

# Anisotropic RTM applied to field data

Philipp Witte, Felix J. Herrmann, October 26, 2015

# Introduction

## Seismic survey by BP from Machar oil field

- ▶ initial 3D marine survey in eastern North Sea in 1989
- ▶ high density OBC multi-azimuth survey in 2011
- ▶ large salt dome with chalk and sandstone oil reservoirs

## Seismic imaging and processing by BP

- ▶ difficult conditions due to weak reservoir reflectivity, multiples and disruption from shallow gas channels
- ▶ post-stack time migration image in 1990
- ▶ pre-stack time migration in 2003
- ▶ anisotropic pre-stack Kirchhoff migration in 2006

# Introduction

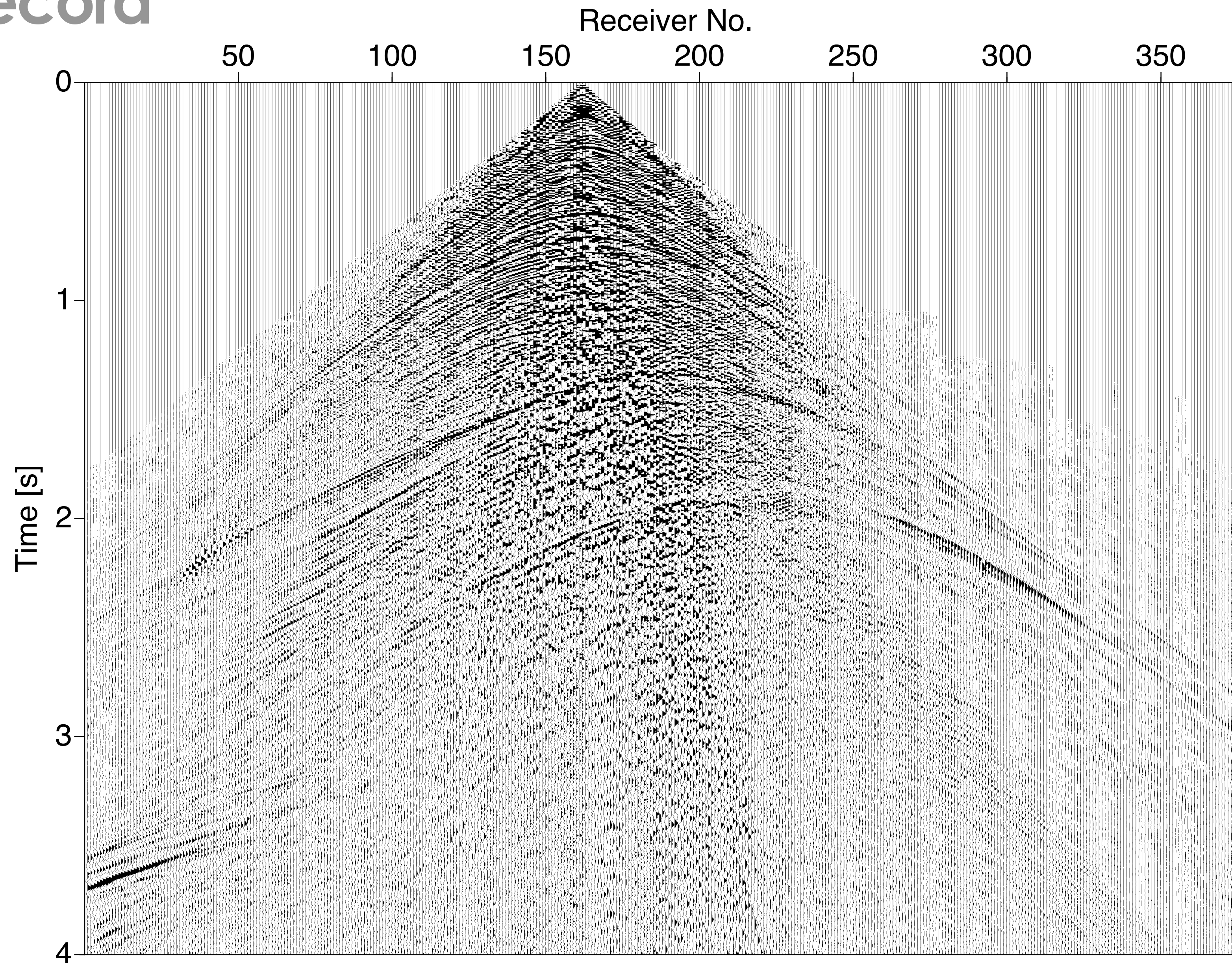
BP supplied us with a 2D line from the 2011 OBC data set

- ▶ 330 Shots with 8 seconds recording time (50 m shot spacing)
- ▶ up to 505 receivers (25 m spacing)
- ▶ background velocity model + anisotropy parameters
- ▶ particular interest in eastern flank of salt dome

The shots were preprocessed by BP

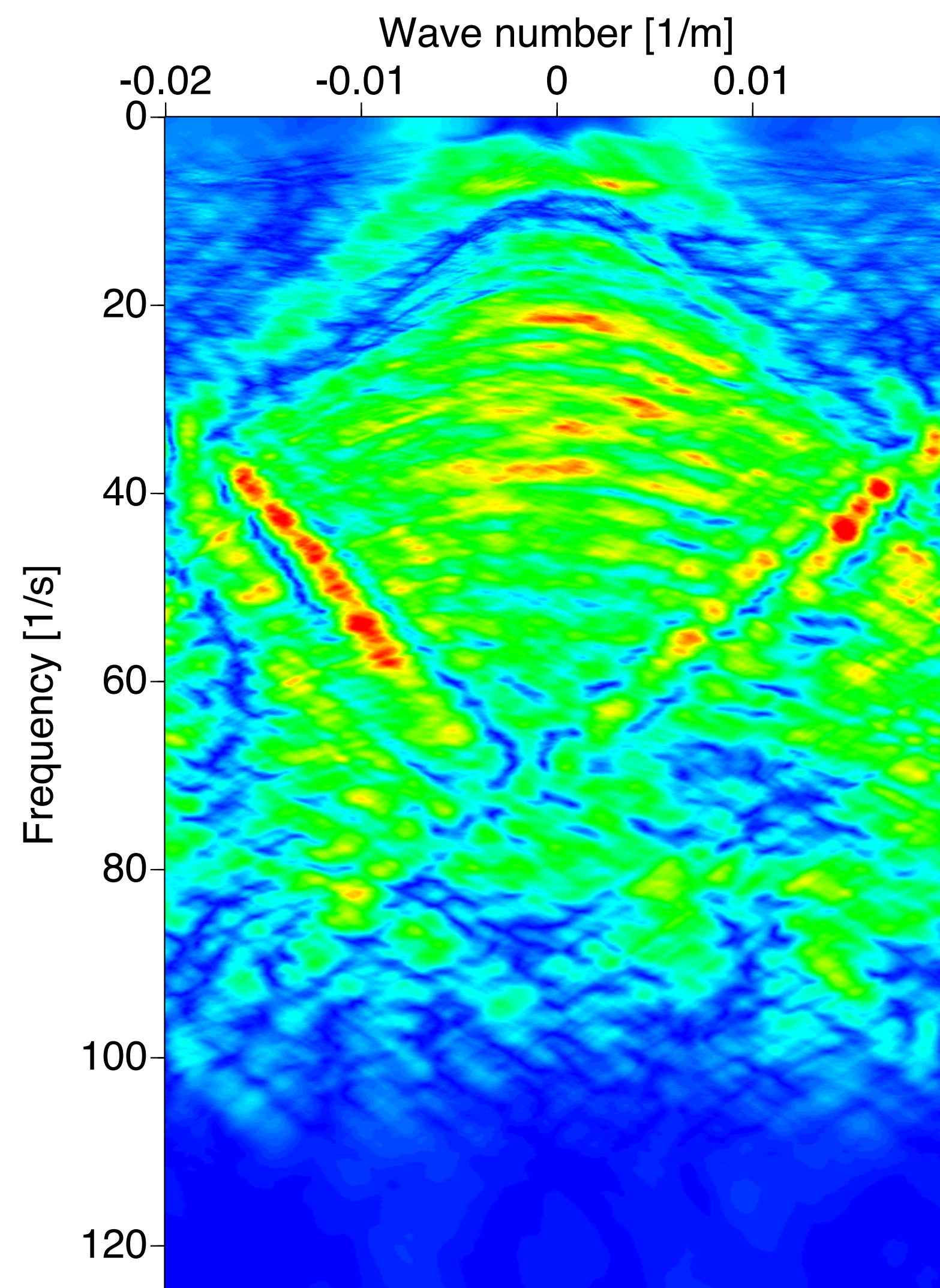
- ▶ source signature
- ▶ mute of direct wave
- ▶ removal of multiples

# Shot record

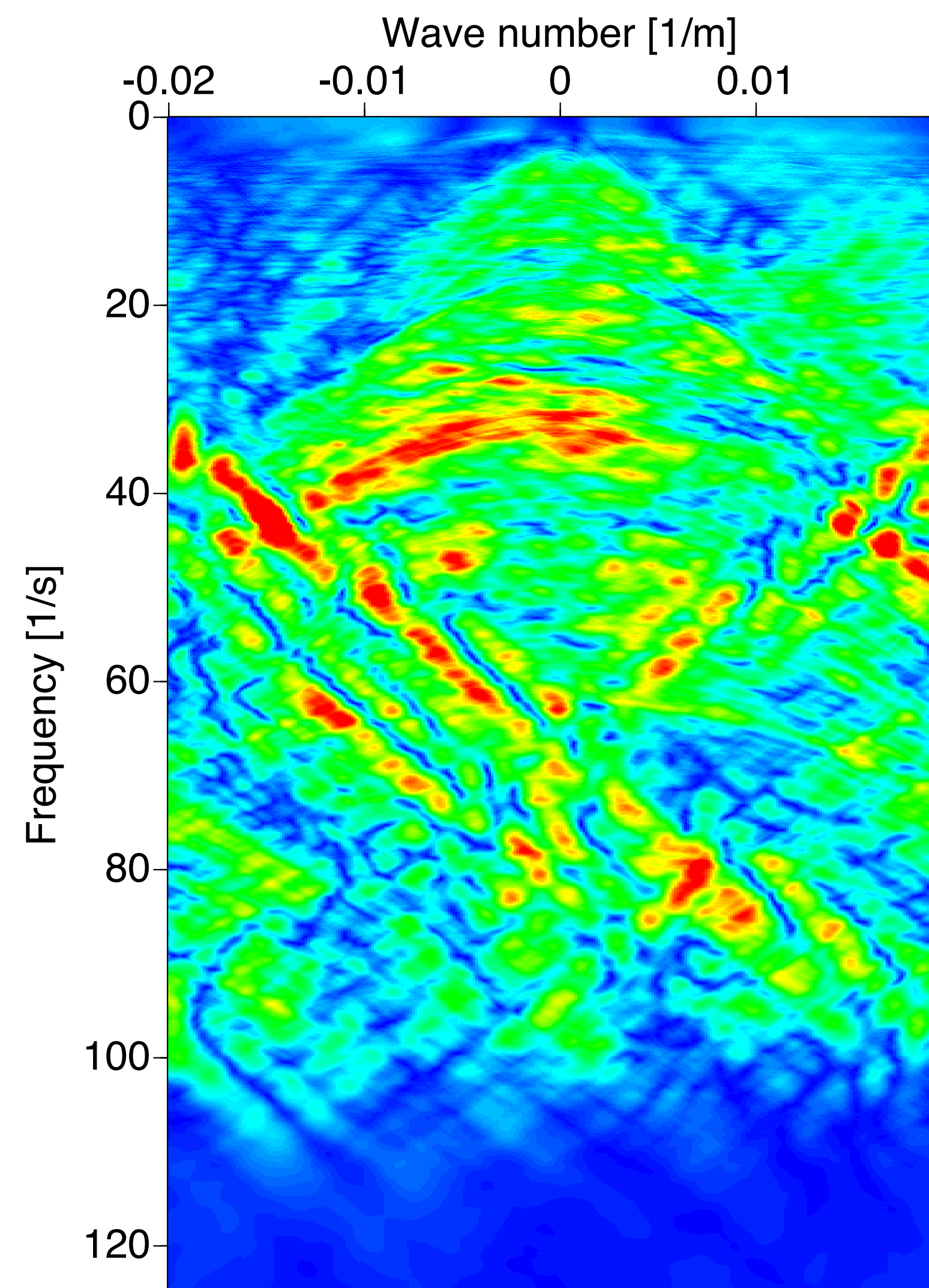


(All shown data and subsurface parameters by courtesy of BP)

