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# Tracking the spatial-temporal evolution of fractures by microseismic source collocation

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### Unconventional Reservoir Schematic

### **Objectives**

- detection of microseismic events in space and time
- estimation of source time function



[Rentsch et al., '07; McMechan, '82; Gajewski et al., '05; Nakata et al.,'16; Bazargani et al.,'16] [Thurber et al., '00; Waldhauser et al.,'00]

# Pre-existing methods

- Arrival time picking based methods:
  - estimate the location and origin time
  - can be challenging in the presence of noise

Imaging based methods:

- It do not require arrival time picking
- based on back propagation
- estimate the location and origin time

require scanning of complete 4D volume (3D in space and 1D in time)



[Sjögreen et al., '14; Wu et al., '96; Kim et al., '11; Michel et al., '14; Kaderli et al., '15] [Rodriguez et al., '12; Ely et al., '13]

# Pre-existing methods

- Dictionary learning based methods:

  - require forming large dictionaries based on
  - require prior knowledge of source-time function
- Full-waveform inversion (FWI) based methods:
  - invert for source parameters
  - some of these methods assume prior knowledge of source-time function source-time function to be a gaussian function

simultaneously estimate location, origin time and source mechanism

number of sources, number of receivers and number of time samples



[Sharan et al.,'16]

# Proposed method w/ sparsity promotion

### Estimates complete source field in:

- space and
- ► time



[Sharan et al.,'16]

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- shape of source-time function
- prior knowledge of source-time function



[Sharan et al.,'16]

# Proposed method w/ sparsity promotion

### Estimates complete source field in:

- space and
- ▶ time

No assumptions on:

- shape of source-time function
- prior knowledge of source-time function

### Needs:

- sufficiently accurate medium velocity model
- position of receivers



# Proposed method w/ sparsity promotion



### Unconventional Reservoir Schematic

### Assumptions

Iocalized in space



# Proposed method w/ sparsity promotion



### Unconventional Reservoir Schematic



Iocalized in space

finite energy along time



[Van Den Berg et al.,'08]



 $\mathbf{Q} \in \mathbb{R}^{n_x imes n_t}$ 

 $n_x$ : number of grid points  $n_t$ : number of time samples



[Van Den Berg et al.,'08]



 $\mathbf{Q} \in \mathbb{R}^{n_x imes n_t}$ 

 $n_x$ : number of grid points  $n_t$ : number of time samples

Similar to classic Basis pursuit denoising (BPDN)



[Lorentz et al., '14; Herrmann et al., '15; Sharan et al., '16]

# Solving w/linearized Bregman

minimize  $\|\mathbf{Q}\|$ subject to  $\|\mathcal{F}\|$ \*where  $\|.\|_F$  is the Frobenius norm

- Recent successful application to seismic imaging problem
- Three-step algorithm simple to implement
- Choice of  $\mu$  controls the trade off between sparsity and the Frobenius norm
- $\mu \uparrow \infty$  corresponds to solving original BPDN problem

$$\begin{aligned} \|\mathbf{2}_{,1} + \frac{1}{2\mu} \|\mathbf{Q}\|_F^2 \\ \mathbf{m}](\mathbf{Q}) - \mathbf{d}\|_2 \le \epsilon \end{aligned}$$



Data d, slowness square m //Input 1. 2. for  $k = 0, 1, \cdots$  $\mathbf{V}_k = \mathcal{F}^{\top}[\mathbf{m}](\Pi_{\epsilon}(\mathcal{F}[\mathbf{m}](\mathbf{Q}_k) - \mathbf{d}))$  //adjoint solve 3.  $\mathbf{Z}_{k+1} = \mathbf{Z}_k - t_k \mathbf{V}_k$  //auxiliary variable update 4.  $\mathbf{Q}_{k+1} = \operatorname{Prox}_{\mu\ell_{2,1}}(\mathbf{Z}_{k+1})$  //sparsity promotion 5. 6. end  $\mathbf{I}(\mathbf{x}) = \sum_{t} |\mathbf{Q}(\mathbf{x}, t)| / \text{Intensity plot}$ 7.



