

## SUMMARY

1. We simulate subsurface CO<sub>2</sub> injection into porous rock with seismic measurements,
2. treat the permeability field as a random variable,
3. apply the EnKF to estimate the CO<sub>2</sub> saturation field,
4. compare the EnKF to two baselines, and
5. test the EnKF's performance with different noise parameters.

## I. MOTIVATION

### A. CO<sub>2</sub> injection

- Carbon-negative strategies are required to mitigate climate change.
- Injecting CO<sub>2</sub> (carbon dioxide) underground is a well-developed technology for the oil industry.
- CO<sub>2</sub> can be injected underground for long-term storage.
- CO<sub>2</sub> storage must be monitored to mitigate risks (e.g., leakage, over-pressure)

### B. Monitoring method

- Seismic measurements are non-intrusive and more informative than wells.
- Seismic measurements are noisy and nonlinear.
- Known fluid dynamics can provide additional information.
- Using both sources of information requires data assimilation techniques.

The EnKF is a scalable, mature technique with success on large, nonlinear systems.

## II. BACKGROUND

- Hidden state:  $\mathbf{x}$ 
  - CO<sub>2</sub> saturation field  $\mathbf{S}$
  - Pressure field  $\mathbf{P}$
  - Permeability  $\mathbf{K}$
- Observation:  $\mathbf{y}$ 
  - Seismic data
- Time  $t$  indexed by  $n$ 
  - Fluid dynamics:  $\mathbf{x}^n = f(\mathbf{x}^{n-1})$
- Seismic imaging:  $\mathbf{y}^n = h(\mathbf{x}^n, \nu\boldsymbol{\eta})$ , comprised of:
  - noise  $\nu\boldsymbol{\eta}$  with signal-to-noise ratio  $-20 \log \nu$  dB
- Rock physics model: maps  $\mathbf{S}$  to seismic velocity  $\mathbf{m}$  and density  $\boldsymbol{\rho}$ 
  - Seismic model: simulates seismic measurements of  $\mathbf{m}$  and  $\boldsymbol{\rho}$

Both the observation and transition operators require numerically solving nonlinear PDEs.

### A. Data assimilation

- Starting with a priori knowledge  $p(\mathbf{x}^0) \equiv p(\mathbf{x}^0 | \mathbf{y}^{1:0})$ :
- For each new observation  $\mathbf{y}^n$ :
  - We have a previous posterior:  $p(\mathbf{x}^{n-1} | \mathbf{y}^{1:n-1})$ .
  - Predict:  $p(\mathbf{x}^n | \mathbf{y}^{1:n-1}) = \int p(\mathbf{x}^n | \mathbf{x}^{n-1})p(\mathbf{x}^{n-1} | \mathbf{y}^{1:n-1}) d\mathbf{x}^{n-1}$
  - Update:  $p(\mathbf{x}^n | \mathbf{y}^{1:n}) \propto p(\mathbf{y}^n | \mathbf{x}^n)p(\mathbf{x}^n | \mathbf{y}^{1:n-1})$

Figure 1: Classical data assimilation predict-update loop

- Kalman filter: classical method that assumes linear operators and Gaussian distributions.

$$\boldsymbol{\mu}_a = \boldsymbol{\mu}_f + K(\mathbf{y}^* - h(\boldsymbol{\mu}_f, \mathbf{0})) \quad K = \text{cov}(\mathbf{x}_f, \mathbf{y}_f)\text{cov}(\mathbf{y}_f)^{-1}$$

$$B_a = (I - KH)B_f$$

- **EnKF**: Monte-Carlo method that represents distributions as samples

- Transitions each sample individually
- Observes each sample individually
- Updates samples based on the measured  $\mathbf{y}$  and the sample covariance

$$\mathbf{y}^* = h(\mathbf{x}^*, \nu^*\boldsymbol{\eta}^*) \quad K = \widehat{\text{cov}}(\mathbf{x}_f, \mathbf{y}_f) \left( \widehat{\text{cov}}(h(\mathbf{x}_f, \alpha\nu\boldsymbol{\eta})) + R \right)^{-1}$$