# FK Spectra

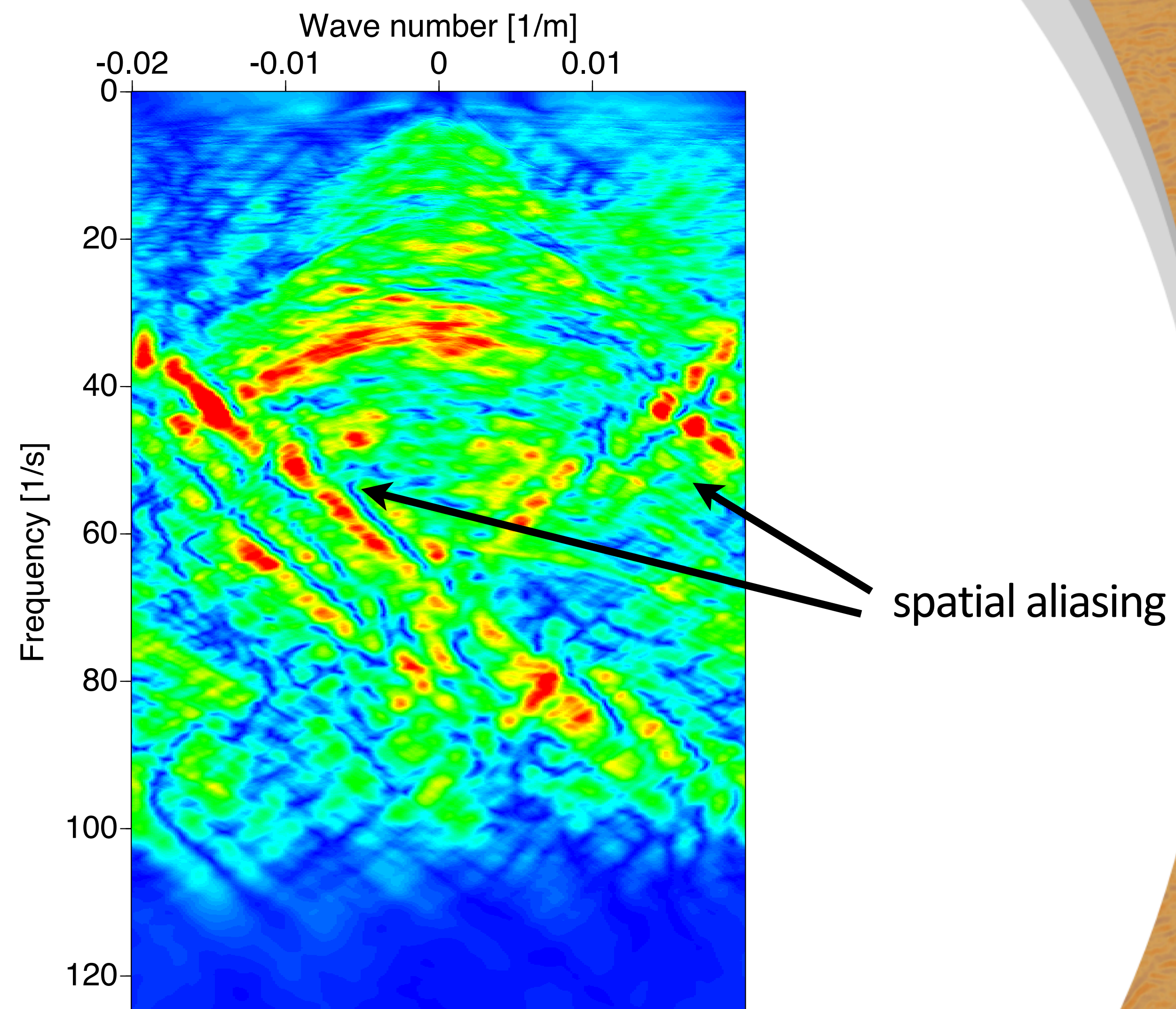
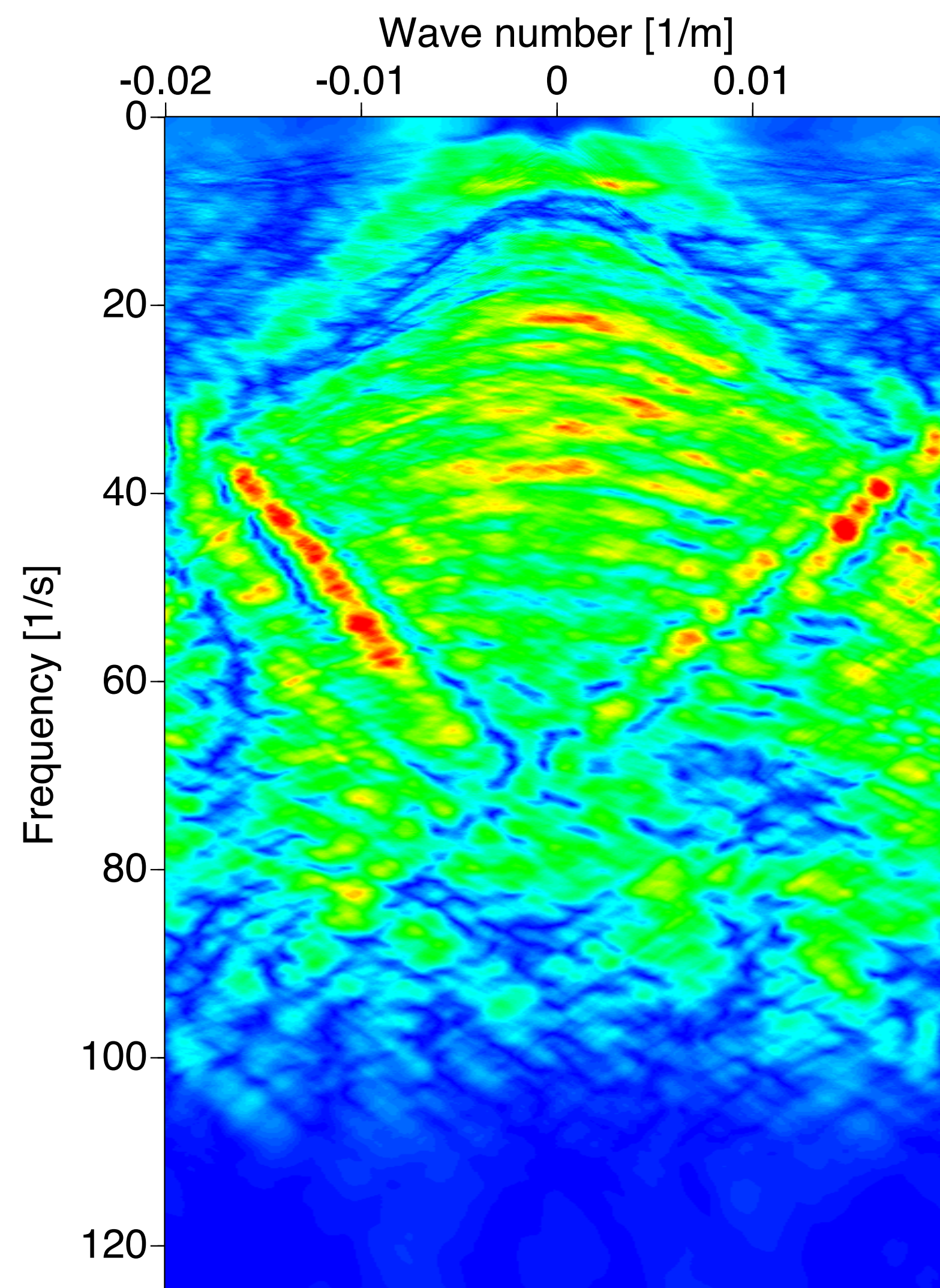