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\*  $\Pi_{\epsilon}(\mathbf{x}) = \max\{0, 1 - \frac{\epsilon}{\|\mathbf{x}\|}\}.(\mathbf{x})$  the projection on to  $\ell_2$  norm ball



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# • Source location: estimated as outlier in intensity plot Source-time function: temporal variation of wavefield at estimated source location





































Friday, October 6, 2017



# Case study: two far sources



### Modeling information:

Model size: 0.7 km x 0.7 km Grid spacing: 5m Receiver spacing: 10m Receiver depth: 20m Fixed spread: 0.69km Sampling interval: 2 ms Recording length: 1s Peak frequency : 30 Hz Dominant wavelength: 46 m



# Data and estimated location







# Data and estimated location







# **Estimated wavelet**



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# What happens when sources are very close?



**Microseismic data** 



# Estimated location after 150 iterations



Estimated location,  $\mu$  = 8e-4


### Estimated location after 150 iterations



Estimated location,  $\mu$  = 8e-4



### Estimated location after 150 iterations





### Estimated location after 150 iterations





### Convergence comparison





### Convergence comparison



# Motivation for locating closely spaced sources: for accurate fracture mapping



### Convergence comparison



Motivation for locating closely spaced sources: for accurate fracture mapping

Challenges with linearized Bregman algorithm:

- need higher value of µ to resolve closely spaces sources
- $\blacktriangleright$  higher values of  $\mu$  needs more iterations



### [Huang et al.,'13; Yin ,'10] Convergence comparison



Motivation for locating closely spaced sources: for accurate fracture mapping

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Acceleration with quasi-Newton:

- Inearized Bregman algorithm is equivalent to solving dual problem by gradient descent
- we accelerate the dual problem using quasi-Newton



[Huang et al., '13; Yin , '10]

# Acceleration with quasi-Newton: Algorithm

1. Initialize dual variable  $y = 10^{-3} d$ 2.  $\hat{\mathbf{y}} = \text{L-BFGS}(f(\mathbf{y}), g(\mathbf{y}), \mathbf{y}, k)$  //Dual solution 3.  $f(\mathbf{y}) = \Psi(\mathbf{y}) - \epsilon \|\mathbf{y}\|_2$  //L-BFGS objective where  $g(\mathbf{y}) = \Psi'(\mathbf{y}) - \epsilon \mathbf{y} / \|\mathbf{y}\|_2$  //L-BFGS gradient and  $\hat{\mathbf{Q}} = \operatorname{Prox}_{\mu\ell_{2,1}}(\mu \mathcal{F}[\mathbf{m}]^{\top}(\hat{\mathbf{y}})) / \operatorname{Primal solution}$ 4. 5.  $\mathbf{I}(\mathbf{x}) = \sum_{t} |\hat{\mathbf{Q}}(\mathbf{x}, t)| / \text{Intensity plot}$ 

\* 
$$\Psi(\mathbf{y}) = \min_{\mathbf{Q}} \|\mathbf{Q}\|_{2,1} + \frac{1}{2\mu} \|\mathbf{Q}\|_F - \mathbf{y}^\top (\mathcal{F}[\mathbf{m}]) \|\mathbf{Q}\|_F$$
  
\*  $\Psi'(\mathbf{y}) = \mathbf{d} - \mathcal{F}[\mathbf{m}] (\operatorname{Prox}_{\mu\ell_{2,1}}(\mu \mathcal{F}[\mathbf{m}]^\top(\mathbf{y})))$  is the gradient

- Data d, slowness square m, number of iterations k //Input

- $\mathbf{Q}) \mathbf{d}$
- t of  $\Psi(\mathbf{y})$



[Huang et al., '13; Yin , '10]

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$$\Psi(\mathbf{y}) = \min_{\mathbf{Q}} \|\mathbf{Q}\|_{2,1} + \frac{1}{2\mu} \|\mathbf{Q}\|_F - \mathbf{y}^\top (\mathcal{F}[\mathbf{m}]) \|\mathbf{Q}\|_F$$
  
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Data d, slowness square m, number of iterations k //Input

lives in much smaller space :

- dimensions equals that of observed data
- better approximation of inverse Hessian by storing more and more dual variable updates

 $\mathbf{Q}) - \mathbf{d}$ 

nt of  $\Psi(\mathbf{y})$ 



[Herrmann et al.,'09;]

## Further acceleration w/ 2D Preconditioning

### Each iteration of L-BFGS requires solving at least one

- wave equation and
- ▶ its adjoint



[Herrmann et al.,'09;]

