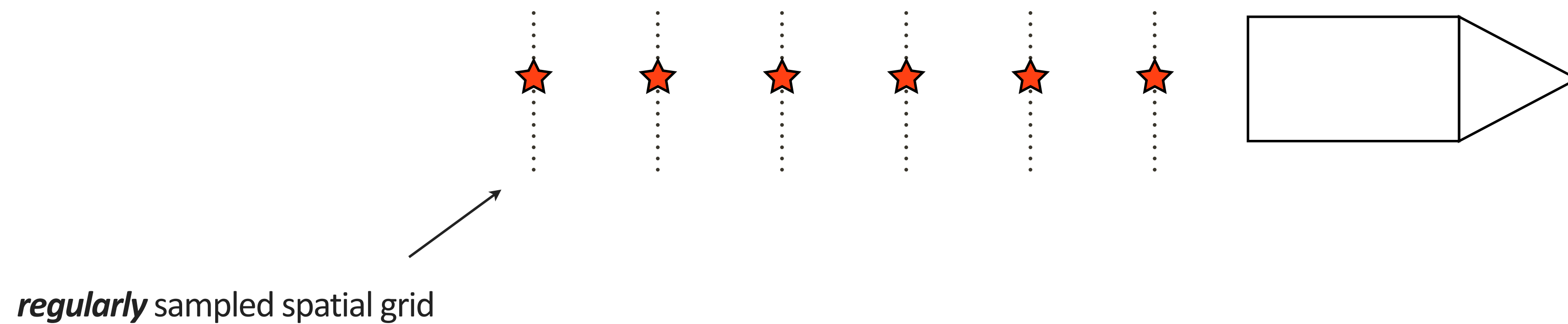


# ***Time-jittered* marine sources**

Haneet Wason and Felix J. Herrmann

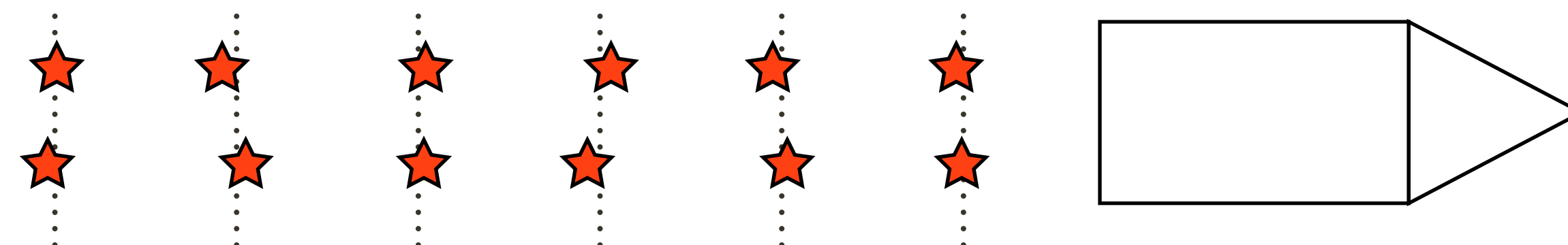
# Marine acquisition - *PAST*



# Marine acquisition - *PRESENT*



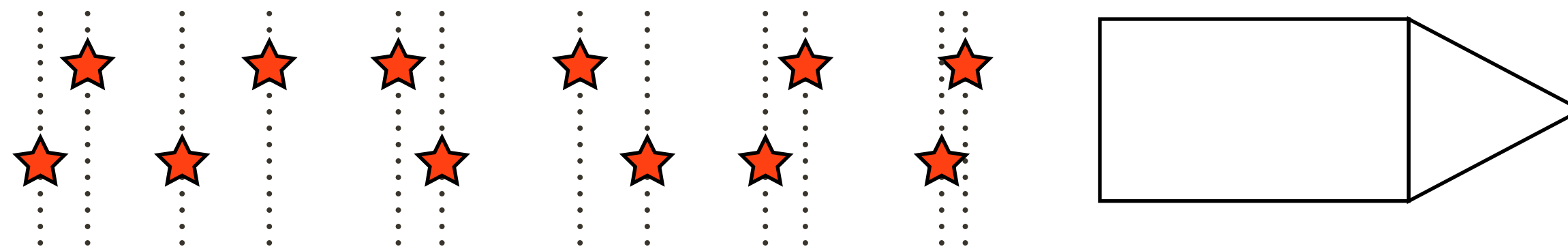
# Simultaneous marine acquisition - *PRESENT*



*regularly* sampled spatial grid  
(almost)

shot-time randomness - **LOW**

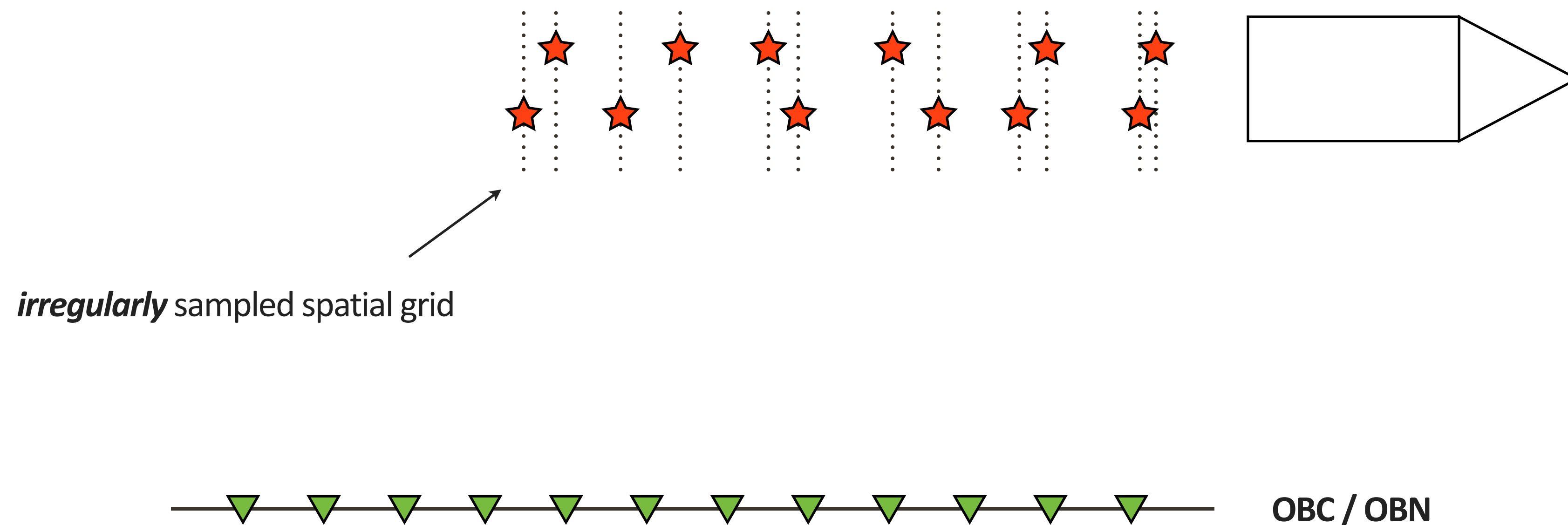
# Simultaneous marine acquisition - *FUTURE* ?



*irregularly* sampled spatial grid

shot-time randomness - **HIGH**

# Simultaneous marine acquisition - *FUTURE* ?





# Current challenges

- ▶ **Need for full sampling**
  - wave-equation based inversion (RTM & FWI)
  - AVO analysis, SRME/EPXI, etc.
  
- ▶ **Full azimuthal coverage**
  - multiple source vessels
  - simultaneous/blended acquisition
  
- ▶ **Deblending or wavefield reconstruction**
  - recover unblended data from blended data
  - challenging to recover weak late events

# Motivation

## ***Rethink marine acquisition***

- sources (and receivers) at *random* locations
- as long as you know the locations afterwards... *it is fine!*

## ***Want more for less ...***

- *shorter* survey times
- *increased* spatial sampling



# Motivation

## **Rethink marine acquisition**

- sources (and receivers) at *random* locations
- as long as you know the locations afterwards... *it is fine!*

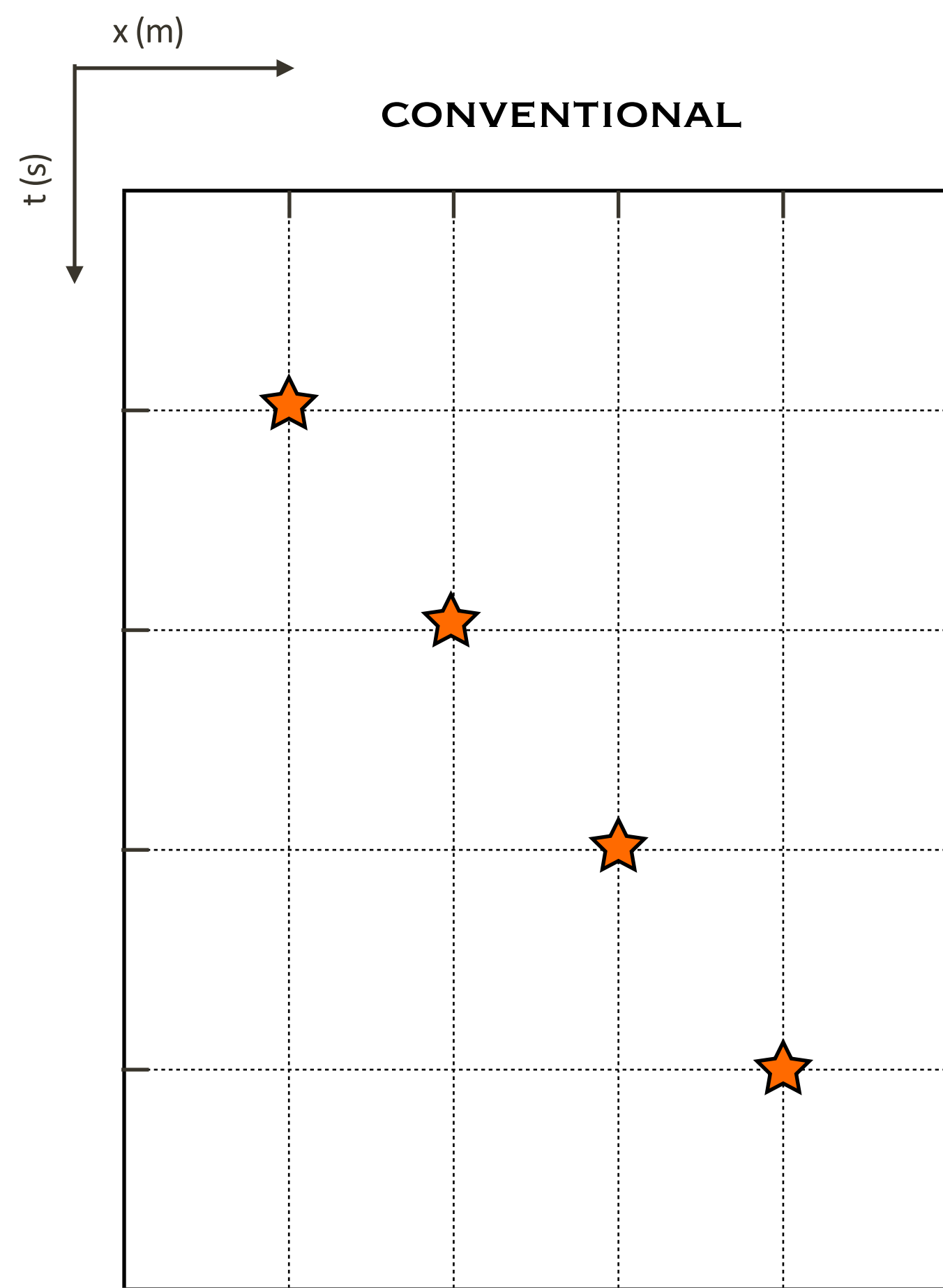
## **Want more for less ...**

- *shorter* survey times
- *increased* spatial sampling

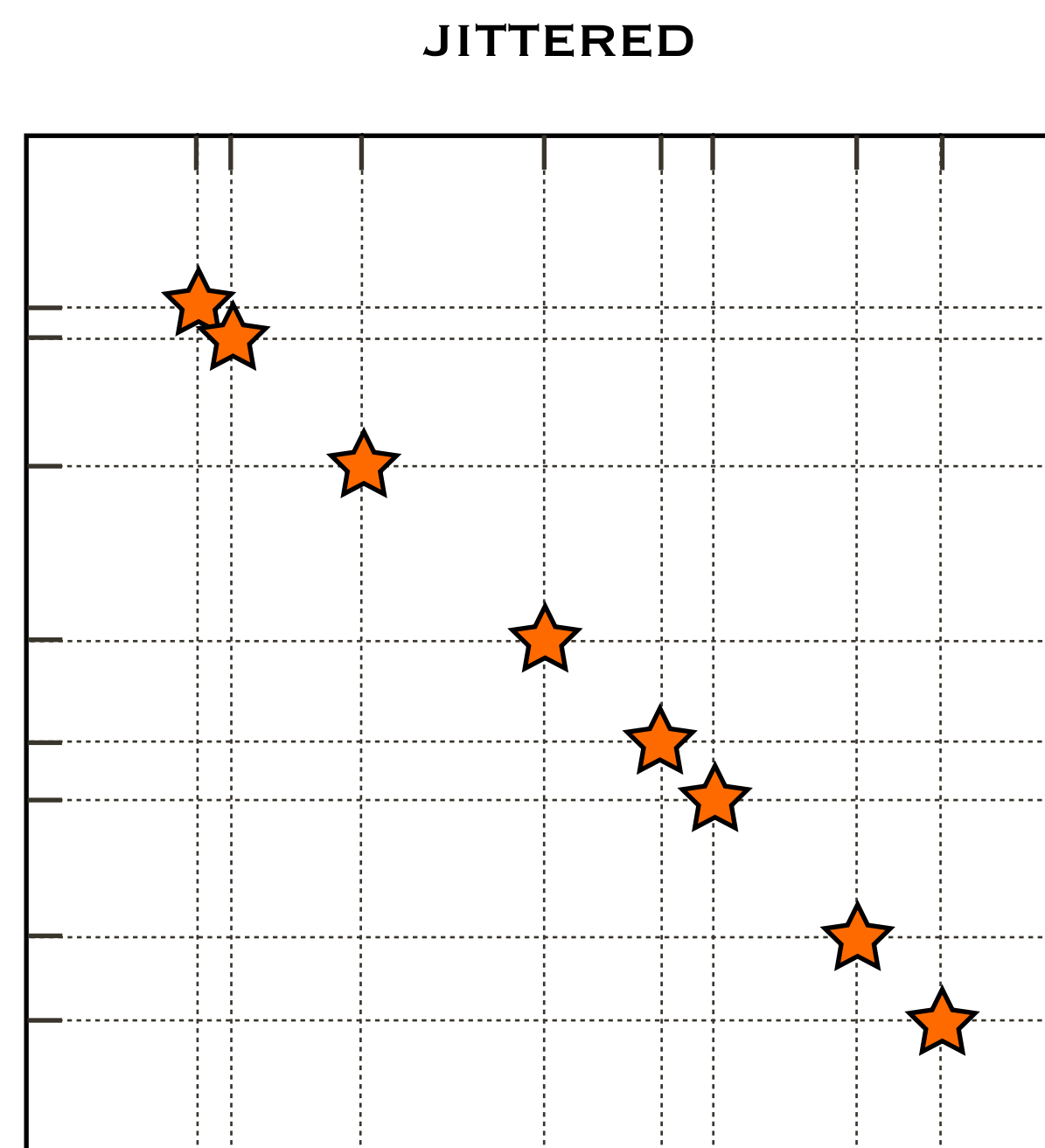
## **How is this possible?**

- (multi-vessel) acquisition w/ *jittered* sampling & “blending” via *compressed randomized inter-shot* firing times
- *sparsity*-promoting recovery using  $\ell_1$  constraints (“deblending”)