Shot No. 80

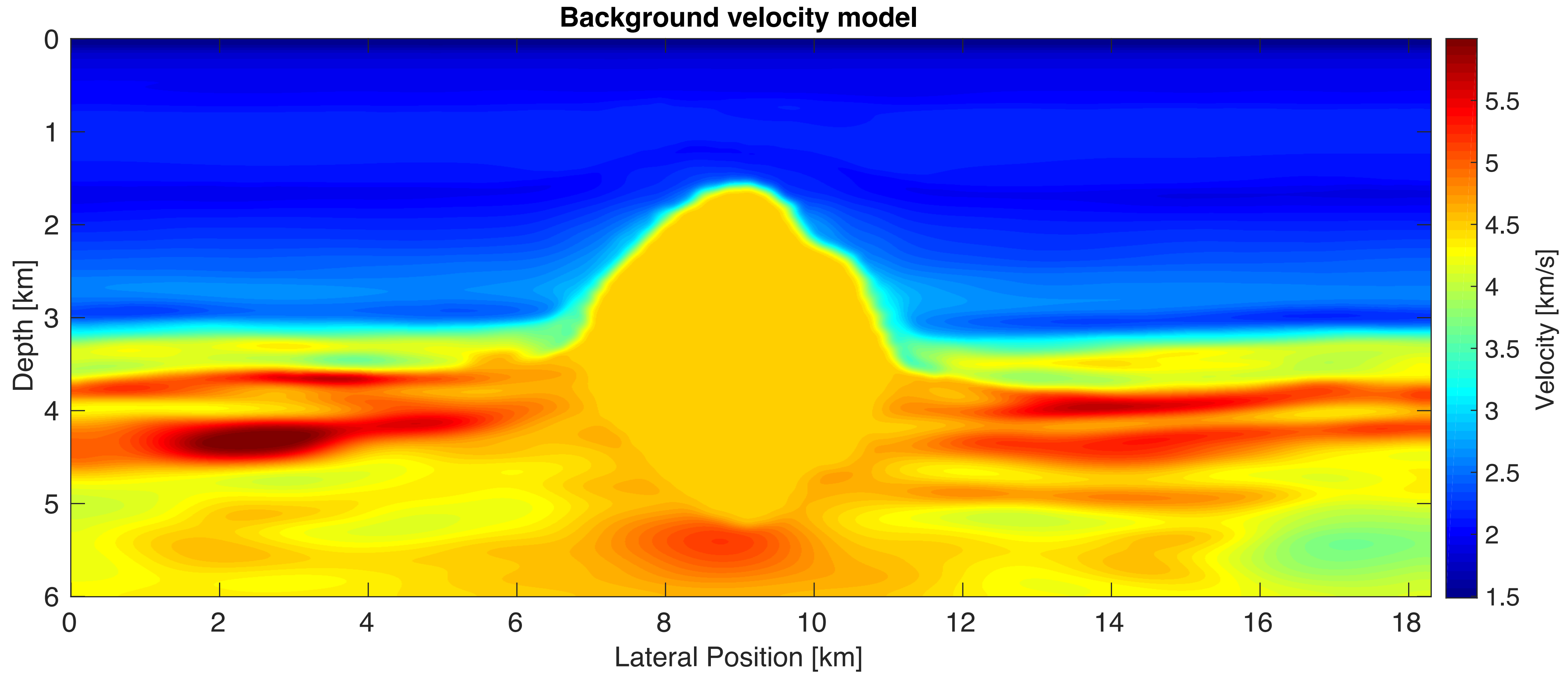


Shot No. 120

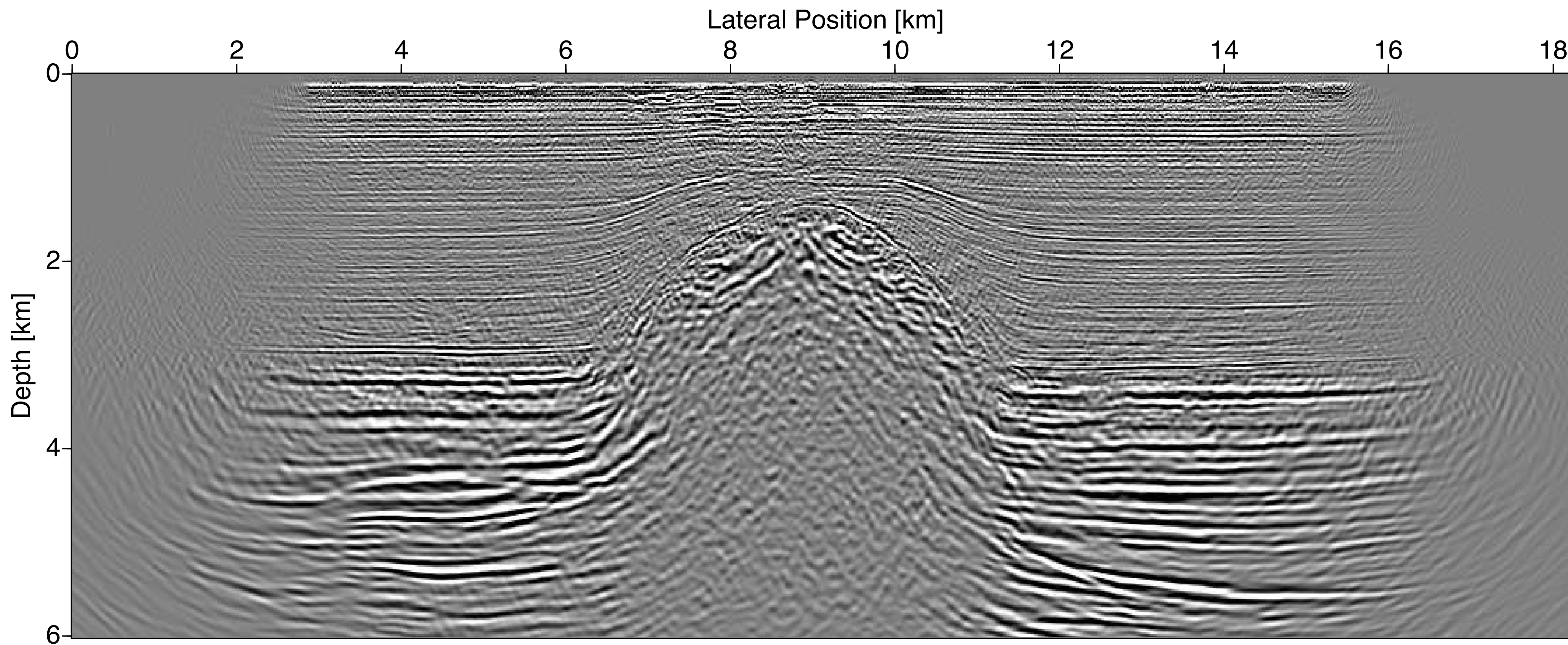
# FK Spectra



# Machar velocity model



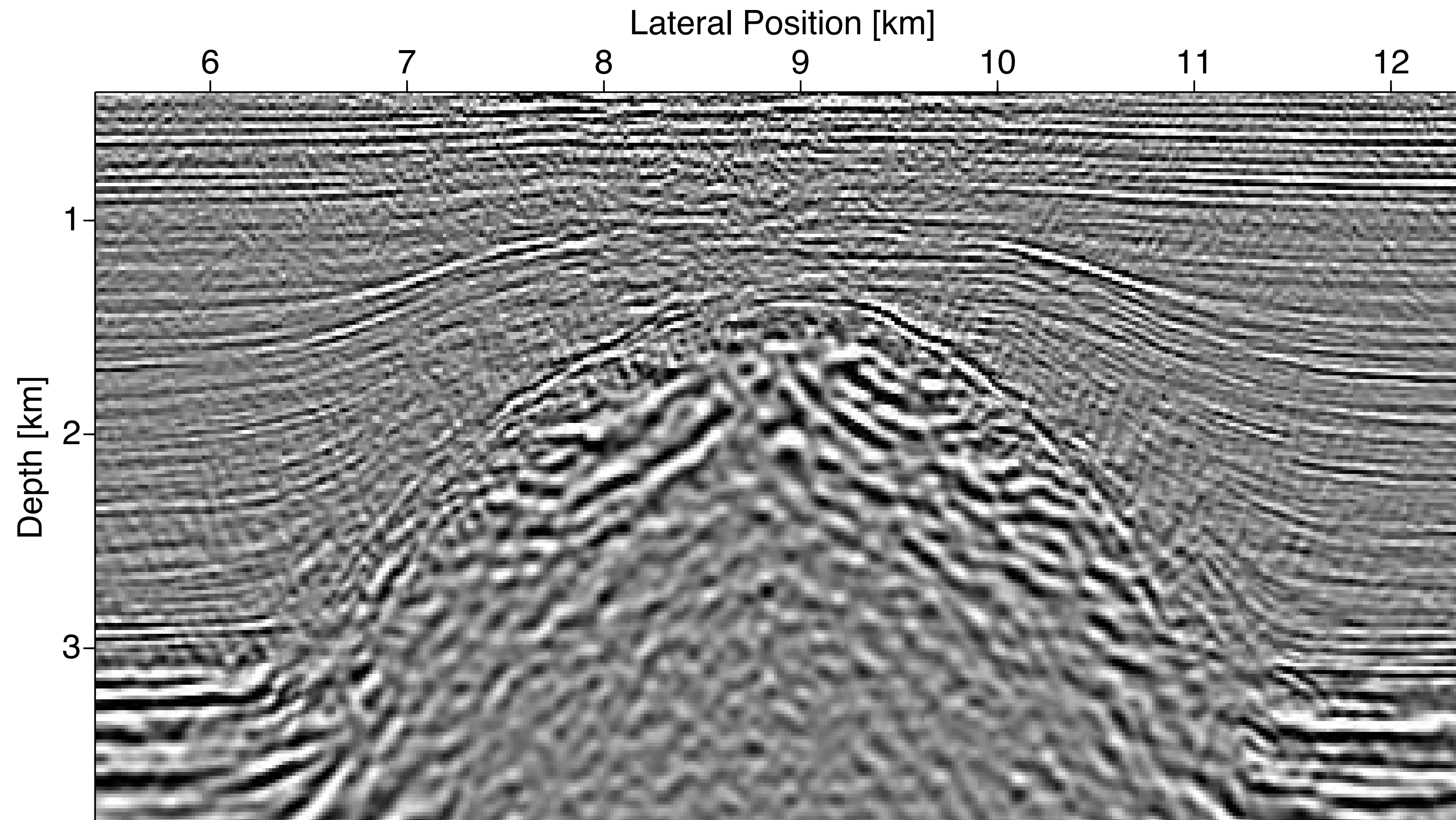
# RTM Image



Result with data supplied by BP



# Close-Up



## Machar data set

### Initial shot records:

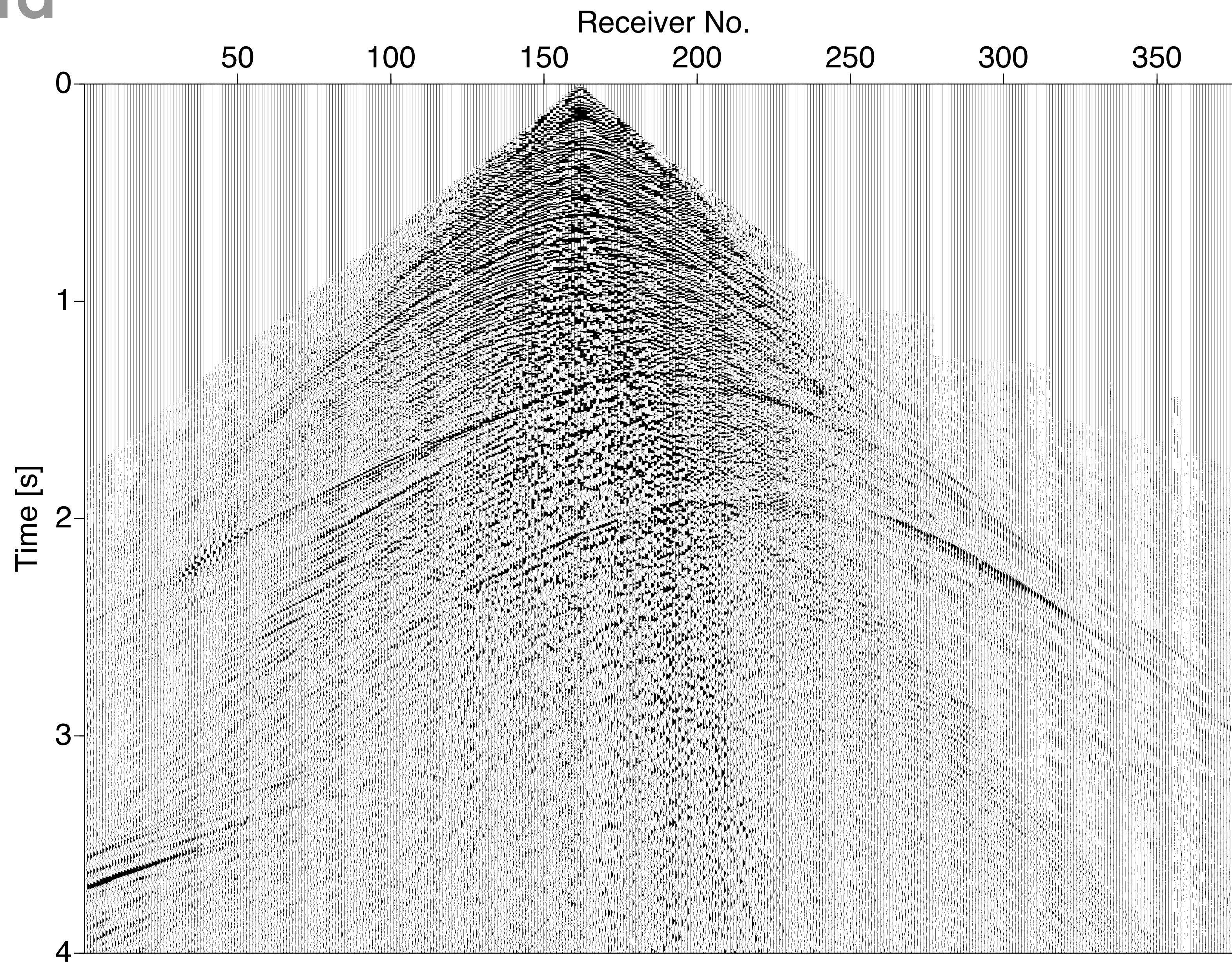
- ▶ spatial aliasing
- ▶ noise/marine ground roll
- ▶ corrupted traces

### SLIM preprocessing:

- ▶ trace interpolation via curvelet-domain basis pursuit
- ▶ FK filtering

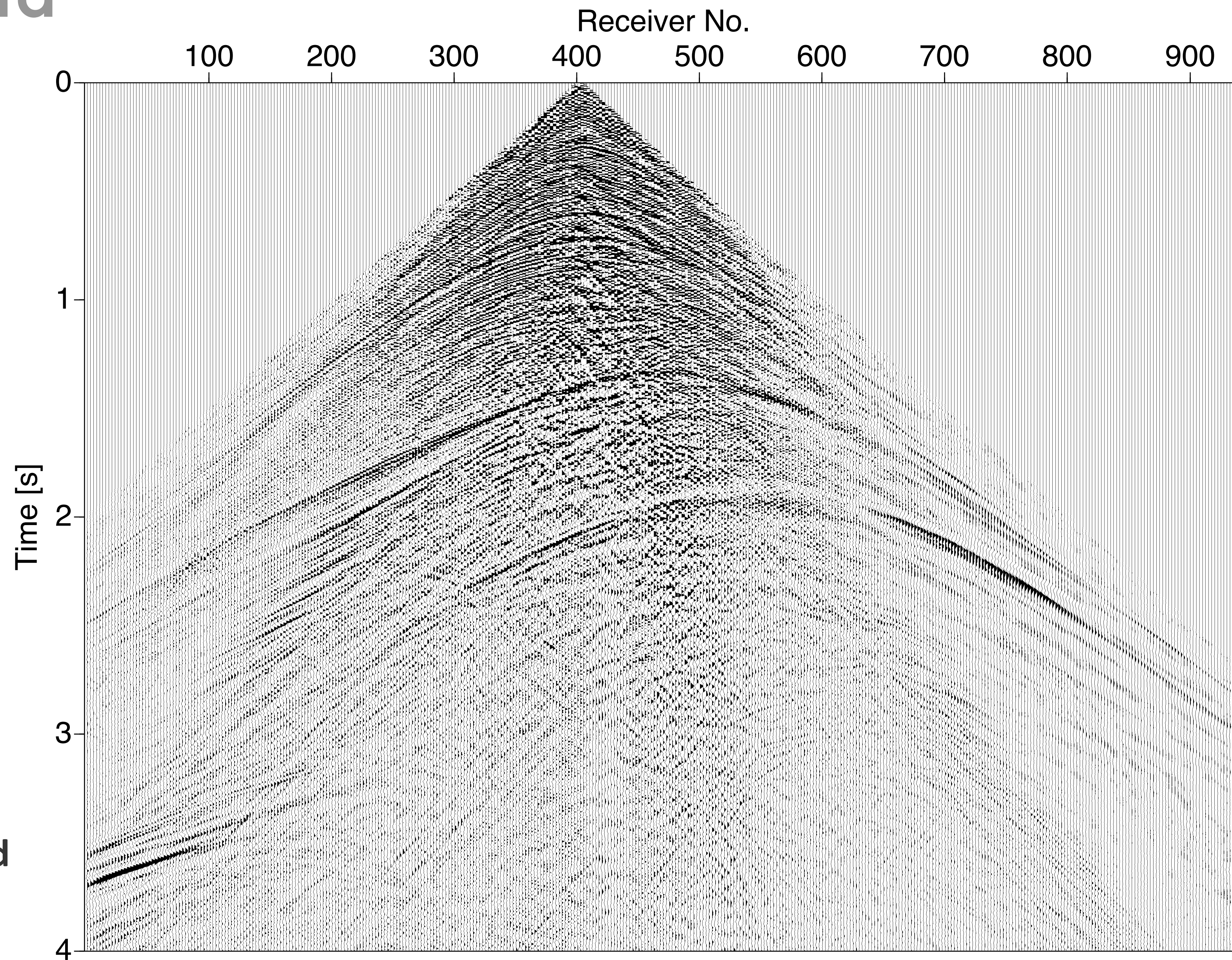
(Ning Tu, Tim Lin, Zhilong Fang (2013): Slim's findings on the Machar data set)

