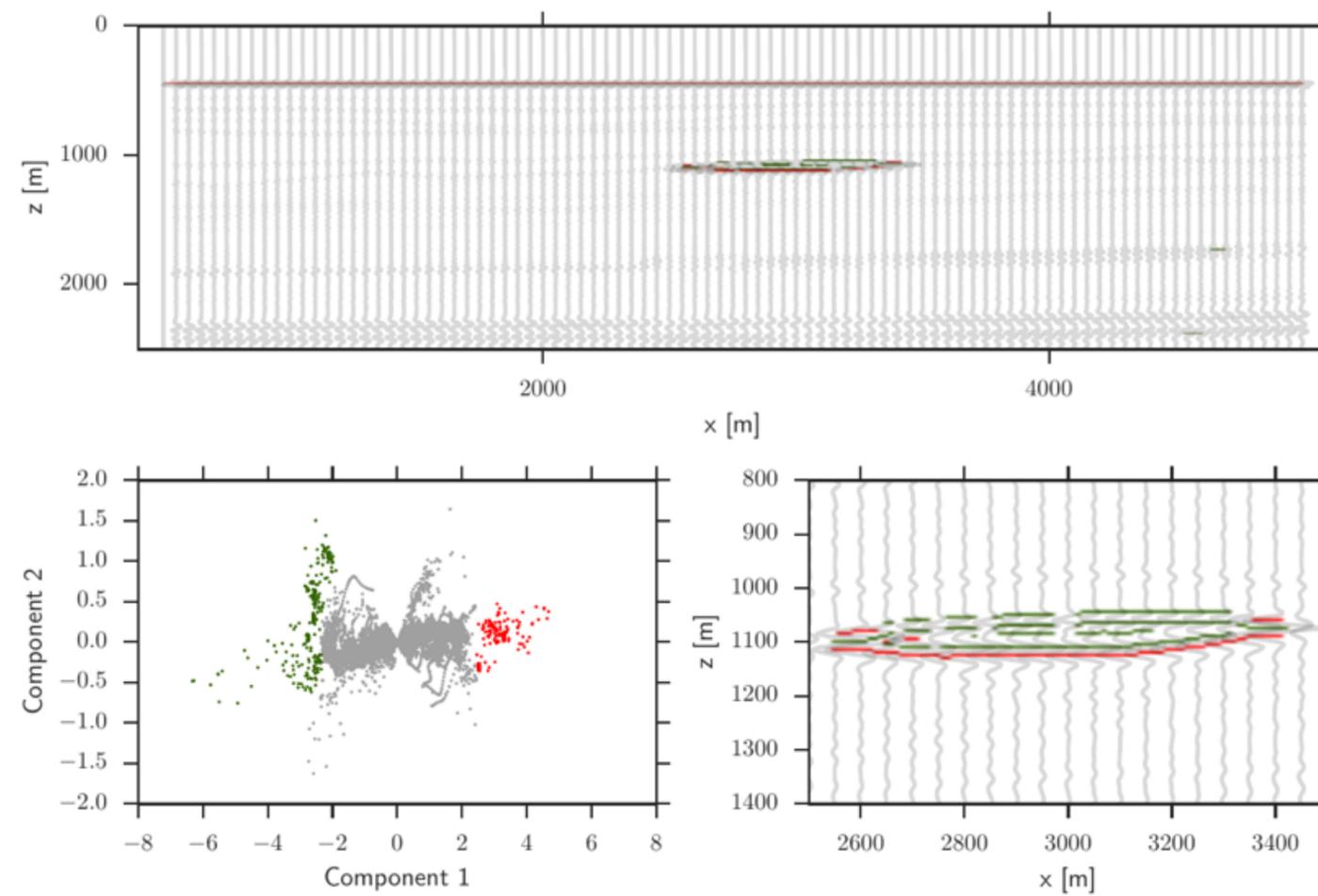
Builds a hierarchy until a *defined* number of classes is reached.