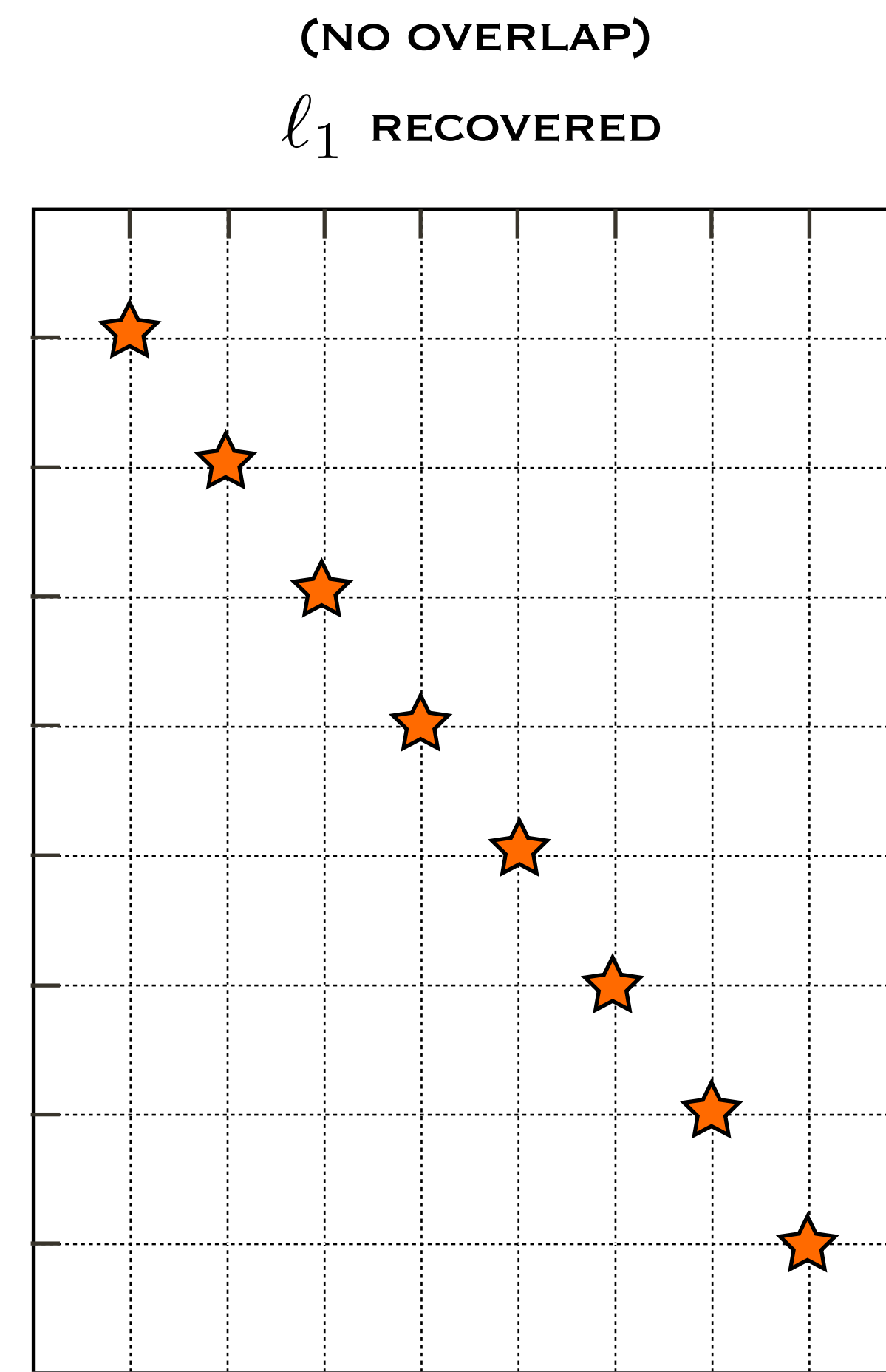
# More for less



PERIODIC-SPARSE-NO OVERLAP



APERIODIC  
COMPRESSED  
OVERLAPPING  
IRREGULAR

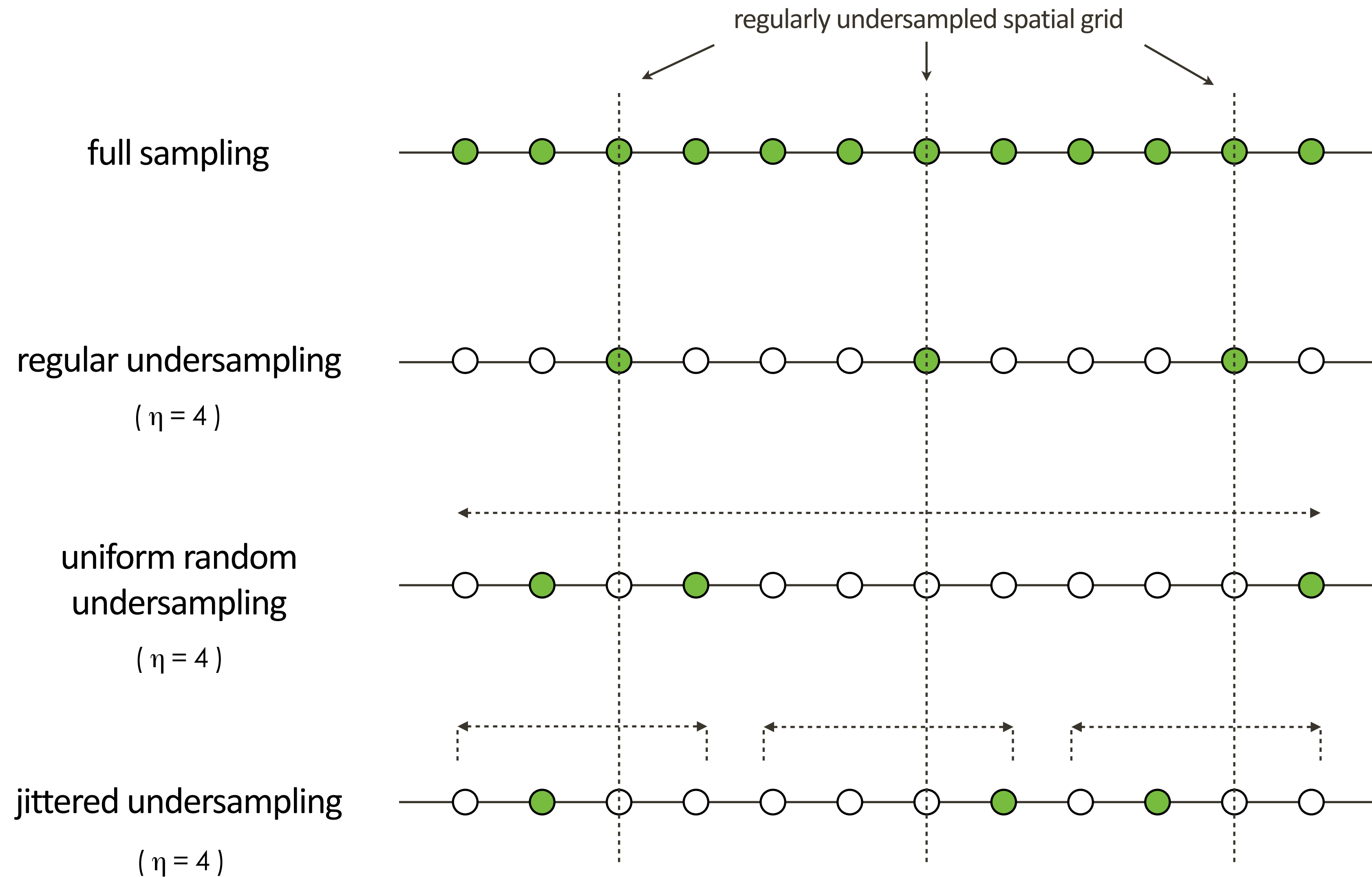


PERIODIC & DENSE

# Outline

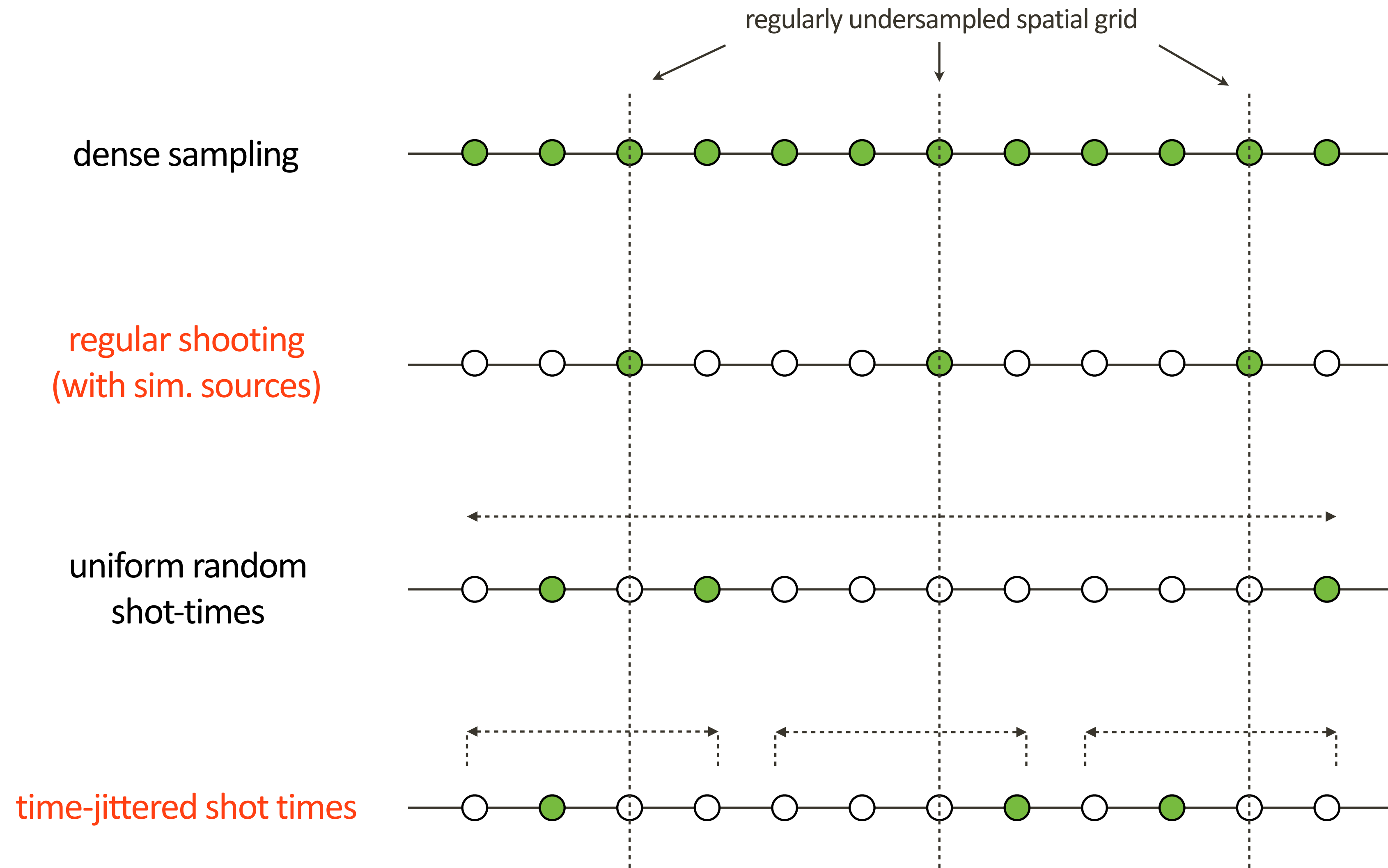
- ▶ Design of *time-jittered* acquisition
  - jitter in *time*  $\Rightarrow$  jittered in *space* (*shot* locations)
  - low vs. high shot-time jitter
- ▶ Recovery strategy
- ▶ Experimental results of *sparsity*-promoting processing
  - wavefield recovery via “*deblending*” & *interpolation* from (coarse) *jittered/irregular* to (fine) *regular* sampling grid

# Sampling schemes



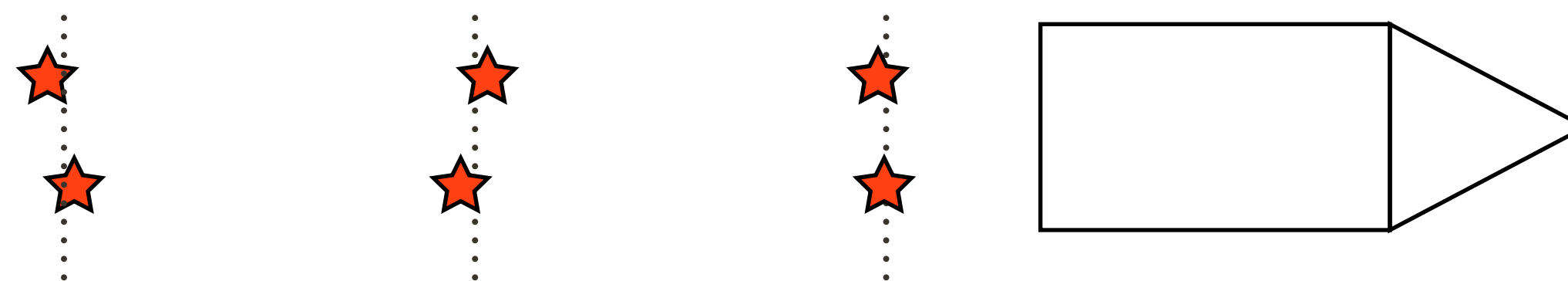


# Sampling schemes

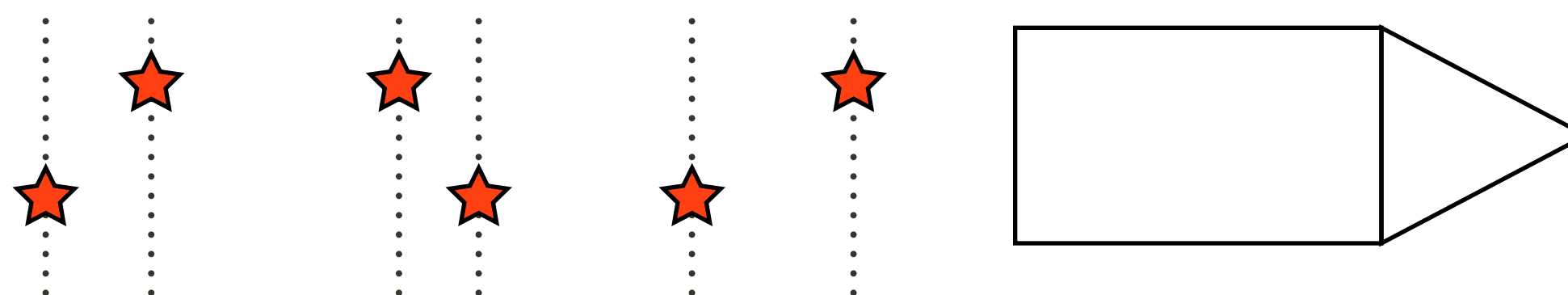


# Regular vs. *jittered* locations

*regularly* sampled spatial grid  
(almost)



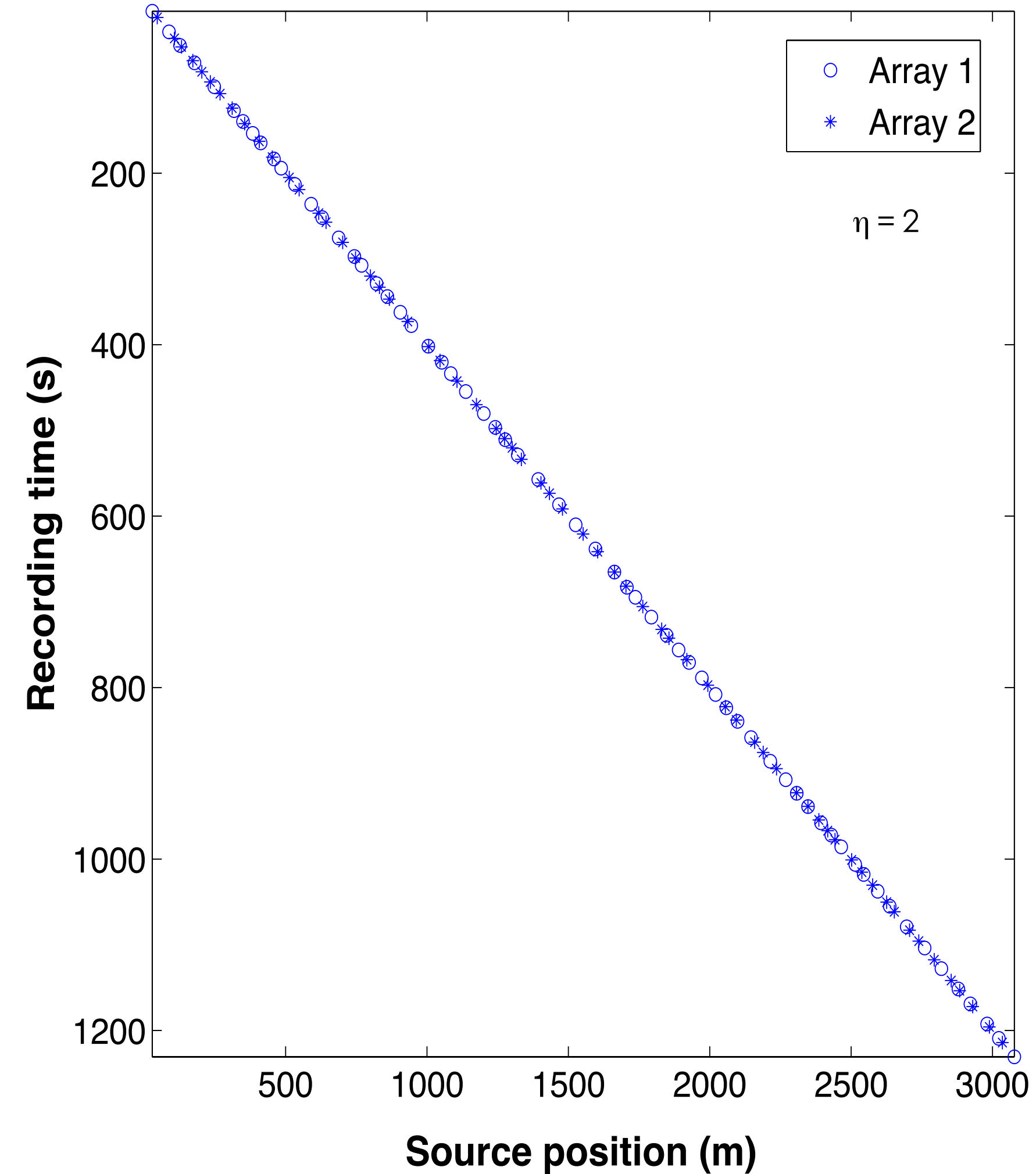
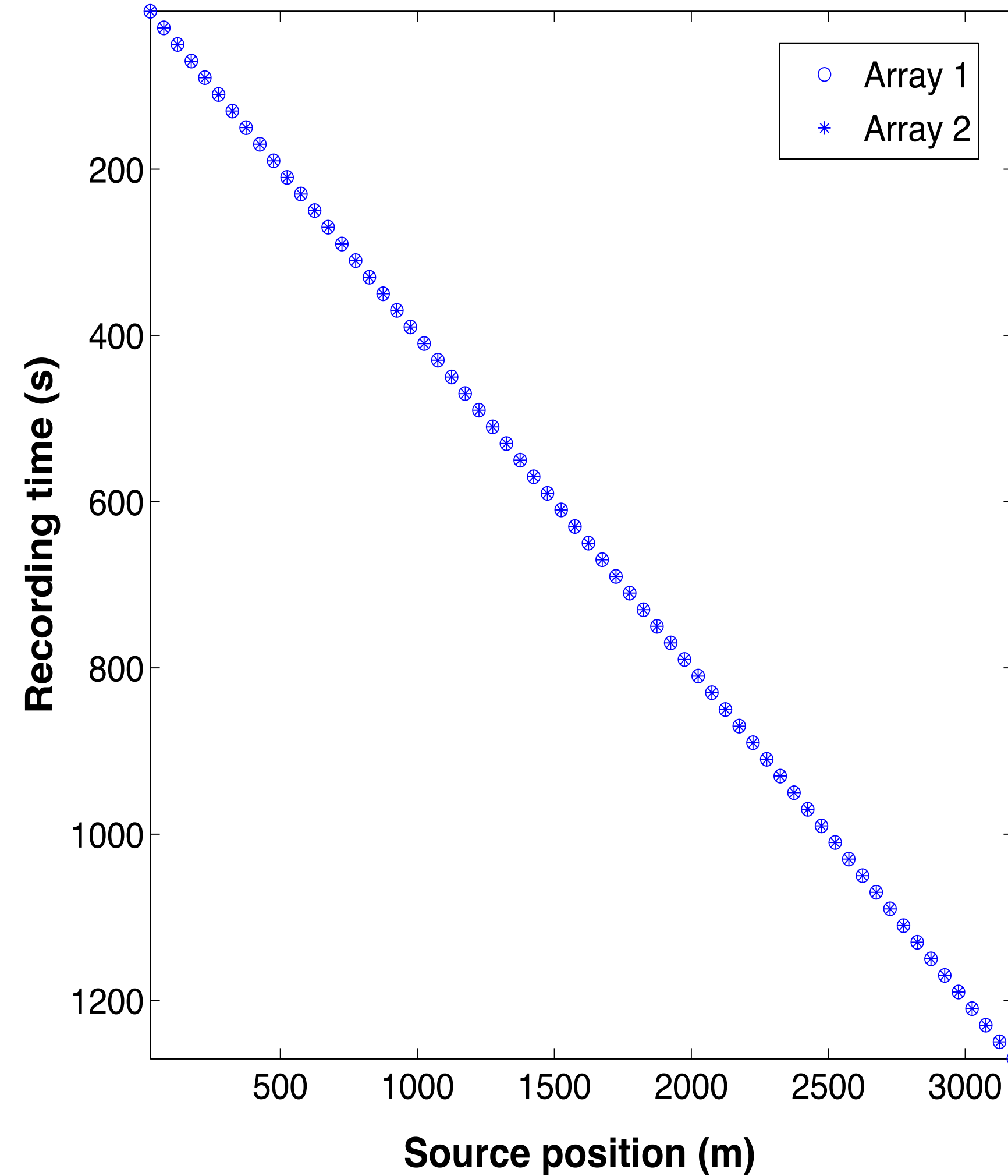
*irregularly* sampled spatial grid





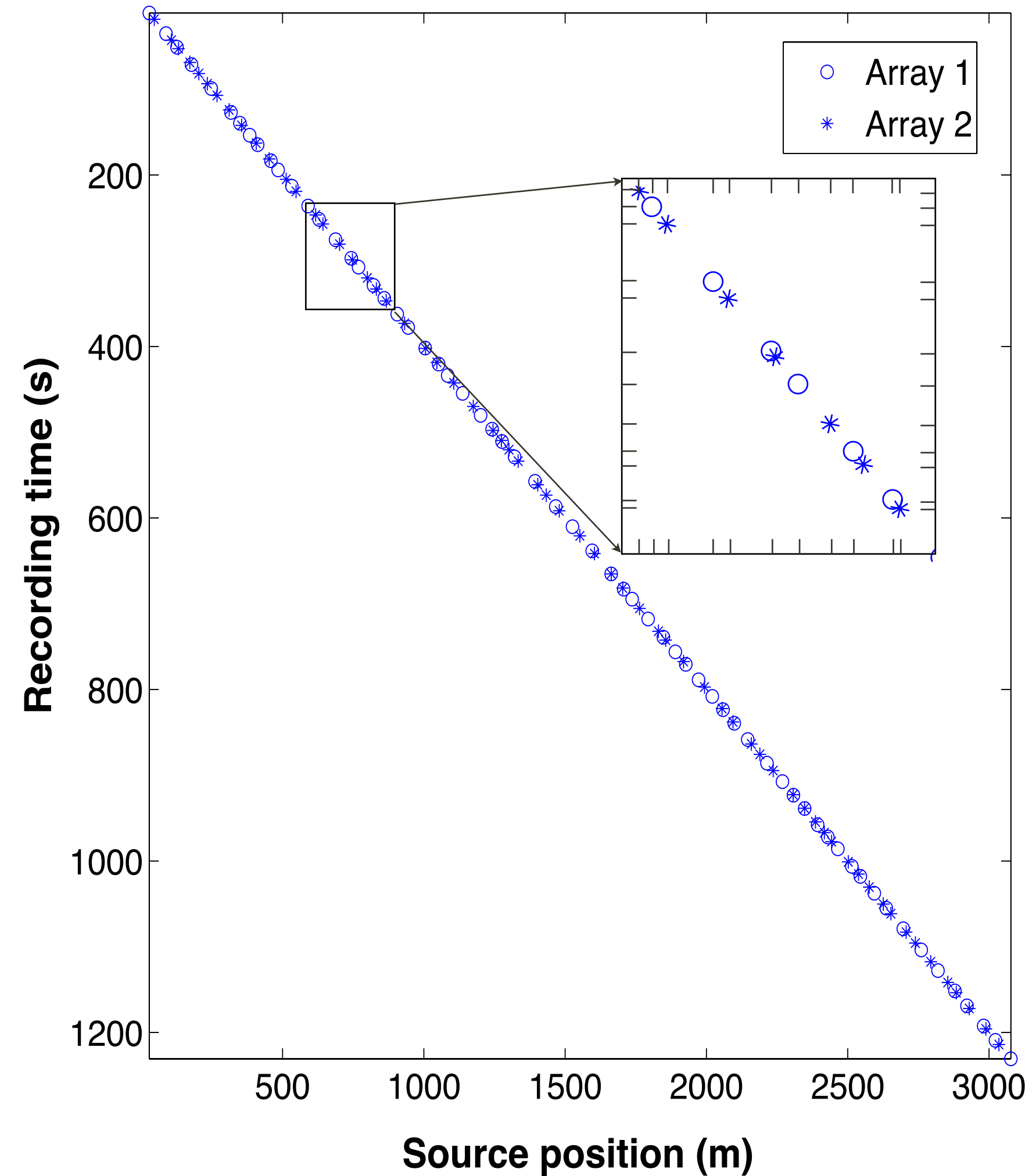
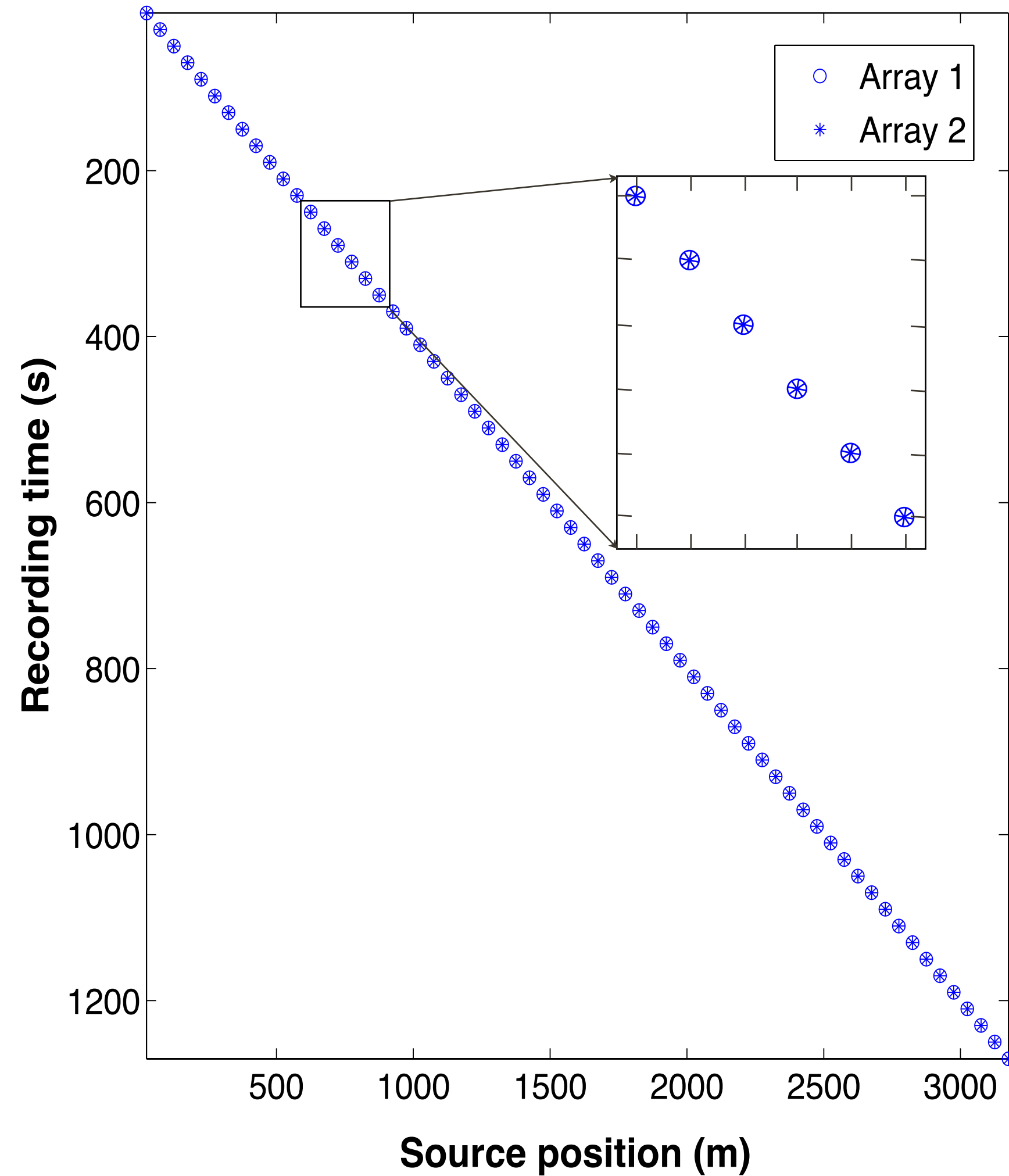
# Regular vs. *jittered* locations