# Shot record



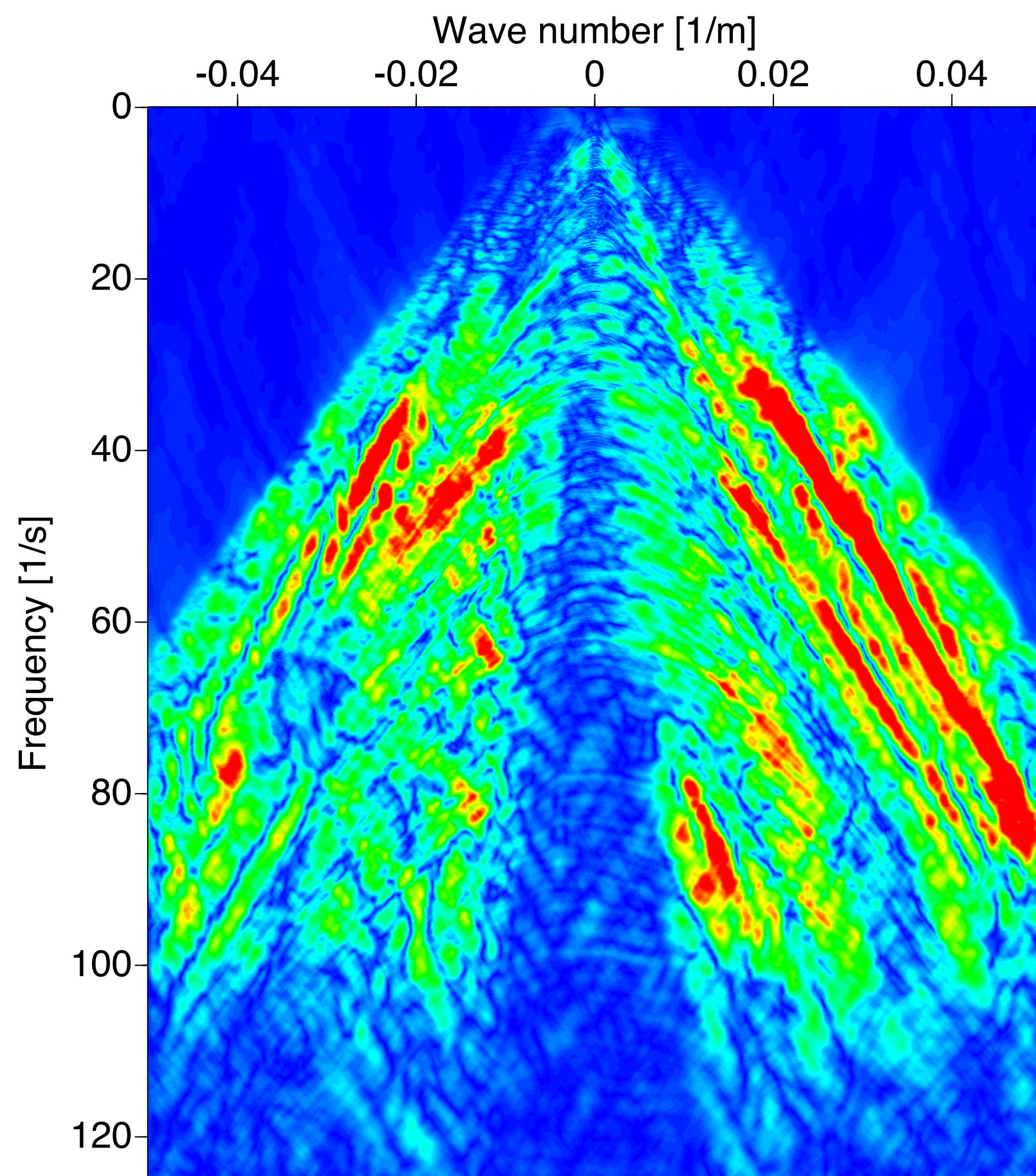
Initial shot record

# Shot record

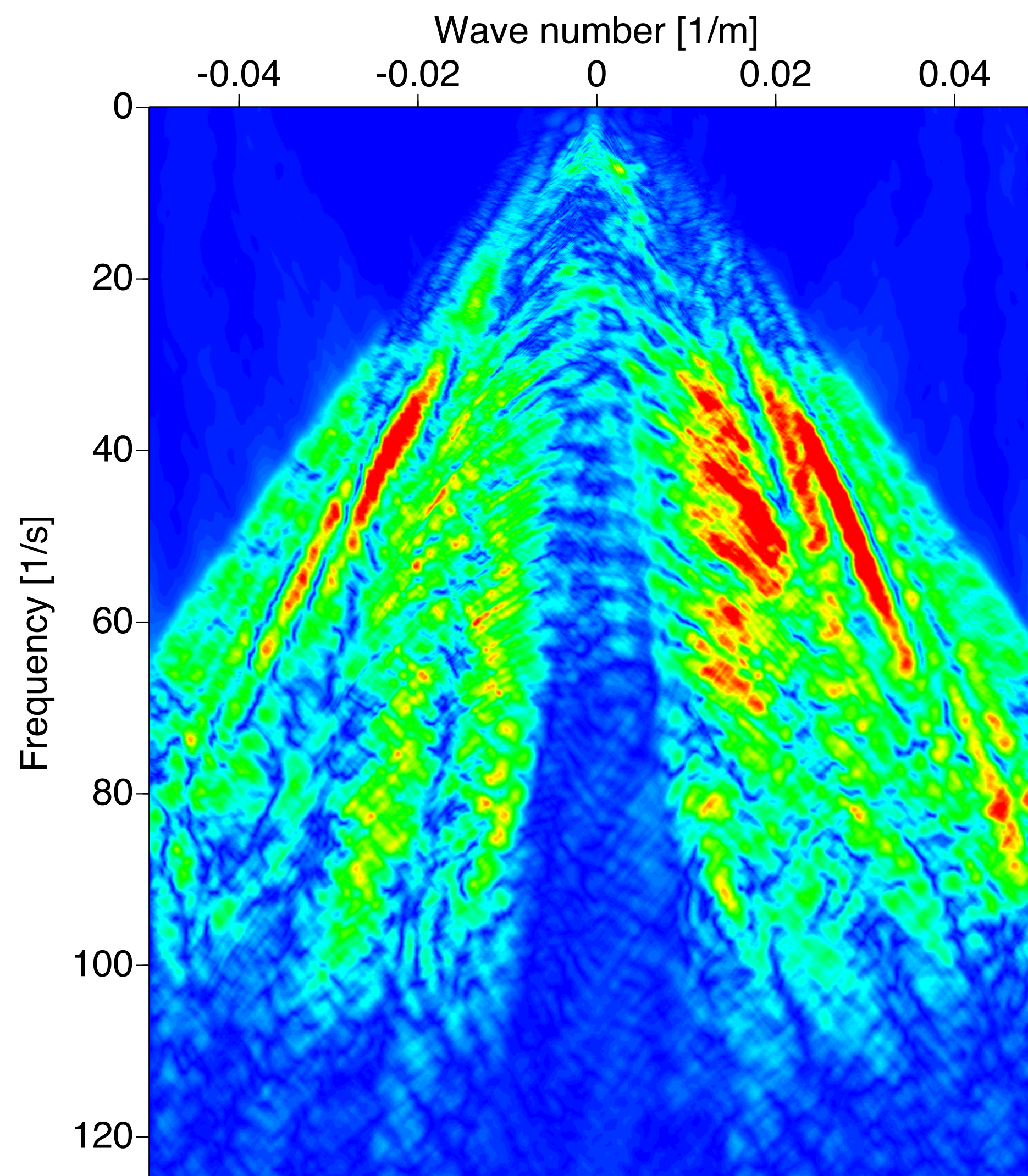


Processed shot record

# FK Spectra

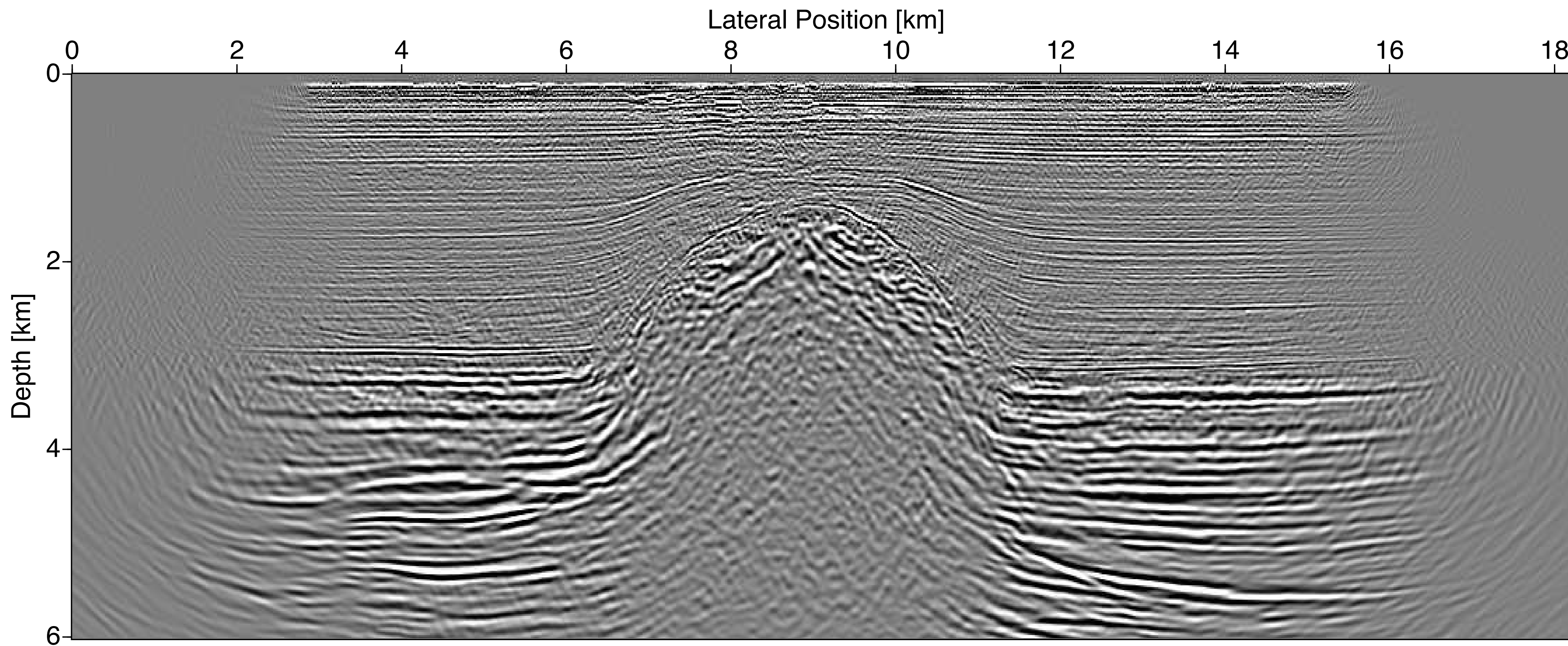


Shot No. 80



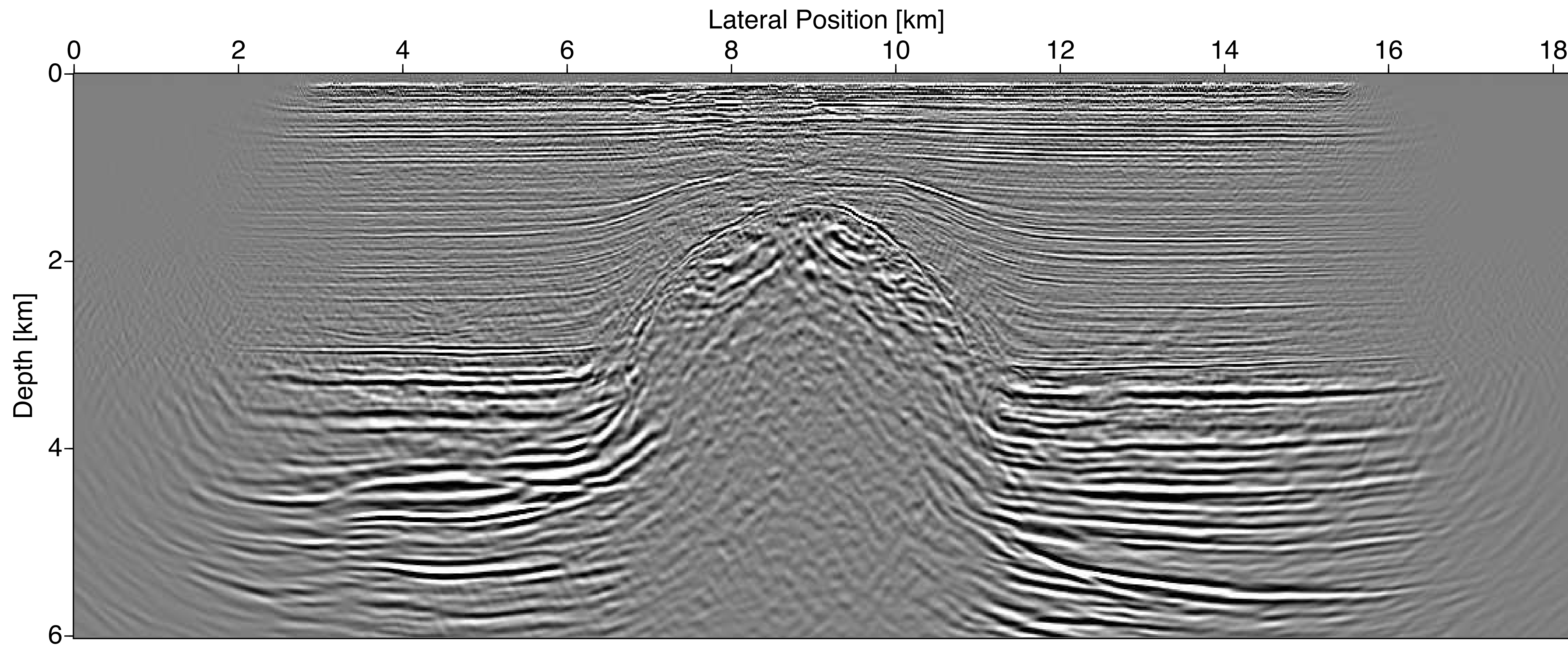
Shot No. 120

# RTM Image



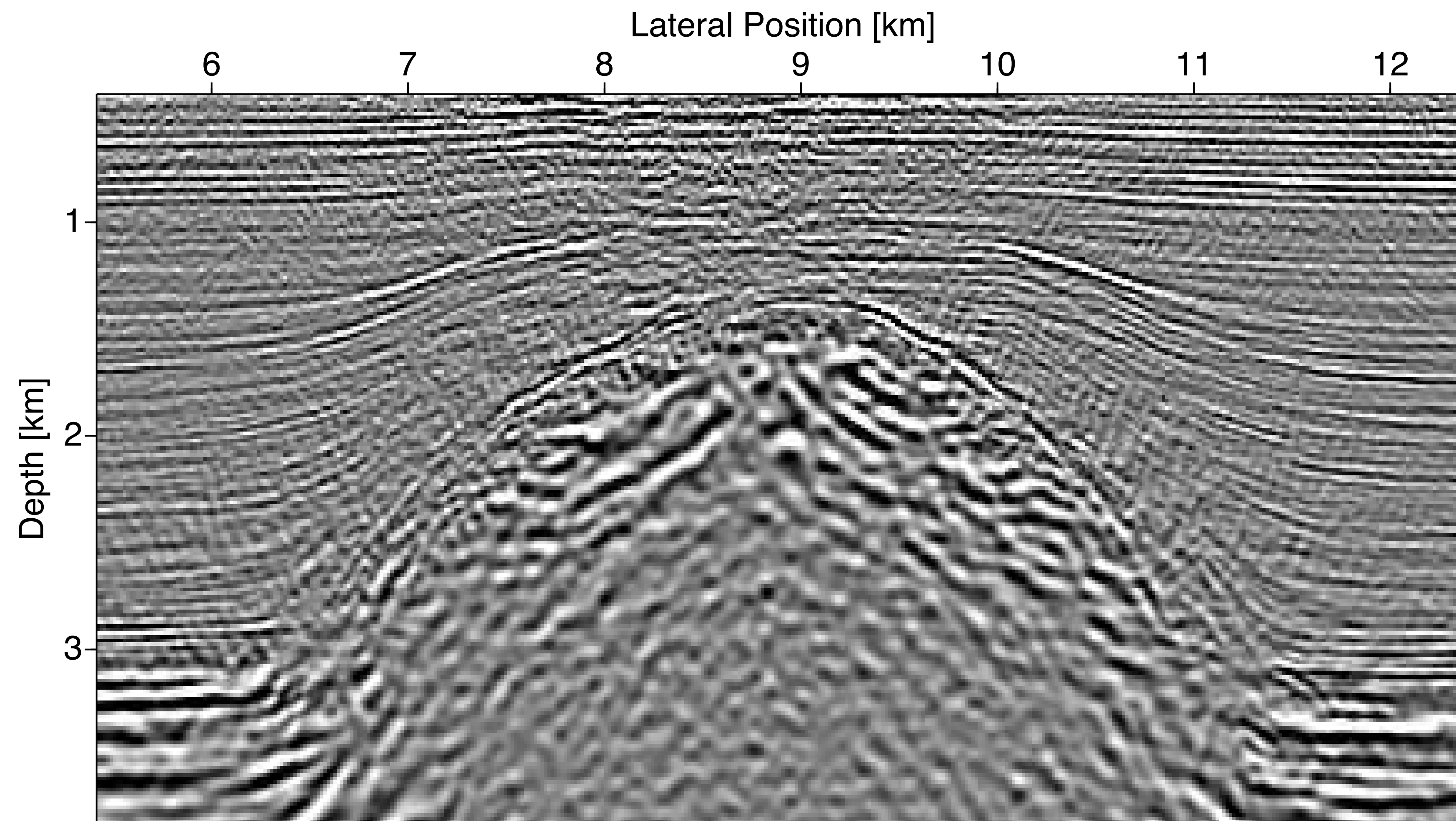
Result with data supplied by BP

# RTM Image



Result with processed data

