

Bayesian signal separation applied to ground-roll removal

Two adaptive separation schemes
Many Problems

Carson Yarham

Introduction

- Introduction
- Adaptive Subtraction Schemes

- Sparsity
- Block Coordinate Relaxation (BCR)
- Bayesian Formulation
- Parameters

- Synthetic Example

- Data
- Benchmark Tests
- Parameter Sensitivity
- Results

- Real Data Example

- Shell Test Data

- Conclusions

- References

Adaptive Subtraction Schemes

- Block Coordinate Relaxation (BCR)
 - Introduced by Starck, Elad, Donoho 2004.
 - Modified for seismic images using curvelets to separate multiples by Herrmann, Boeniger and Verschuur, 2007.
 - Used for ground roll removal by Yarham, Boeniger and Herrmann, 2006.
- Bayesian Separation
 - Developed at SLIM by Saab, Wang, Yilmaz and Herrmann, 2007.
 - Adapted to Multiple and Ground Roll Separation.

Adaptive Subtraction Schemes

Formulate The Problem...

b Recorded Data

$$\mathbf{b} = \mathbf{s}_1 + \mathbf{s}_2 + \mathbf{n}$$

s₁ Signal 1 (**Reflectors**)

N = 2 Signals

s₂ Signal 2 (**Surface Wave**)

$$\mathbf{s}_i = \mathbf{A}_i \mathbf{x}_i + \mathbf{n}_i \quad i \dots N$$

A_i Sparsity Promoting Transform

b₁ Predicted Reflectors

$$\mathbf{b} = \mathbf{b}_1 + \mathbf{b}_2$$

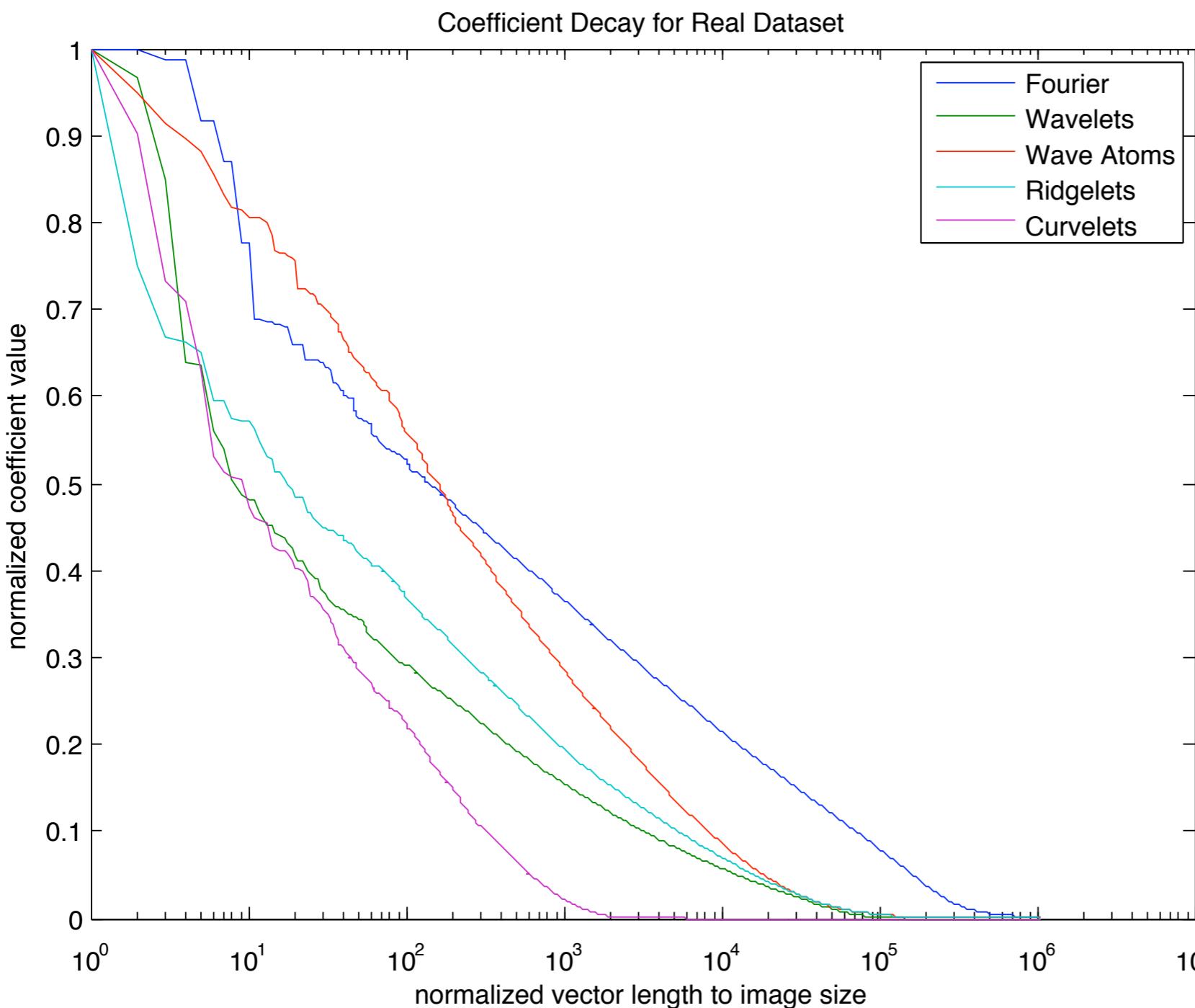
b₂ Predicted Surface Wave

Adaptive Subtraction Schemes

Sparsity

A

Sparsity Promoting Transform



Curvelets are the most sparse representation of seismic data.

How do we take advantage of this?