# Results - PCA

## Clustered physically consistent data

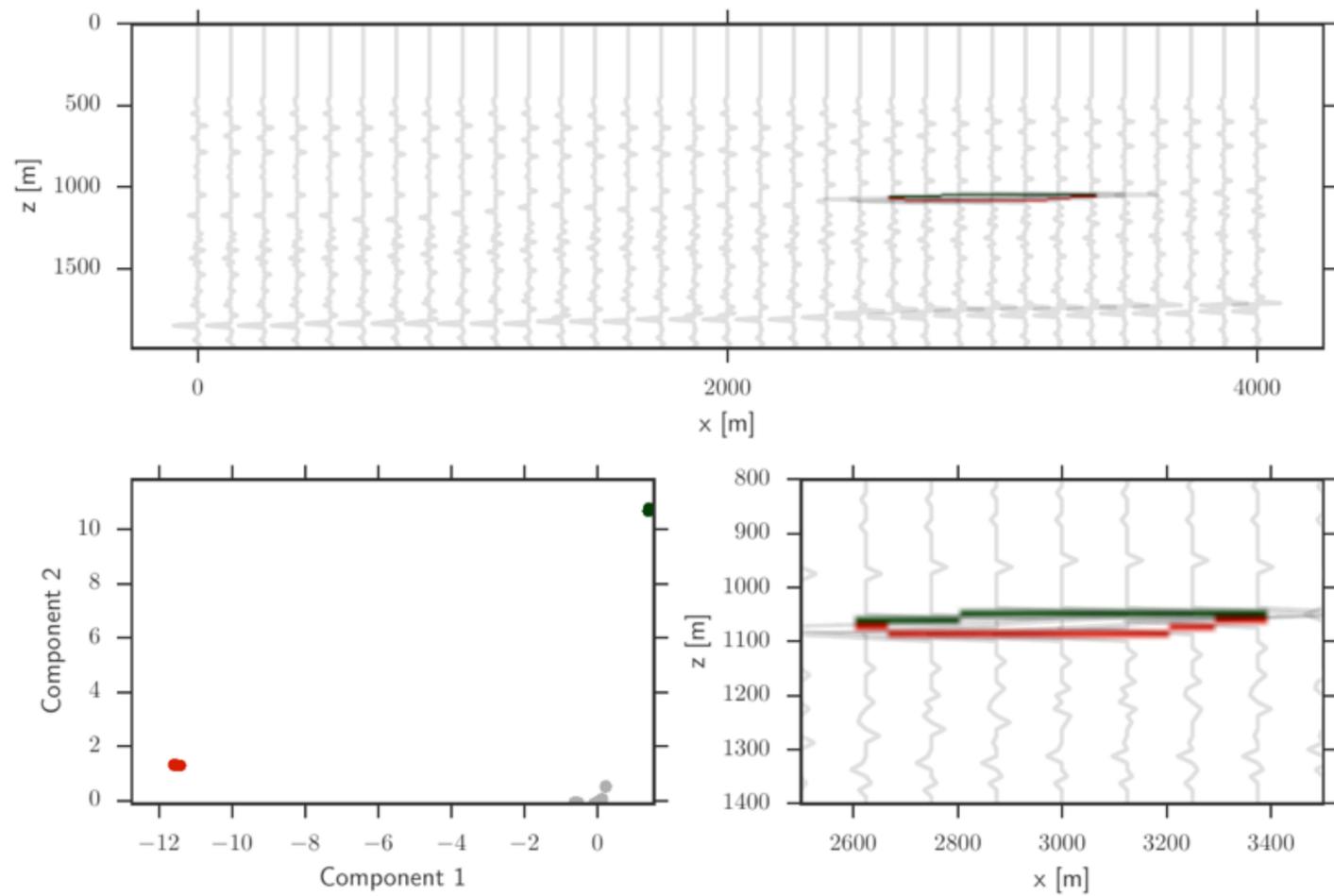


## Clustered migrated data

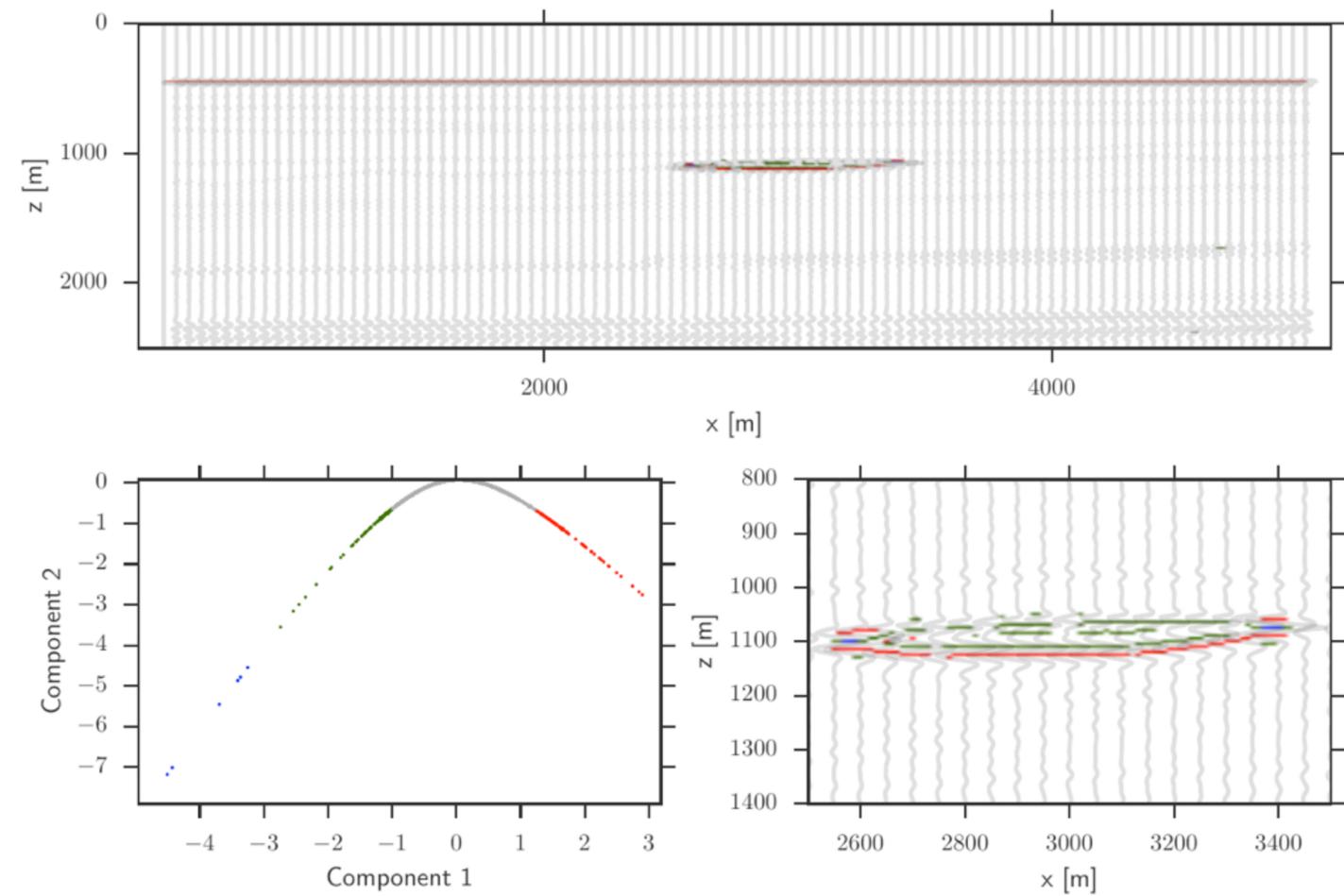


# Results - Kernel PCA

## Clustered physically consistent data



## Clustered migrated data



## Summary

### **Successes:**

Each projection could segment the reservoir.

Kernel PCA provided advantageous multivariate geometries (linearly separable).

### **Challenges:**

Clustering is highly sensitive to user chosen parameters.

Kernel PCA is computationally expensive and lacks interpretation.

## Robust PCA

### Problem:

Find a sparse set of outlying reflectivity responses against a background trend.

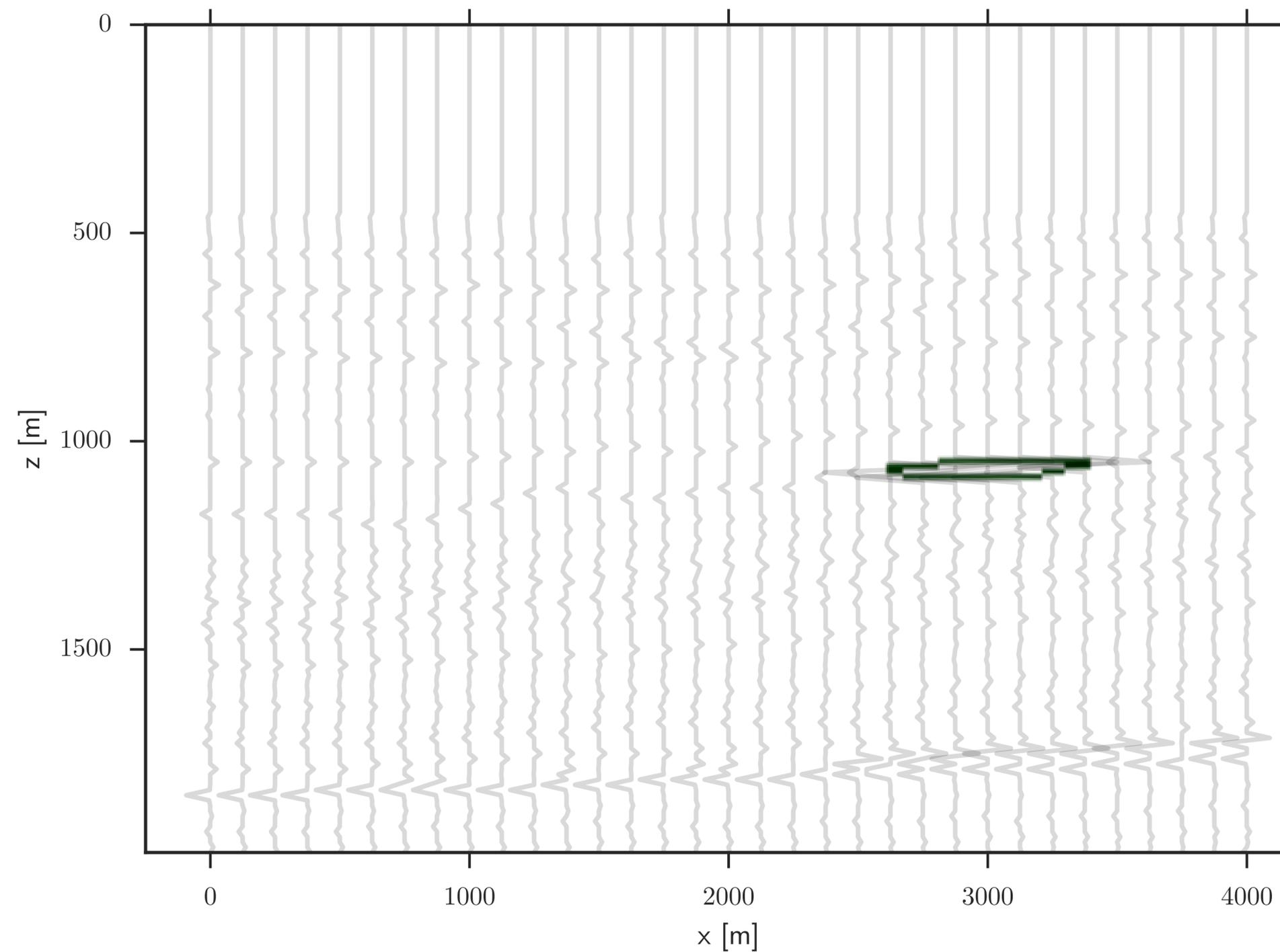
### Assumption:

The background trend of similar curves is highly redundant, which forms a low rank matrix.