[Speed of source vessel = 5 knots  $\approx$  2.5 m/s]

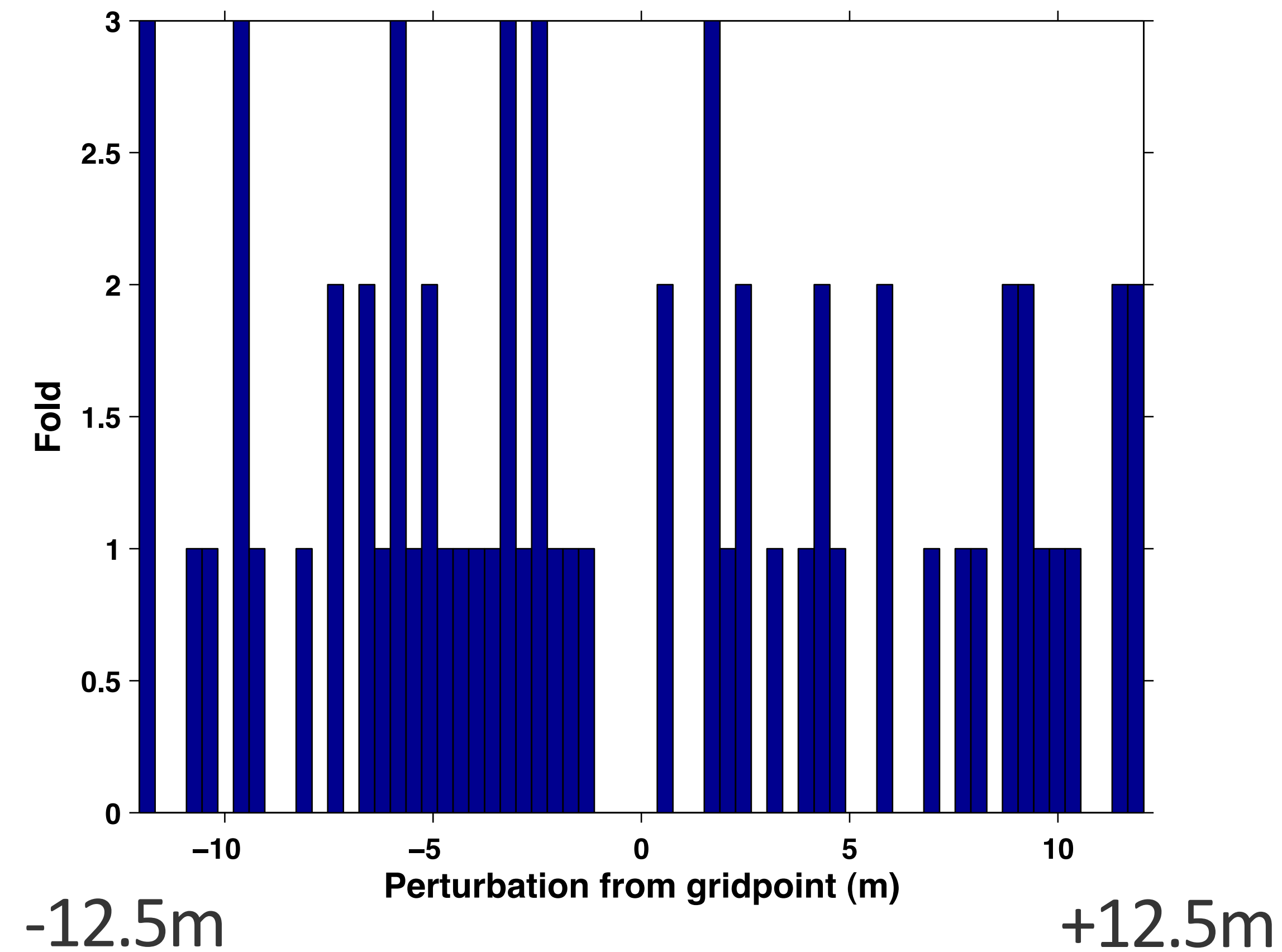
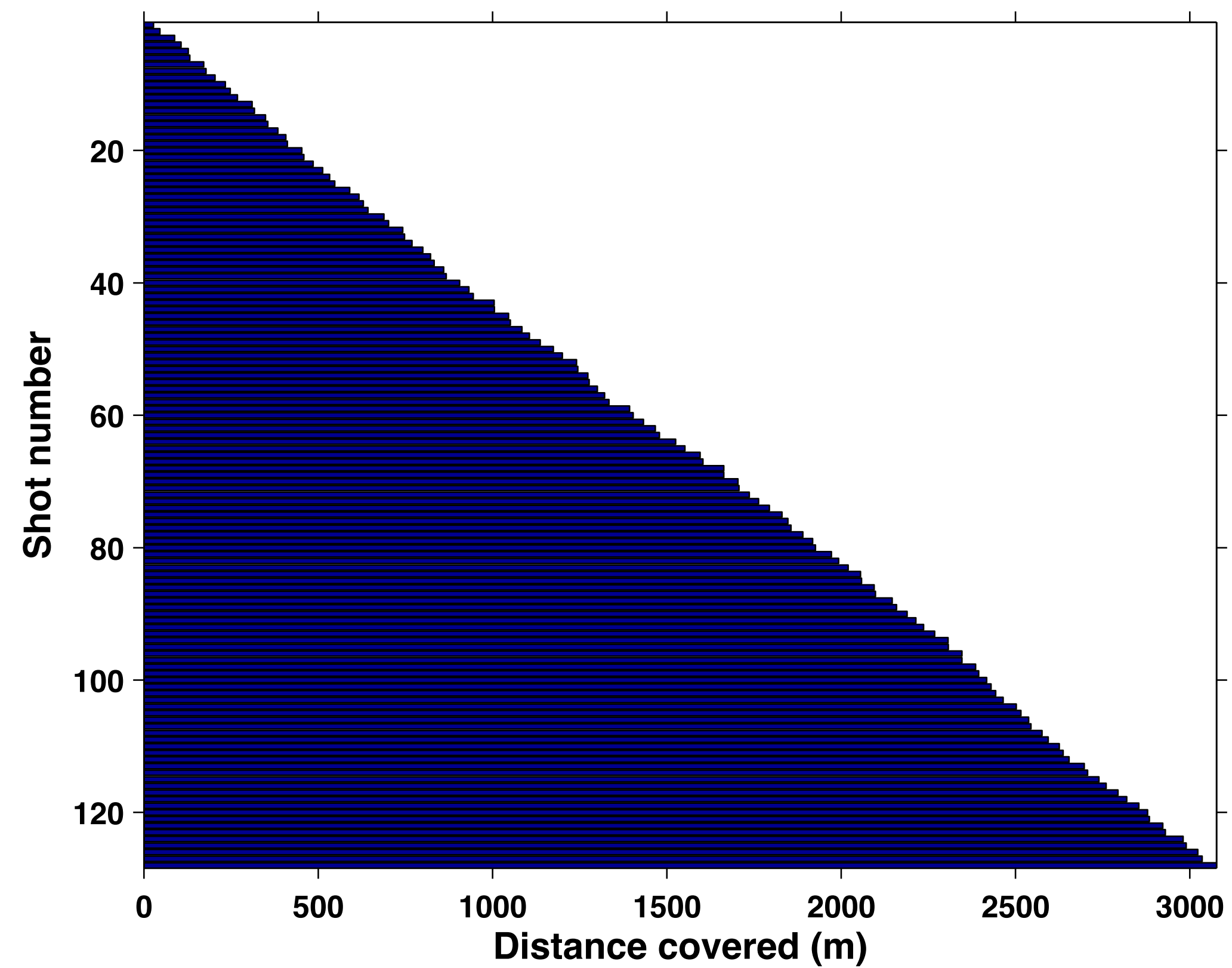


# Regular vs. *jittered* locations

[Speed of source vessel = 5 knots  $\approx$  2.5 m/s]

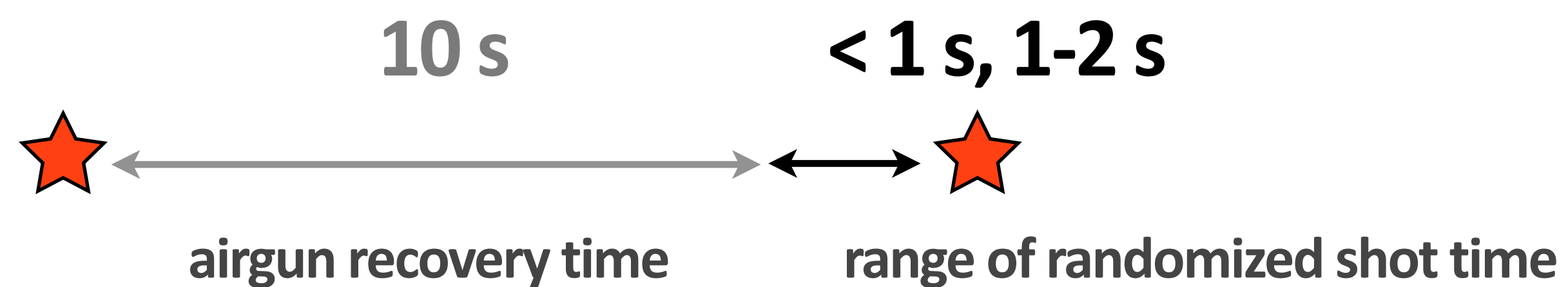


# Significant spatial jittering

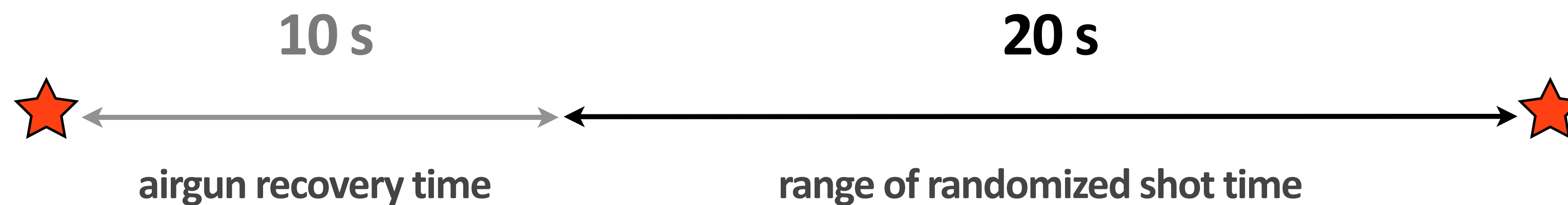


# Design of time-jittered shots

## Low variation

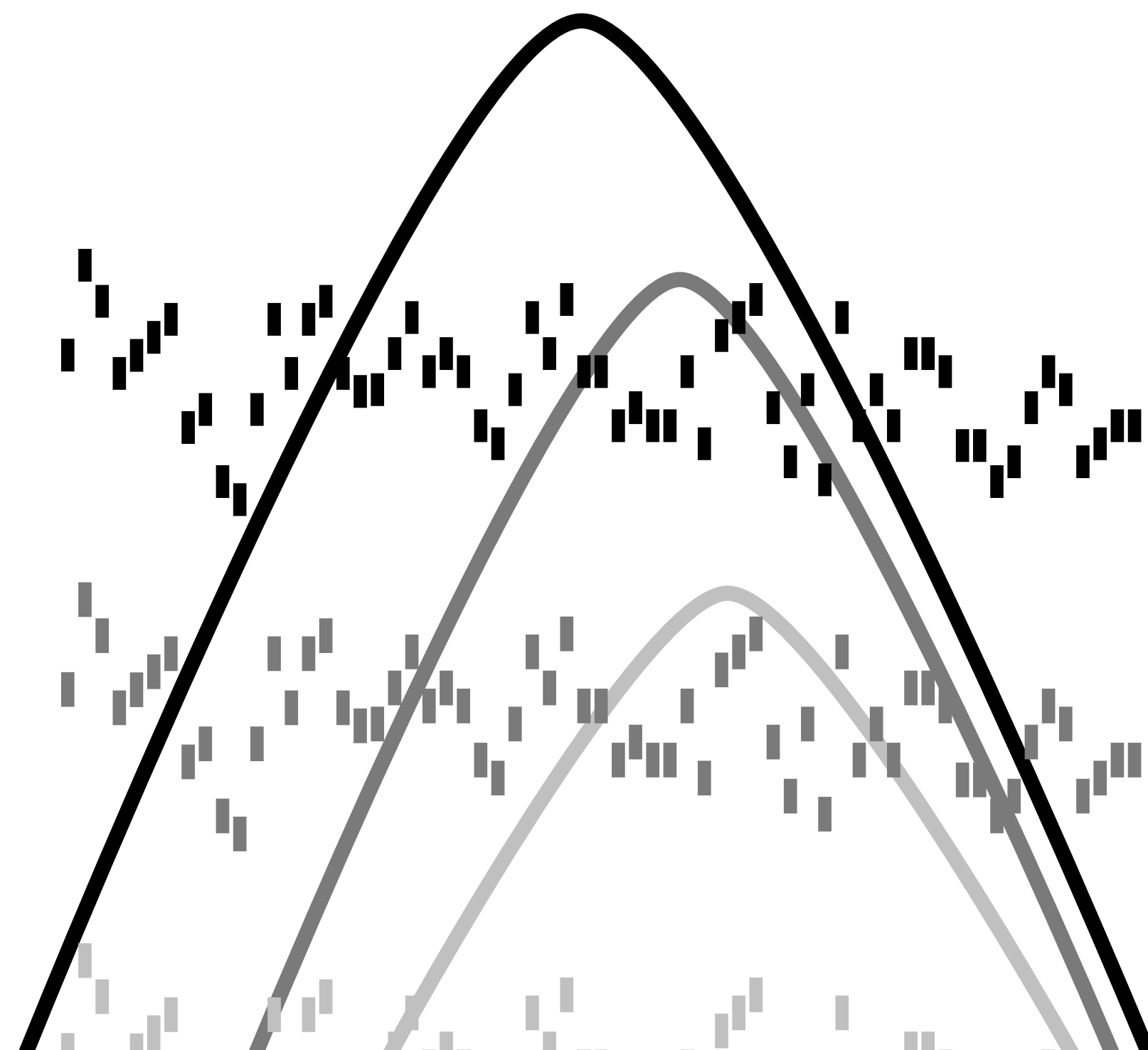


## High variation



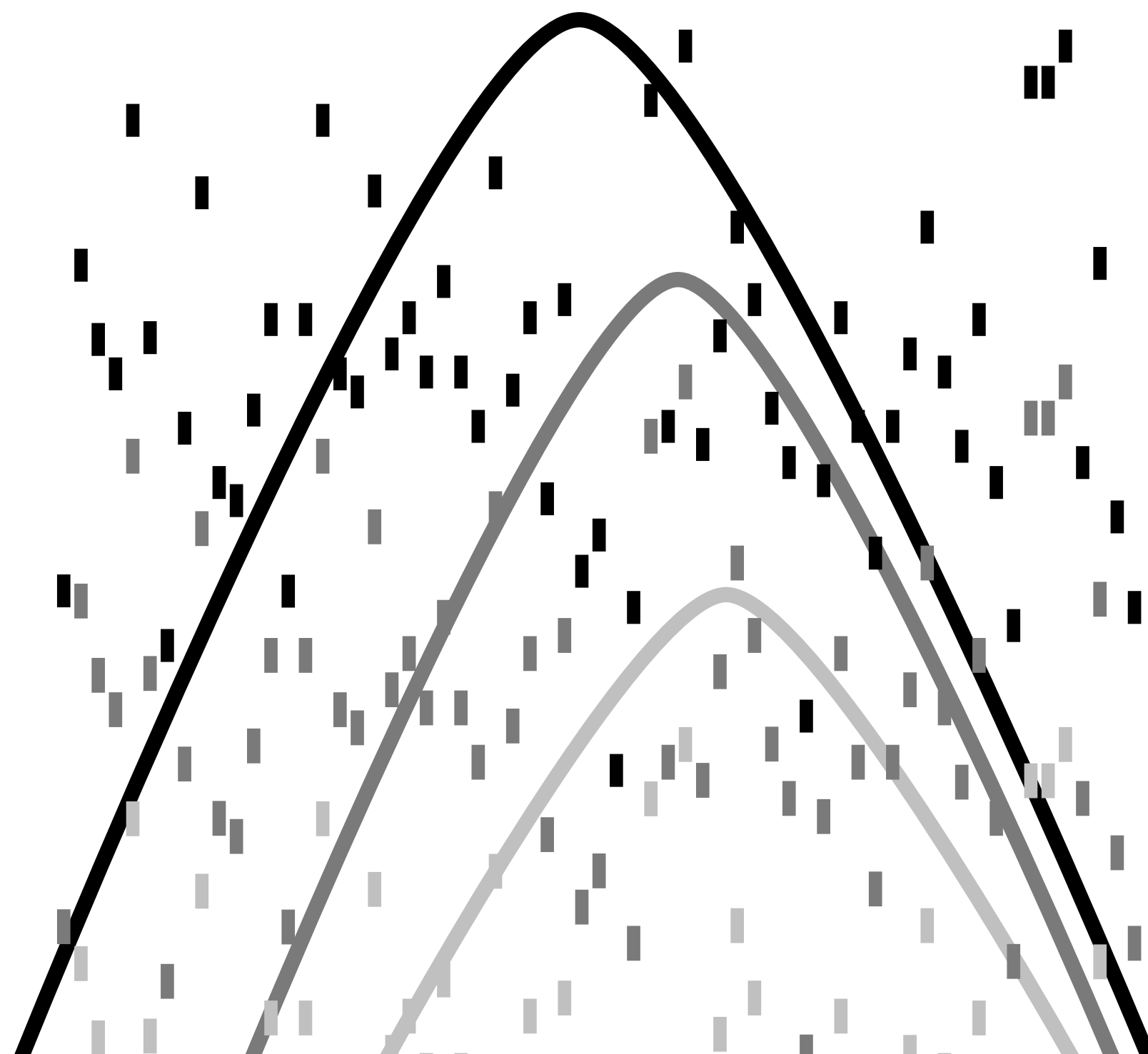


# Shot-time randomness



low variability

# Shot-time randomness



high variability,  
easier to separate,  
better low-frequency recovery(?)