We apply weights to the thresholds that define the 1-norm minimization

Adaptive Subtraction Schemes

Block Coordinate Relaxation

$$\min_x \|x\|_{\mathbf{w},1} \quad \text{subject to} \quad \|\mathbf{b} - \mathbf{Ax}\|_2 \leq \epsilon$$
$$\hat{\mathbf{b}}_1 = \mathbf{A}_i \hat{\mathbf{x}}_i \quad i \dots N$$

given: \mathbf{b}_1 and $\mathbf{w}(\mathbf{b}, \mathbf{b}_1)$

$$\hat{\mathbf{x}}_j = \arg \min_{\mathbf{x}_j} \frac{1}{2} \|\mathbf{b} - \mathbf{A}_j \mathbf{x}_j - \sum_{i \neq j} \mathbf{A}_i \mathbf{x}_i\|_2^2 + \|\mathbf{x}_j\|_{1,\gamma \cdot \mathbf{w}_j}$$

Algorithm derived in paper:

Nonlinear primary-multiple separation with directional curvelet frames
F. J. Herrmann and U. Boeniger and D. J. Verschuur, 2007

Adaptive Subtraction Schemes

Bayesian Formulation

n Recorded Noise

n₁ Reflector Prediction Noise

$$\mathbf{n} = \mathbf{n}_1 + \mathbf{n}_2 \quad N(0, \sigma_2^2)$$

Rewrite surface wave and reflectors as:

$$\mathbf{b}_2 = \mathbf{Ax}_2 + \mathbf{n}_2$$

$$\mathbf{b}_1 = \mathbf{Ax}_1 + \mathbf{n} - \mathbf{n}_2$$

Adaptive Subtraction Schemes

Bayesian Formulation

We need to find the curvelet vectors that maximize
the posterior probability

$$P(\mathbf{x}_1, \mathbf{x}_2 | \mathbf{b}_1, \mathbf{b}_2) = \frac{P(\mathbf{x}_1, \mathbf{x}_2) P(\mathbf{b}_1 | \mathbf{x}_1, \mathbf{x}_2) P(\mathbf{b}_2 | \mathbf{b}_1, \mathbf{x}_1, \mathbf{x}_2)}{P(\mathbf{b}_1, \mathbf{b}_2)}$$

We have independent and identically distributed white gaussian noise distributions with a priori information in the form of predictions

$$\arg \max_{x_1, x_2} P(x_1, x_2 | b_1, b_2) = \arg \min_{x_1, x_2} f(x_1, x_2)$$

Adaptive Subtraction Schemes

Bayesian Formulation

Minimize the function:

$$f(\mathbf{x}_1, \mathbf{x}_2) = \lambda_1 \|\mathbf{x}_1\|_{1, \mathbf{w}_1} + \lambda_2 \|\mathbf{x}_2\|_{1, \mathbf{w}_2} \\ + \|\mathbf{A}\mathbf{x}_2 - \mathbf{b}_2\|_2^2 + \eta \|\mathbf{A}(\mathbf{x}_1 + \mathbf{x}_2) - \mathbf{b}\|_2^2$$

Algorithm is derived in technical report:

Bayesian wavefield separation by transform-domain sparsity promotion
Deli Wang, Rayan Saab, Ozgur Yilmaz and Felix J. Herrmann, 2008

η

Confidence parameter

λ_1

Reflector expected sparsity parameter

λ_2

Surface wave expected sparsity parameter

Adaptive Subtraction Schemes

Parameters

Block Coordinate Relaxation:

c_1 Reflector 1-norm minimization threshold decay rate

c_2 Surface wave 1-norm minimization threshold decay rate

Bayesian Formulation:

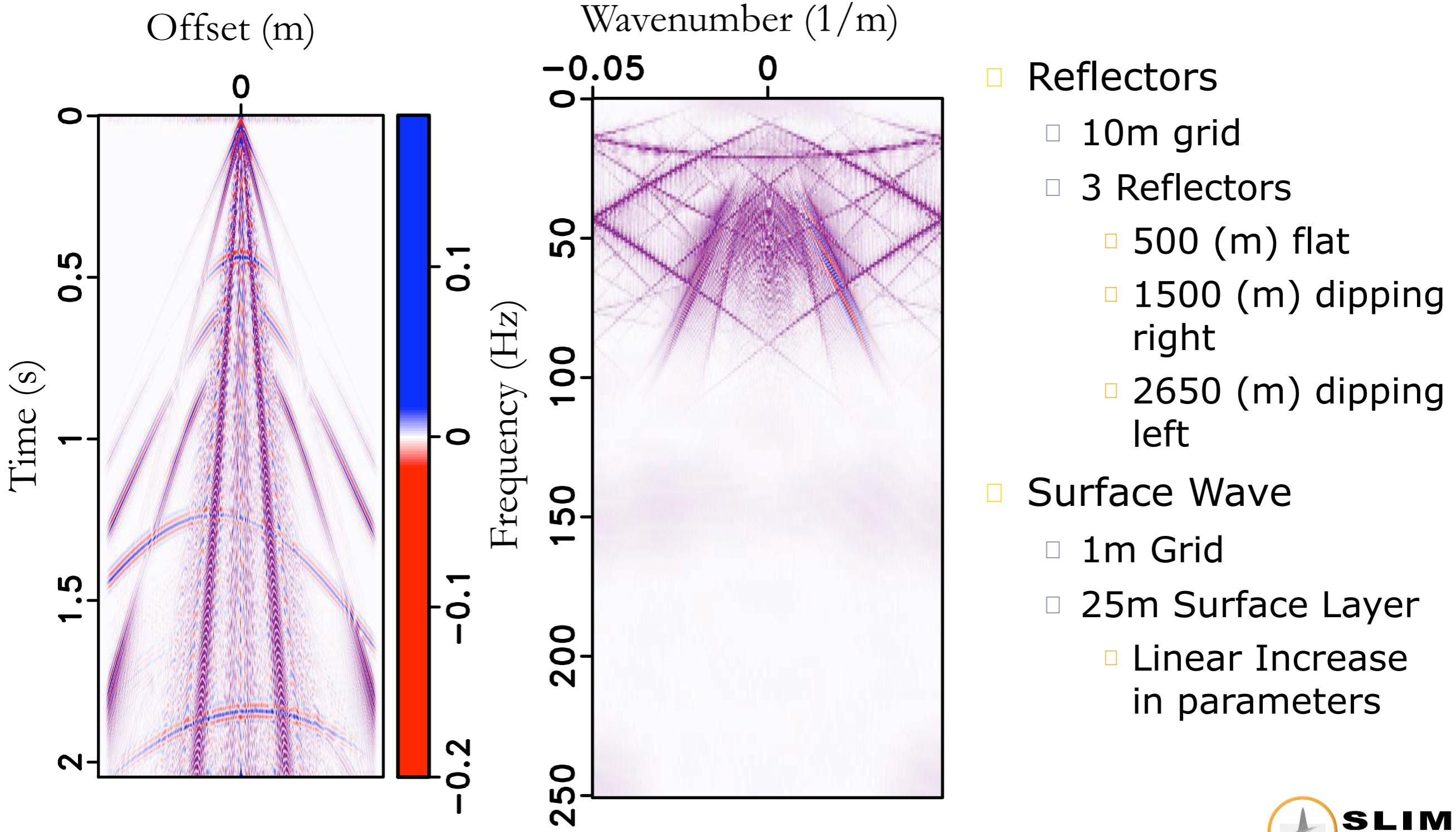
η Confidence parameter

λ_1 Reflector expected sparsity parameter

λ_2 Surface wave expected sparsity parameter

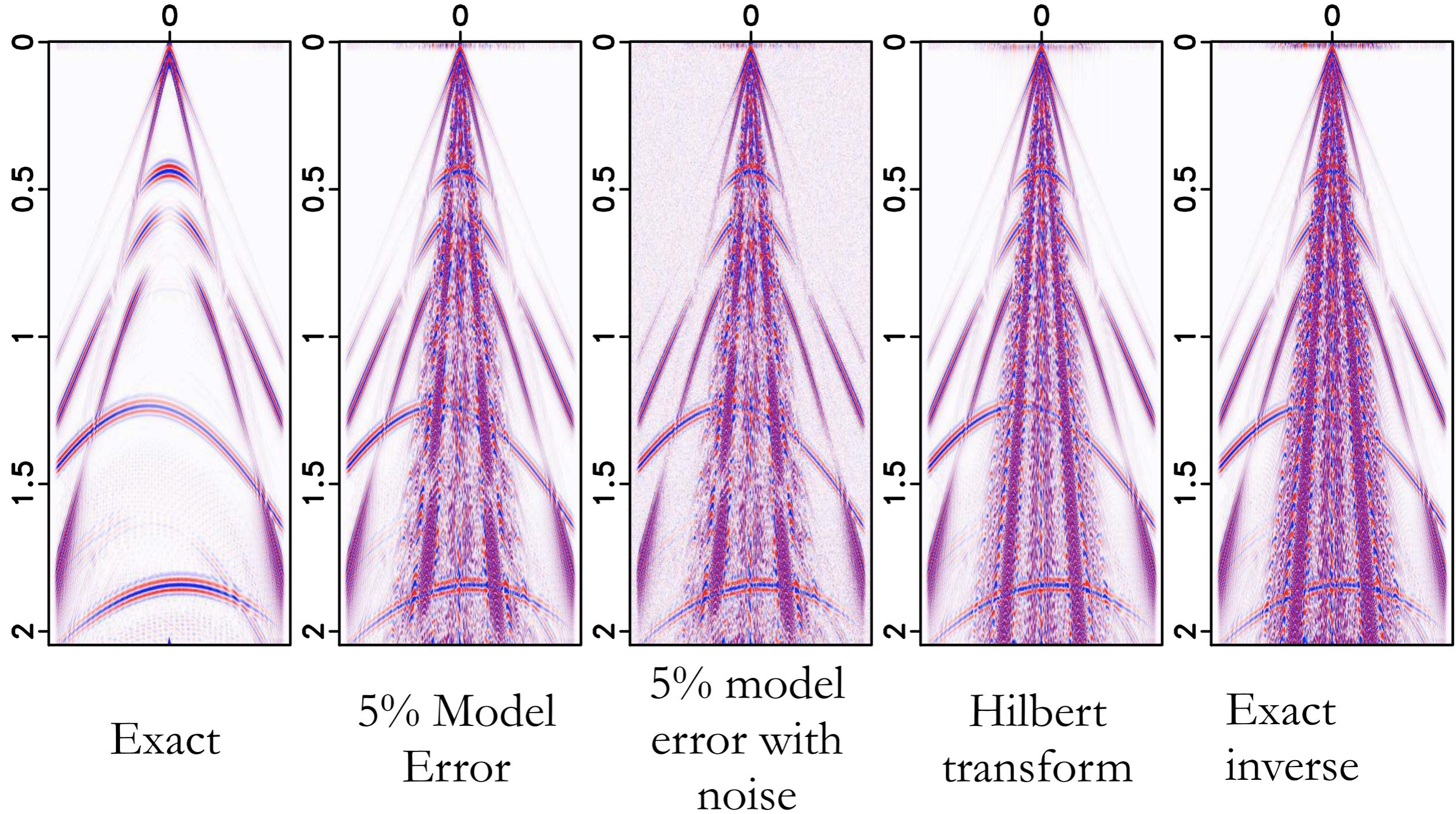
Synthetic Example

Data - Elastic Finite Difference



Synthetic Example

Benchmark Tests - Predictions



Synthetic Example

Benchmark Tests - Results

Noise Prediction	Initial SNR	Subtraction	Bayesian	Block Coordinate Relaxation
Exact Noise	-1.673	147.960	17.922	15.504
5% Model Error	-1.673	-4.377	9.592	9.424
5% Model Error + Noise	-1.923	-4.515	9.470	3.528
Hilbert Transform	-1.673	-4.670	13.103	13.331
Phase Inverse	-1.673	-7.694	14.083	13.099

Synthetic Example

Parameter Sensitivity - Bayesian Solver

SNR (dB)	$0.1 \cdot (\lambda_1^*, \lambda_2^*)$	$2 \cdot \lambda_1^*, \lambda_2^*$	λ_1^*, λ_2^*	$\lambda_1^*, 2 \cdot \lambda_2^*$	$10 \cdot (\lambda_1^*, \lambda_2^*)$
$0.1 \cdot \eta^*$	8.349	3.331	4.457	4.458	1.558
$0.5 \cdot \eta^*$	1.860	5.828	8.875	9.001	3.332
η^*	1.758	6.925	9.592	9.023	4.454
$2 \cdot \eta^*$	-3.899	6.479	1.266	2.782	5.974
$10 \cdot \eta^*$	-4.280	-2.561	-3.384	-3.180	8.052