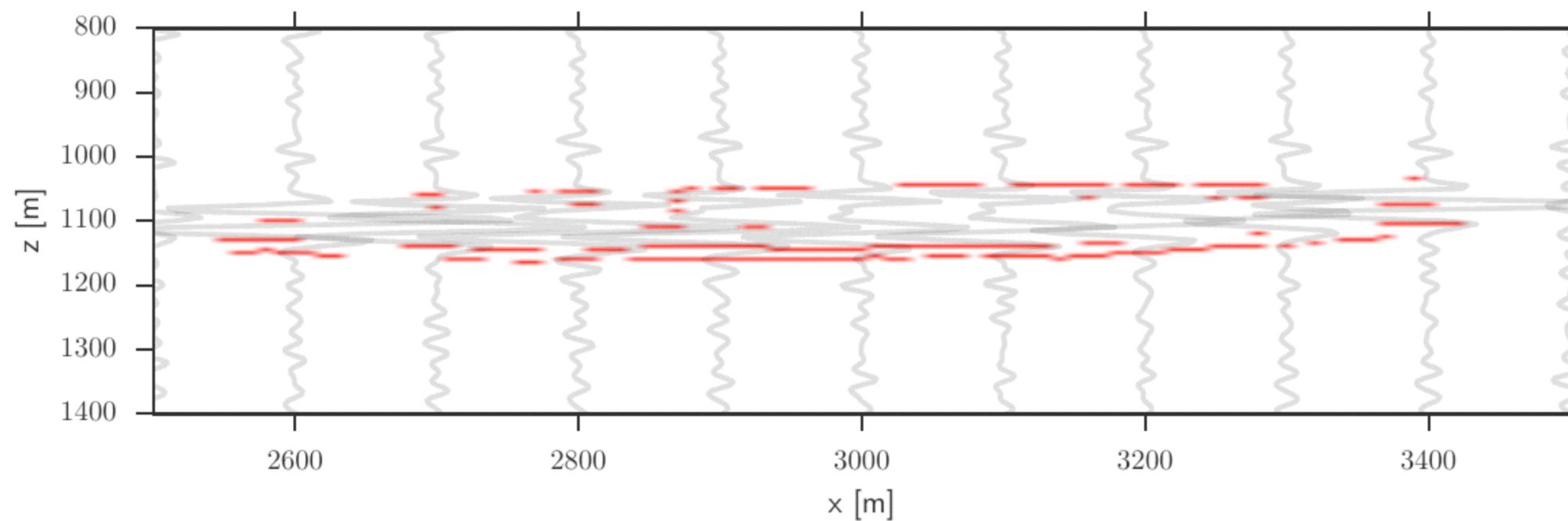
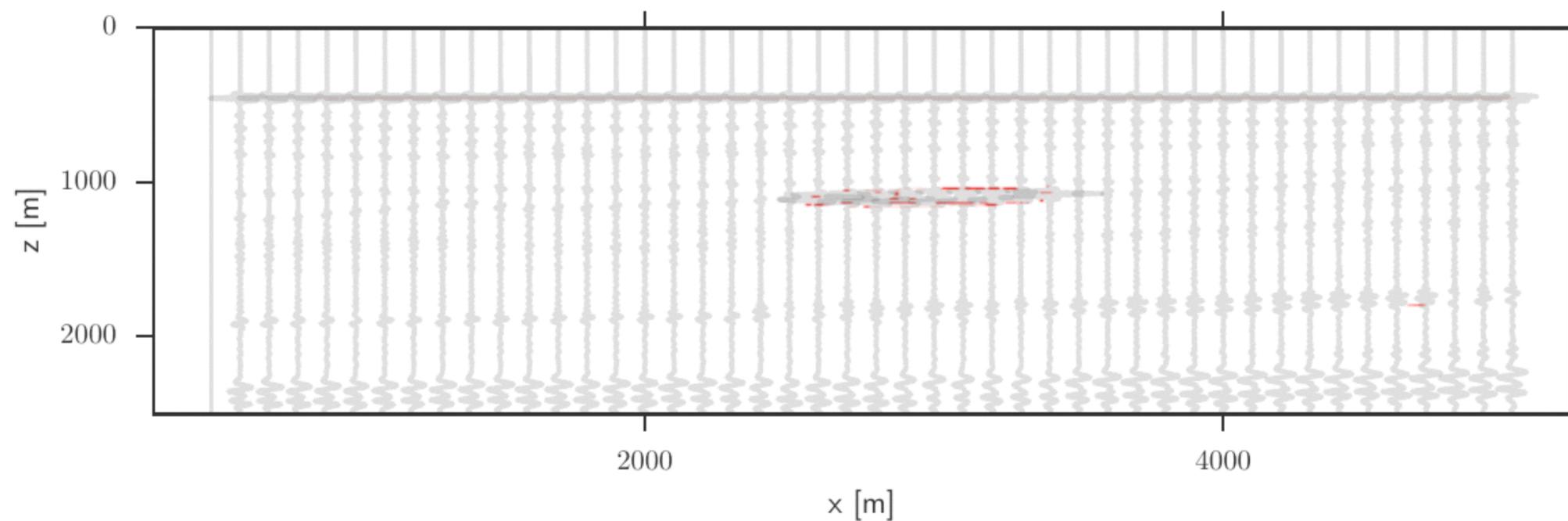
### Solution:

$$\min_{L,S} \|L\|_* + \lambda \|S\|_{1,\infty} \text{ s.t. } L + S = X$$

# Results - physically consistent data



# Results - migrated seismic



## Summary

### **Successes:**

Segmentation of reservoir in both images.

Physically interpretable segmentation without clustering.