# Simultaneous source acquisition & deblending

- *A new look at simultaneous sources by Beasley et. al., '98, '08*
- *High quality separation of simultaneous sources by sparse inversion by Abma et. al., '10*
- *Continued development of simultaneous source acquisition for ocean bottom surveys by Abma et. al., '13*
- *Method and system for separating seismic sources in marine simultaneous shooting acquisition by Baardman et. al., '13*
- *Changing the mindset in seismic data acquisition by Berkhout, '08*
- *Utilizing dispersed source arrays in blended acquisition by Berkhout et. al., '12*
- *Random sampling: a new strategy for marine acquisition by Moldoveanu, '10*
- *Multi-vessel coil shooting acquisition by Moldoveanu, '10*
- *Simultaneous source separation by sparse radon transform by Akerberg et. al., '08*
- *Simultaneous source separation using dithered sources by Moore et. al., '08*
- *Simultaneous sources - processing and applications by Moore, '10*
- *Simultaneous source separation via multi-directional vector-median filter by Huo et. al., '09*
- *Separation of blended data by iterative estimation and subtraction of blending interference noise by Mahdad et. al., '11*

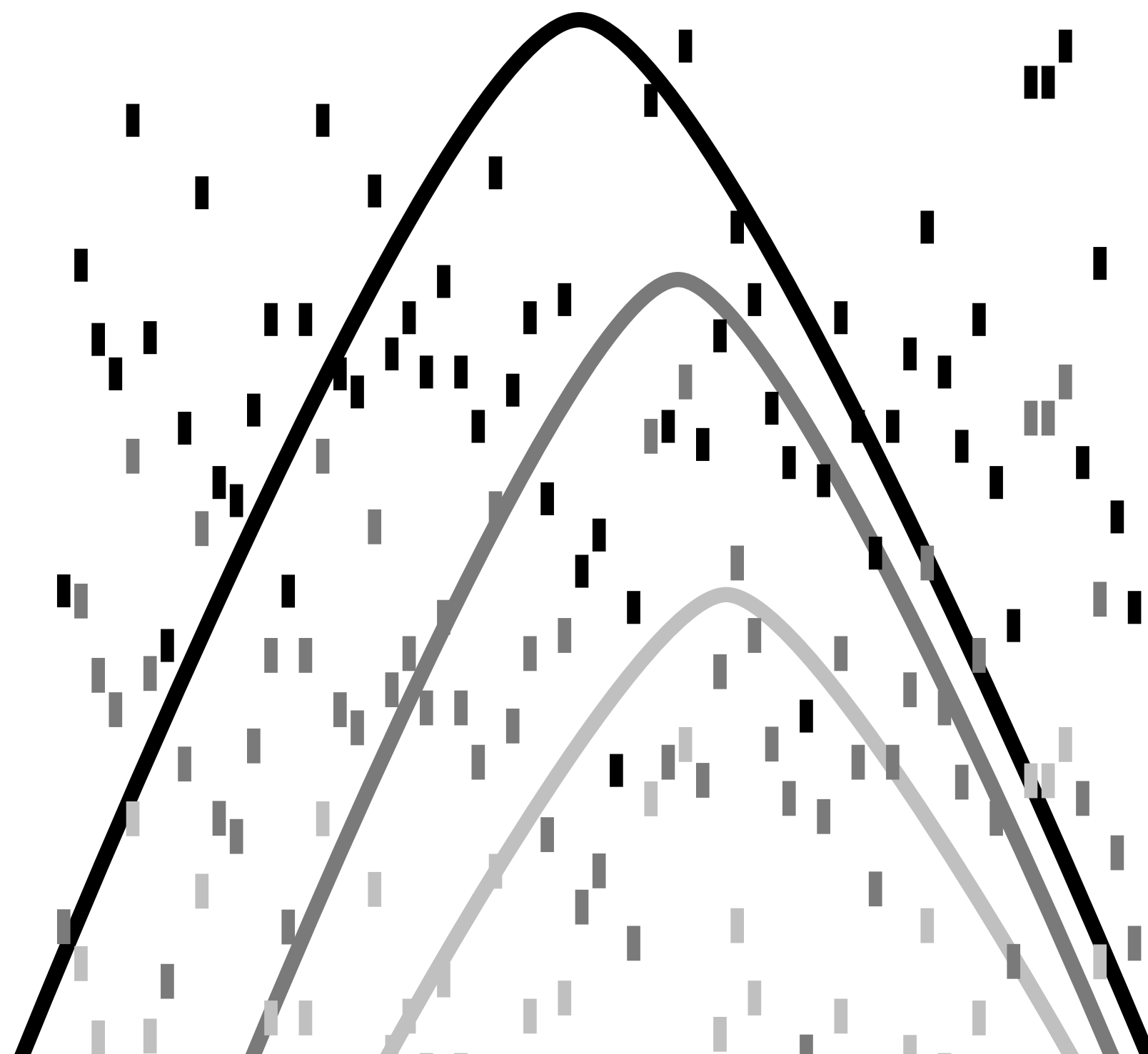
# Our approach

## Combination of

- ▶ multiple-source *time-jittered* acquisition
  - *random jitter* in time  $\implies$  *jitter* in *space* for a constant speed  
(favours recovery compared to *periodic* sampling)
  - shorter acquisition times
- ▶ *sparsity*-promoting processing
  - *data* is *sparse* in *curvelets*
  - *optimization*: use  $\ell_1$  constraints

Address two challenges - *overlap* and *jittered* sampling (regularize & interpolate)

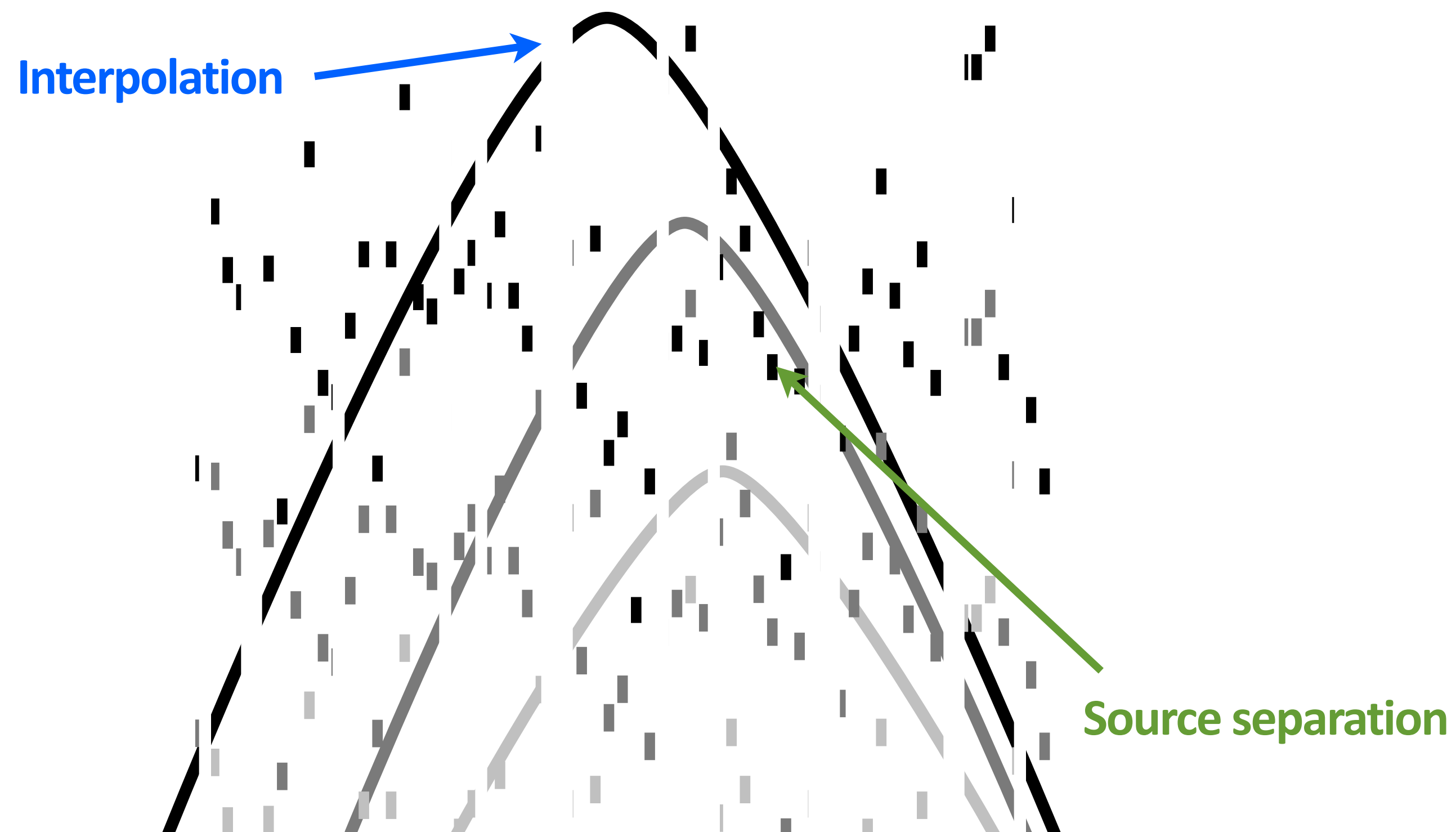
# Shot-time randomness



high variability,  
easier to separate,  
better low-frequency recovery(?)



# Shot-time randomness



high variability  
leads to  
source separation  
+  
regularization  
+  
interpolation

# Outline

- ▶ Design of *time-jittered* acquisition
  - jitter in *time*  $\Rightarrow$  jittered in *space* (*shot* locations)
  - low vs. high shot-time jitter
- ▶ **Recovery strategy**
- ▶ Experimental results of *sparsity*-promoting processing
  - wavefield recovery via “*deblending*” & *interpolation* from (coarse) *jittered/irregular* to (fine) *regular* sampling grid

# Compressed Sensing

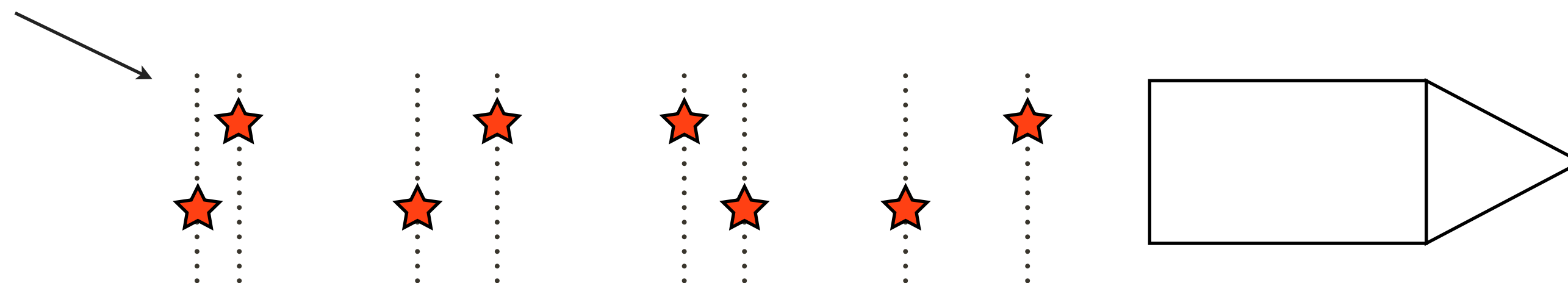
## Successful sampling & reconstruction scheme

- ▶ exploit *structure* via *sparsifying* transform
- ▶ *subsampling* – decreases sparsity
- ▶ large scale *optimization* – look for *sparsest* solution



# Time-jittered acquisition

*irregularly* sampled spatial grid

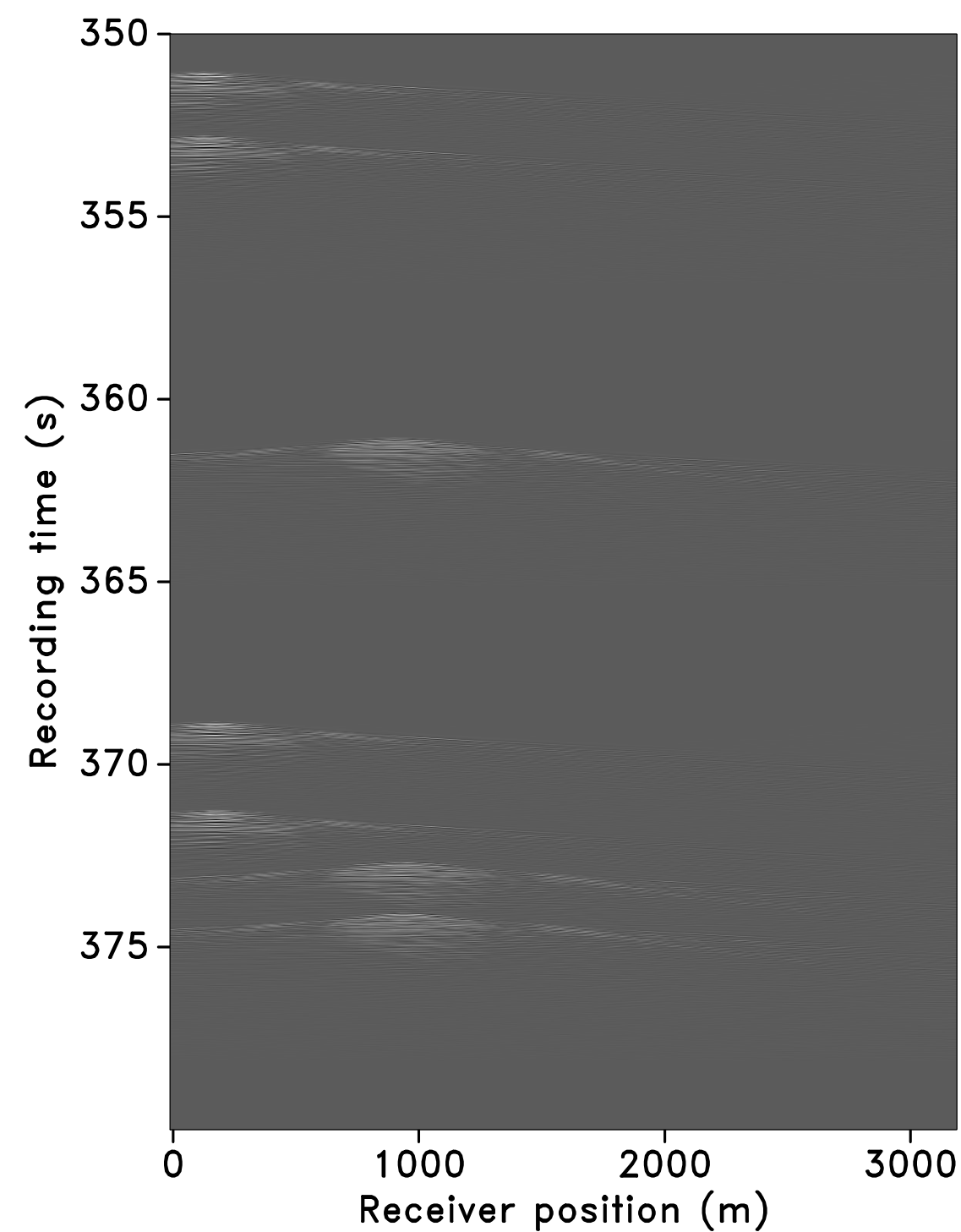


continuous recording  
*START*

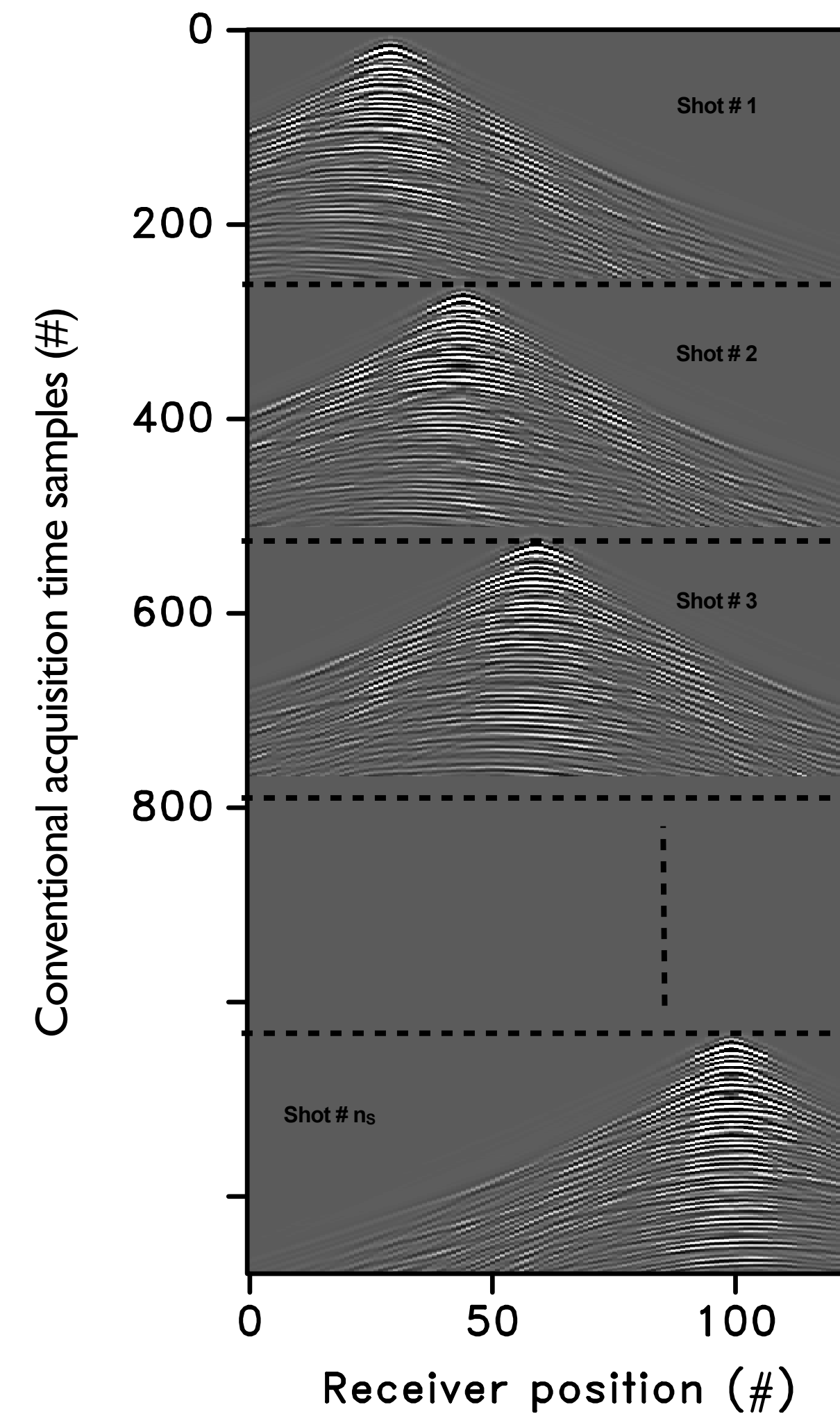
continuous recording  
*STOP*



acquire in the field on *irregular* grid  
(*subsampling* shots *w/ overlap*  
between shot records)

**b****=****ΓR**

would like to have on *regular* grid  
(*all* shots *w/o overlaps* between  
shot records)

**d**

# Sparsity-promoting recovery

$$\mathbf{d} = \mathbf{S}^H \mathbf{x}$$

$$\tilde{\mathbf{x}} = \arg \min_{\mathbf{x}} \|\mathbf{x}\|_1 \quad \text{subject to} \quad \mathbf{A}\mathbf{x} = \mathbf{b}$$

$\mathbf{x}$	a choice of curvelet coefficients for $\mathbf{d}$
$\mathbf{S}^H$	a transform domain synthesis
$\mathbf{A}$	measurement operator : $\mathbf{\Gamma R S}^H$ $\mathbf{\Gamma}$ is blending operator, $\mathbf{R}$ is regularization operator
$\mathbf{b}$	blended data
$\tilde{\mathbf{x}}$	estimated curvelet coefficients for source separated wavefield
$\tilde{\mathbf{d}}$	( $= \mathbf{S}^H \tilde{\mathbf{x}}$ ) estimated source separated wavefield