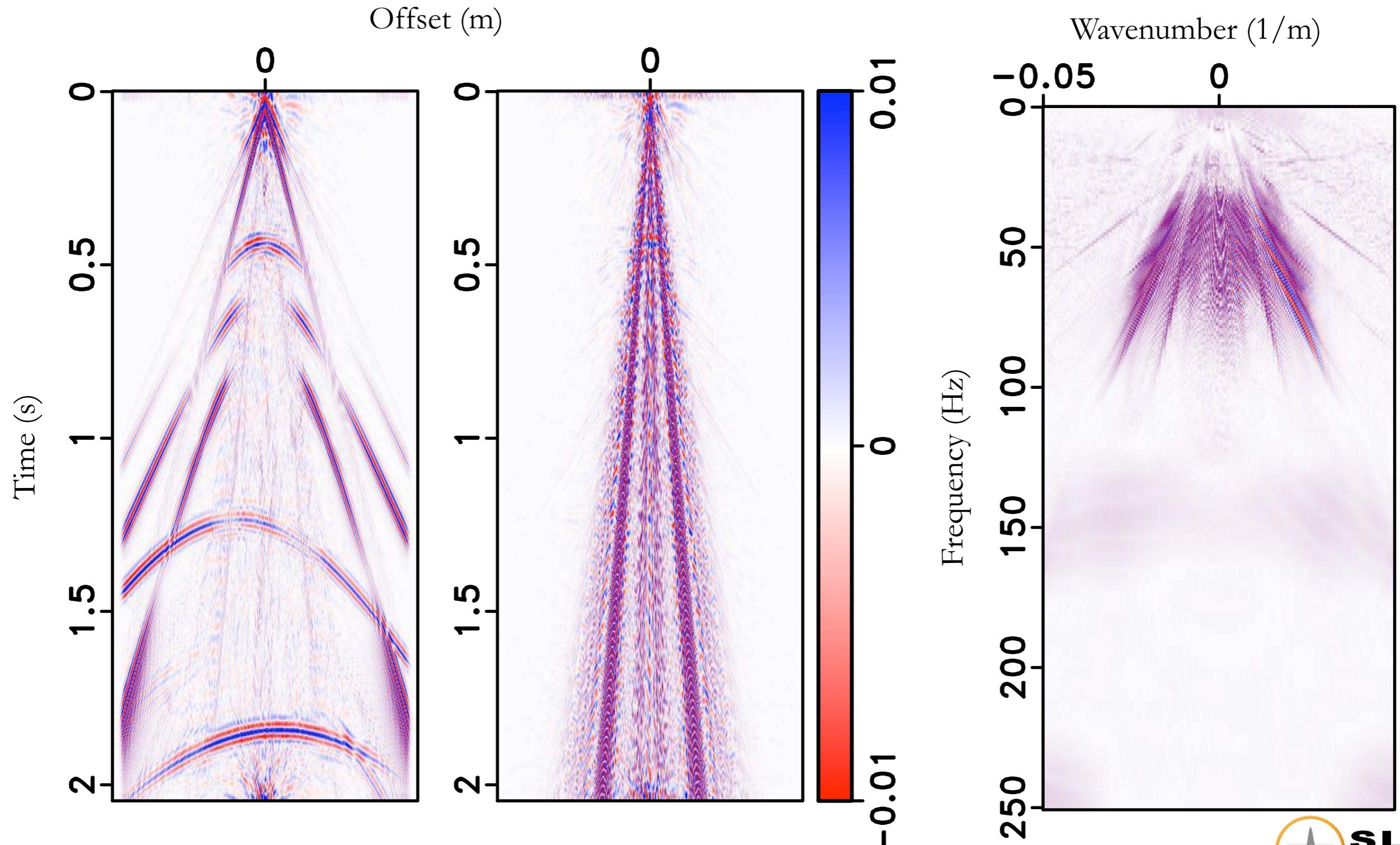
Synthetic Example

Parameter Sensitivity - BCR Solver

SNR (dB)	$0.1 \cdot c_1^*$	$0.5 \cdot c_1^*$	c_1^*	$2 \cdot c_1^*$	$10 \cdot c_1^*$
$0.1 \cdot c_2^*$	6.242	0.353	2.995	-1.566	-1.672
$0.5 \cdot c_2^*$	4.085	8.829	0.618	-1.348	-1.659
c_2^*	2.995	5.011	9.414	-0.556	-1.240
$2 \cdot c_2^*$	1.658	2.468	4.021	7.846	8.420
$10 \cdot c_2^*$	0.002	0.005	0.121	0.145	0.211