$$\mathbf{y}_{f,i} = h(\mathbf{x}_{f,i}, \nu\boldsymbol{\eta}_i) \quad R = \nu^2\beta^2 I$$

$$\mathbf{x}_{a,i} = \mathbf{x}_{f,i} + K(\mathbf{y}^* - \mathbf{y}_{f,i})$$

- $\nu^*$ : true noise scale
- $\beta$ : regularization scale
- $\nu$ : estimated noise scale
- $\alpha$ : 0 or 1 to choose whether noise is used in  $\text{cov}(\mathbf{y}_f)$

## III. EXPERIMENTS

We apply EnKF to a seismic monitoring example using scalable, open-source tools (JutulDarcy.jl, JUDI.jl).

Simplifying assumptions:

1. All information is known a priori except for  $\mathbf{K}$ .
2. We can generate 256 samples of possible  $\mathbf{K}$ .

We compare EnKF to two baselines for estimating  $\mathbf{S}$ :

- **JustObs**: solely uses  $\mathbf{y}$  and observation function
- **NoObs**: solely uses samples of  $\mathbf{K}$  and transition function

We also test EnKF performance for modified  $\alpha$ ,  $\beta$ ,  $\nu$ , and  $\nu^*$ .

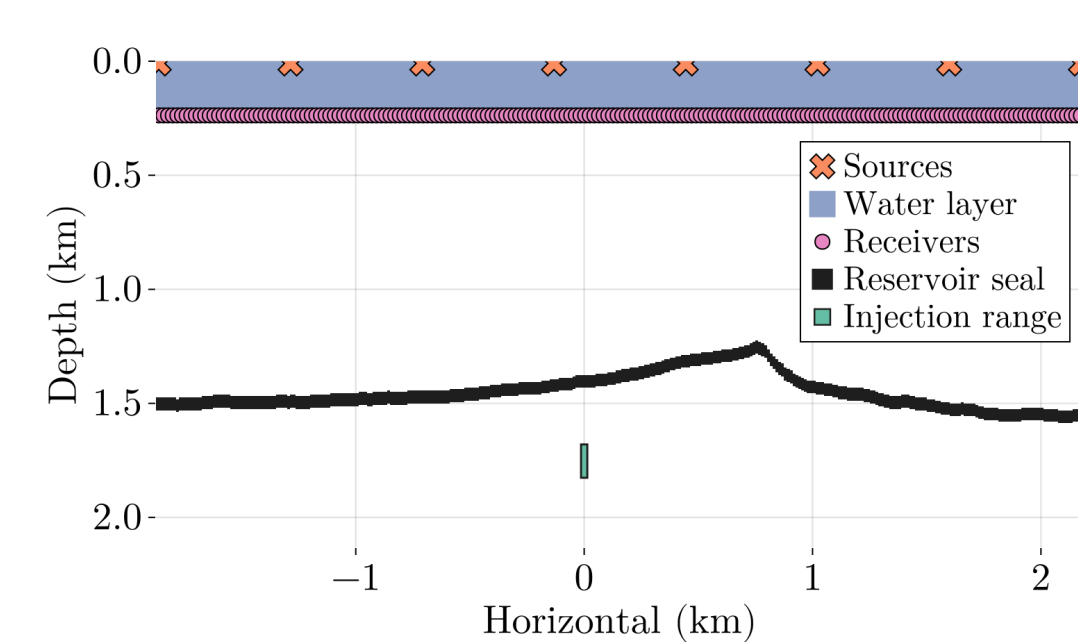


Figure 2: Experimental setup

# Seismic monitoring of CO<sub>2</sub> using ensemble Kalman filtering

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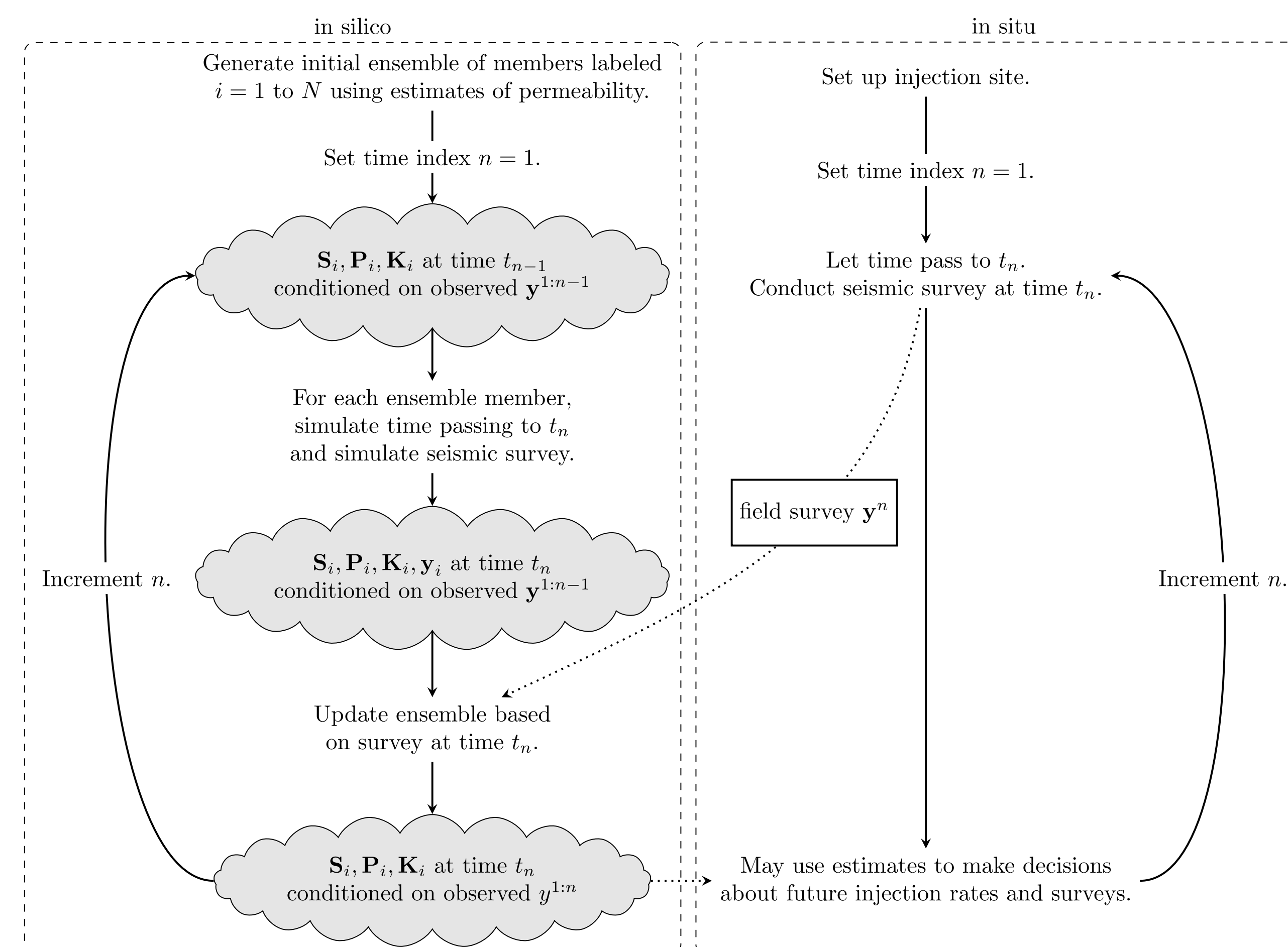