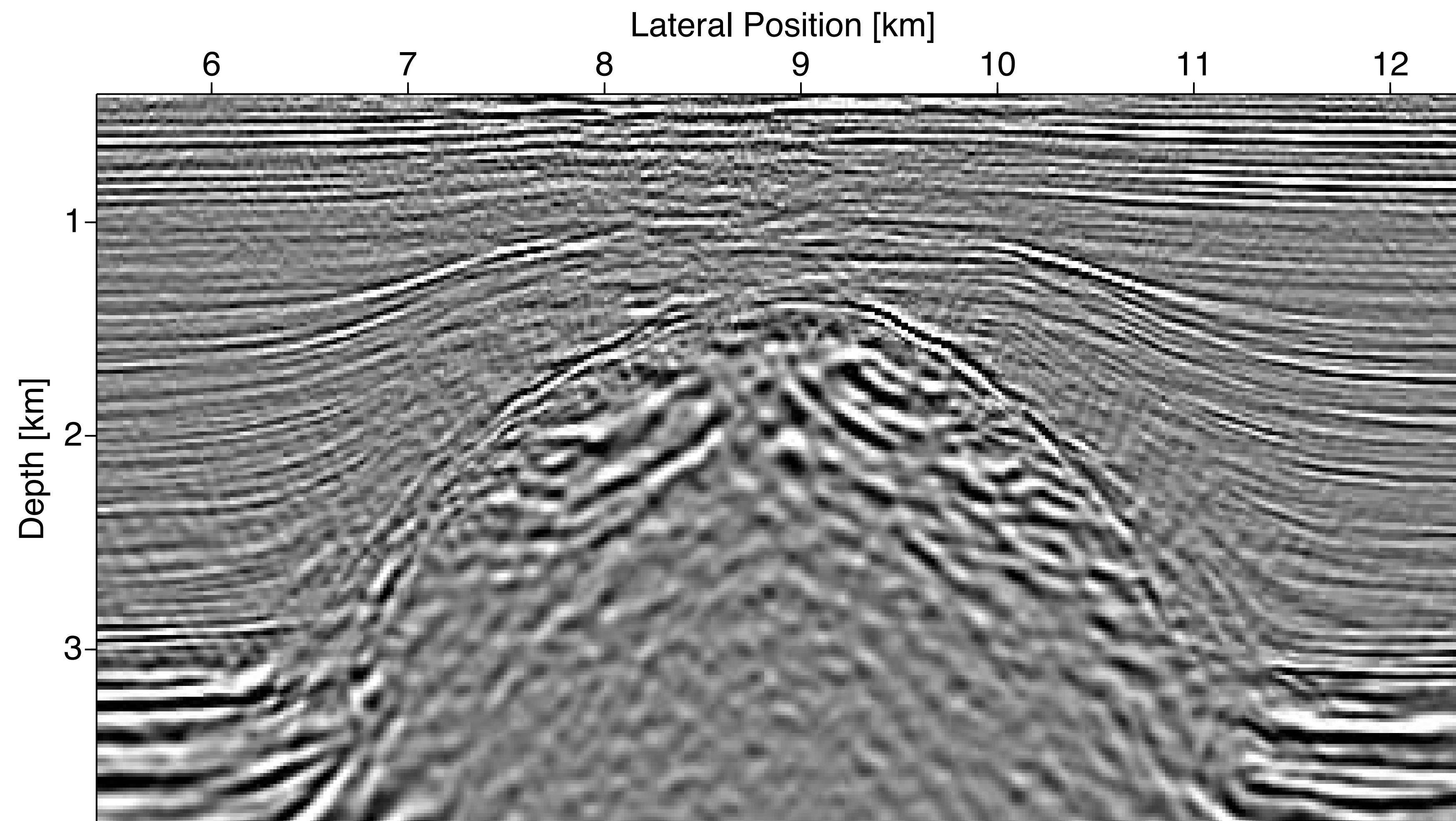
# Close-Up



**Result with data supplied by BP**



# Close-Up



Result with processed data

## RTM

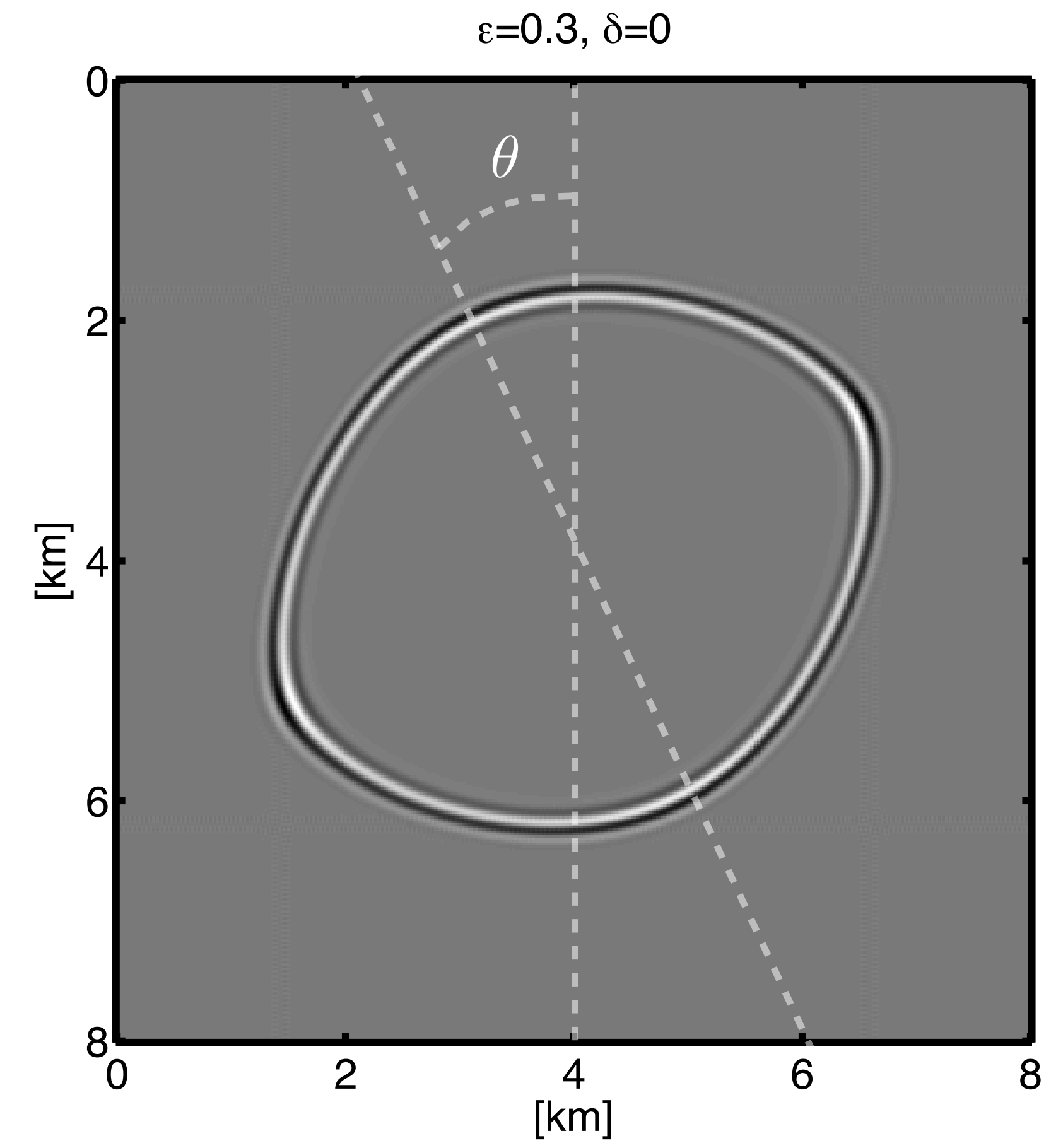
RTM image still has low quality

- ▶ many reflectors discontinuous
- ▶ salt dome flanks poorly imaged
- ▶ low seismic coherence on eastern part of the flank

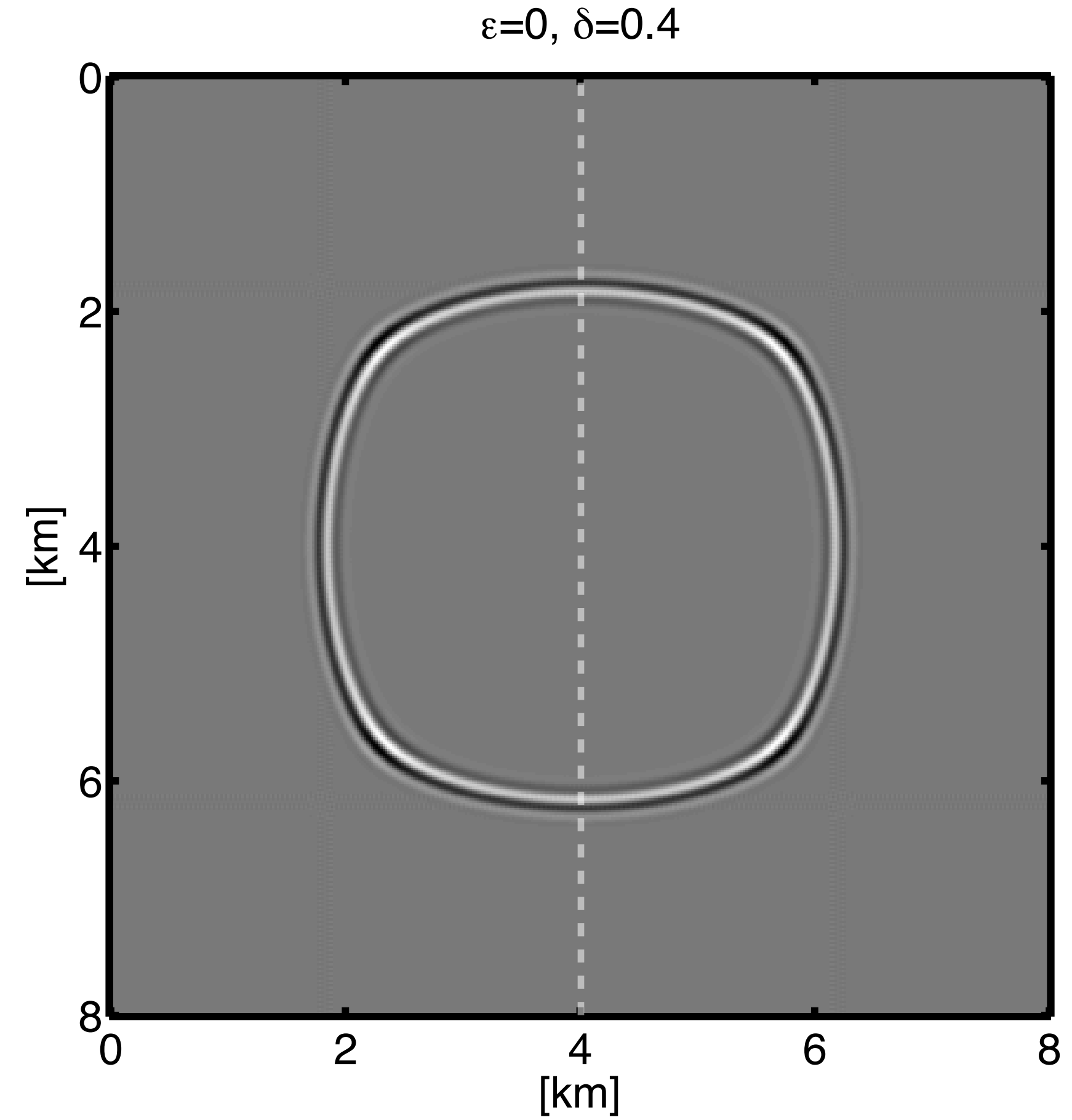
So far: imaging with acoustic wave equation