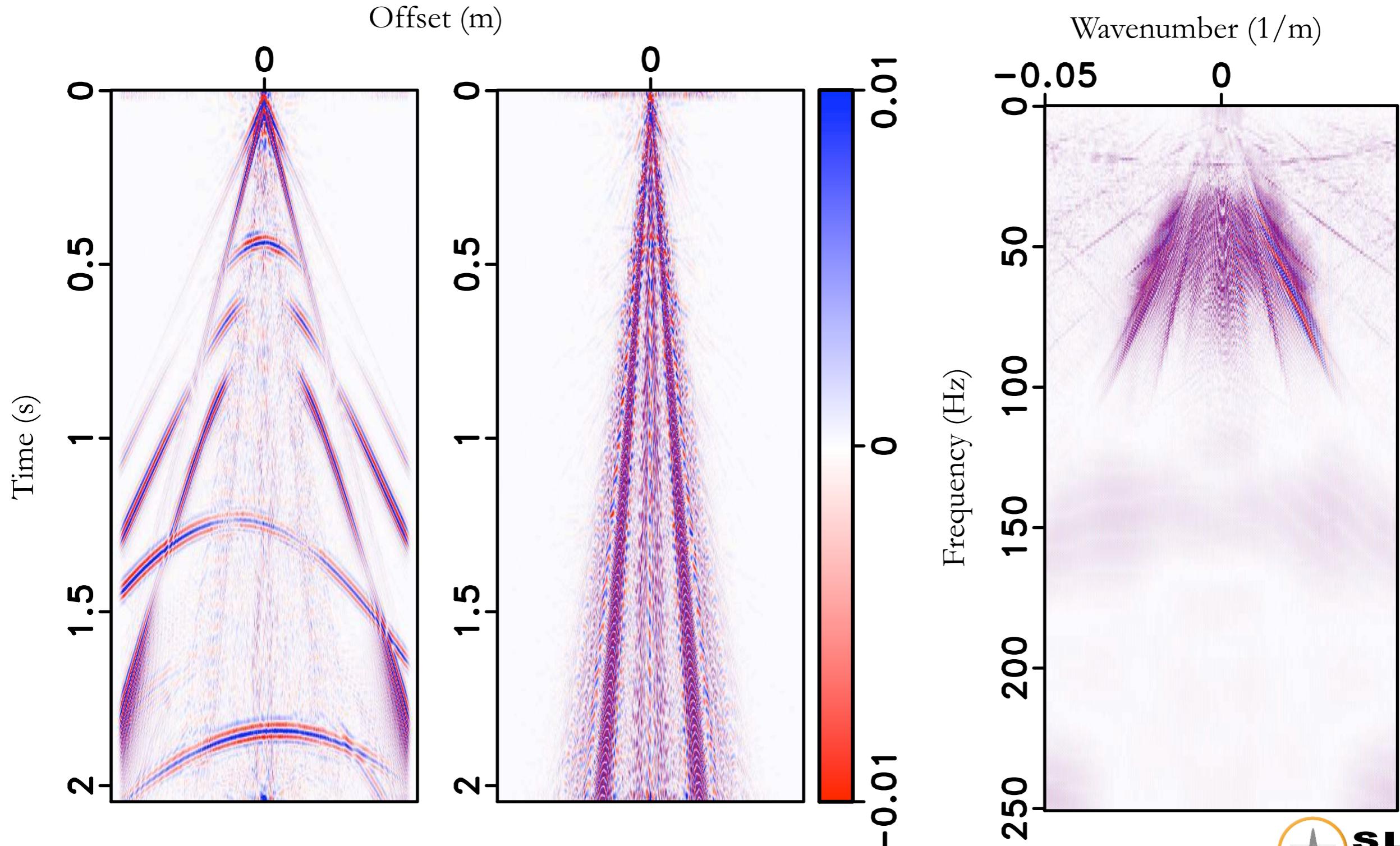
Synthetic Example

Results - Block Coordinate Relaxation



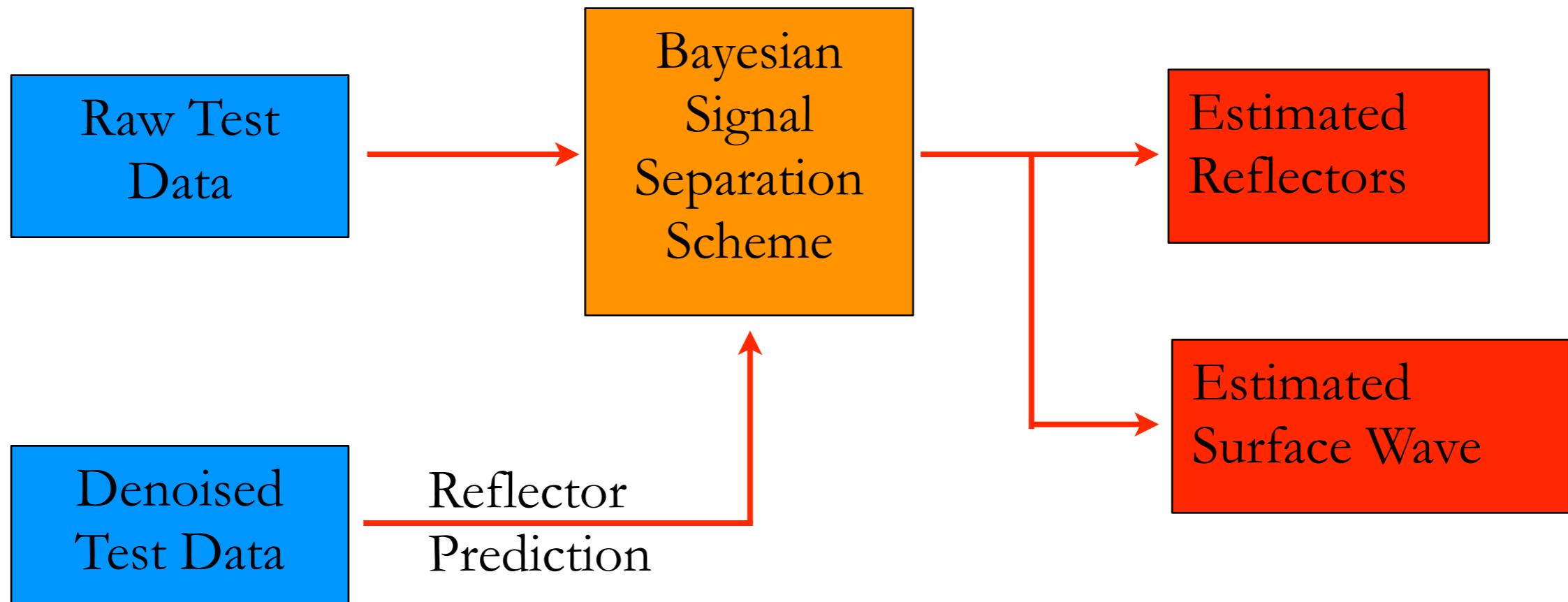
Synthetic Example

Results - Bayesian Formulation