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### Each iteration of L-BFGS requires solving at least one

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### Requires further reduction in the total number of iterations due to:

- the problem size and
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[Herrmann et al.,'09;]

# Further acceleration w/ 2D Preconditioning

### Each iteration of L-BFGS requires solving at least one

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### Left preconditioner:

- accelerates the convergence

 $\blacktriangleright$  reduces the condition number of 2D forward modeling operator  $\mathcal{F}$ 



# Further acceleration w/ 2D Preconditioning

- In 2D, a point source implicitly assumes
  - ▶ a line source
  - extending infinitely in the out of plain direction

### This causes wavefields to have:

- amplitude and
- b phase differ from the wavefields of a true point source

### We introduce:

- a symmetric half differentiation correction along time corrects for the amplitude and phase of 2D wavefield which acts as a left preconditioner



## Modified problem w/ 2D Preconditioning

minimize  $\|\mathbf{Q}\|_{2,1} + \frac{1}{2\mu} \|\mathbf{Q}\|_F^2$ 

\*with  $\mathcal{M}_L := \partial_{|t|}^{1/2}$  is the half differentiation correction \*where  $\partial_{|t|}^{1/2} = \mathbf{F}^{-1} |\omega|^{1/2} \mathbf{F}$ \***F** is the Fourier transform and  $\omega$  is the frequency  $\gamma$  is the noise level

subject to  $\|\mathcal{M}_L \mathcal{F}[\mathbf{m}](\mathbf{Q}) - \mathcal{M}_L \mathbf{d}\|_2 \leq \gamma$ 



### Result for two close sources



# With L-BFGS and 2D preconditioner

### 10 iterations



### Result for two close sources



# With L-BFGS and 2D preconditioner

### 10 iterations



# **Convergence comparison: LBR vs L-BFGS**



**Convergence** comparison

• Using same value of  $\mu$ 

Improvement in convergence with Dual formulation and

D Preconditioning



# Numerical Experiment: BG Compass model



#### **BG Compass model**

<sup>3</sup> Modeling information:

Model size: 2.25 km x 0.915 km Grid spacing: 5 m Total number of sources: 2 Peak frequency : 30 Hz Receiver spacing: 10m Receiver depth: 20m Sampling interval: 0.5 ms Recording length: 1 s Free surface: No



# Numerical Experiment: BG Compass model



#### **BG Compass model**

Adjacent sources are located within half a wavelength with overlapping source-time functions

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### Data







### Estimated source location in 10 iterations

#### w/noise free data and true velocity model







### Estimated source location in 10 iterations

#### w/noise free data and true velocity model



















Marmousi model

Modeling information:

**Model size:** 3.15 km x 1.08 km Grid spacing: 5 m **Total number of sources:** 7 Peak frequency: 22 Hz, 25 Hz & 30 Hz Receiver spacing: 10m Receiver depth: 20m Sampling interval: 0.5 ms Recording length: 1 s Free surface: No



### Numerical Experiment: Marmousi model [km/s]4 3.5 <u>د</u> 0.5 3 Ν 2.5 2 3 0 x [km]

Marmousi model

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### **Evolving seismicity**



# x [km]



### **Evolving seismicity**





### Data



Noise free microseismic data





# Estimated source location in 10 iterations

#### w/noise free data and true velocity model



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#### w/noisy data and smooth velocity model



# Estimated source location in 10 iterations

#### w/noise free data and true velocity model



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#### w/noisy data and smooth velocity model

















#### Peak frequency: 30 Hz









#### Peak frequency: 22 Hz



### Conclusions

### Sparsity promotion based method:

- wavelength
- works w/ sources of different frequencies & origin times



• can provide locations of fractures by resolving microseismic sources within half a



### Conclusions

- Sparsity promotion based method:

  - wavelength
  - works w/ sources of different frequencies & origin times

Dual formulation provides a computationally efficient scheme.



• can provide locations of fractures by resolving microseismic sources within half a


## Future work

#### Elastic data validation



Iocate microseismic sources from P-phase data using acoustic inversion codes



## Future work

#### Elastic data validation

#### Extension to 3D



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### Future work

#### Elastic data validation

Iocate microseismic sources from P-phase data using acoustic inversion codes

#### Extension to 3D

#### Work on field data





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## Thank you !!