# Outline

- ▶ Design of *time-jittered* acquisition
  - jitter in *time*  $\Rightarrow$  jittered in *space* (*shot* locations)
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- ▶ Experimental results of *sparsity*-promoting processing
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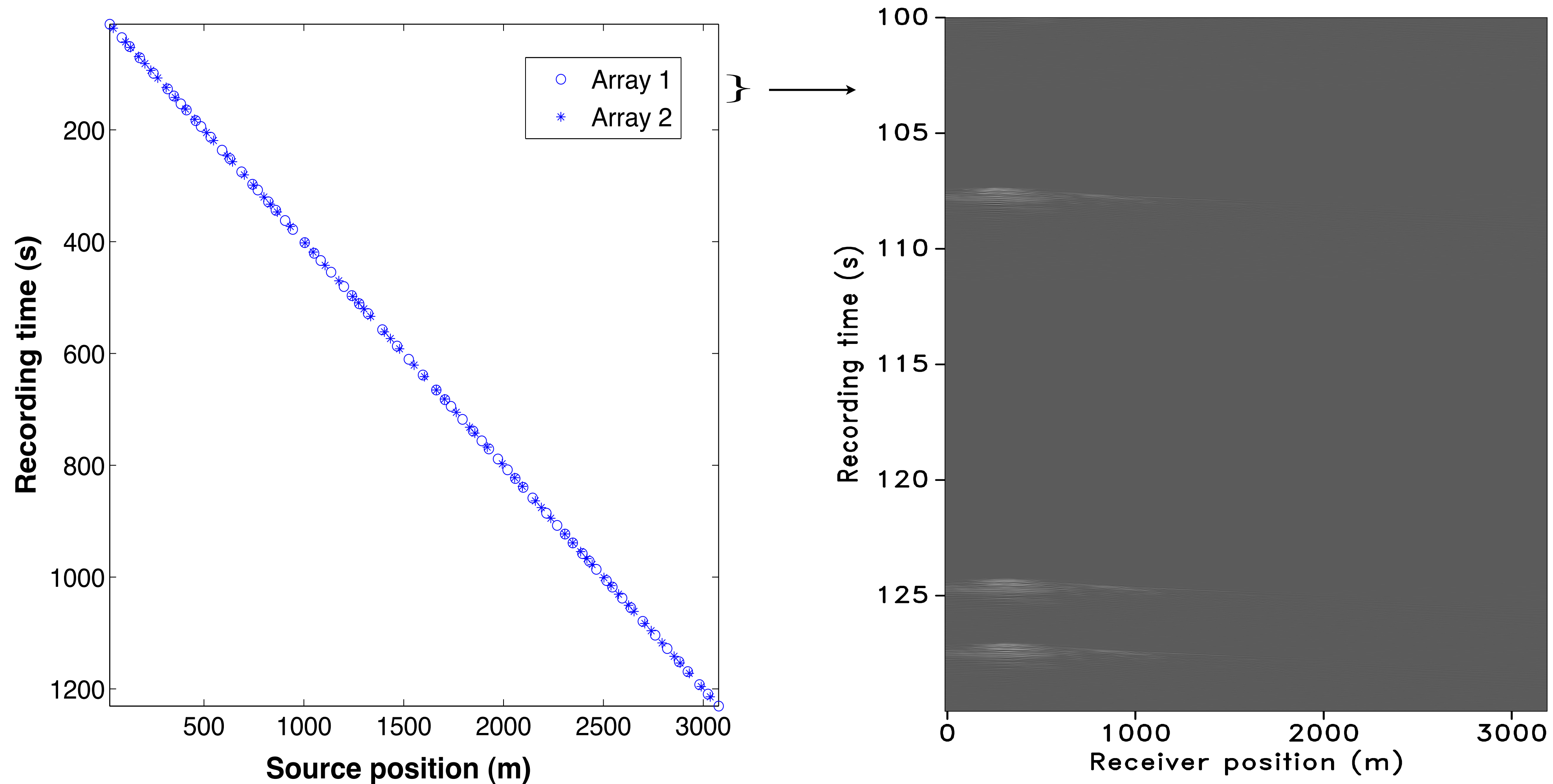


# Time-jittered OBC acquisition

[1 source vessel, speed = 5 knots, underlying grid: 25 m]

[no. of *jittered* source locations is *half* the number of sources (per array) in *ideal* periodic survey w/o overlap]

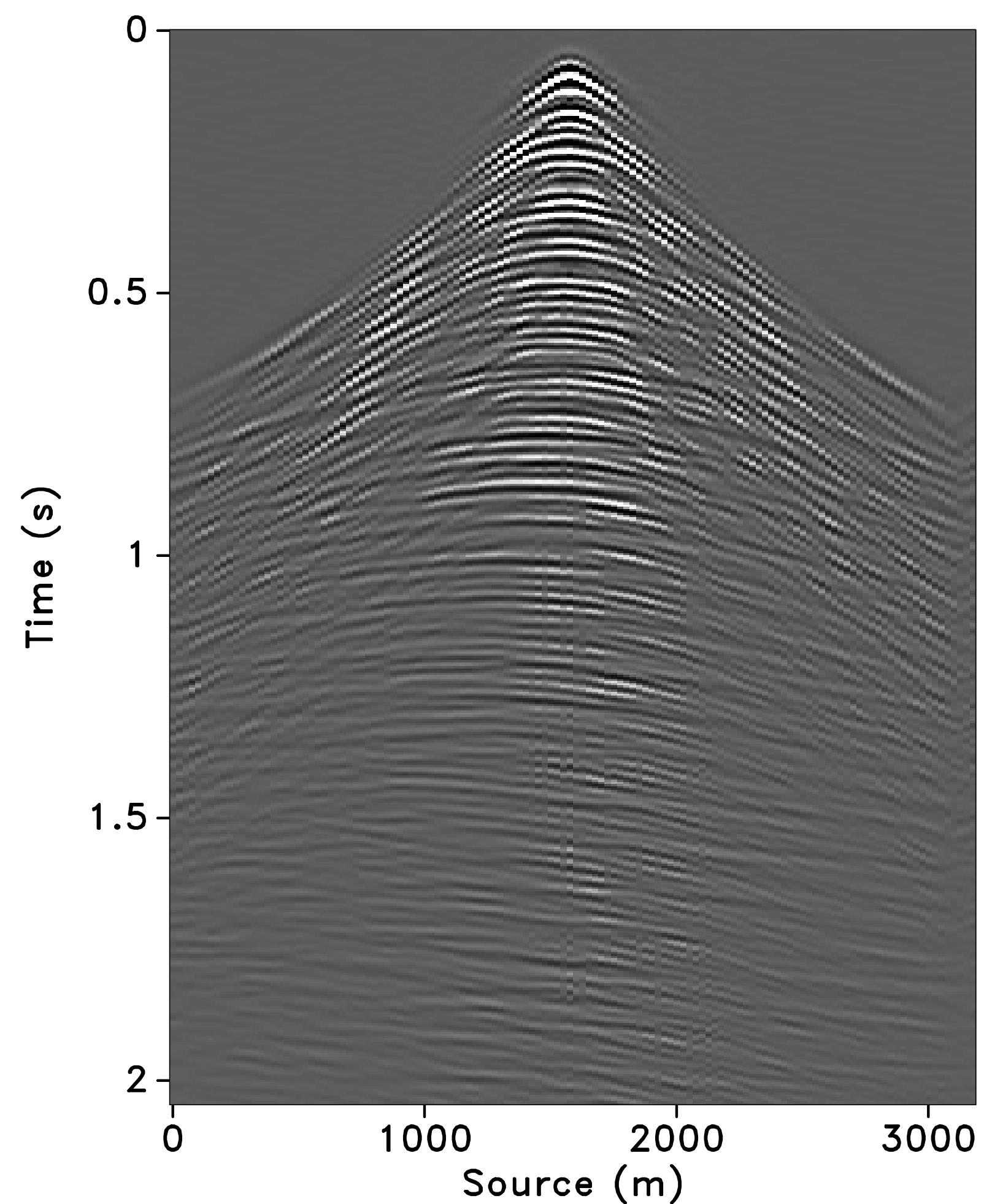
MEASUREMENTS (b)



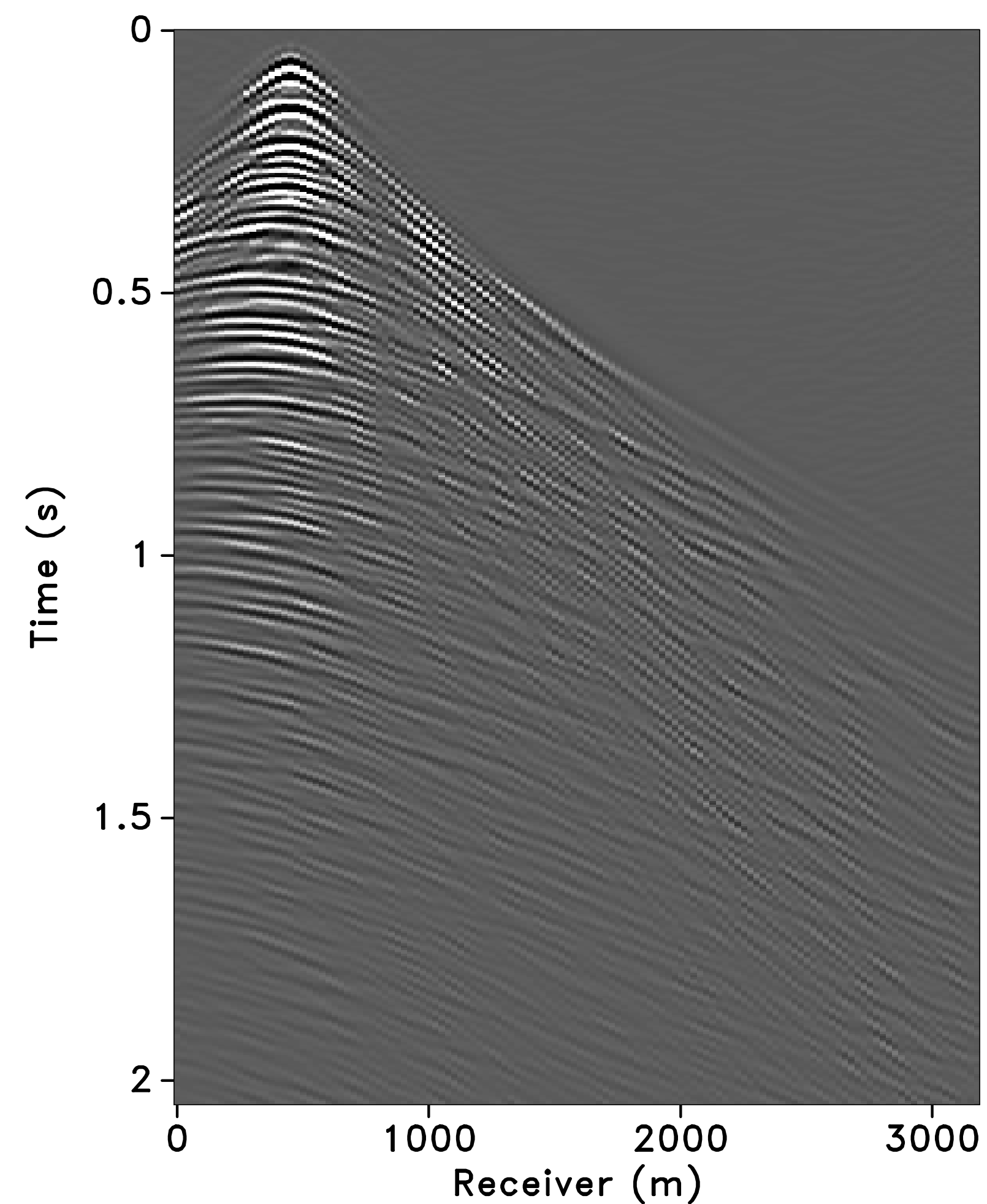
# Sparsity-promoting recovery on the grid (14.2 dB)

["deblending" from *jittered* 50m grid to *regular* 25m grid]

RECEIVER GATHER



SHOT GATHER

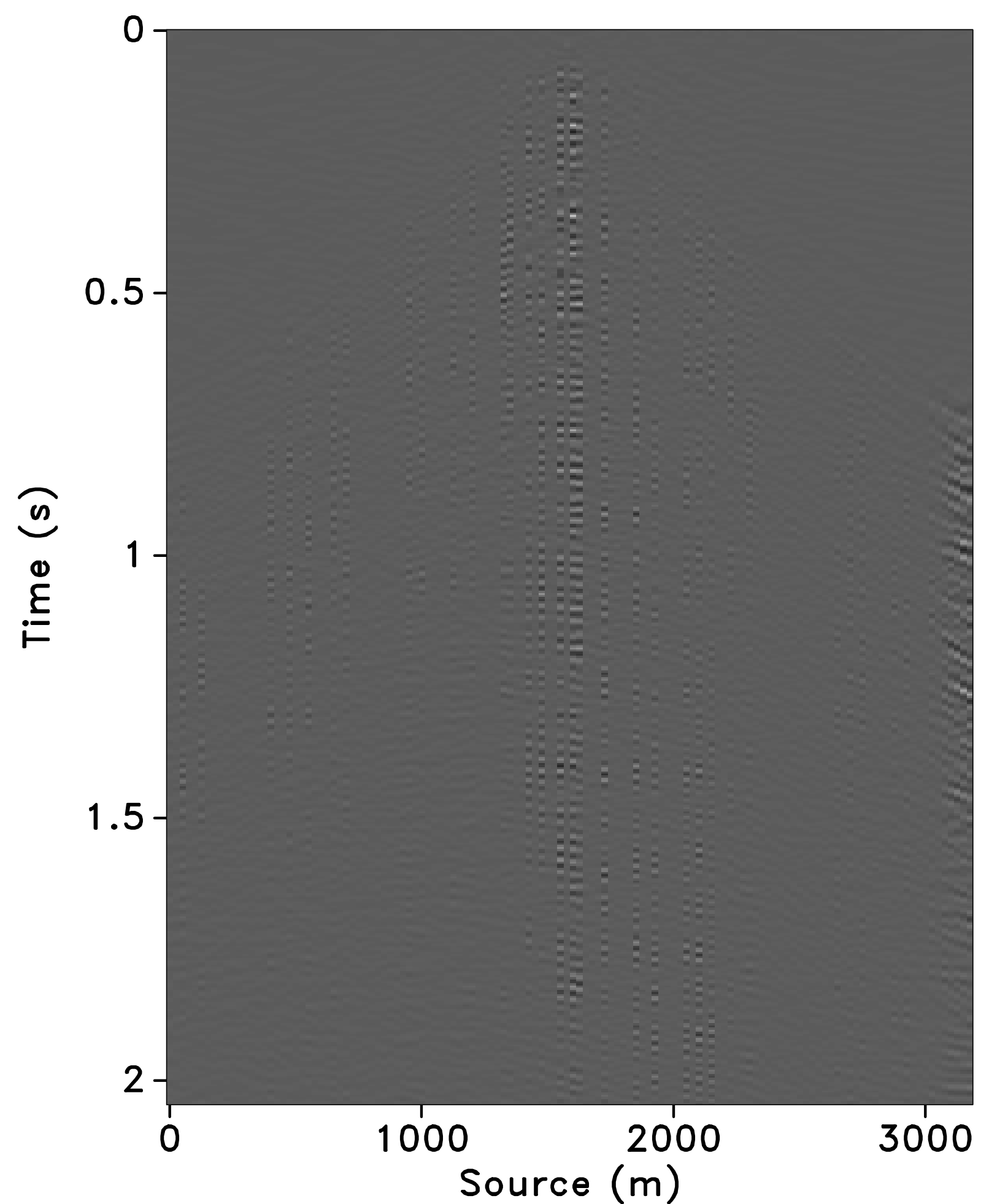




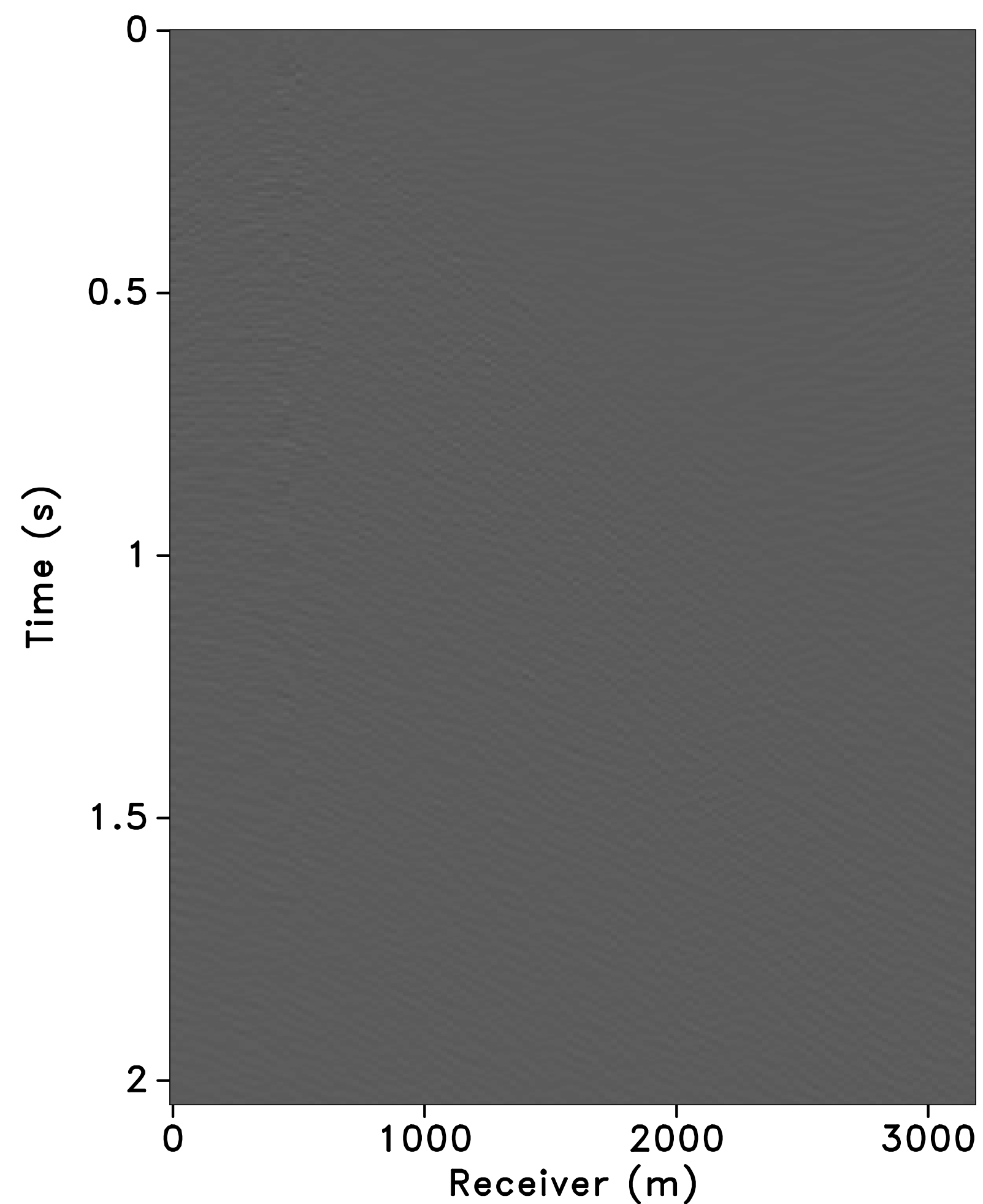
# Sparsity-promoting recovery on the grid (14.2 dB)

["deblending" from *jittered* 50m grid to *regular* 25m grid] (difference)