Figure 3: Workflow diagram

## IV. RESULTS

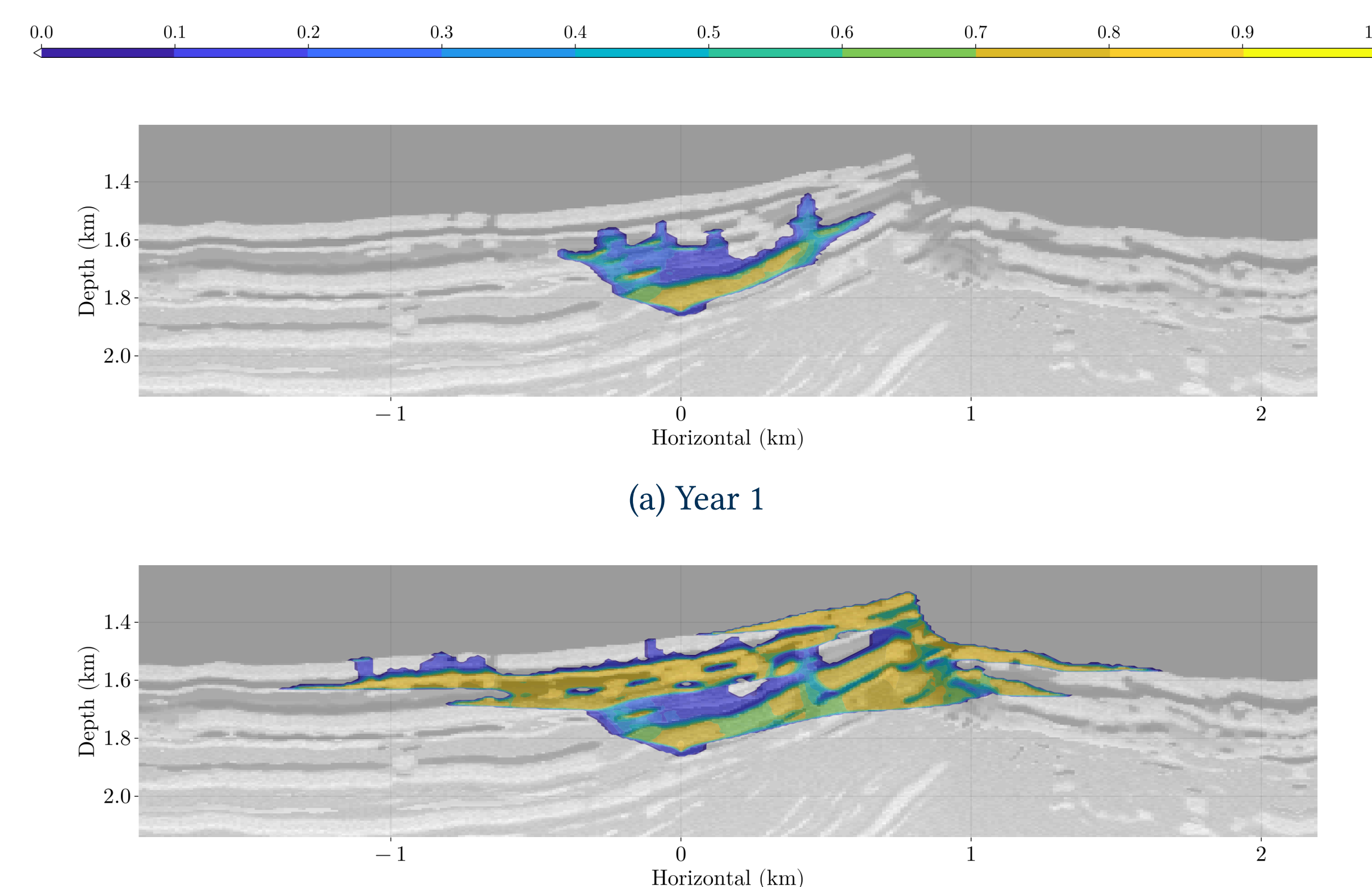


Figure 4: Ground-truth saturation field  $\mathbf{S}$  overlaid on permeability  $\mathbf{K}$