- ▶ migration with vertical velocity
- ▶ anisotropy not accounted for

# Anisotropy – Thomson Parameters

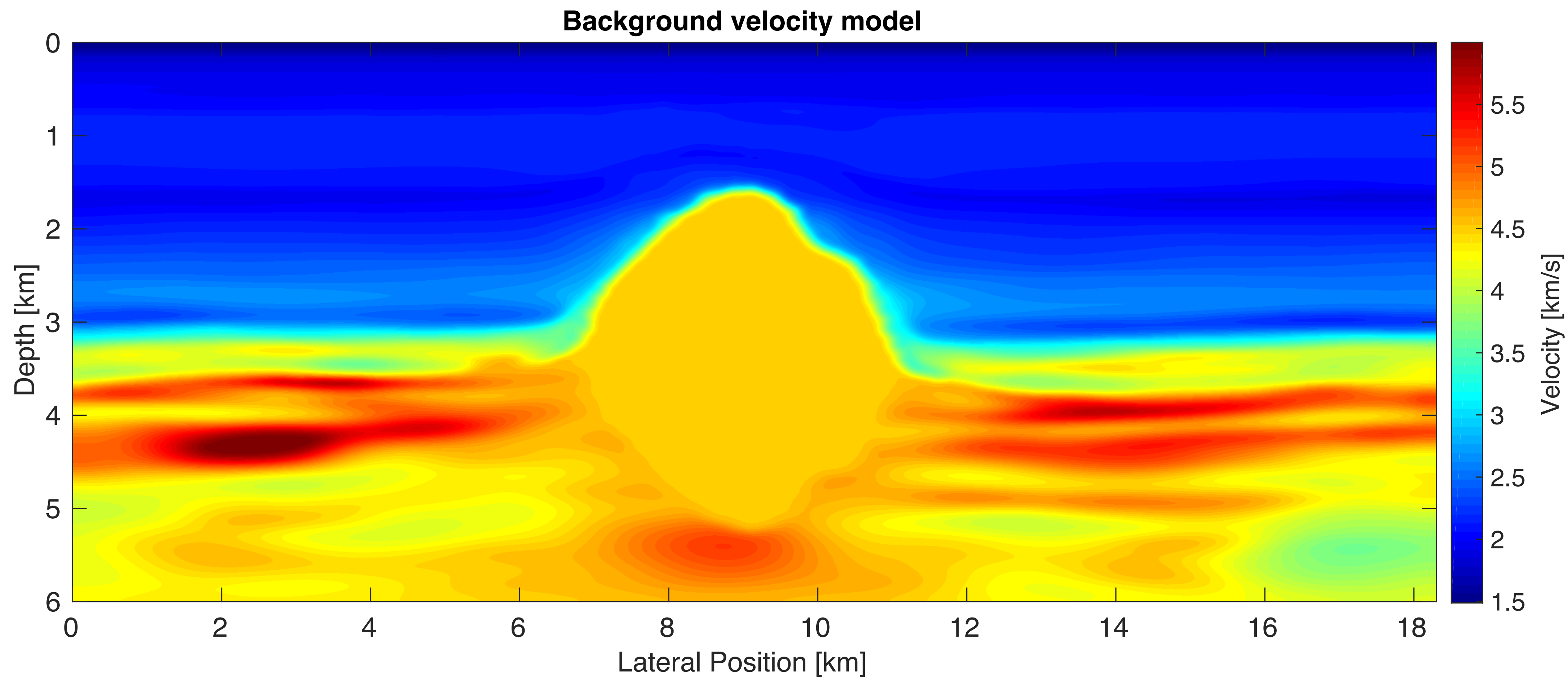


$$v_{p_x} = v_{p_z} \sqrt{1 + 2\epsilon}$$

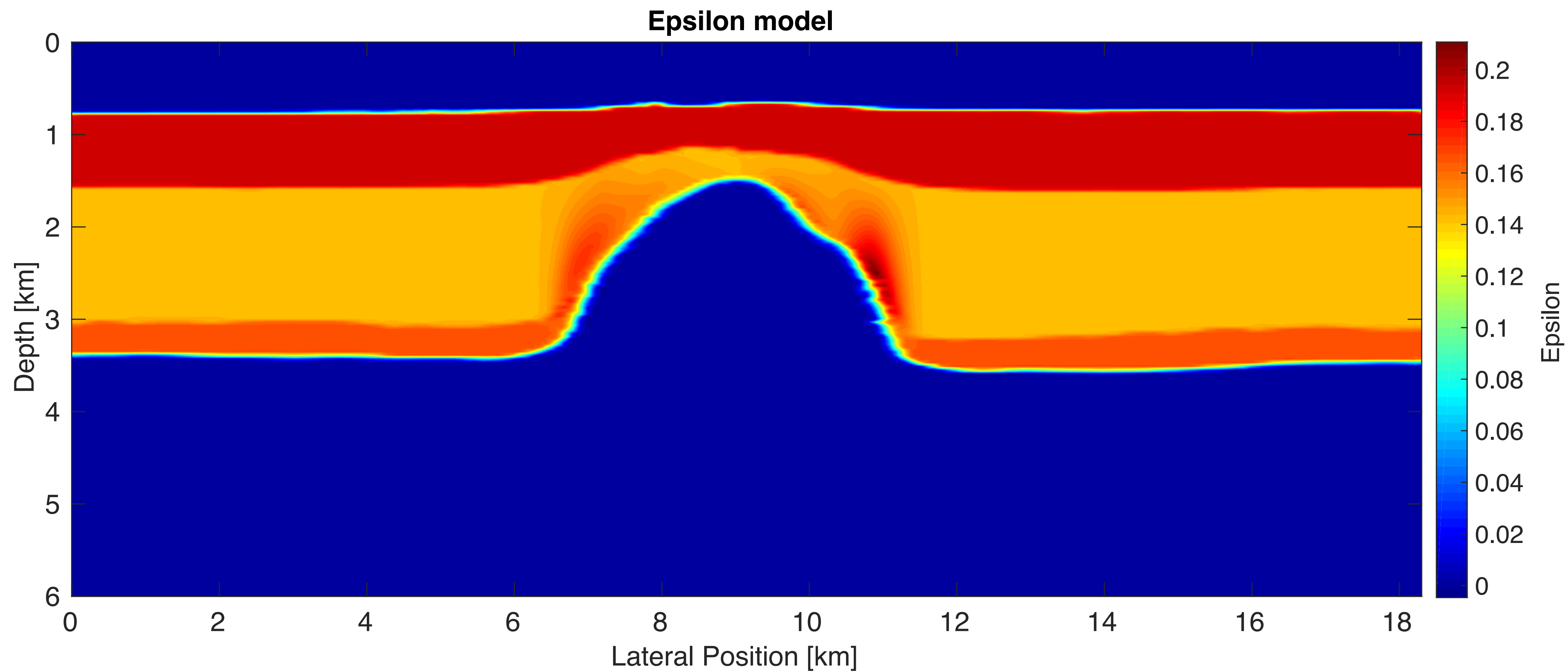


$$v_{p_n} = v_{p_z} \sqrt{1 + 2\delta}$$

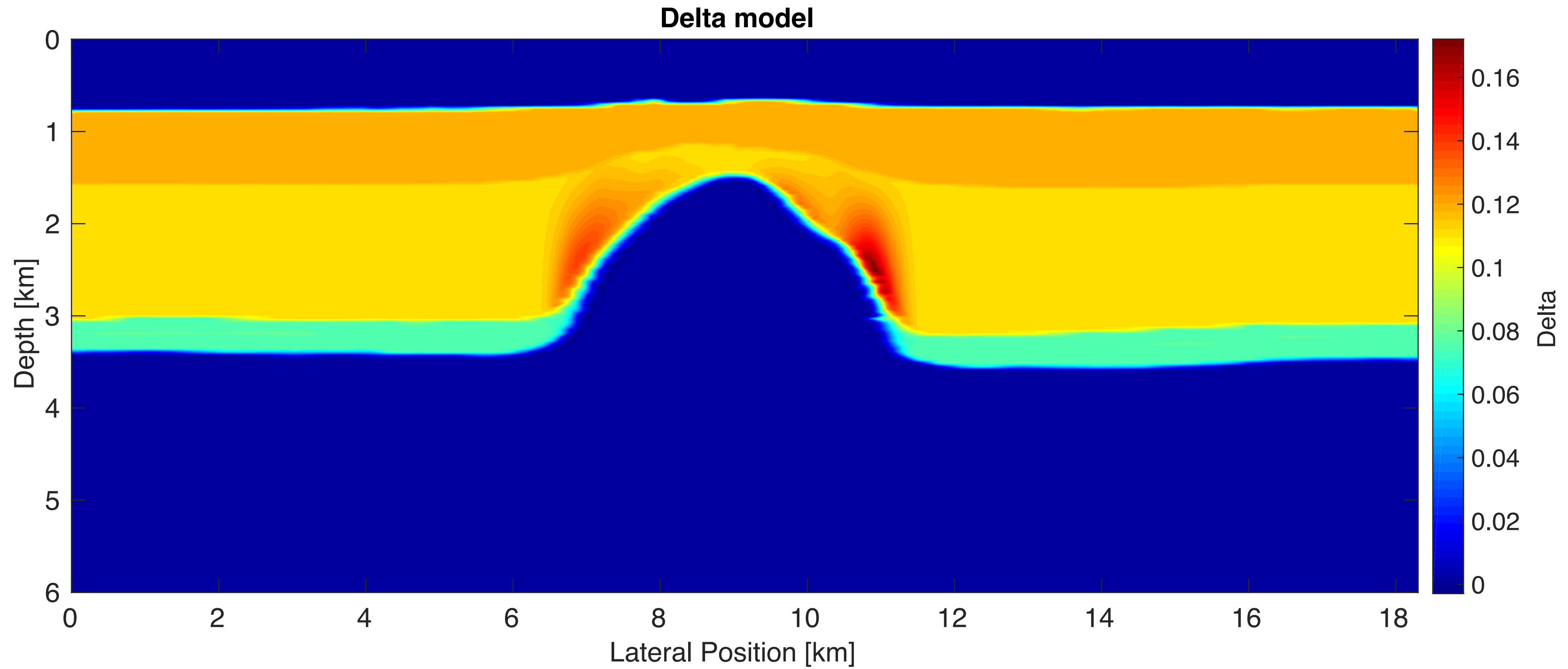
# Machar: model parameters



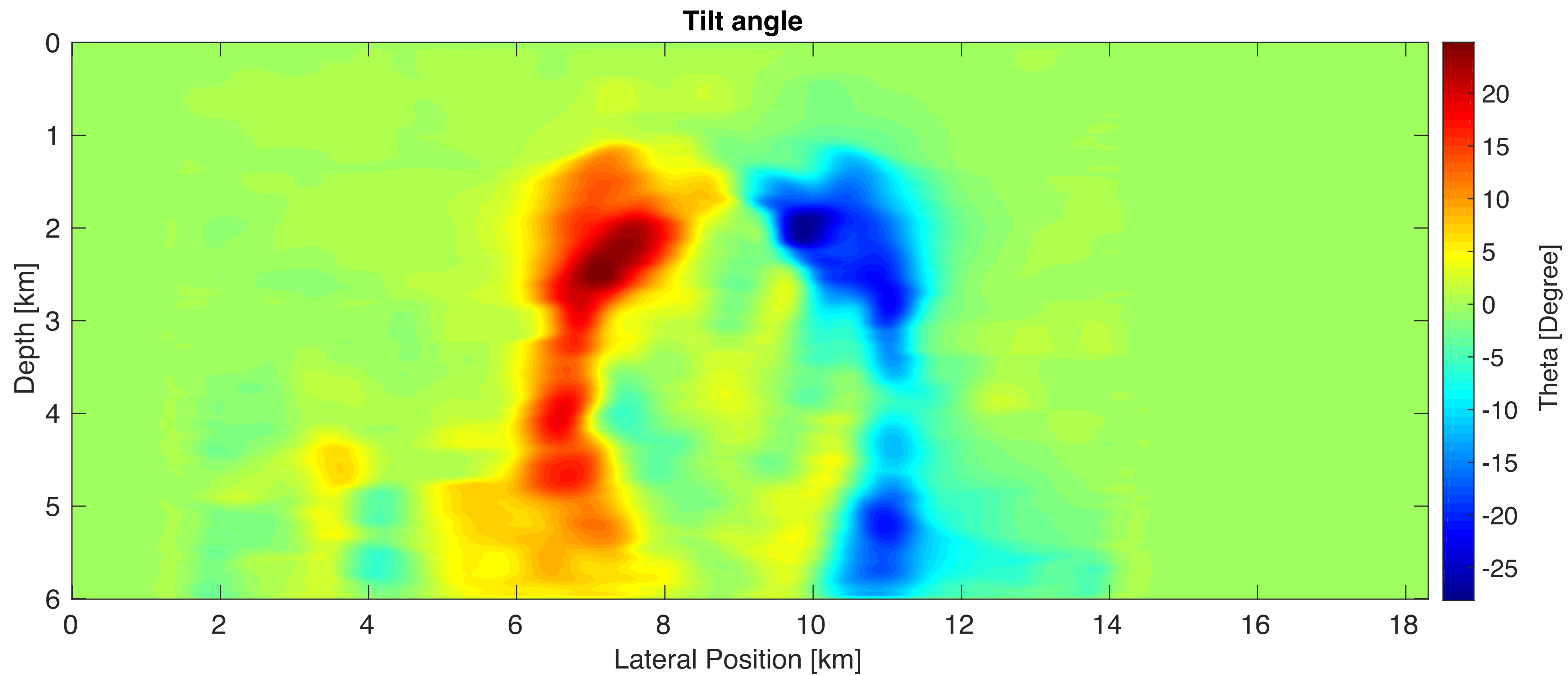
# Machar: model parameters



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# Machar: model parameters



# Anisotropic wave equation

## 2D pure p-wave equation /w PS methods

$$\begin{aligned} \frac{\partial U}{\partial t^2} = & c_{xx} \mathcal{F}^{-1} \{ -k_x^2 \bar{U} \} + c_{zz} \mathcal{F}^{-1} \{ -k_z^2 \bar{U} \} + c_{xz} \mathcal{F}^{-1} \{ -k_x k_z \bar{U} \} \\ & + c_{xxxx} \mathcal{F}^{-1} \left\{ \frac{k_x^4}{k_x^2 + k_z^2} \bar{U} \right\} + c_{zzzz} \mathcal{F}^{-1} \left\{ \frac{k_z^4}{k_x^2 + k_z^2} \bar{U} \right\} \\ & + c_{xxxxz} \mathcal{F}^{-1} \left\{ \frac{k_x^3 k_z}{k_x^2 + k_z^2} \bar{U} \right\} + c_{xzzz} \mathcal{F}^{-1} \left\{ \frac{k_x k_z^3}{k_x^2 + k_z^2} \bar{U} \right\} \\ & + c_{xxzz} \mathcal{F}^{-1} \left\{ \frac{k_x^2 k_z^2}{k_x^2 + k_z^2} \bar{U} \right\} \end{aligned}$$

$k_x$ : spatial wavenumber in x-direction  
 $\bar{U}$ : wavefield in frequency domain  
 $\mathcal{F}$ : 2D Fourier transform

(Chunlei Chu, Brian K. Macy and Phil D. Anno, 2011)



## Reverse time migration

Modeling operator  $\mathcal{F}(\mathbf{m})$ : generates data  $\mathbf{d}$  for model  $\mathbf{m}$   
( $\mathbf{m}$ : slowness squared)

Taylor expansion of operator w.r.t. background model  $\mathbf{m}_0$

$$\mathcal{F}(\mathbf{m}) = \mathcal{F}(\mathbf{m}_0) + \frac{\partial \mathcal{F}(\mathbf{m}_0)}{\partial \mathbf{m}} \delta \mathbf{m} + \mathcal{O}(\delta \mathbf{m}^2)$$

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observed field data

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observed field data

modeled data for  
background model

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observed field data

modeled data for  
background model

Jacobian

## Reverse time migration

Modeling operator  $\mathcal{F}(\mathbf{m})$ : generates data  $\mathbf{d}$  for model  $\mathbf{m}$

Taylor expansion of operator w.r.t. background model  $\mathbf{m}_0$

$$\mathcal{F}(\mathbf{m}) = \mathcal{F}(\mathbf{m}_0) + \frac{\partial \mathcal{F}(\mathbf{m}_0)}{\partial \mathbf{m}} \delta \mathbf{m} + \mathcal{O}(\delta \mathbf{m}^2)$$

observed field data

modeled data for  
background model

seismic image

## Reverse time migration

Modeling operator  $\mathcal{F}(\mathbf{m})$ : generates data  $\mathbf{d}$  for model

Taylor expansion of operator w.r.t. background model  $\mathbf{m}_0$

$$\mathcal{F}(\mathbf{m}) - \mathcal{F}(\mathbf{m}_0) \approx \frac{\partial \mathcal{F}(\mathbf{m}_0)}{\partial \mathbf{m}} \delta \mathbf{m} \iff \delta \mathbf{d} \approx \mathbf{J} \delta \mathbf{m}$$

RTM: apply adjoint Jacobian on data residual:  $\delta \mathbf{m} \approx \mathbf{J}^* \delta \mathbf{d}$

## Workflow

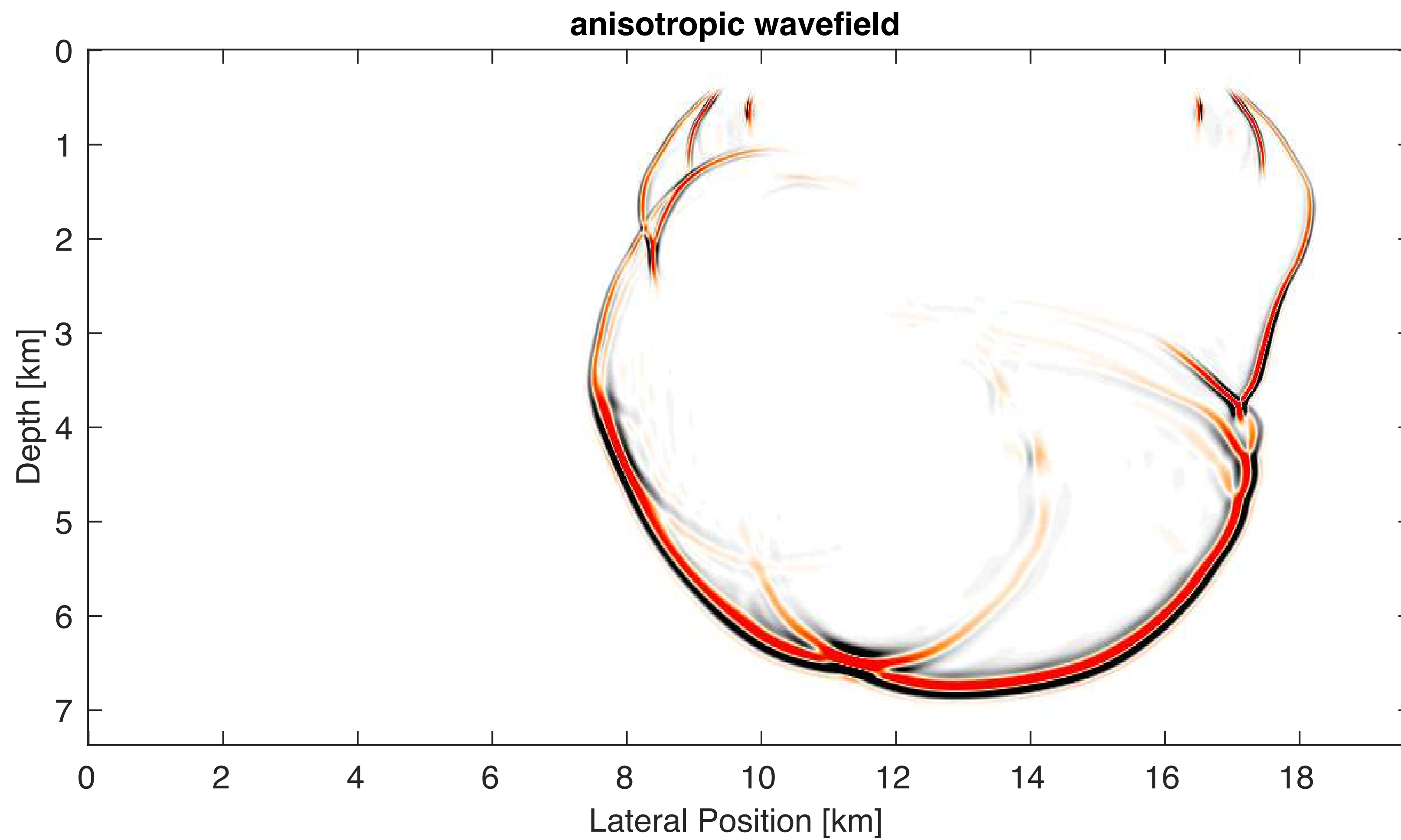
### Anisotropic RTM in time-domain:

- ▶ direct backpropagation of input data
- ▶ no source estimation (Ricker wavelet at 29 Hz for forward wavefield)
- ▶ pure p-wave TTI equation
- ▶ grid size of 17 m (3 gridpoints/wavelength)

### Plots:

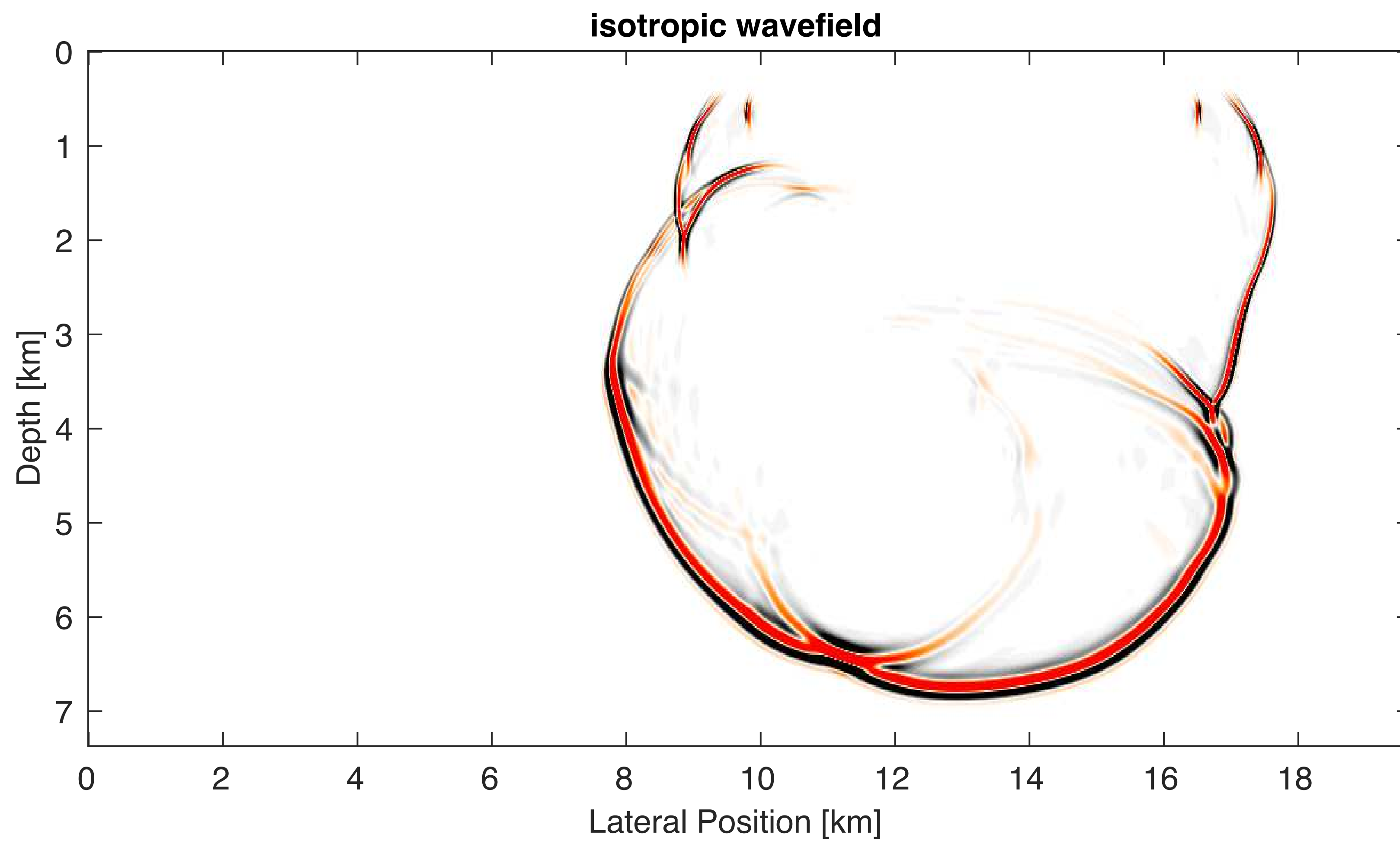
- ▶ bandpass filtered images
- ▶ depth scaling
- ▶ clipped to 97 % of max. amplitudes