RECEIVER GATHER

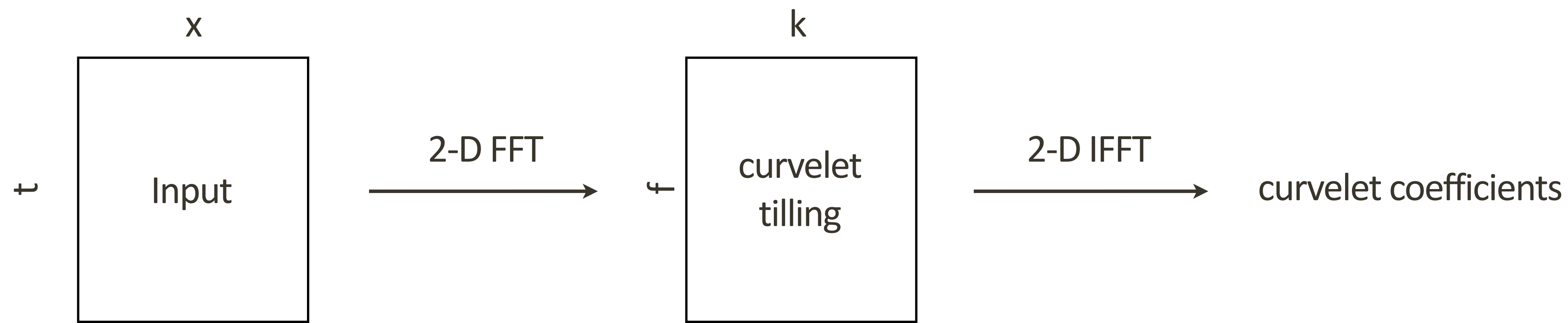


SHOT GATHER

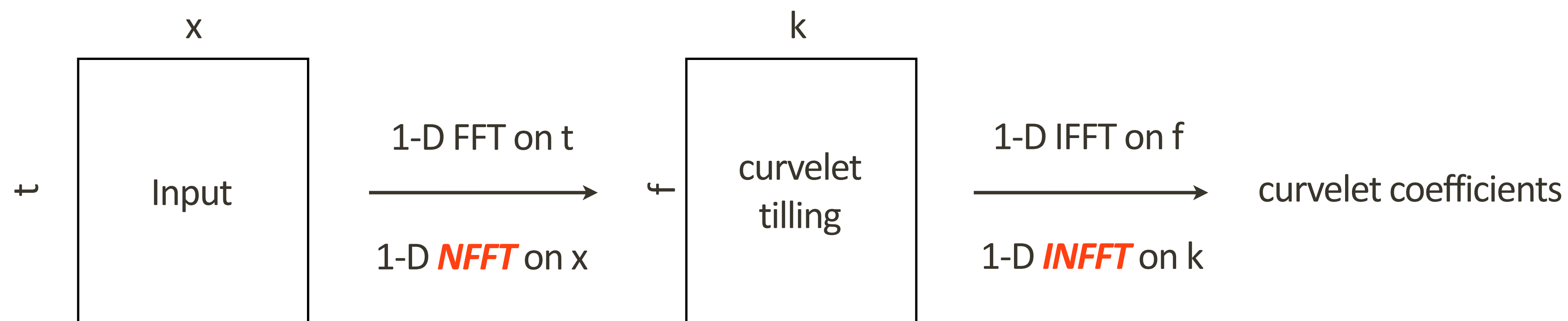


# FDCT vs. NFDCT

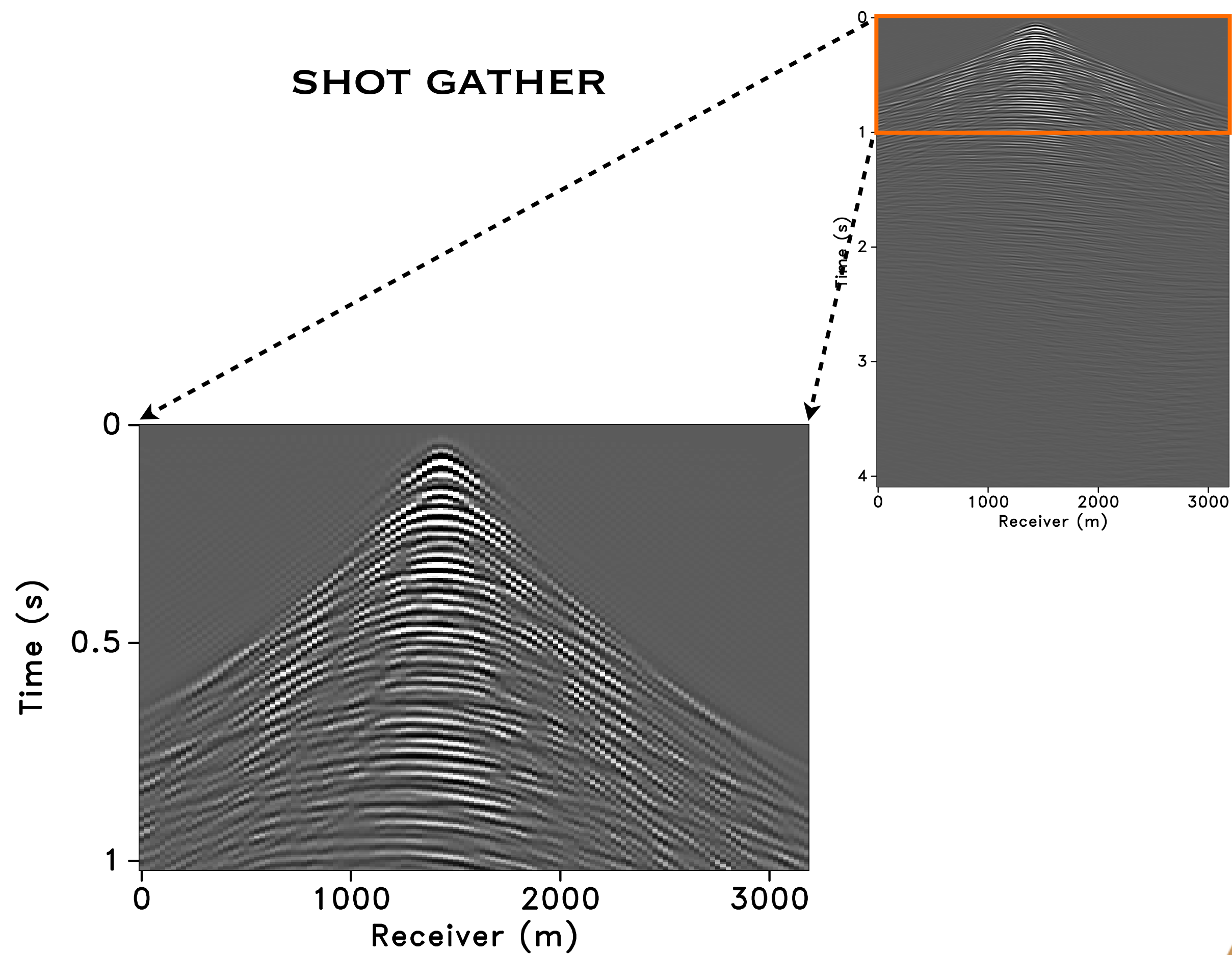
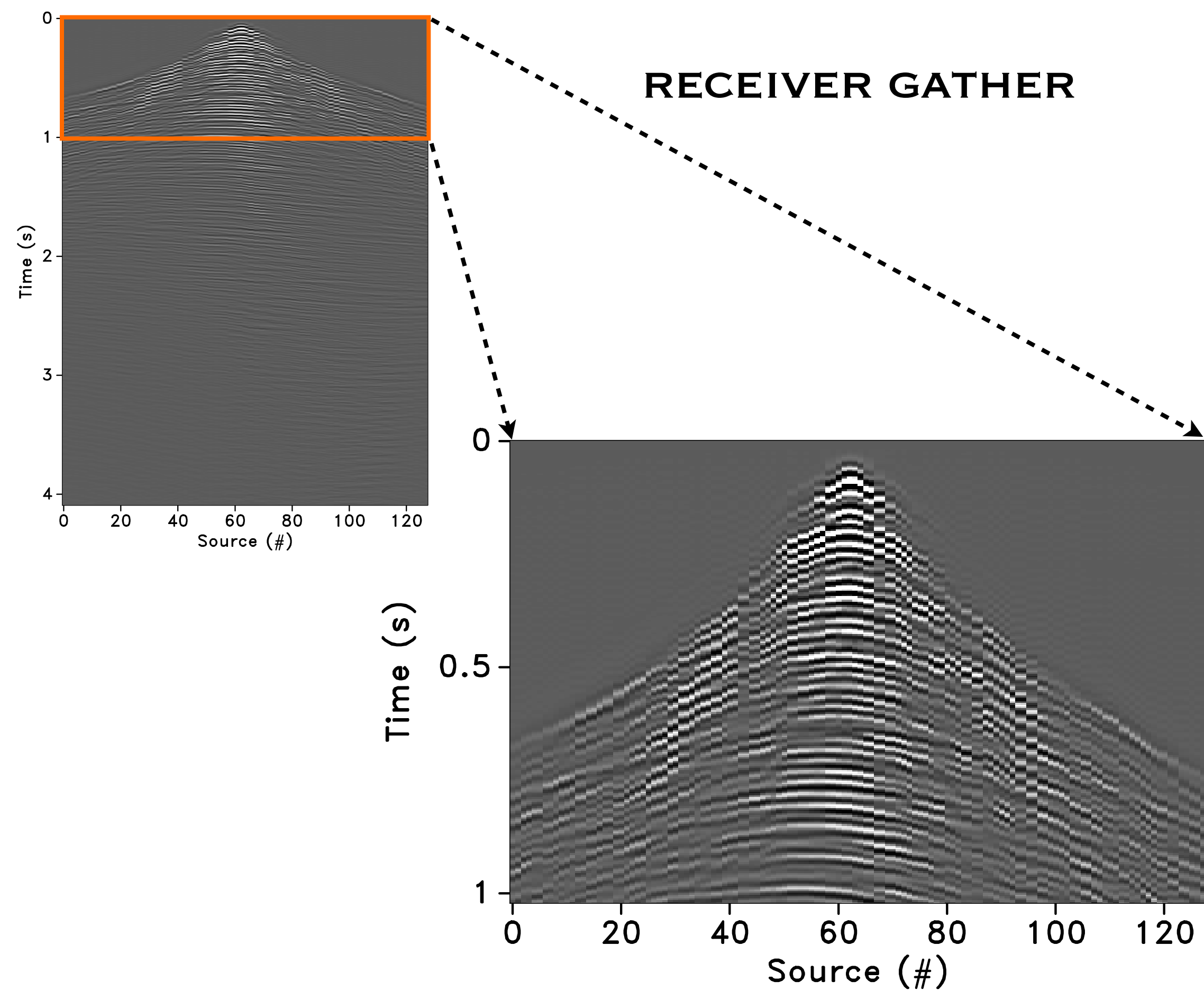
## Fast Discrete Curvelet Transform



## Non-equispaced Fast Discrete Curvelet Transform



# Irregular traces

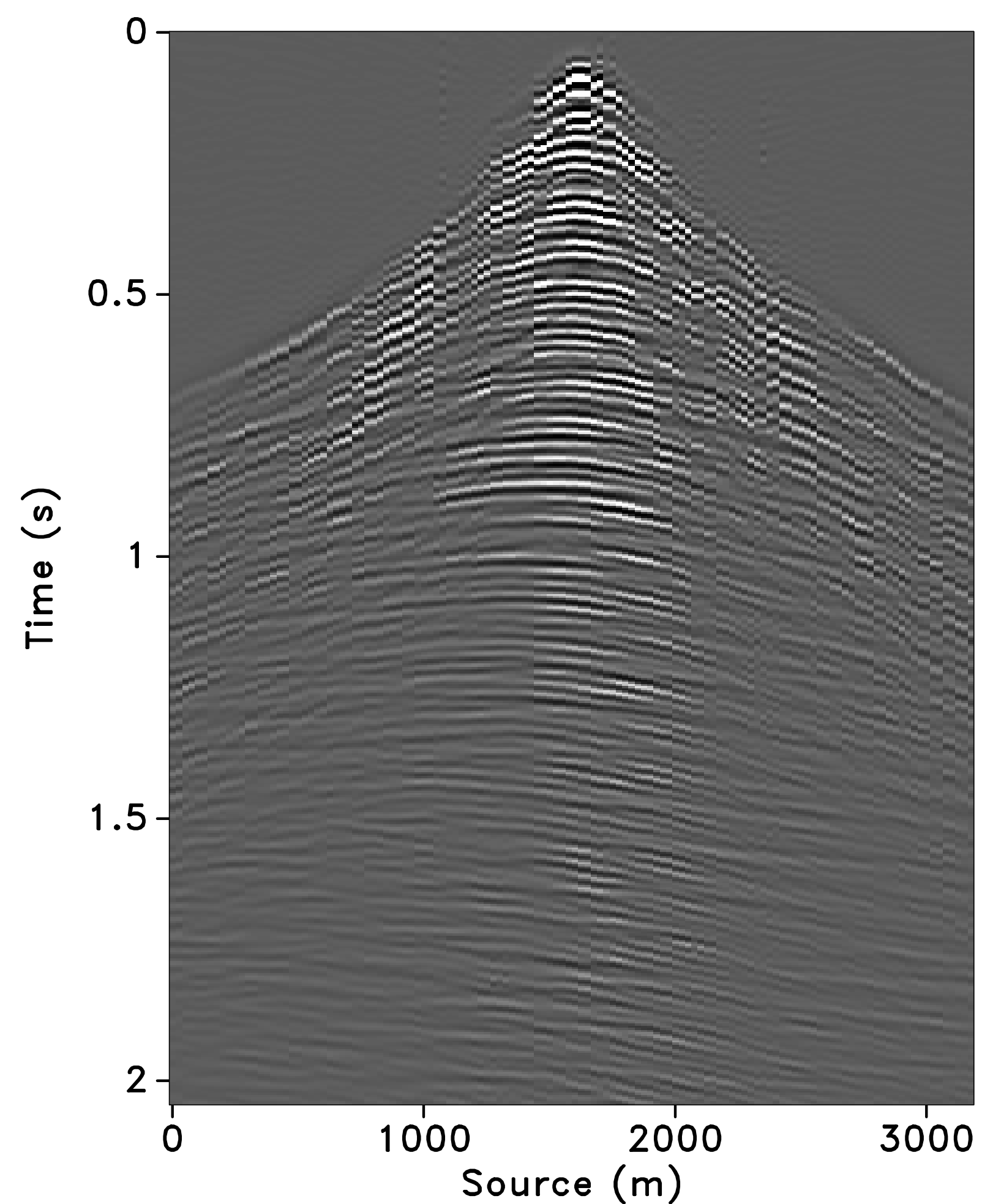




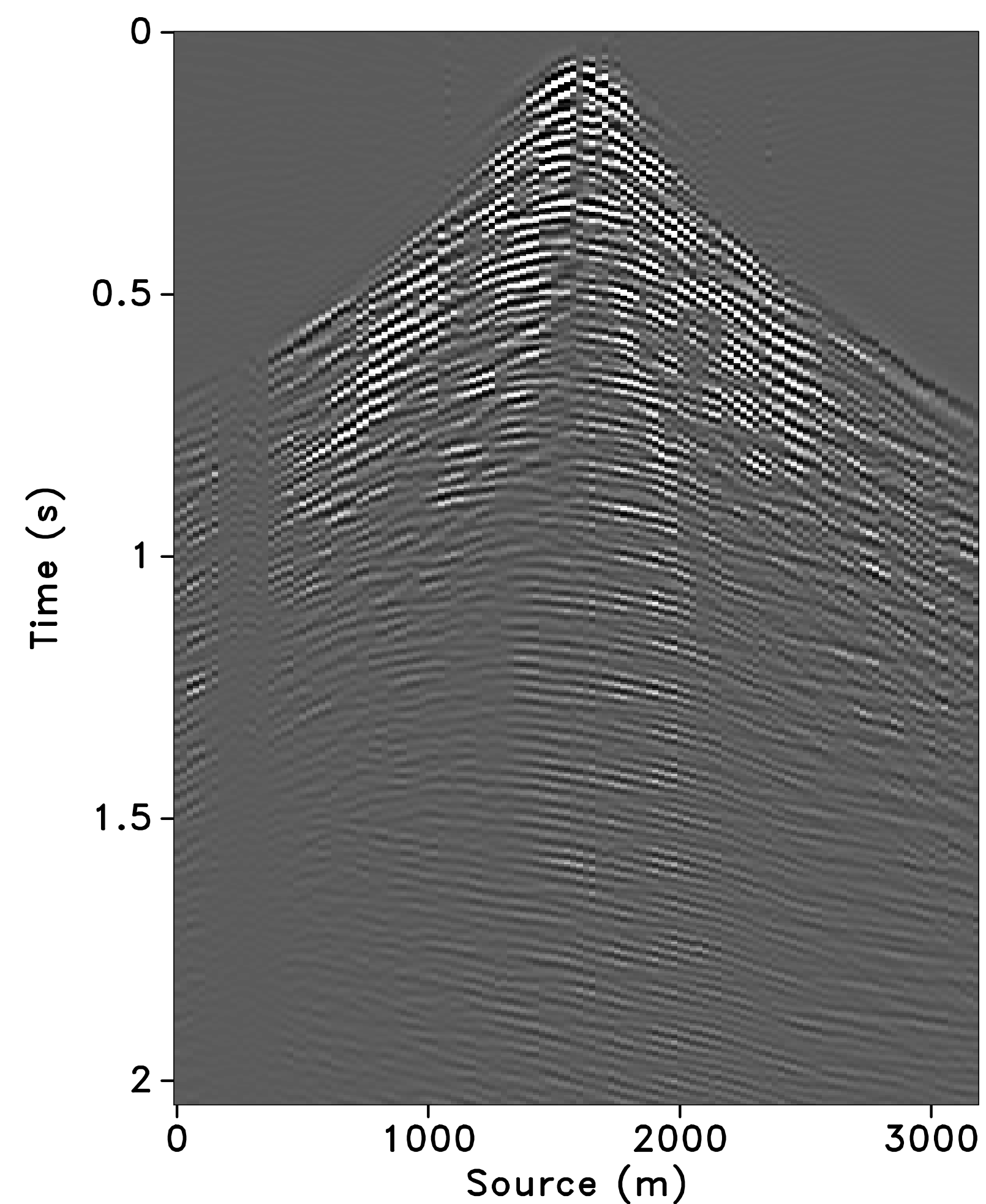
# Recovery with *FDCT* ('binning')

["deblending" from *jittered* 50m grid to *regular* 25m grid]

RECEIVER GATHER



DIFFERENCE

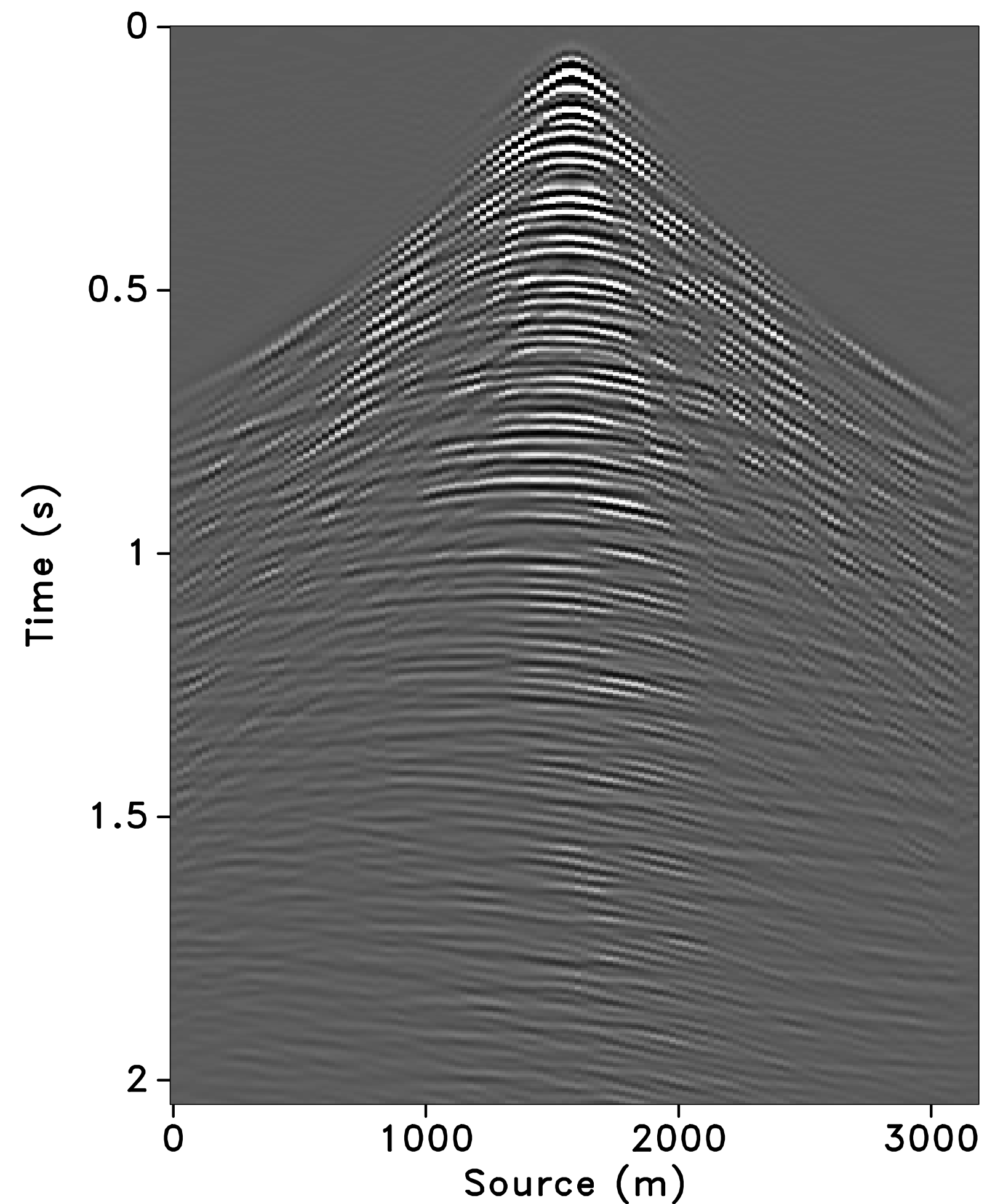




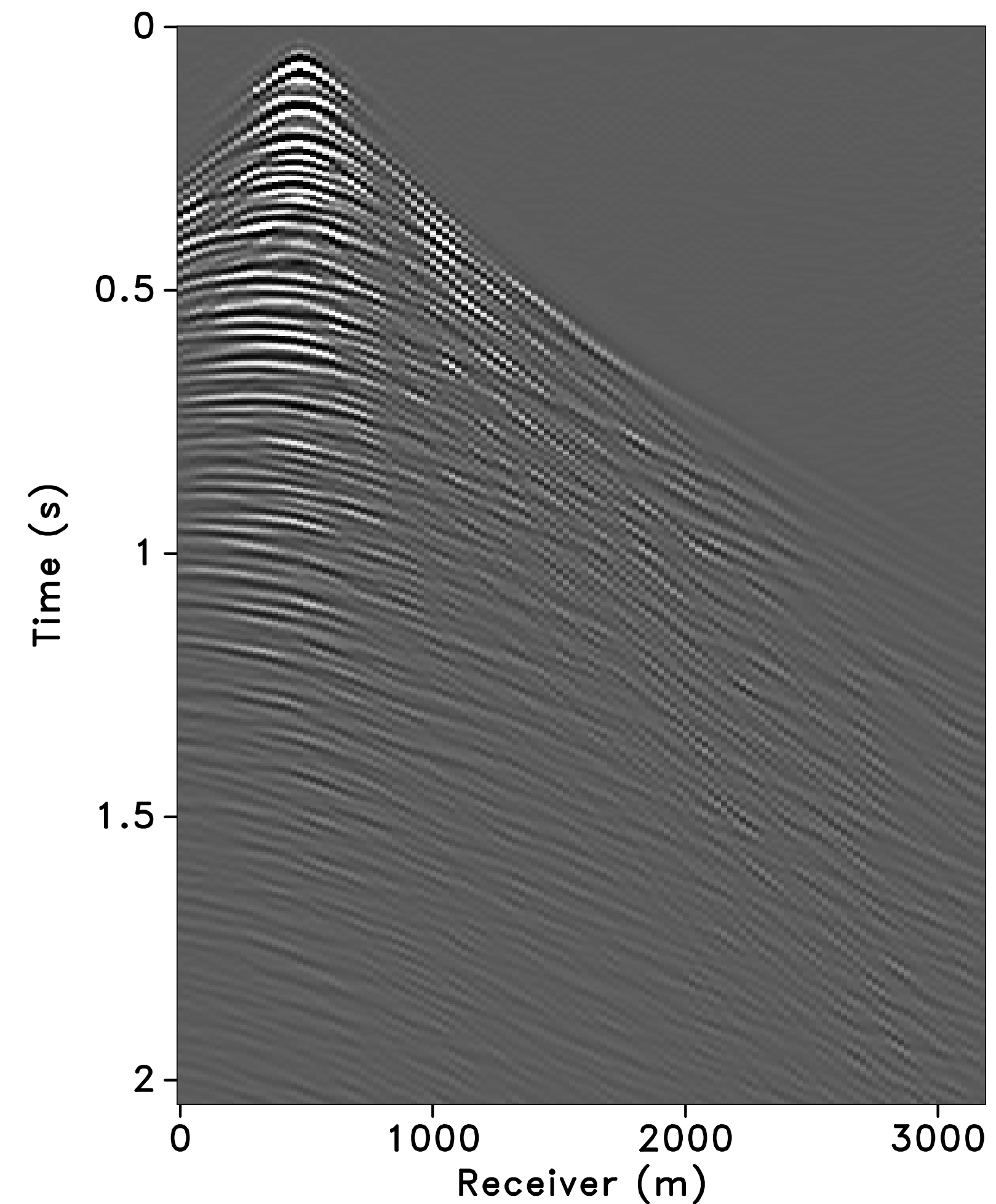
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (17.1 dB)