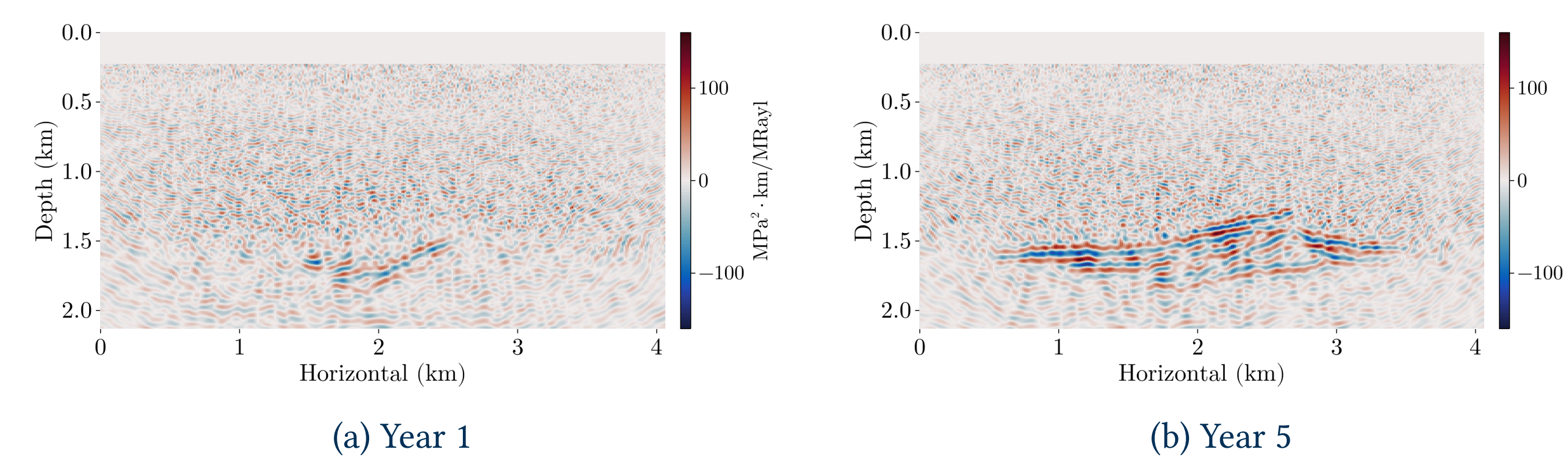


Figure 5: Ground-truth seismic measurements

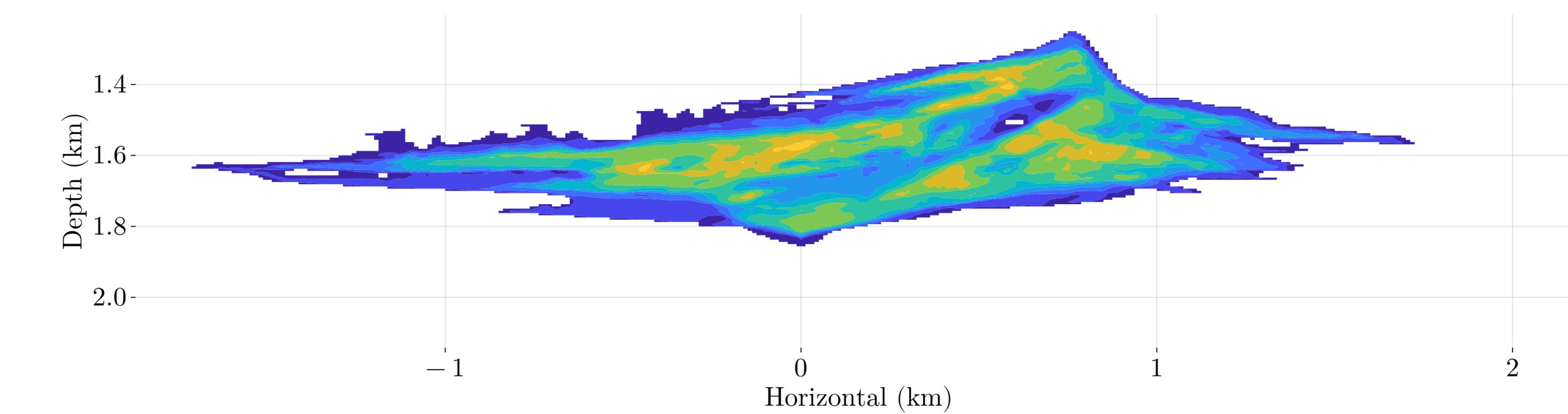


Figure 6: NoObs prediction at year 5

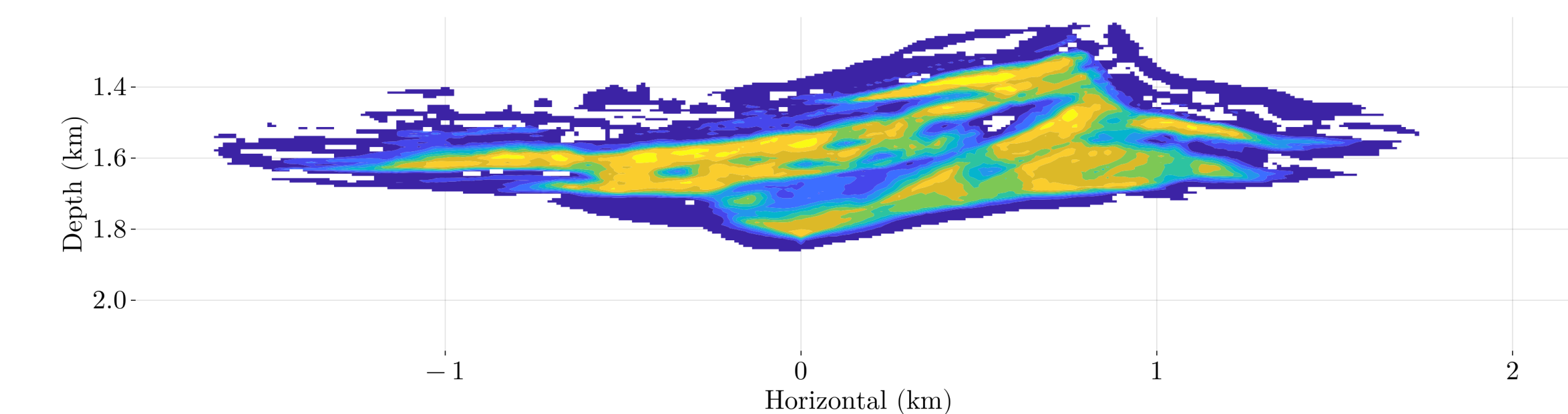


Figure 7: EnKF analysis at year 5