Real Data Example

Shell Test Data



η

Prediction Confidence Parameter - Set to 2.0

λ_1

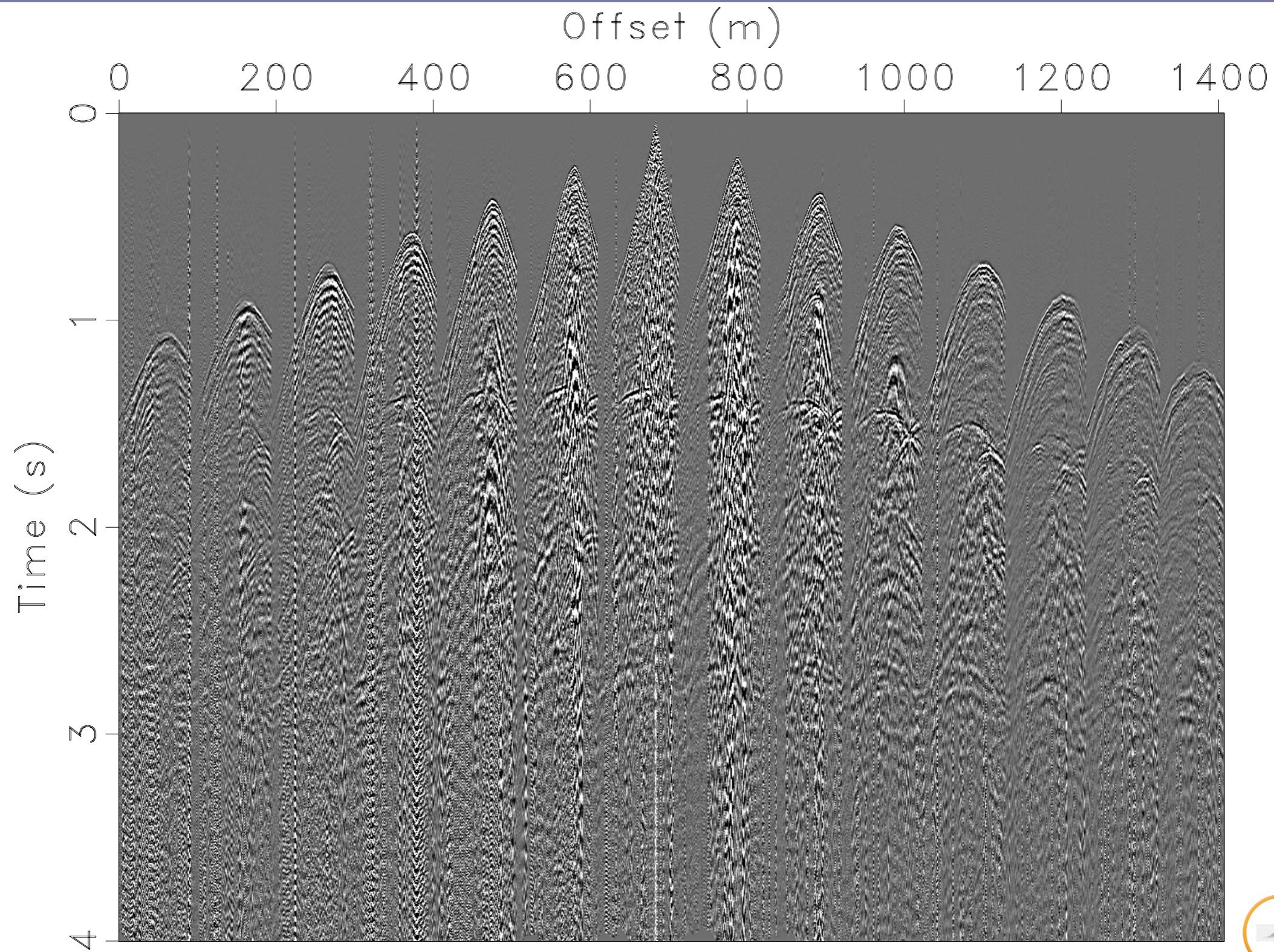
Reflector Sparsity Parameter - Set to 1.0