["deblending" from *jittered* 50m grid to *regular* 25m grid]

RECEIVER GATHER



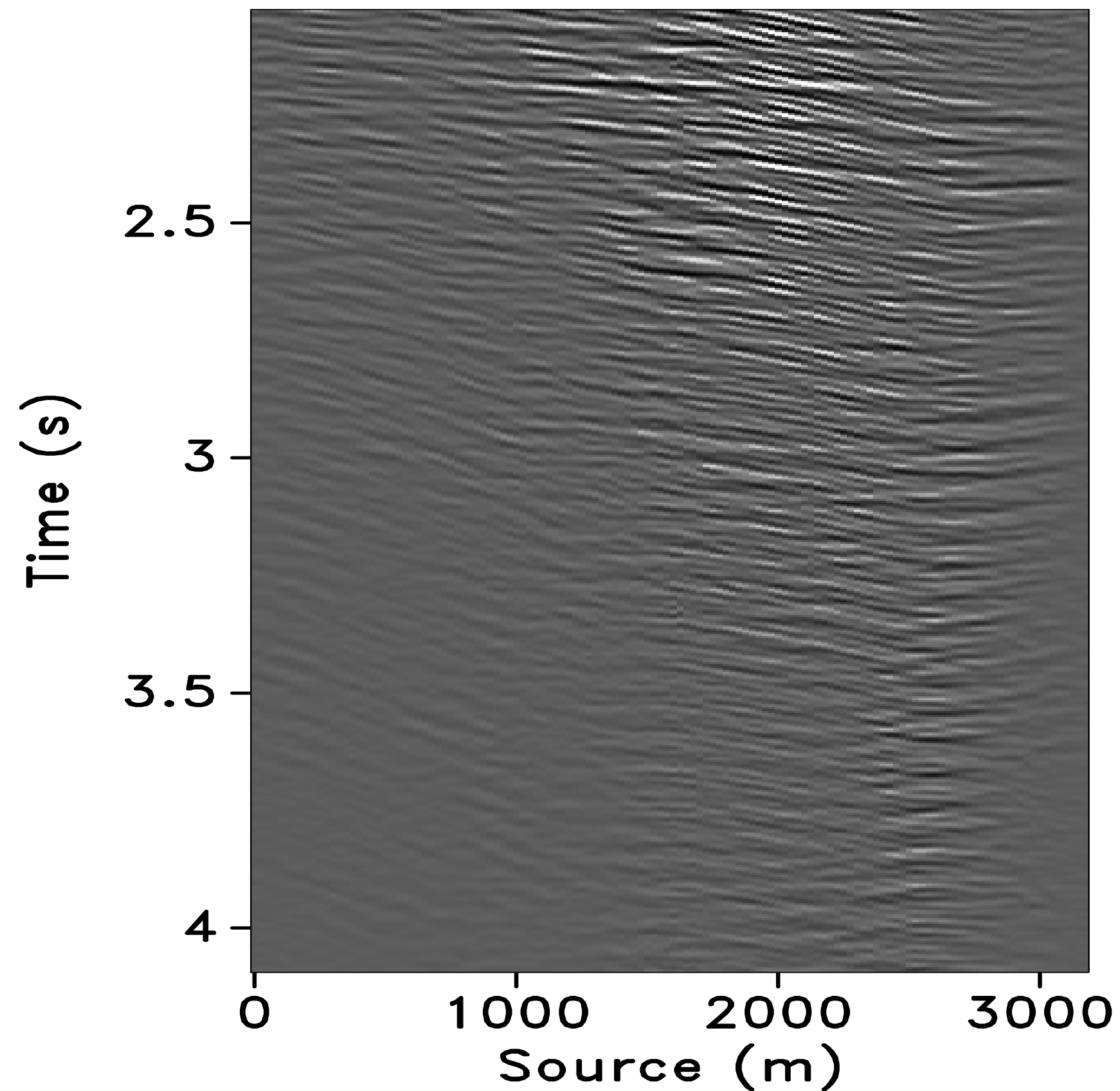
SHOT GATHER



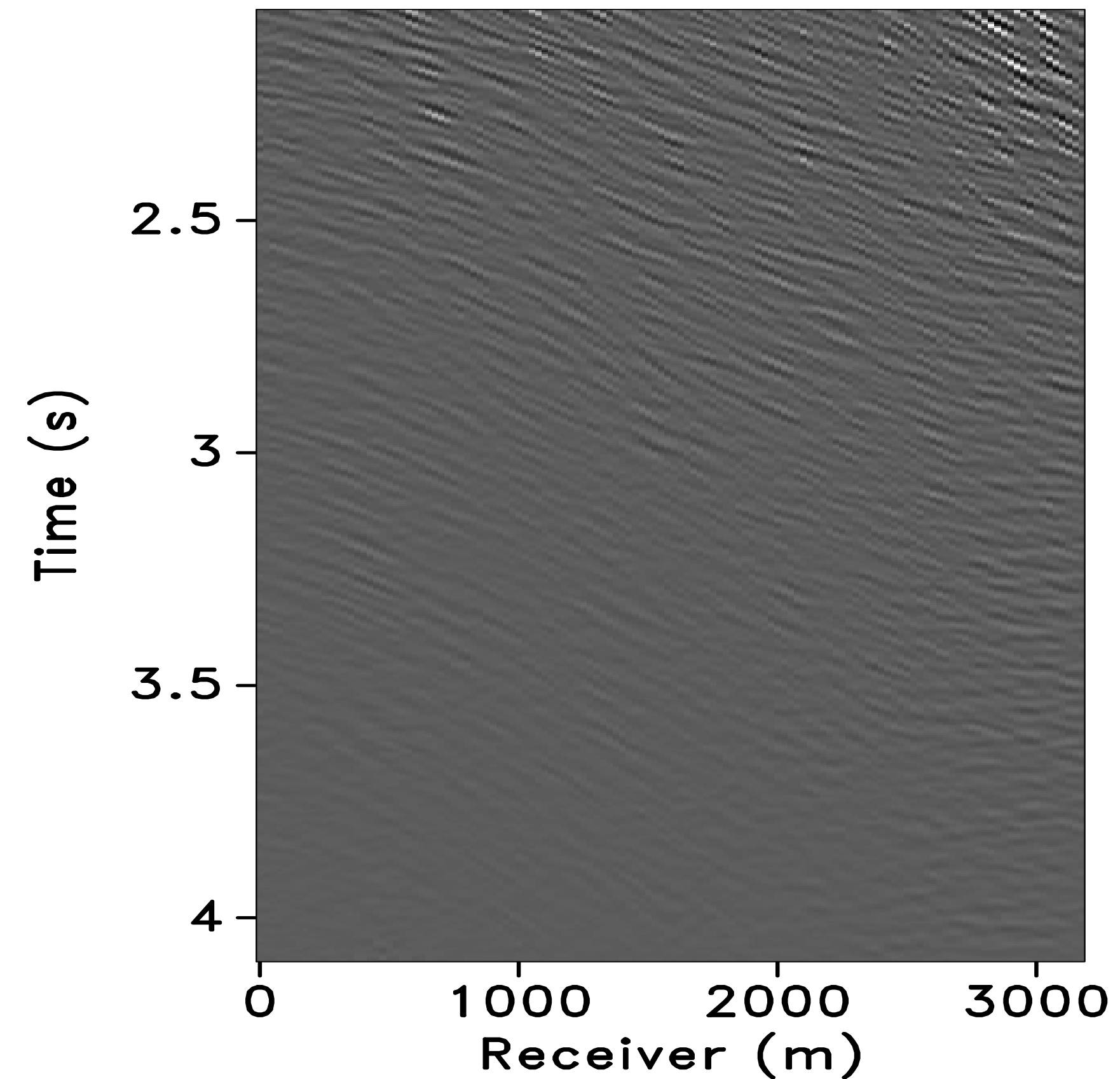
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (17.1 dB)

["deblending" from *jittered* 50m grid to *regular* 25m grid]

RECEIVER GATHER



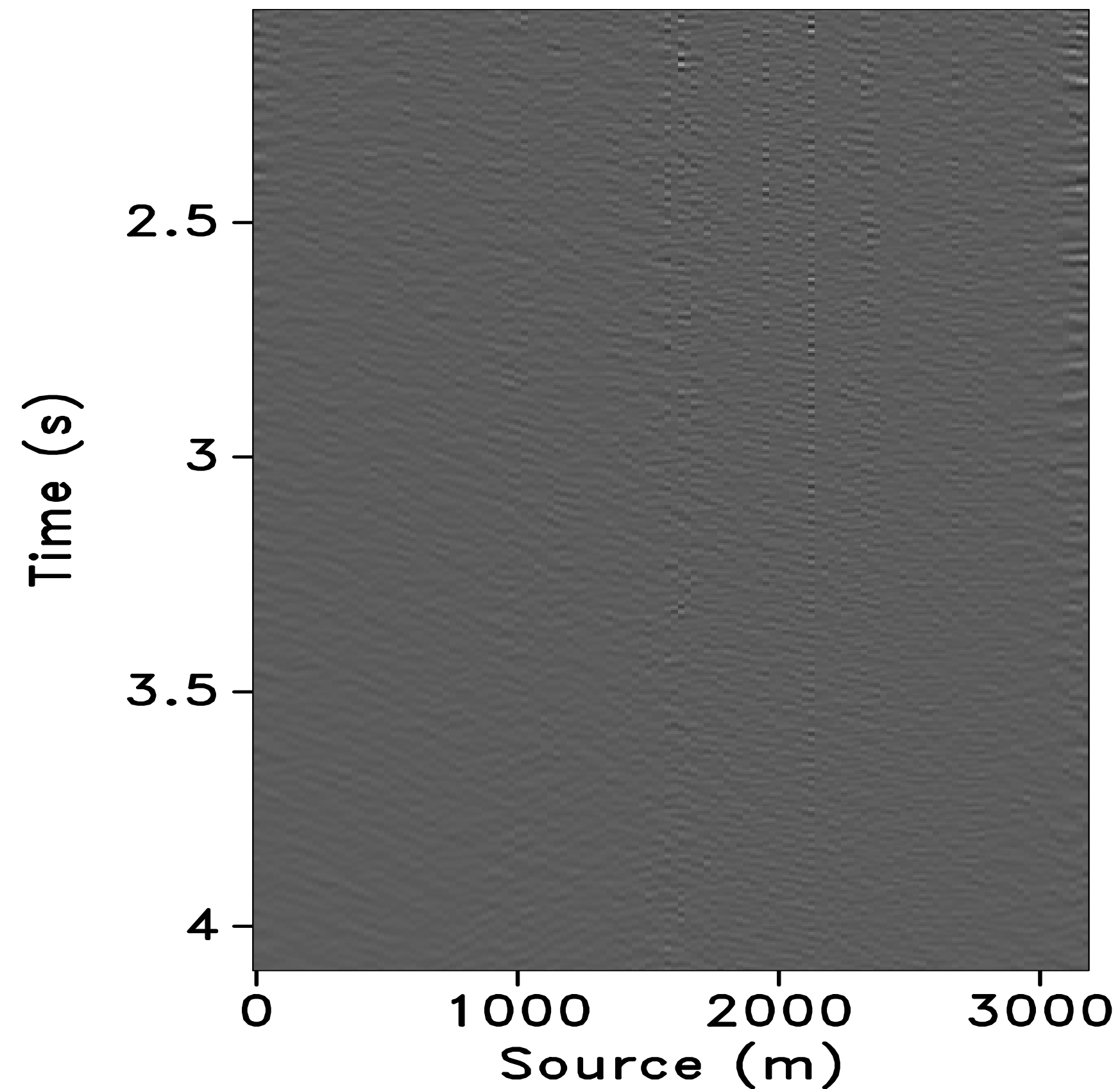
SHOT GATHER



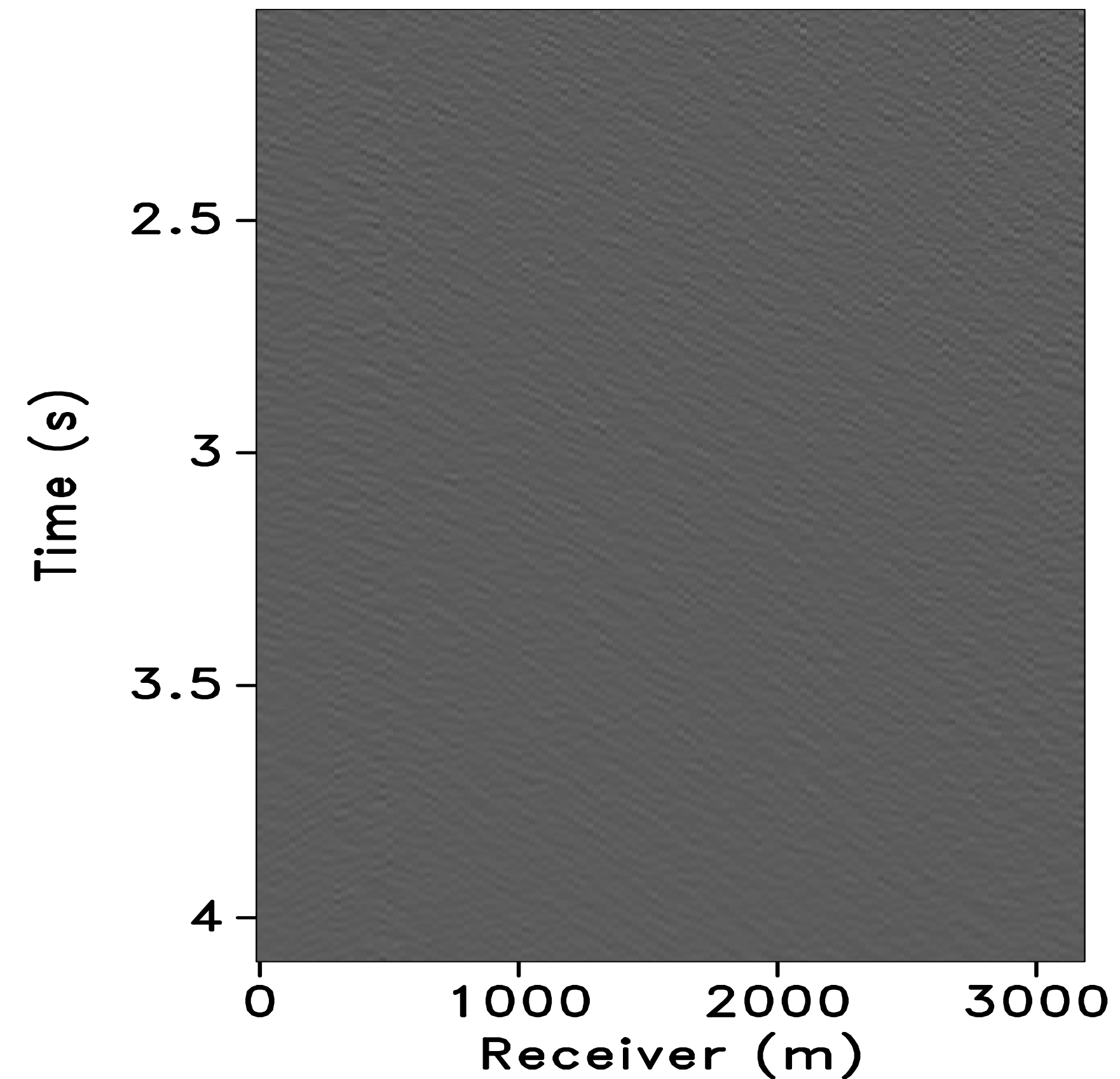
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (17.1 dB)

["deblending" from *jittered* 50m grid to *regular* 25m grid] (difference)