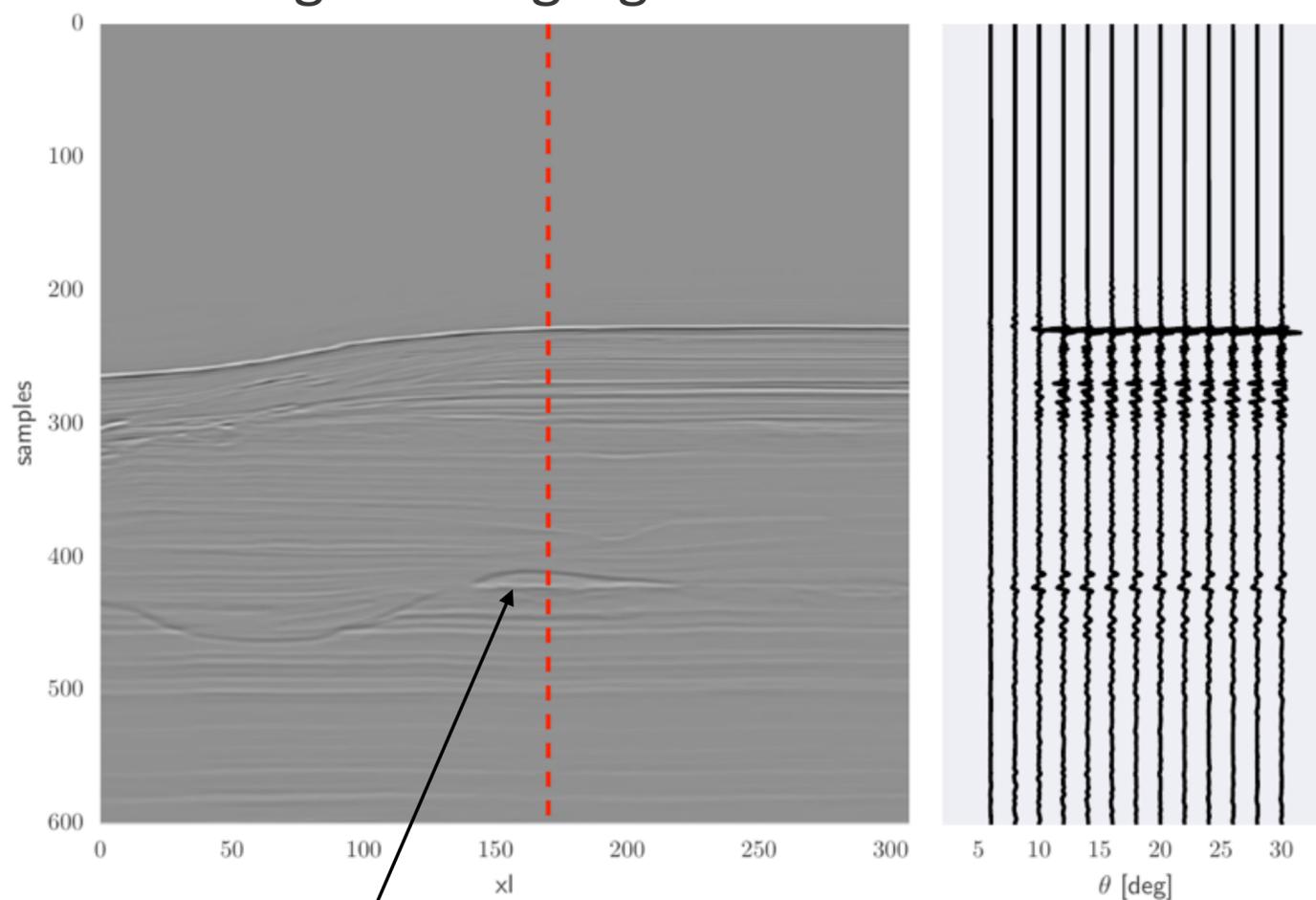
### **Challenges:**

Requires tuning of one optimization trade off parameter.

Convergence sensitive to the rank of outliers, not well understood.

# Comparison on field data

Migrated angle gathers



potential gas target

Data provided by BG group.

Interpreted to contain a potential gas reserve.

Compare unsupervised methods to BG group's approach: Dynamic Intercept Gradient Inversion (DIGI).

Note: Clustering approaches were not directly useful.

## DIGI-inverse problem

$$\begin{bmatrix} \mathbf{d} \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} W & W \sin^2 \theta \\ \lambda \nabla & \lambda \nabla \\ W(\theta_{me}) \cos(\chi_{me}) & W(\theta_{me}) \sin(\chi_{me}) \end{bmatrix} \begin{bmatrix} \mathbf{i} \\ \mathbf{g} \end{bmatrix}$$

Convolution forward model:  $d(x, t, \theta) = w(x, t, \theta) * r(x, t, \theta)$

- *ill-posed*,  $\lambda \nabla$  term forces a smooth answer

Further augmented by extended elastic reflectivity (EER) term:

$$EER(\chi_{me}) = i \cos(\chi_{me}) + g \sin(\chi_{me})$$

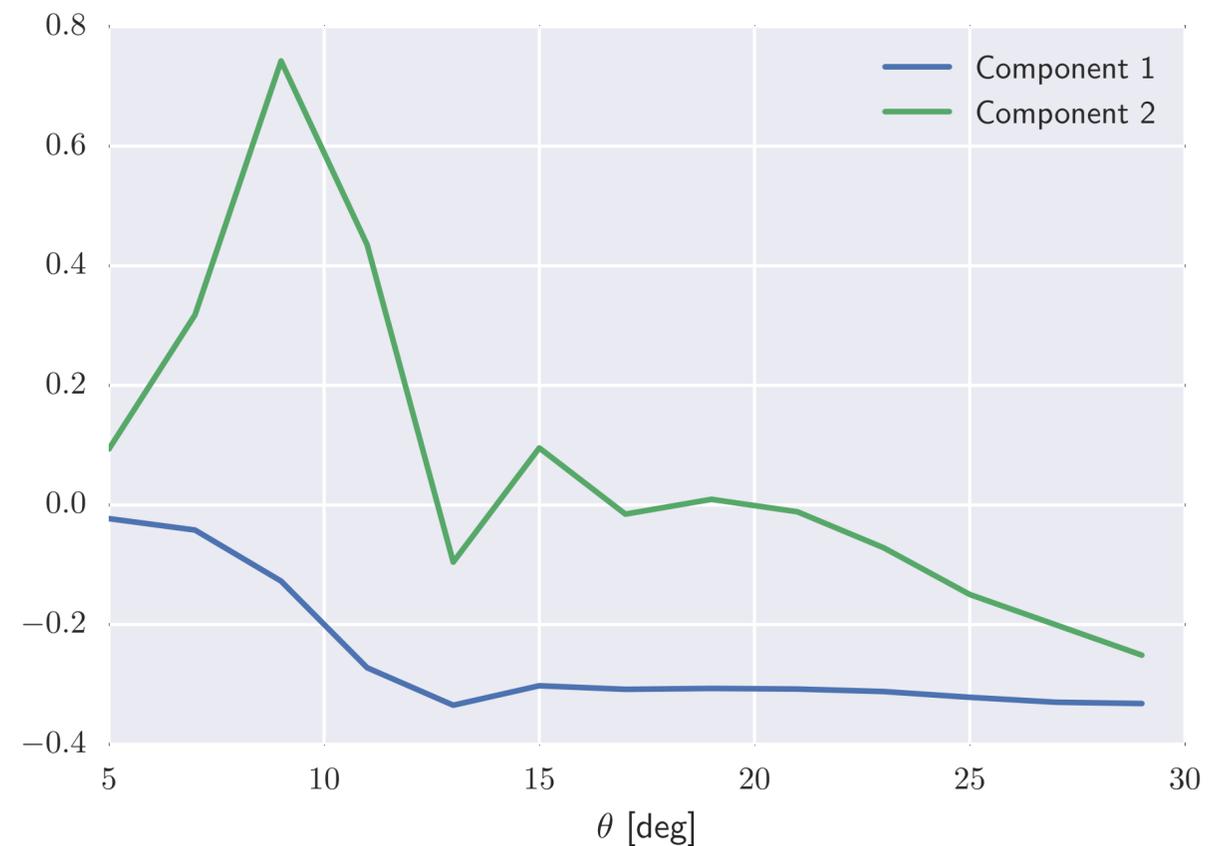
- promotes correlation between  $i$  and  $g$
- $\chi_{me}$  is related a priori geological information

System is solved using the conjugate gradient based algorithm LSQR.