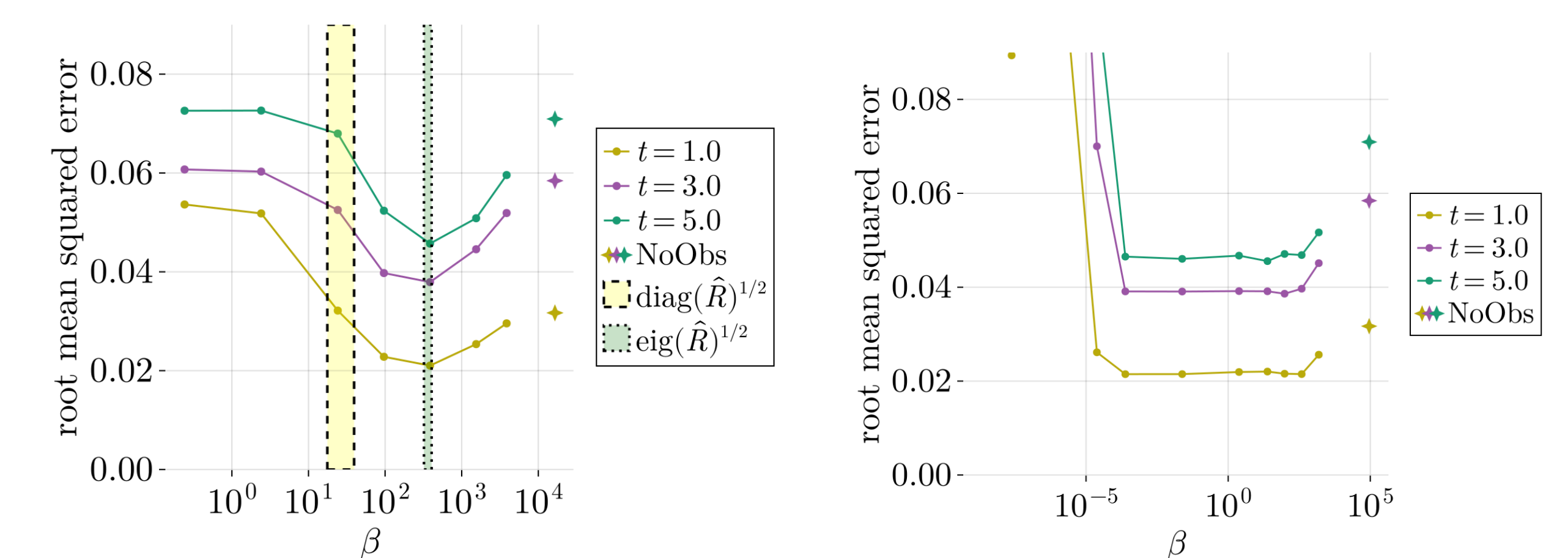


Figure 8: Change  $\beta$  when  $\alpha = 0$

Figure 9: Change  $\beta$  when  $\alpha = 1$

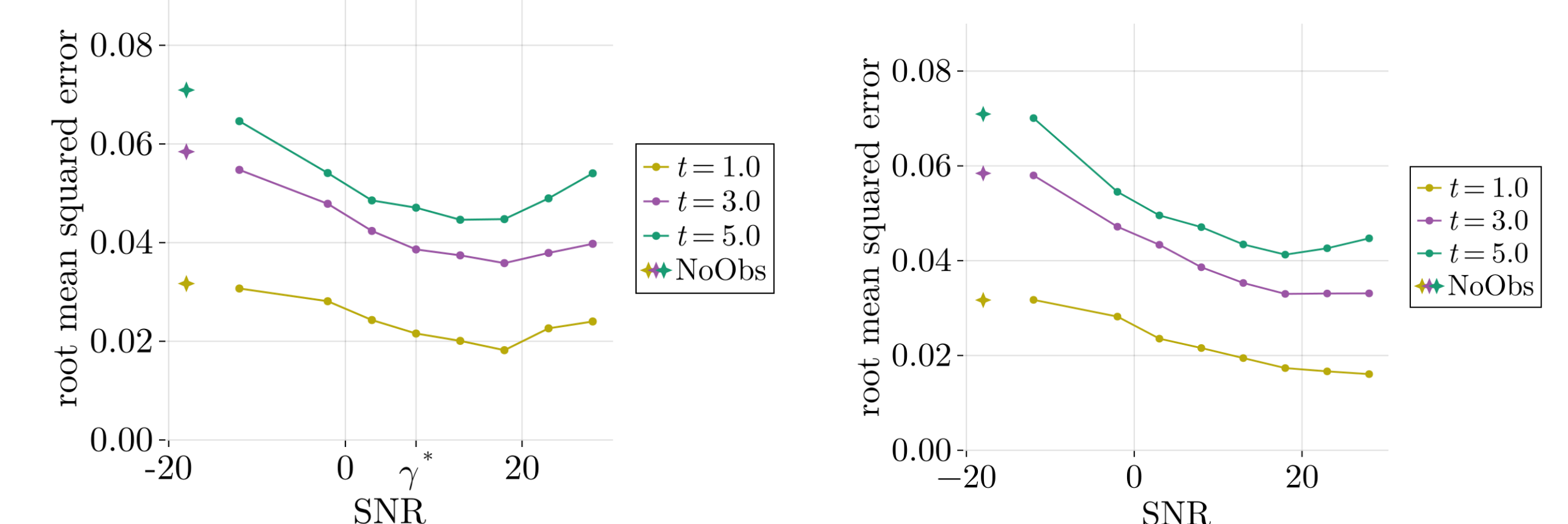


Figure 10: Change  $\nu$

Figure 11: Change  $\nu^*$ , keeping  $\nu = \nu^*$