RECEIVER GATHER



SHOT GATHER

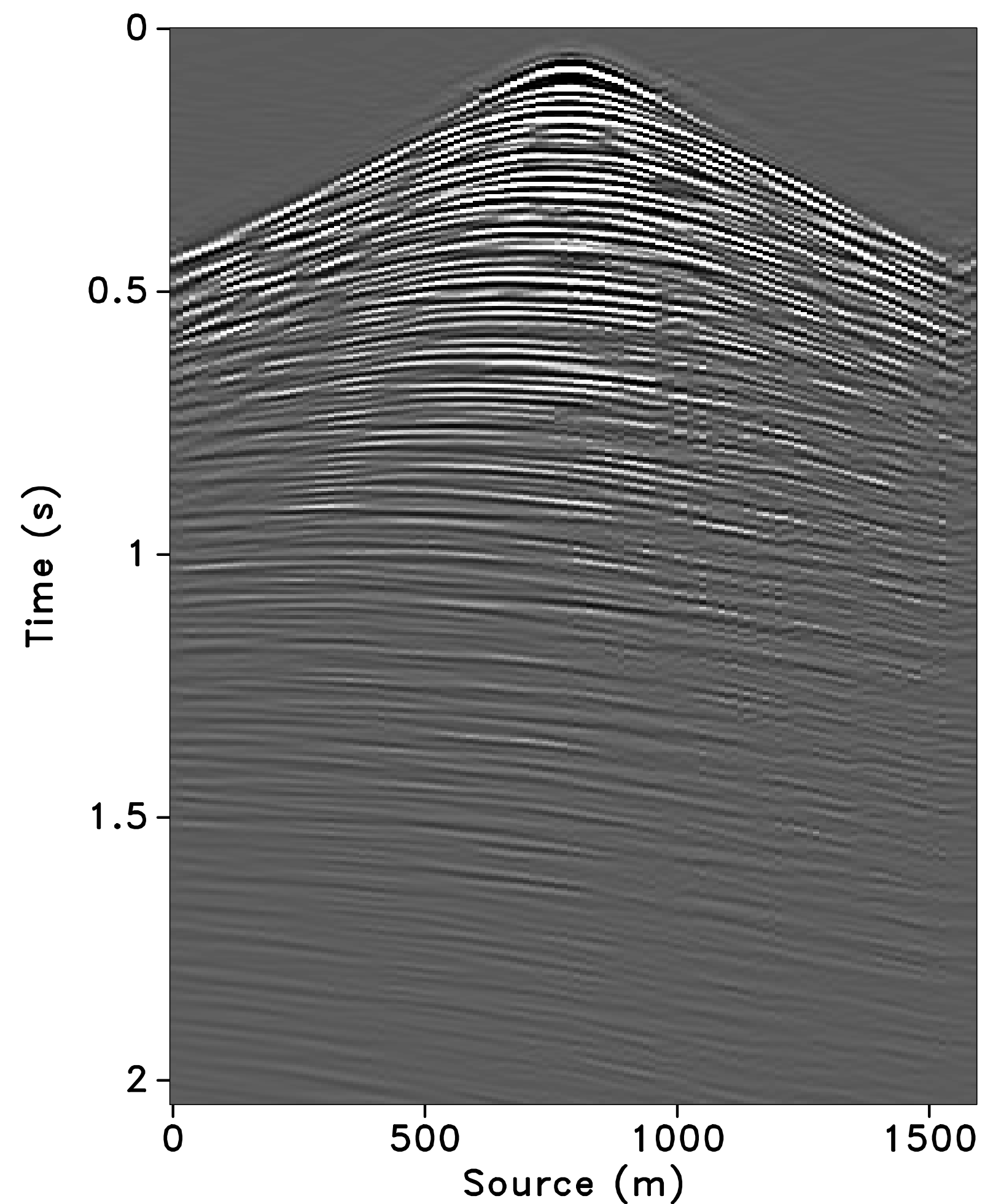




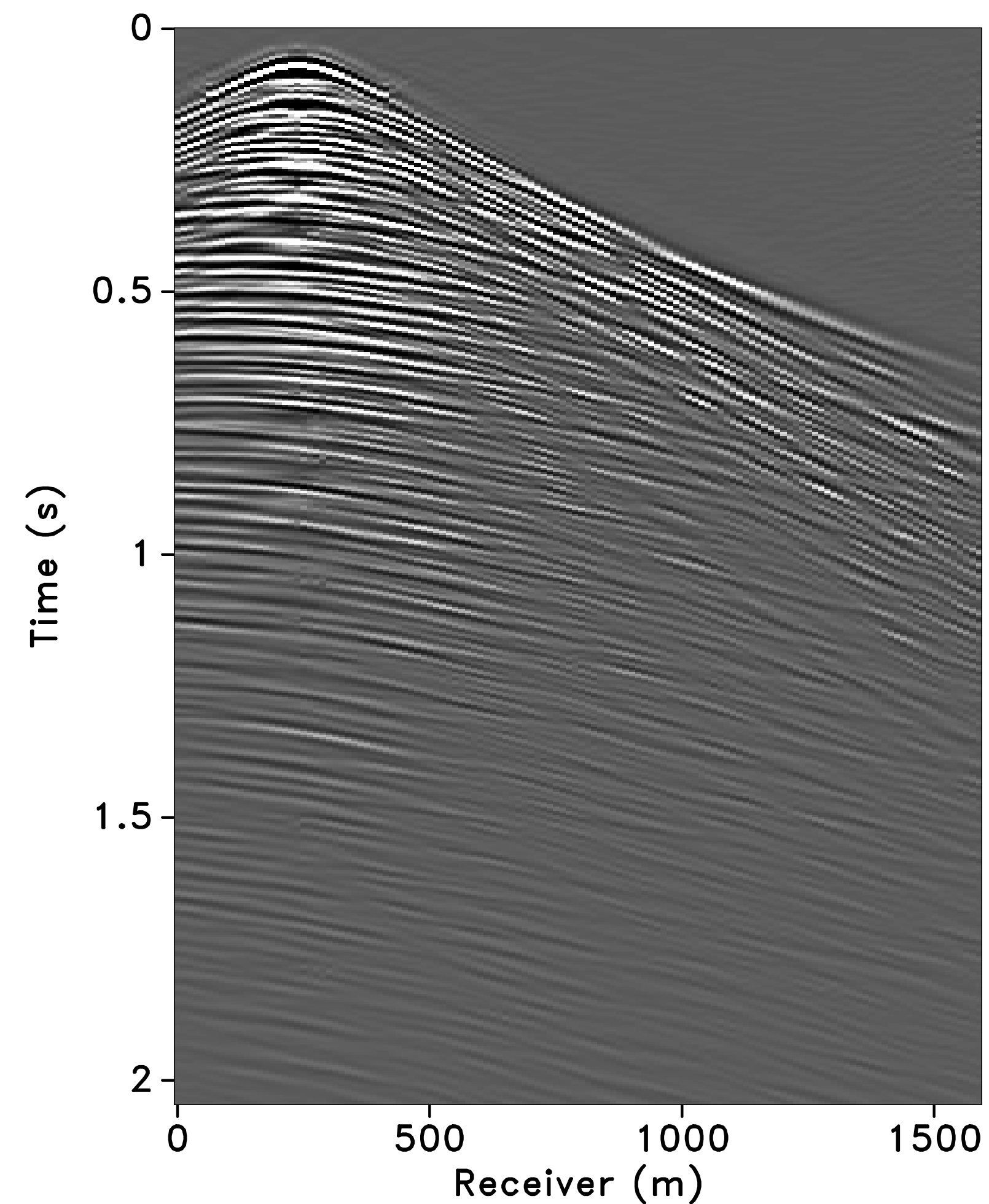
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (12.5 dB)

["deblending" + interpolation from *jittered* 50m grid to *regular* 12.5m grid]

RECEIVER GATHER



SHOT GATHER

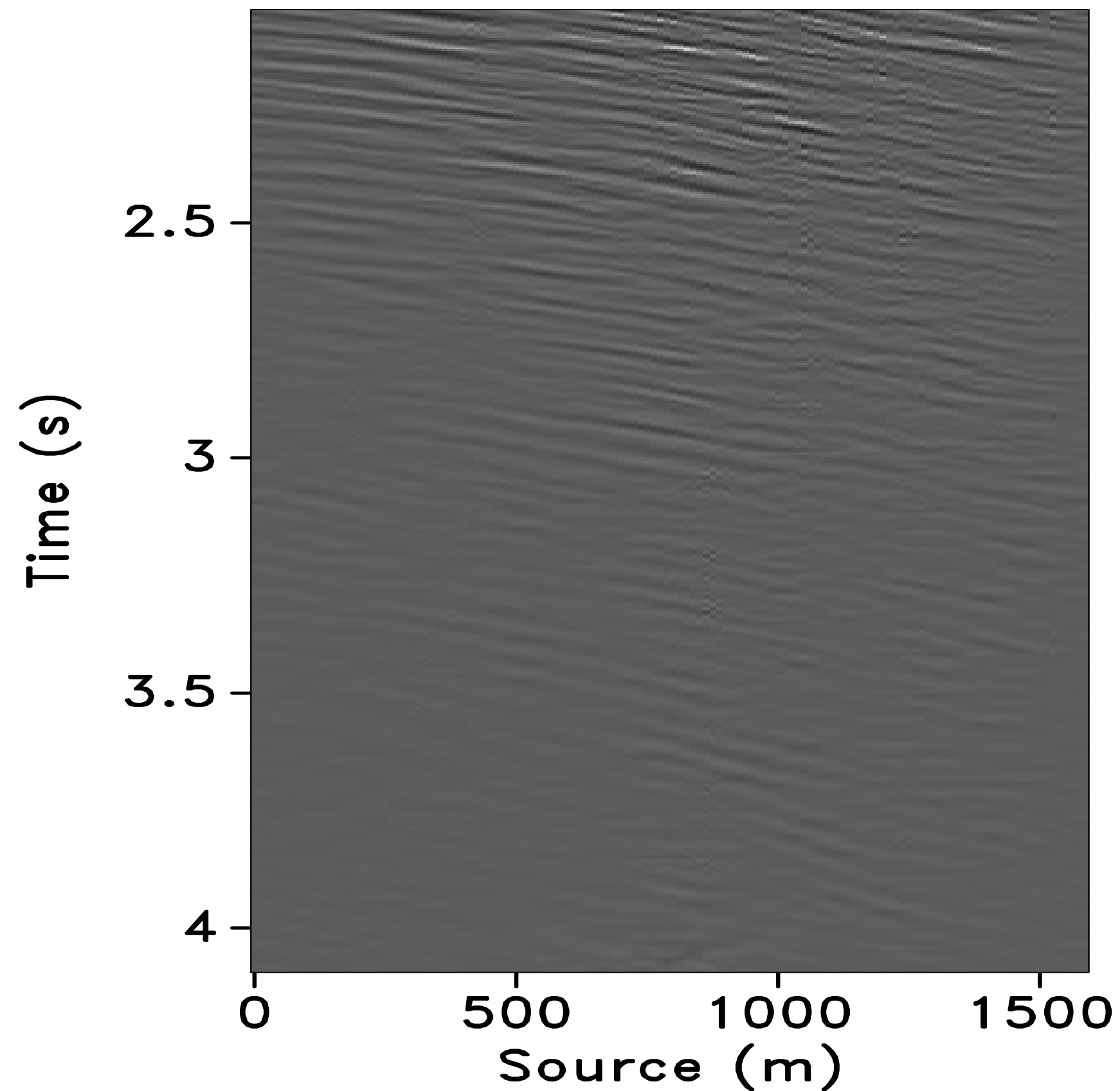




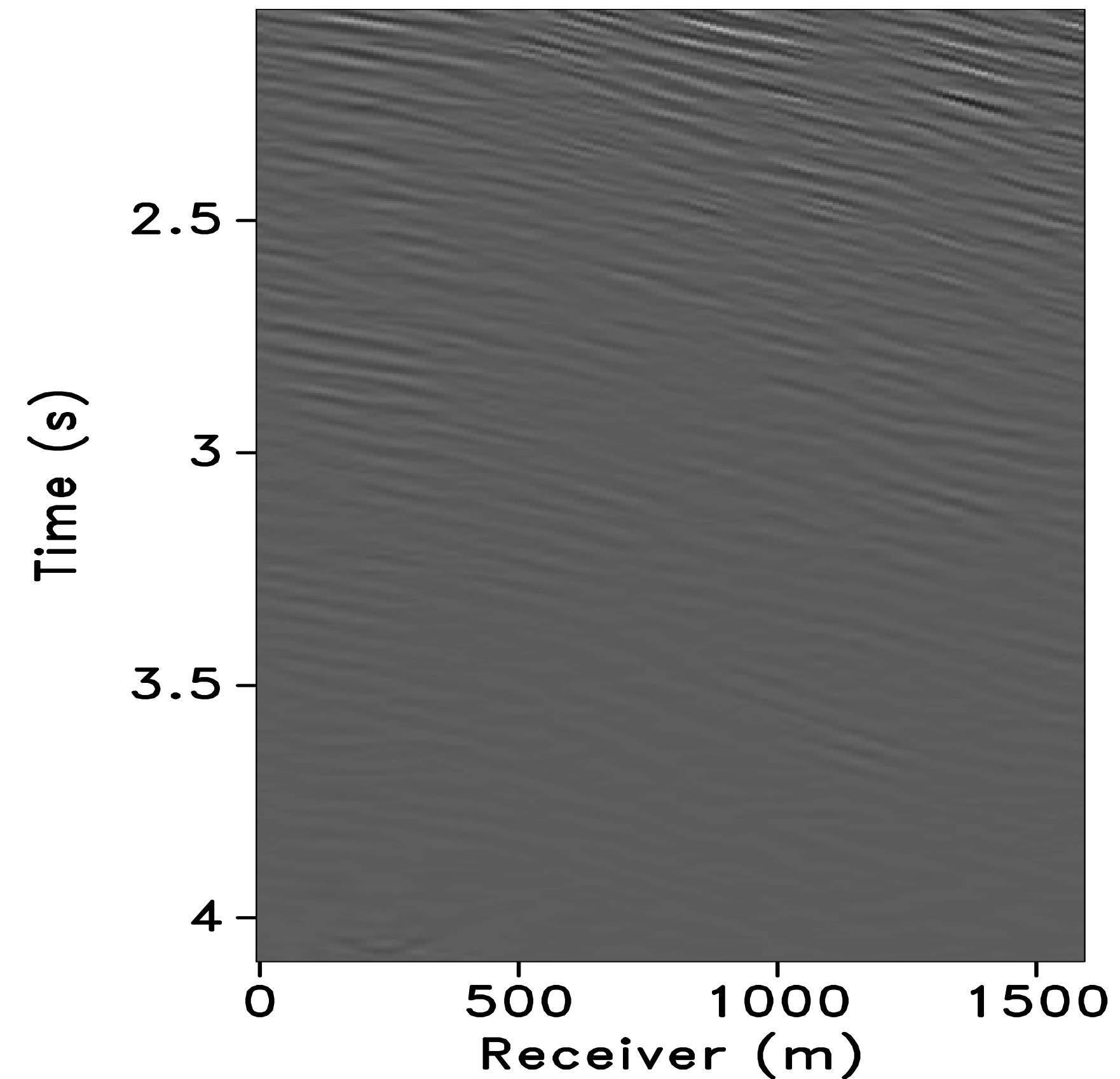
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (12.5 dB)

["deblending" + interpolation from *jittered* 50m grid to *regular* 12.5m grid]

RECEIVER GATHER



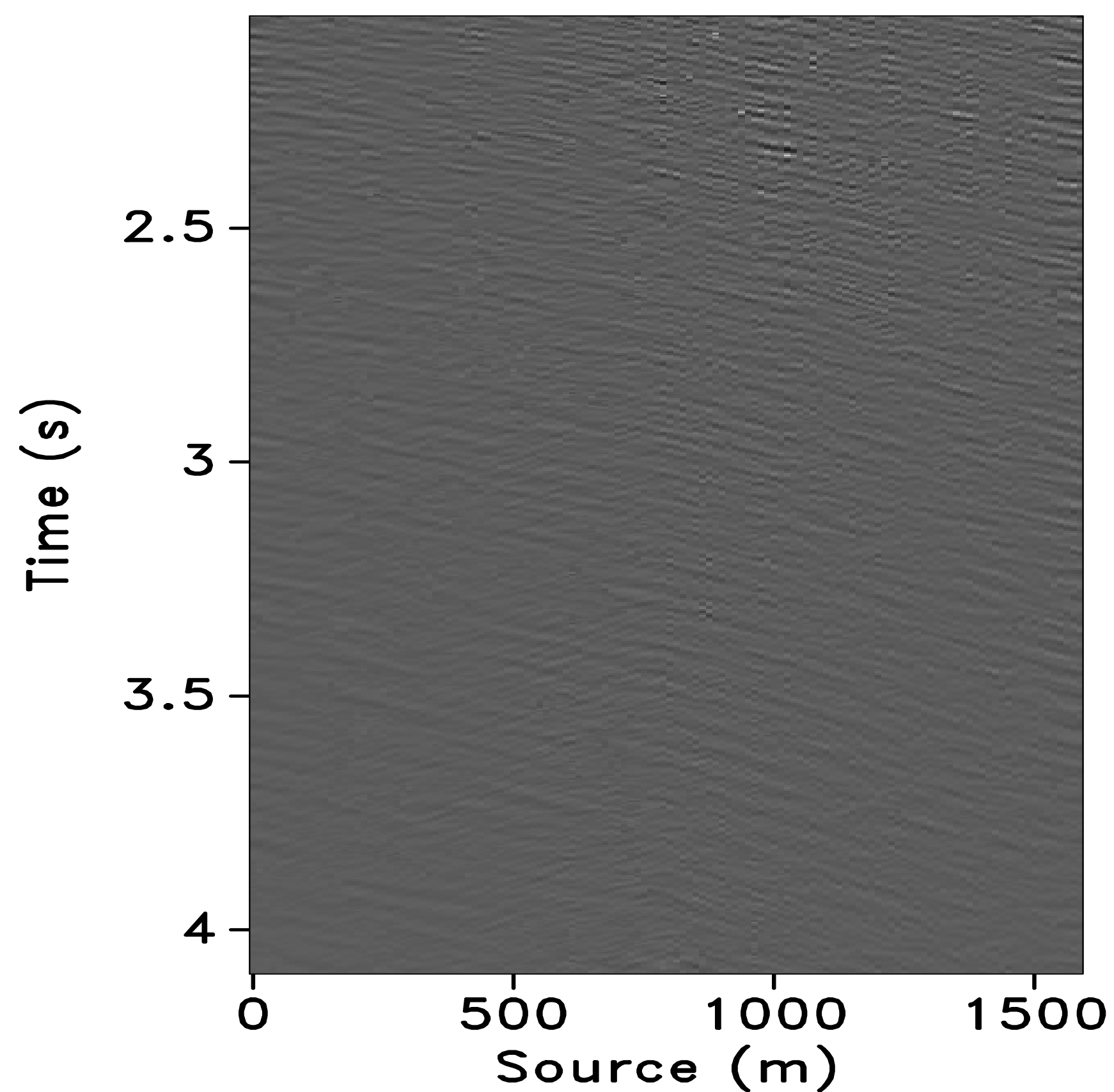
SHOT GATHER



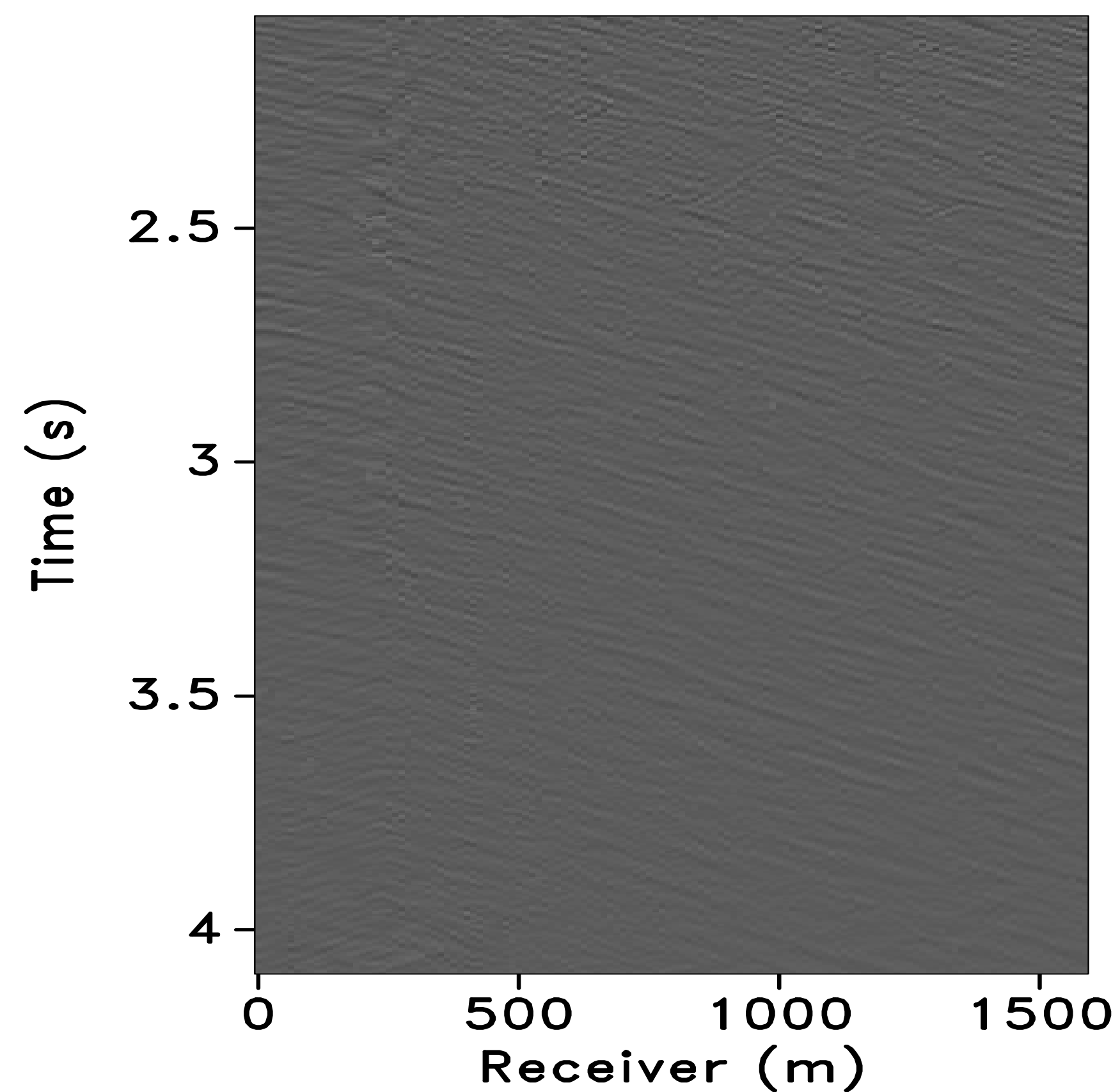
# Sparsity-promoting recovery on *irregular* grid with *NFDCT* (12.5 dB)

["deblending" + interpolation from *jittered* 50m grid to *regular* 12.5m grid] (difference)

RECEIVER GATHER



SHOT GATHER



# Performance

Improvement spatial sampling ratio (50m to 12.5m)

$$= \frac{\text{no. of spatial grid points recovered from jittered sampling via sparse recovery}}{\text{no. of spatial grid points in conventional sampling}}$$

$$= \frac{128}{64} = 2$$

# Summary

	jittered to regular (m)	recovery with <b>FDCT</b> [SNR (dB)]	recovery with <b>NFDCT</b> [SNR (dB)]
1 source vessel (2 airgun arrays)	50 to 25	14.2	17.1
	50 to 12.5	11.1	12.5
2 source vessels (2 airgun arrays per vessel)	50 to 25	19.7	21.5
	50 to 12.5	15.0	16.3



# Observations

- ▶ Larger variability in shot-times seems desirable
  - *incoherent* aliasing
  - wavenumber diversity
- ▶ *Source separation* and *interpolation* can be treated as sparse inversion problems - *together*
- ▶ With *sparsity*-promoting recovery we can
  - *deblend*, recover the wavefield
  - *regularize*, from a *jittered/irregular* to a *regular* grid
  - *interpolate*, from a *coarse jittered* (50m) grid to a *fine regular* grid (25m, 12.5m, and finer)

## Future work

- ▶ How much randomness (in shot-times) is sufficient to ensure good source separation?
- ▶ Source separation for small variability in shot-times
  - towed streamer acquisition
- ▶ Comparisons with rank minimization technique for source separation

# Acknowledgements

Thank you!



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**Donoho, D. L., 2006**, Compressed sensing: *IEEE Trans. Inform. Theory*, 52, 1289–1306.

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