# Forward Modeling Snapshots

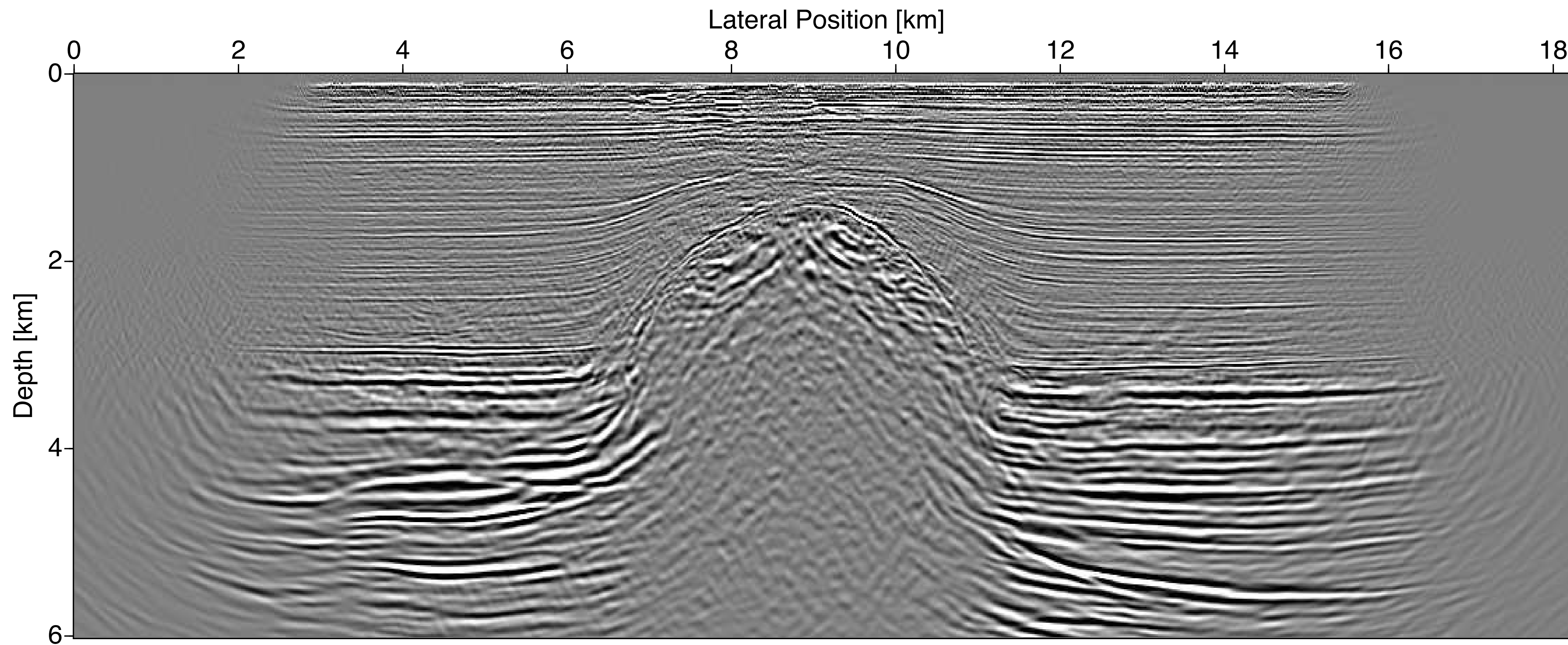




# Forward Modeling Snapshots

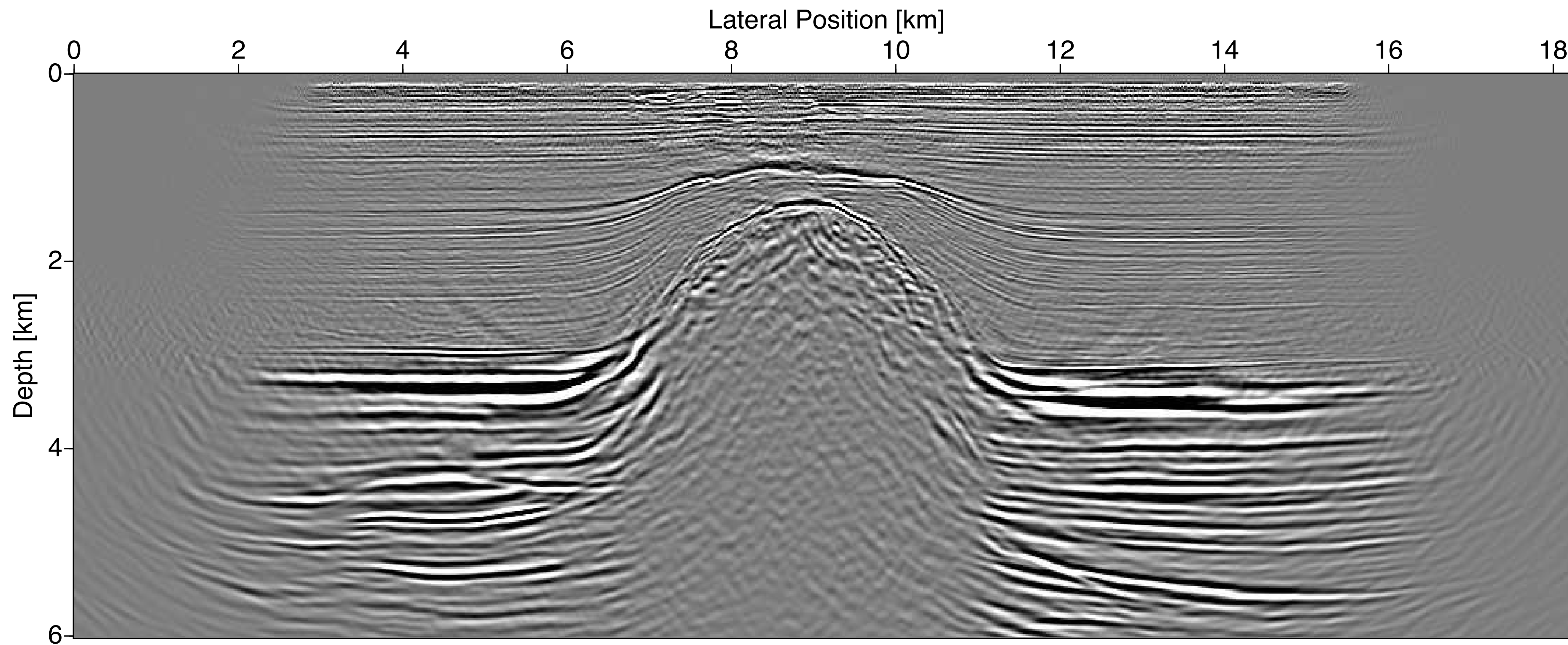


# RTM Image



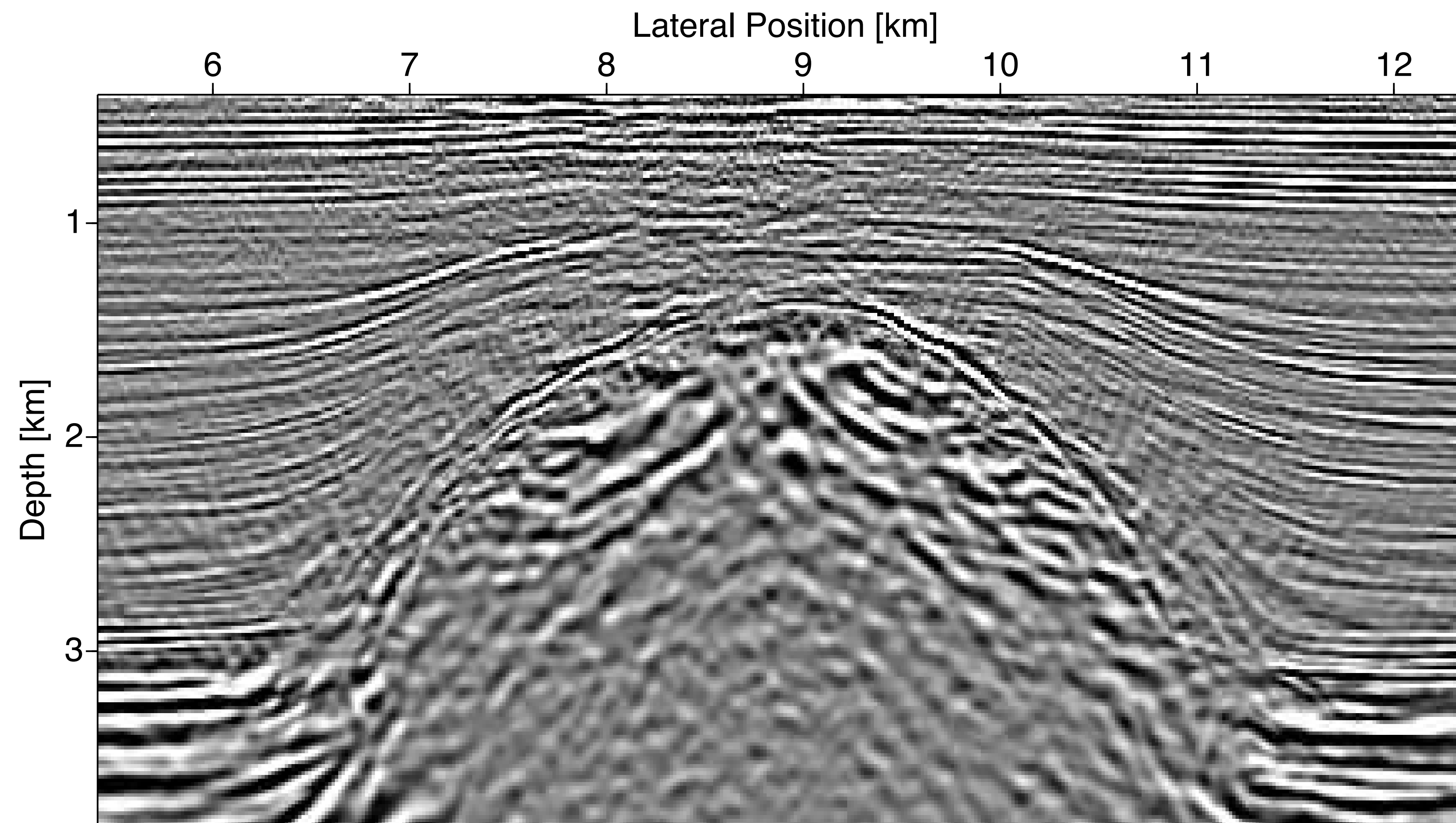
Isotropic RTM

# RTM Image



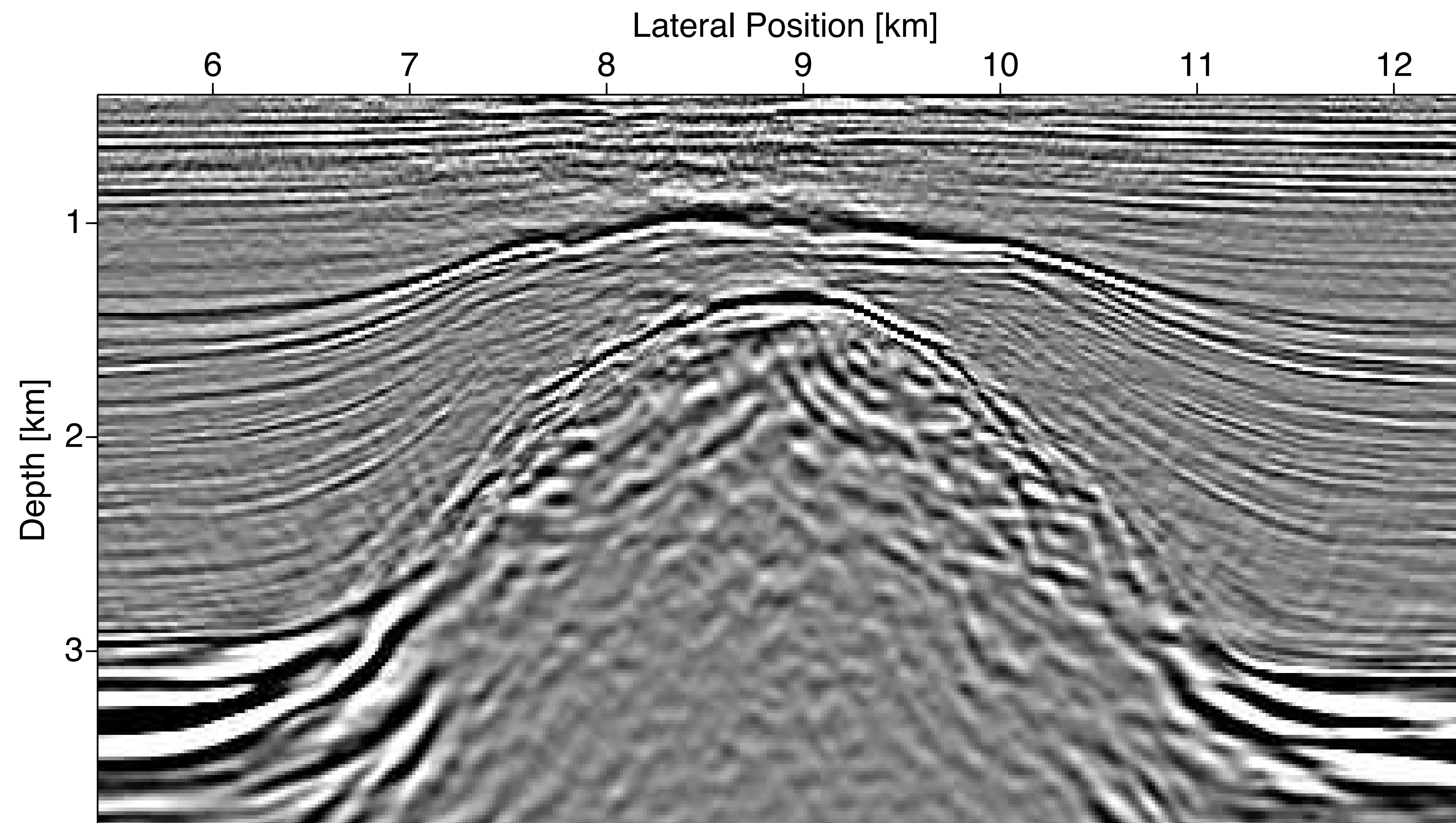
Anisotropic RTM

# Close-up



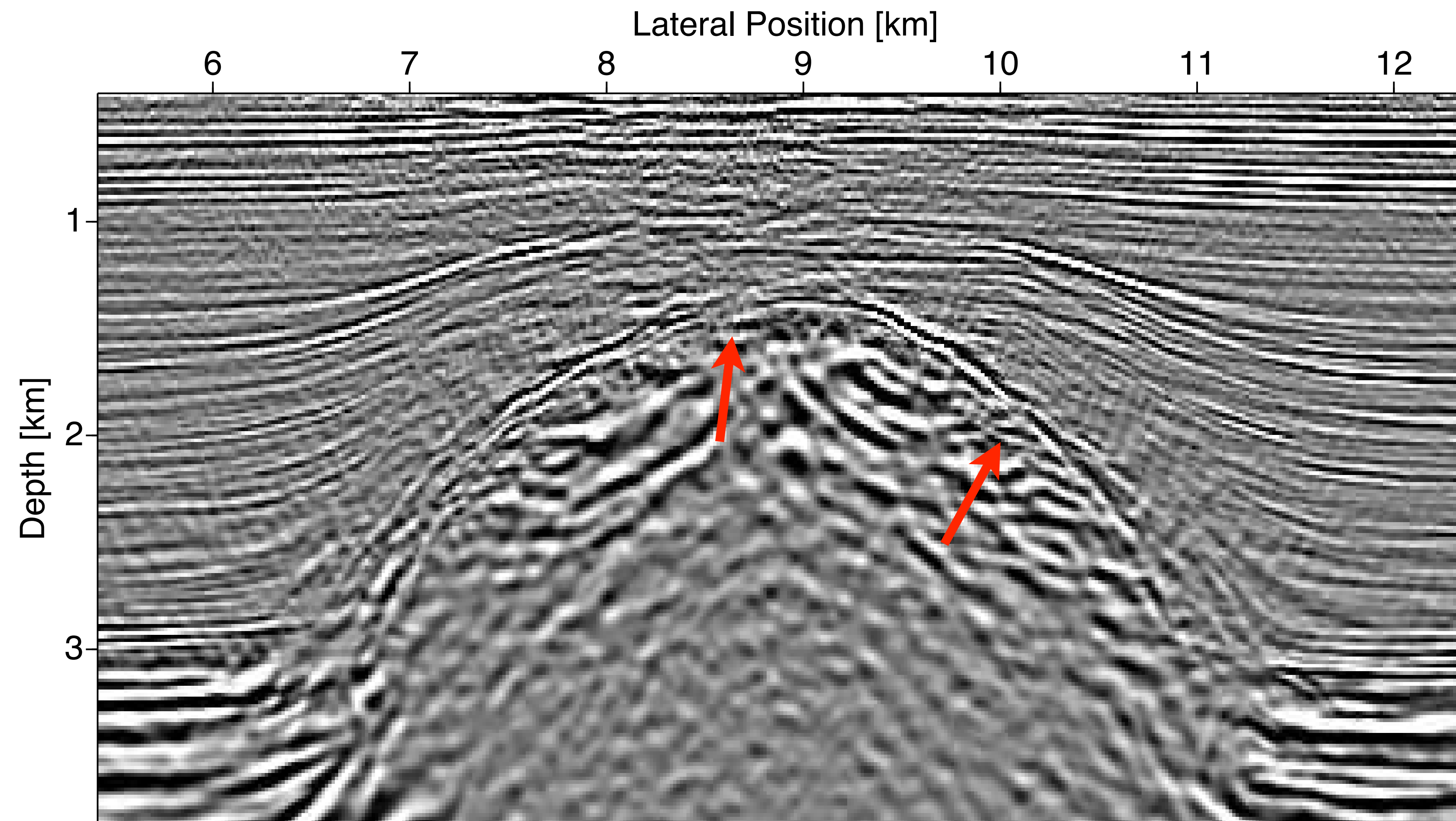
Isotropic RTM

# Close-up



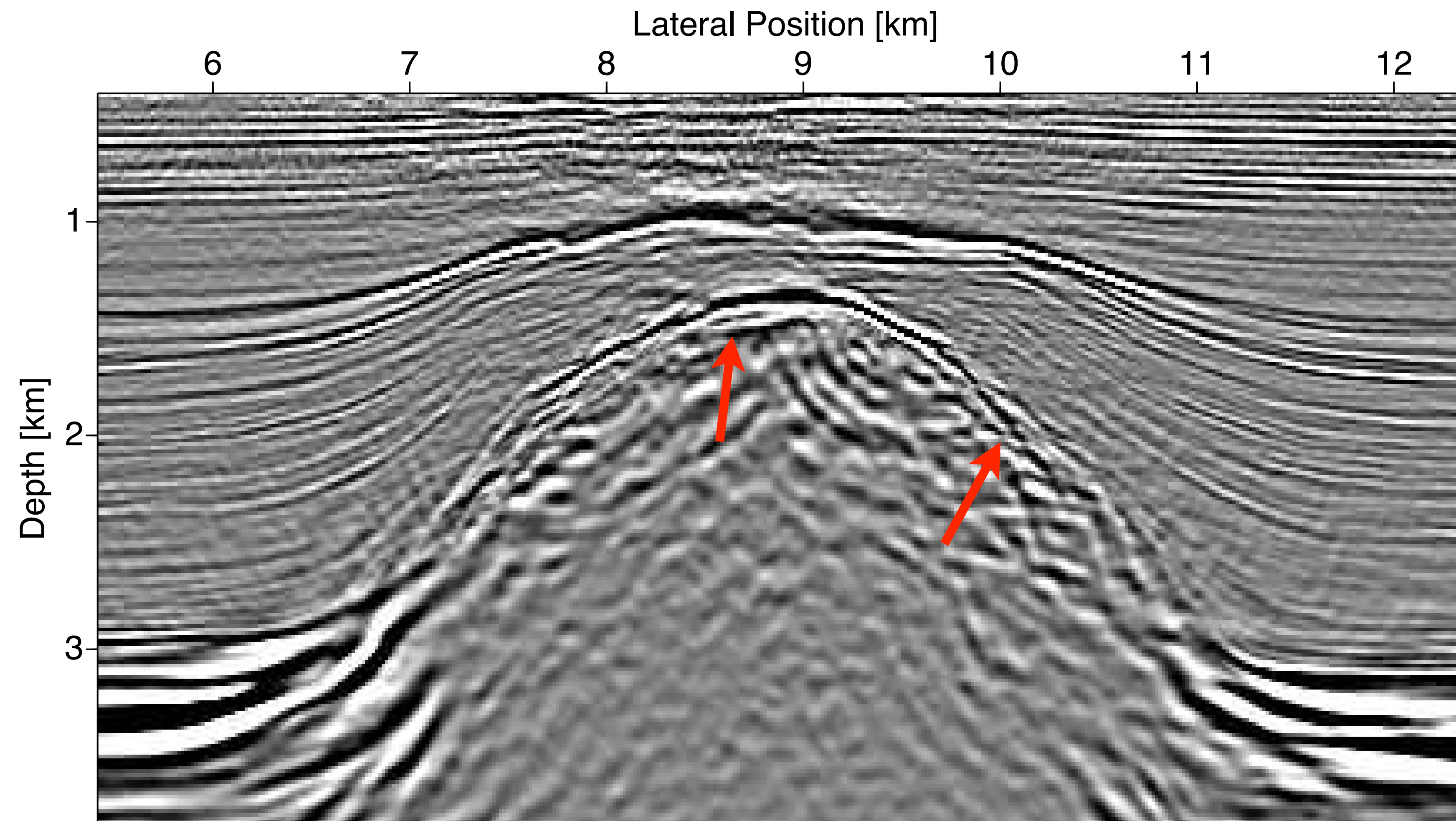
Anisotropic RTM

# Close-up



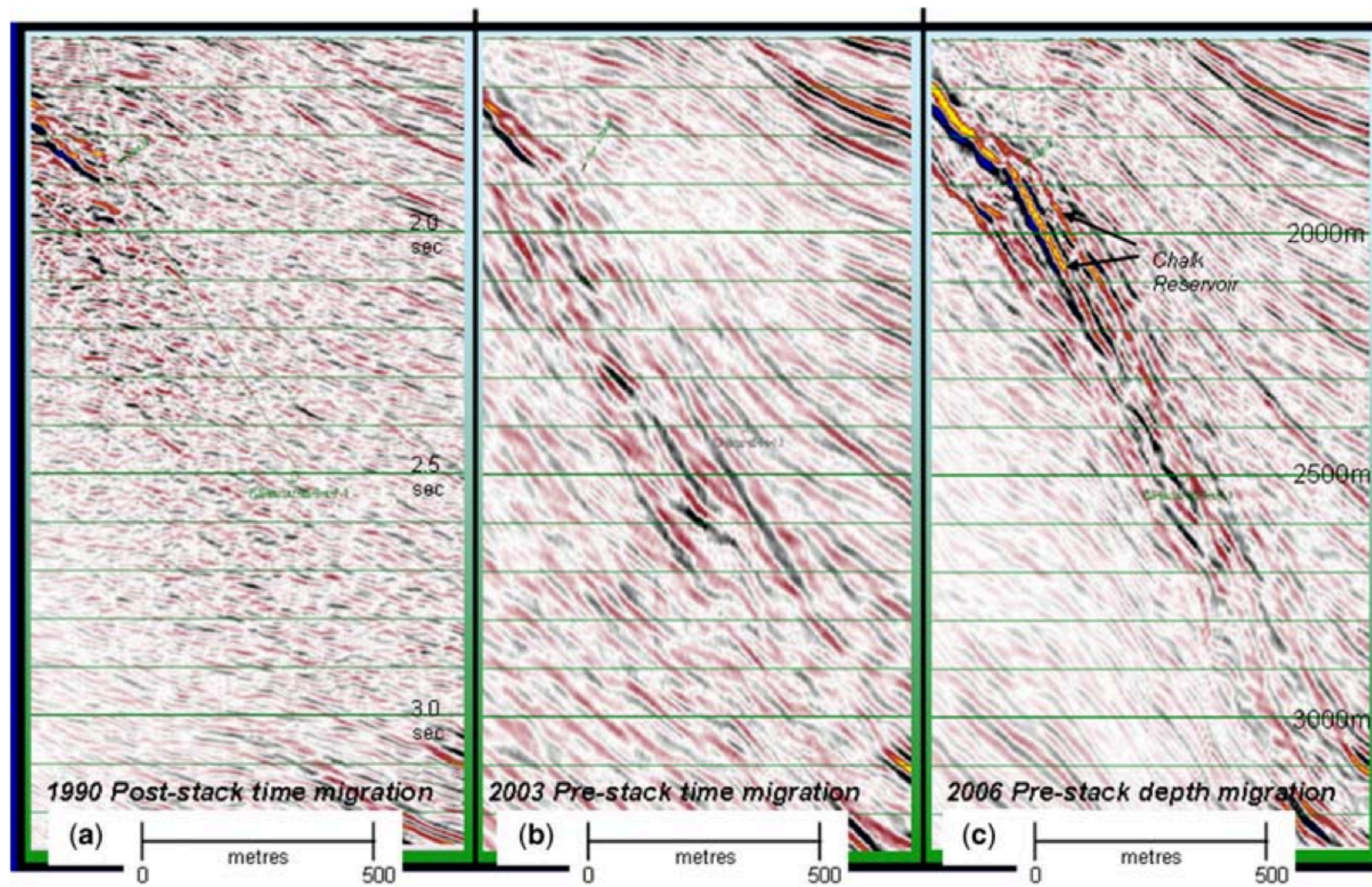
Isotropic RTM

# Close-up



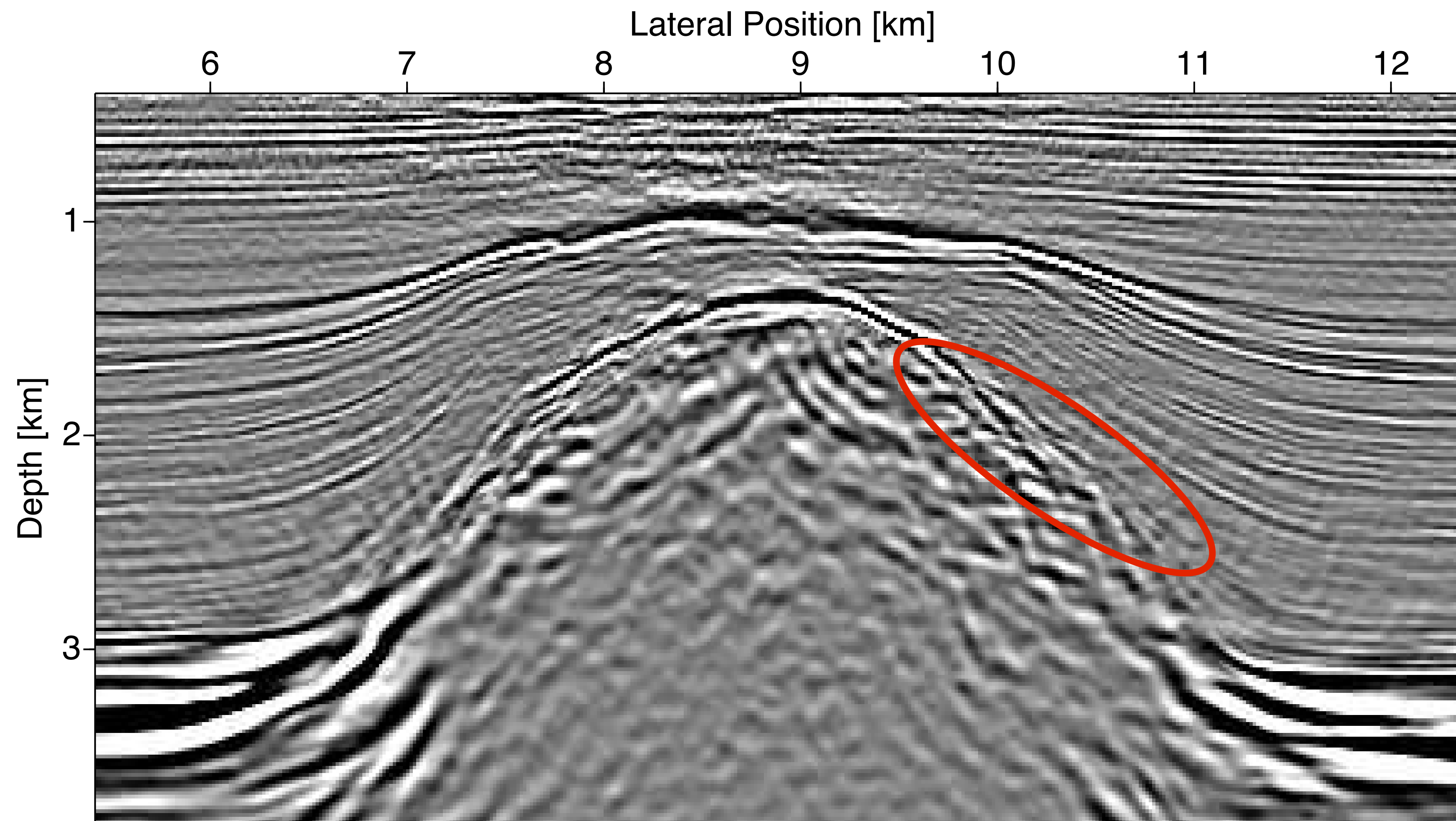
Anisotropic RTM

# BP migration results (1989 data set)





# Close-up



chalk reservoir

Anisotropic RTM

# Conclusions

## RTM with TTI wave equation

- ▶ more coherent events in the parts of the model with high anisotropy
- ▶ position of salt diapir flanks shifted significantly

## Future work

- ▶ better strategy to deal with RTM imaging artifacts, alternative imaging condition
- ▶ sparsity-promoting least-squares RTM

## Acknowledgements

Thank you for your attention and thanks to BP for supplying us with this data set!

<https://www.slim.eos.ubc.ca>



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