λ_2

Surface Wave Sparsity Parameter - Set to 1.0

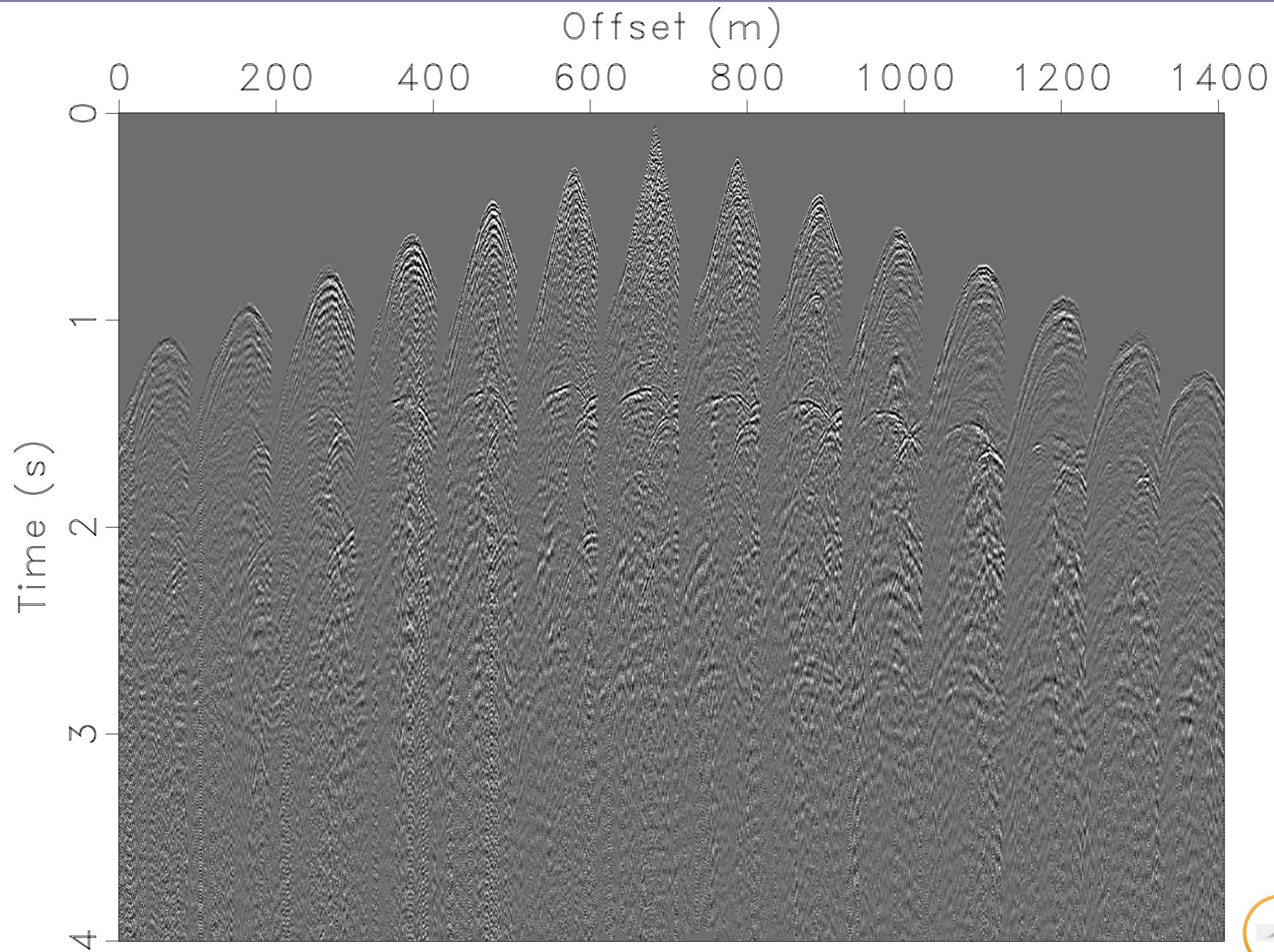
Real Data Example

Shell Test Data



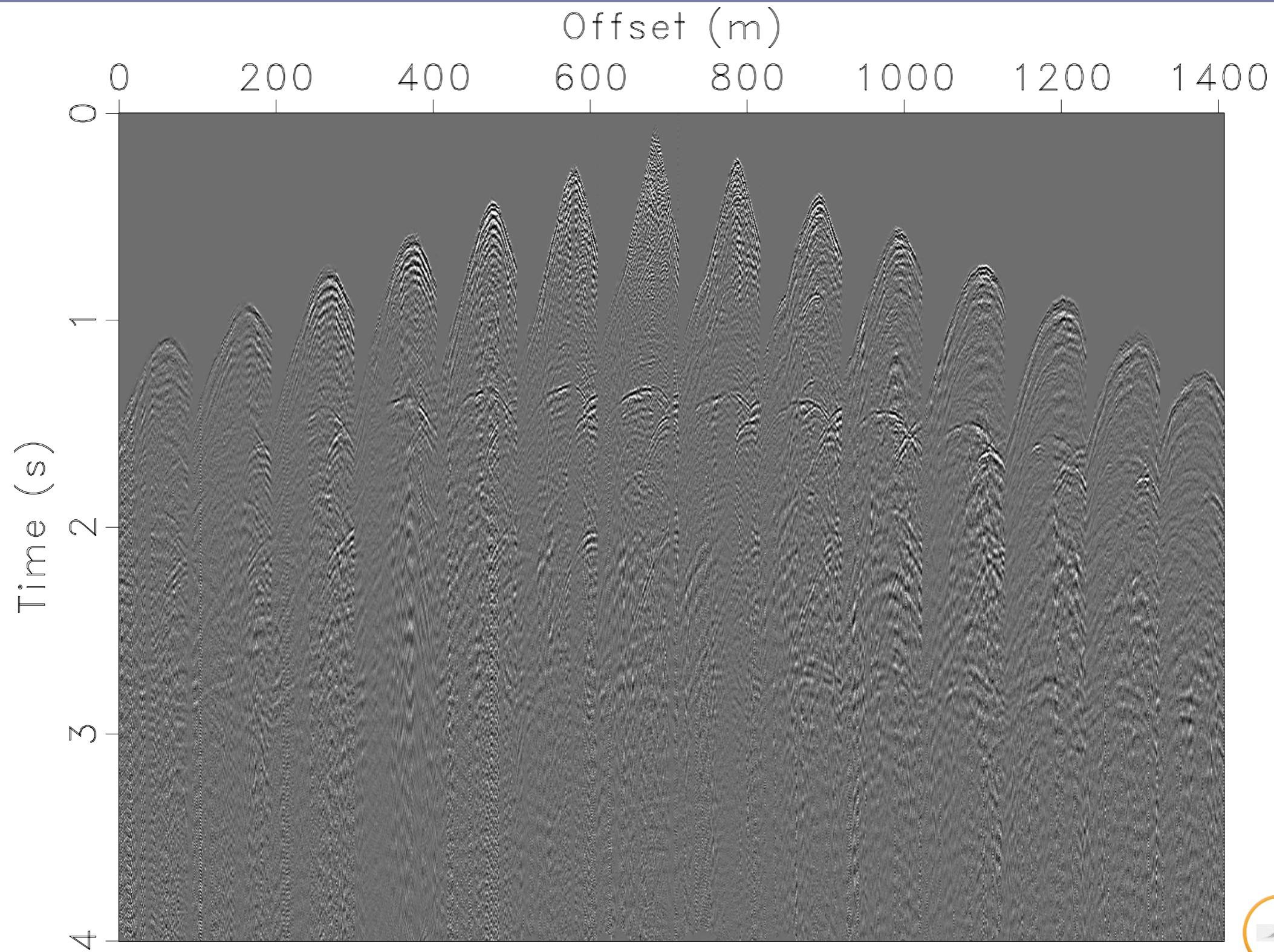
Real Data Example