## PCA extended DIGI

$$\begin{bmatrix} \mathbf{d} \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} W & W \sin^2 \theta \\ \lambda \nabla & \lambda \nabla \\ W(\theta_{me}) \cos(\chi_{me}) & W(\theta_{me}) \sin(\chi_{me}) \end{bmatrix} \begin{bmatrix} \mathbf{i} \\ \mathbf{g} \end{bmatrix} \longrightarrow \begin{bmatrix} \mathbf{d} \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} W \mathbf{c}_1 & W \mathbf{c}_2 \\ \lambda \nabla & \lambda \nabla \\ W(\theta_{me}) \cos(\chi_{me}) & W(\theta_{me}) \sin(\chi_{me}) \end{bmatrix} \begin{bmatrix} \mathbf{i} \\ \mathbf{g} \end{bmatrix}$$

Same inverse problem, but use the two largest principle components instead of the Shuey terms.



## Minimum energy projection

$$EER(\chi_{me}) = i \cos(\chi_{me}) + g \sin(\chi_{me})$$

forms an image where large values correspond to uncorrelated  $i$  and  $g$  terms.

Thresholding this image will therefore segment outliers.

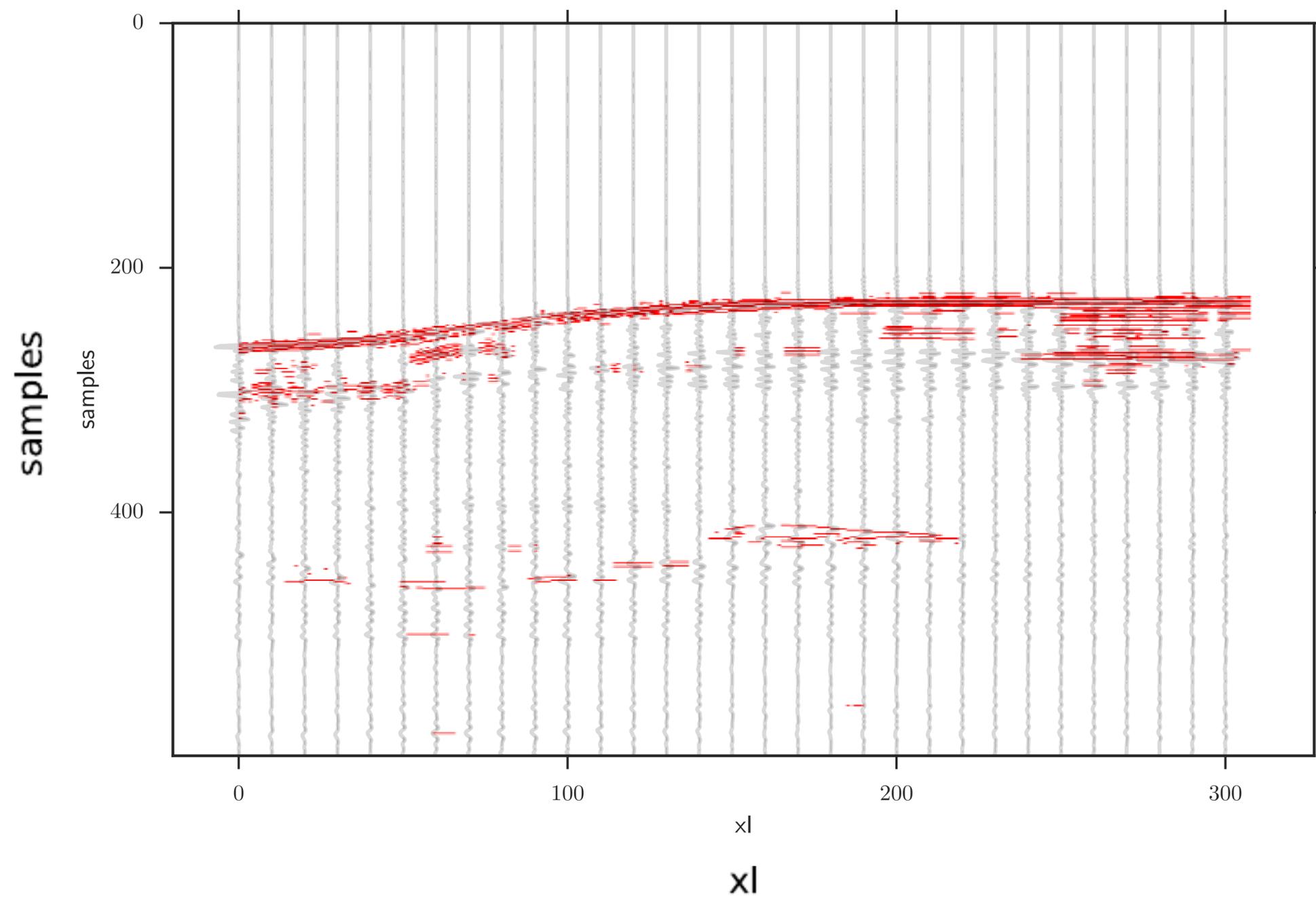
## Comparison method

Manually threshold the image to segment the potential hydrocarbon reserve while maintaining the least amount of spurious segmentation.

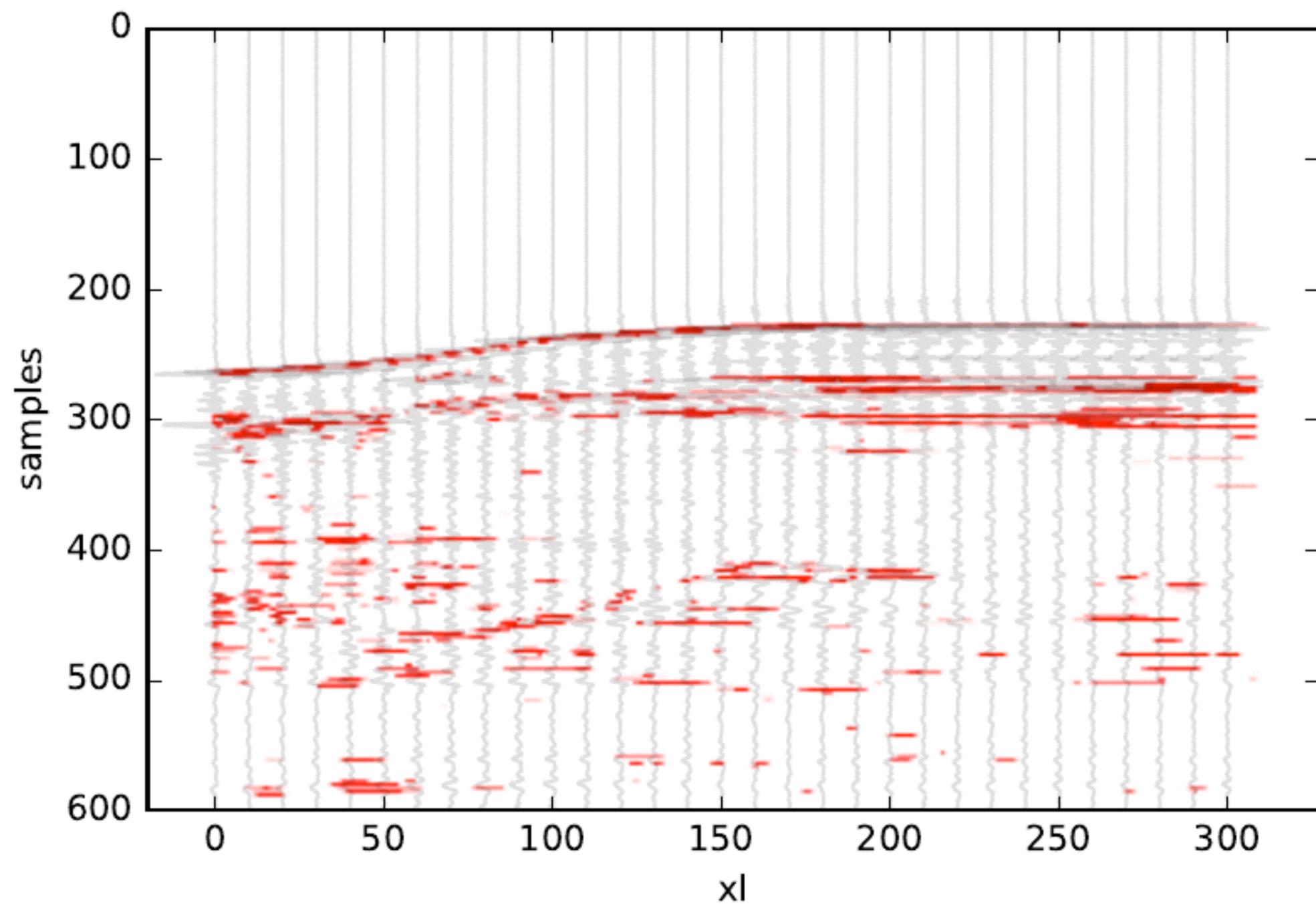
Compare:

- Robust PCA
- DIGI
- PCA extended

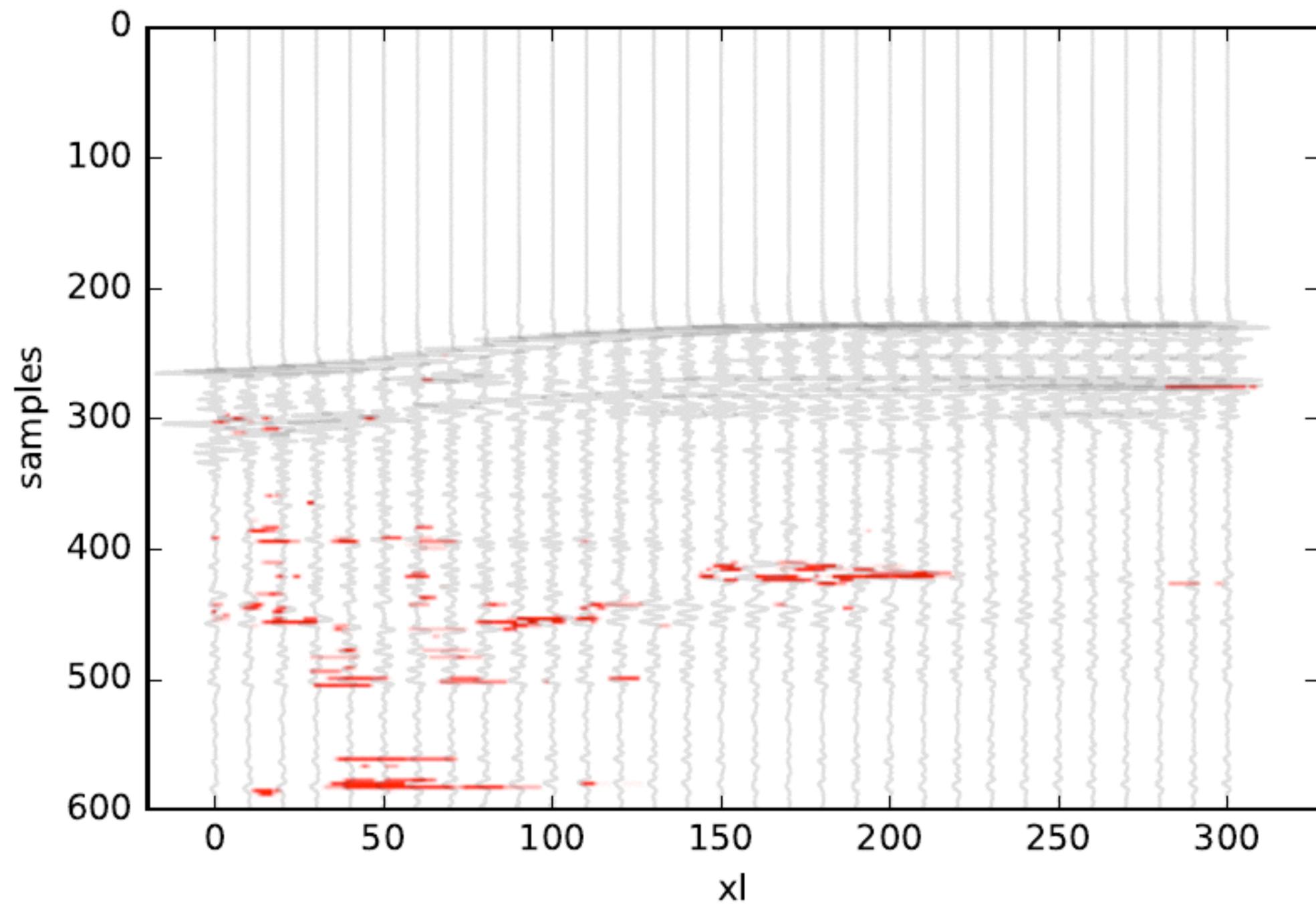
# Results - robust PCA



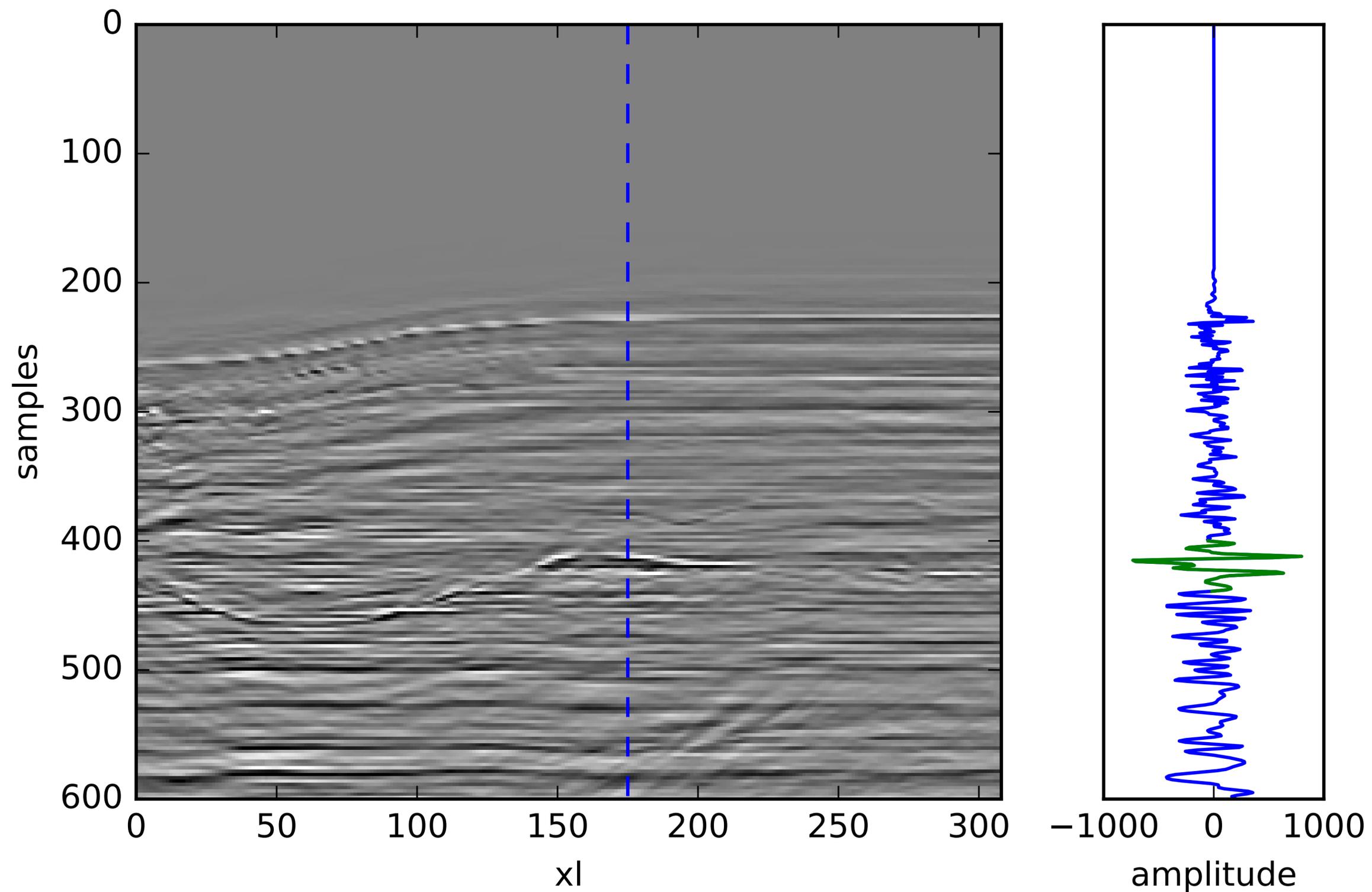
# Results - DIGI



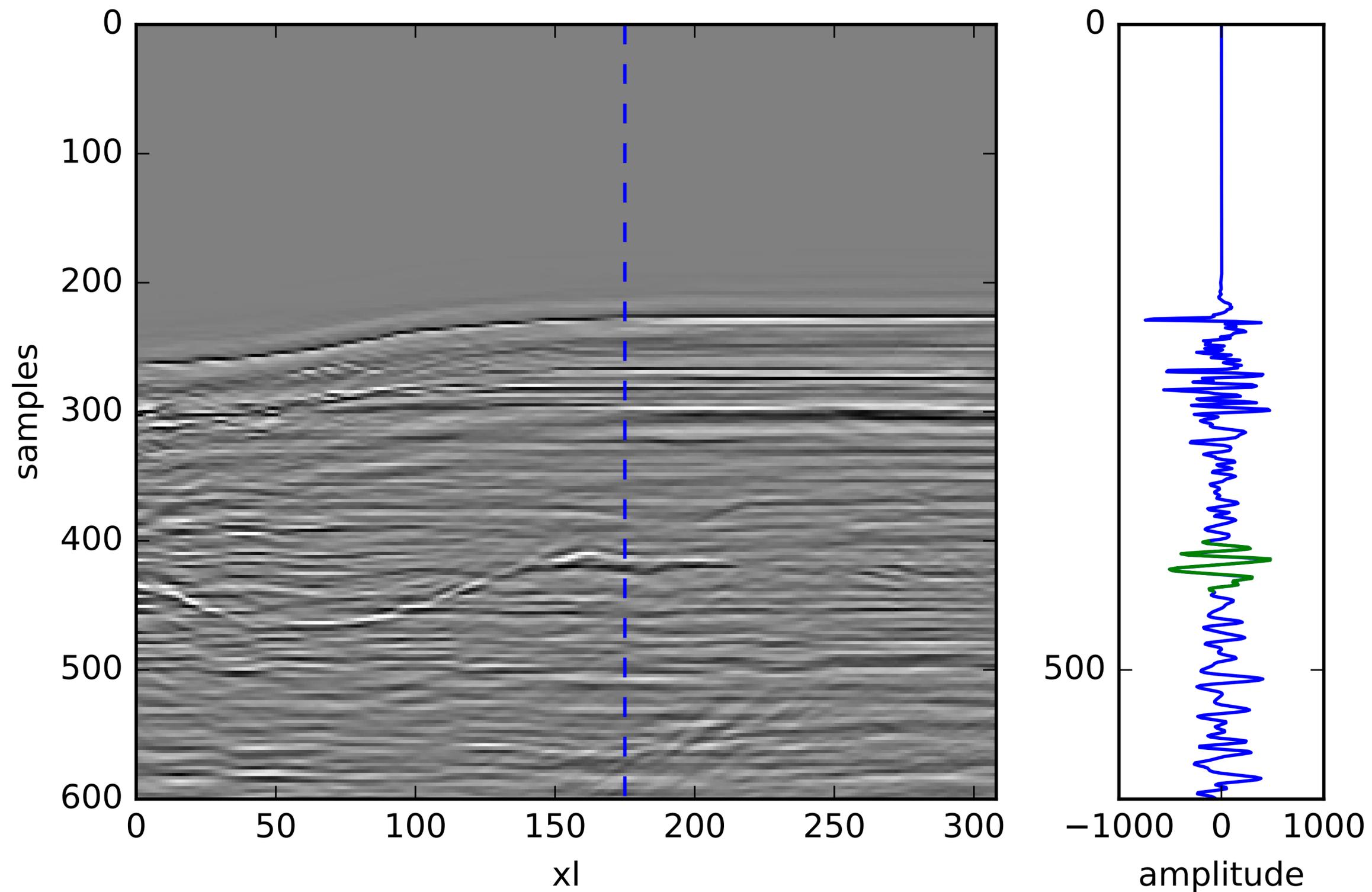
# Results - PCA extend DIGI



# Results - EER using PCA extended DIGI

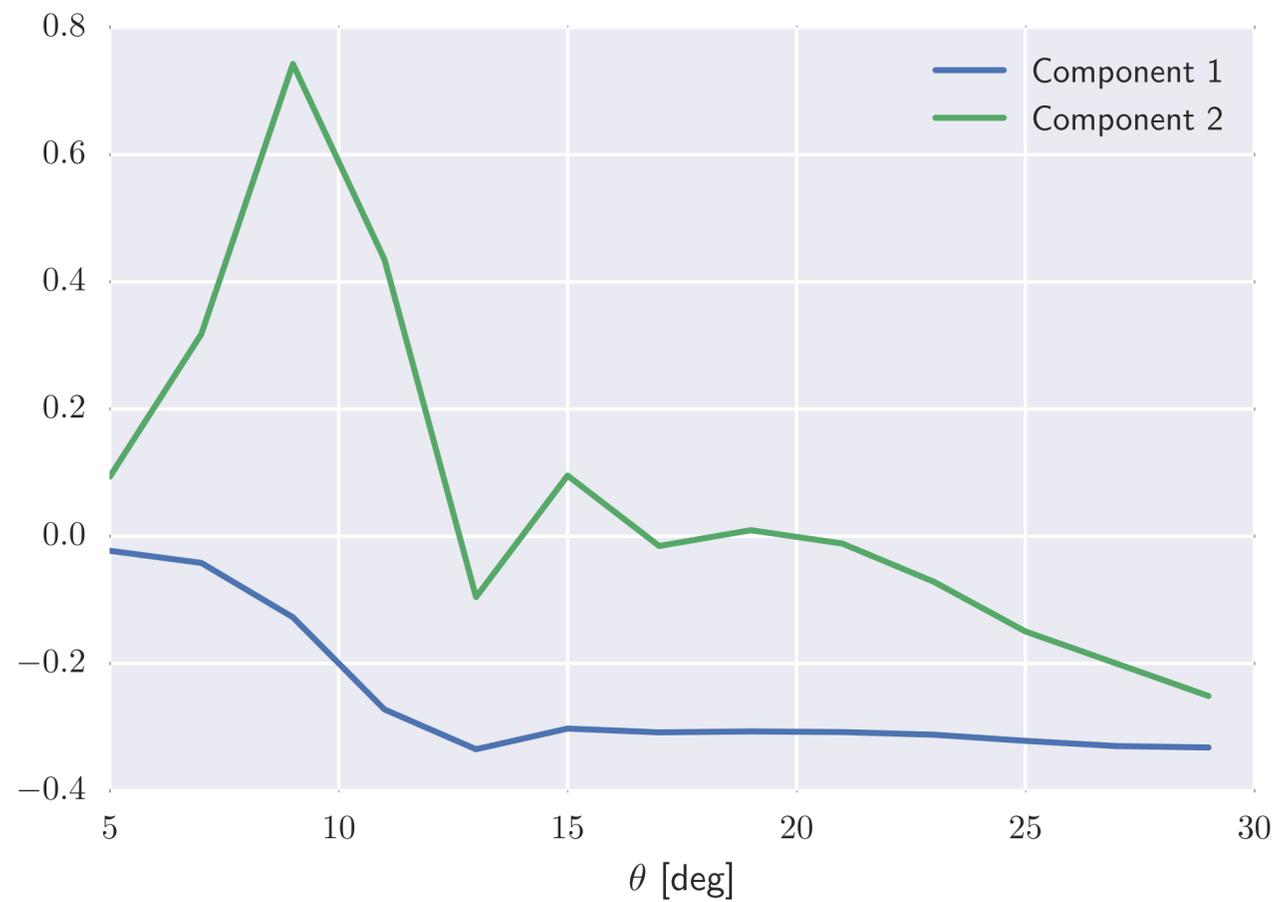


# Results - EER using DIGI

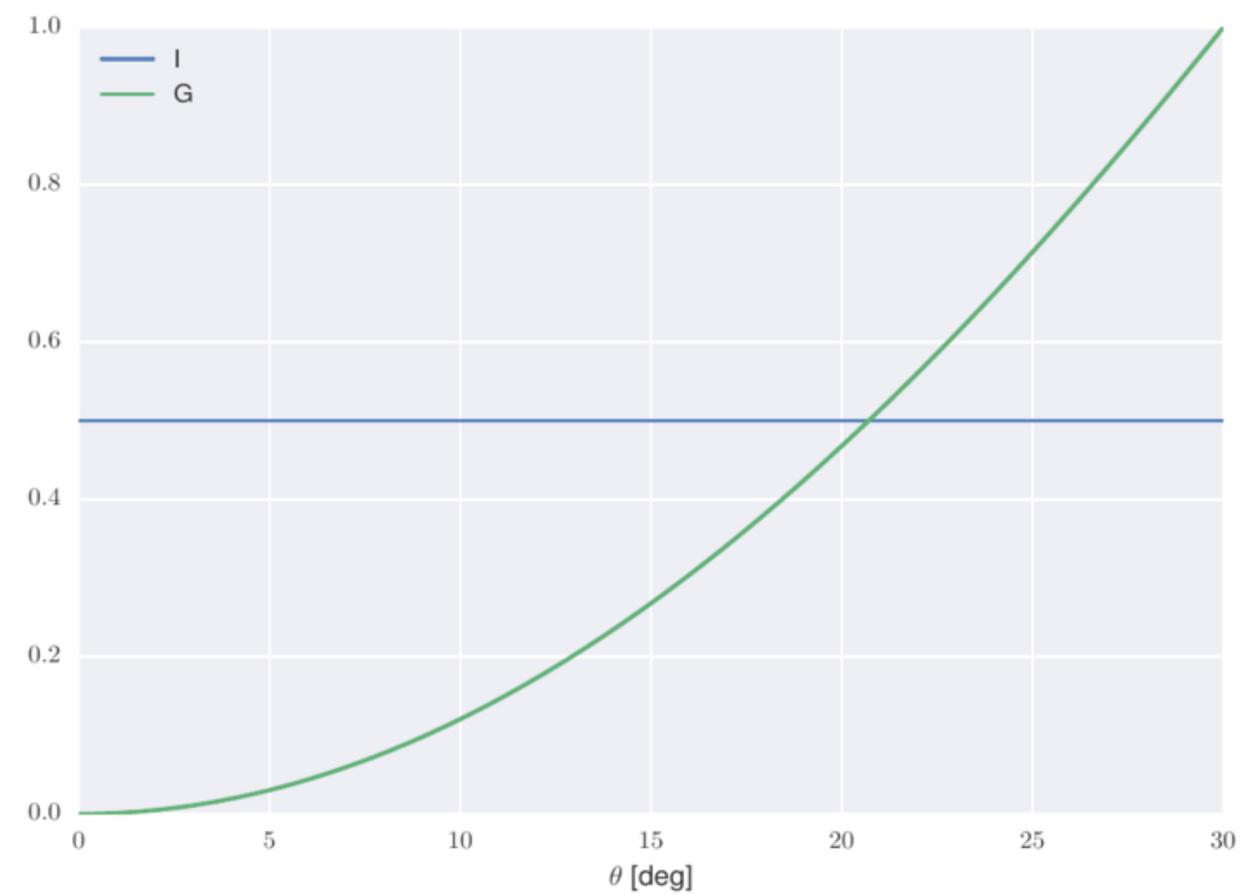


# Why the difference?

## Principle components



## Shuey terms



Principle components can explain more features in the data.

## Summary

- Robust PCA provided the best image segmentation.
- PCA extended DIGI better separated the potential reservoir from the background trend.