## V. CONCLUSIONS

- EnKF error < JustObs error and NoObs error.
- For  $\alpha = 0$ ,
  - sensitive to noise parameters
  - best results using noise eigenvalues
- For  $\alpha = 1$ ,
  - insensitive over large range
  - similar error to lowest  $\alpha = 0$  error

**EnKF is a promising data assimilation method for monitoring subsurface CO<sub>2</sub> with seismic measurements.**

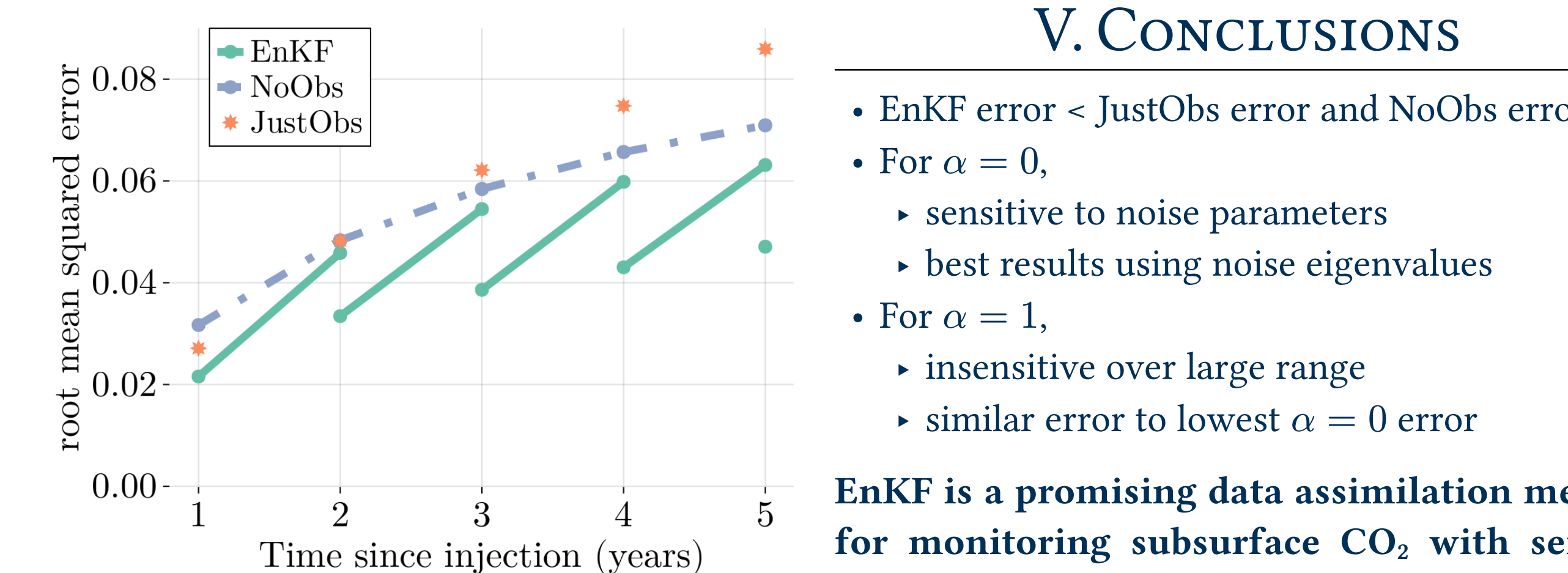


Figure 12: RMSE for 3 methods over time



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