- The extracted principle components showed significantly different shapes than the Shuey vectors.

## Epilogue

### **Outcome:**

Generalized a conventional analysis approach using unsupervised learning models.

Successful in segmented potential hydrocarbon reserves from seismic data

### **Future:**

More data, standardized datasets

Quantitative benchmarks

---

**Thanks**

## References

- [1] Zoeppritz, K., 1919, VII b. Über Reflexion und Durchgang seismischer Wellen durch Unstetigkeitsflächen: Nachrichten von der Gesellschaft der Wissenschaften zu Göttingen, Mathematisch-Physikalische Klasse, 1919, 66–84
- [2] Shuey, R. T., 1985, A simplification of the Zoeppritz equations: Geophysics, 50, 609–614.
- [3] Gardner, G. H. F., L. W. Gardner, and A. R. Gregory, 1974, Formation velocity and density; the diagnostic basics for stratigraphic traps: Geophysics, 39, 770–780.
- [4] Castagna, J. P., M. L. Batzle, and R. L. Eastwood, 1985, Relationships between compressional-wave and shear-wave velocities in clastic silicate rocks: Geophysics, 50, 571–581.
- [5] Castagna, J. P., H. W. Swan, and D. J. Foster, 1998, Framework for AVO gradient and intercept interpretation: Geophysics, 63, 948–956.
- [6] Edgar, J., and J. Selvage, 2013, Dynamic Intercept-gradient Inversion