Provided Reflectors



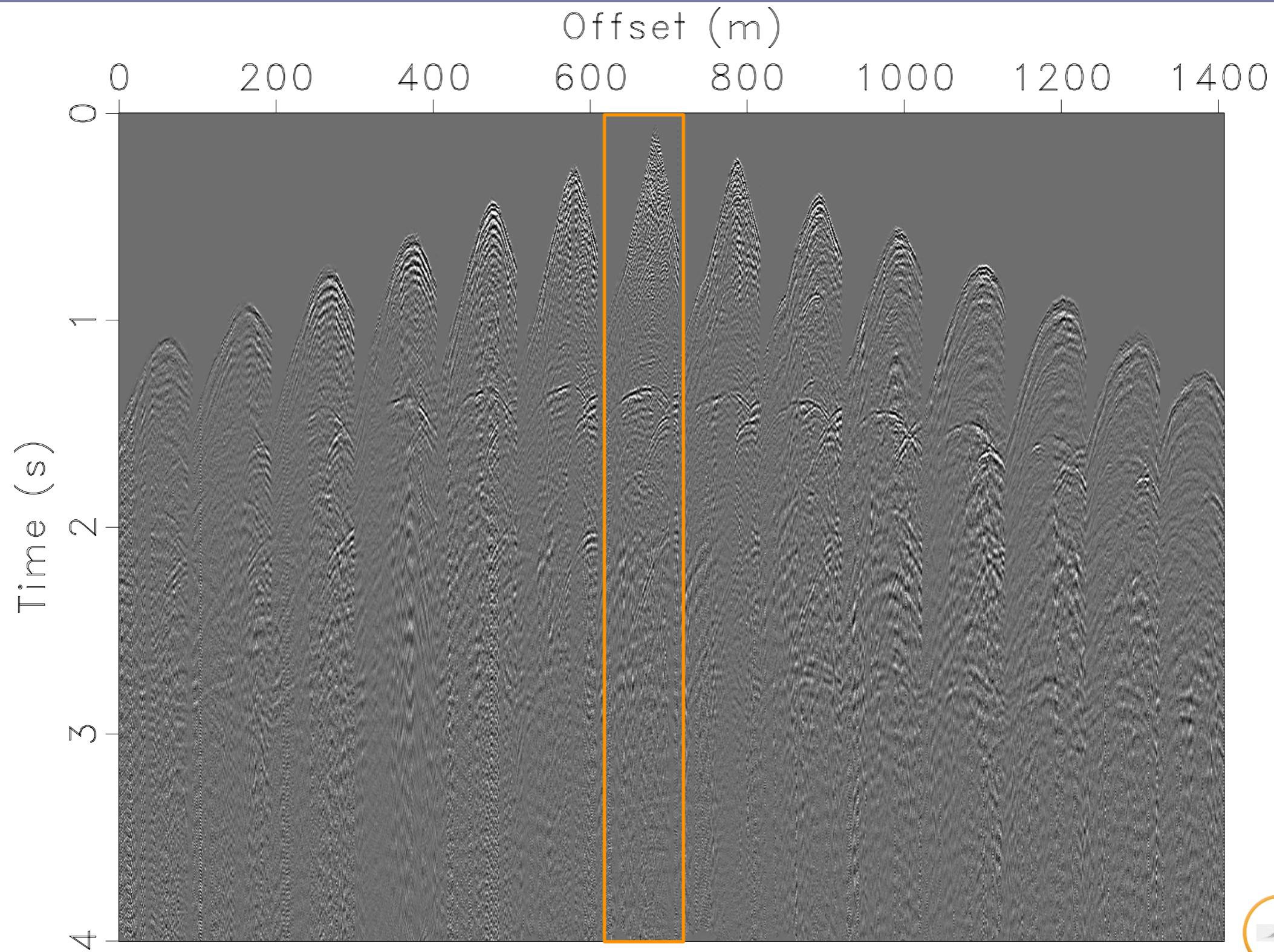
Real Data Example

Estimated Reflectors



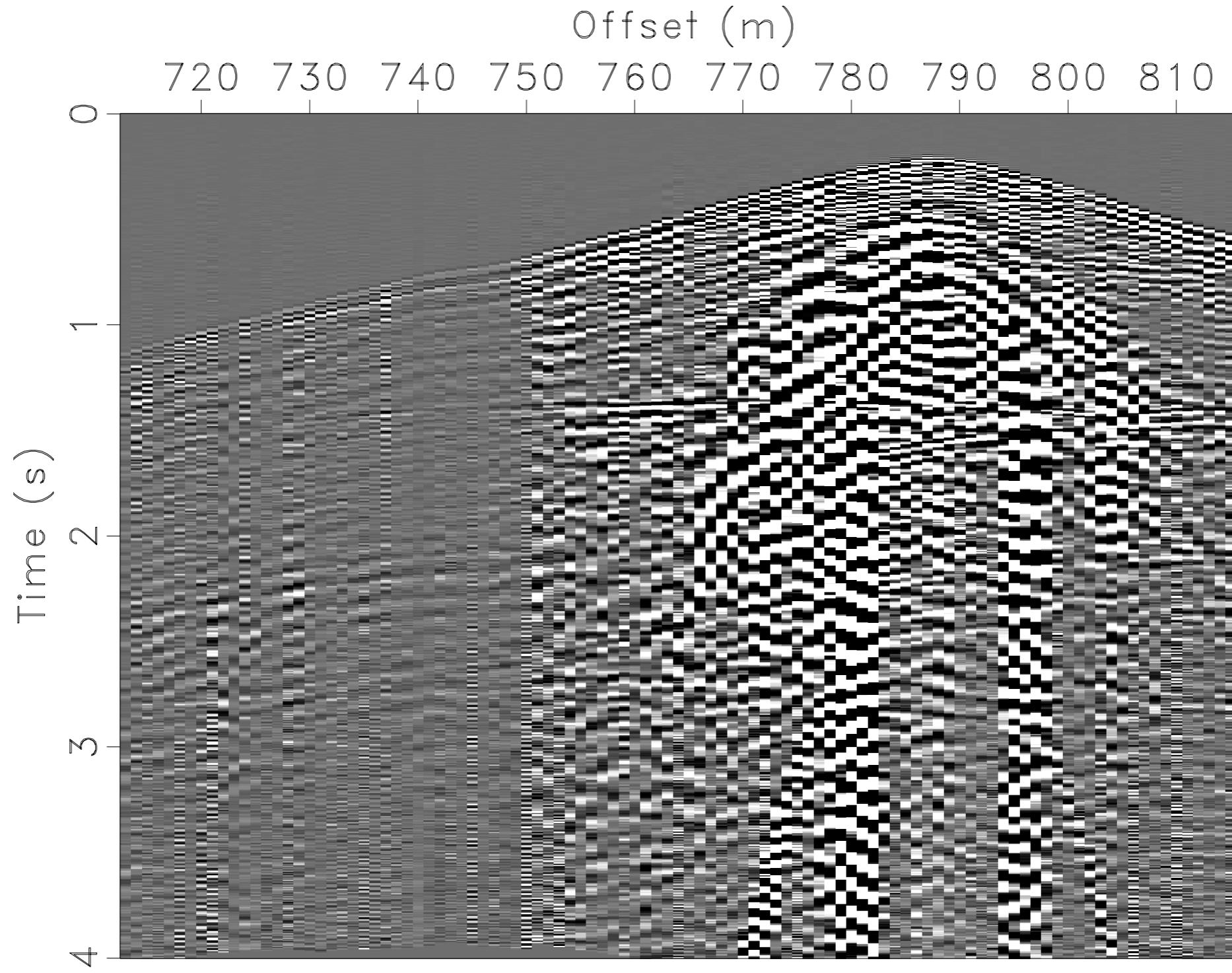
Real Data Example

Estimated Reflectors



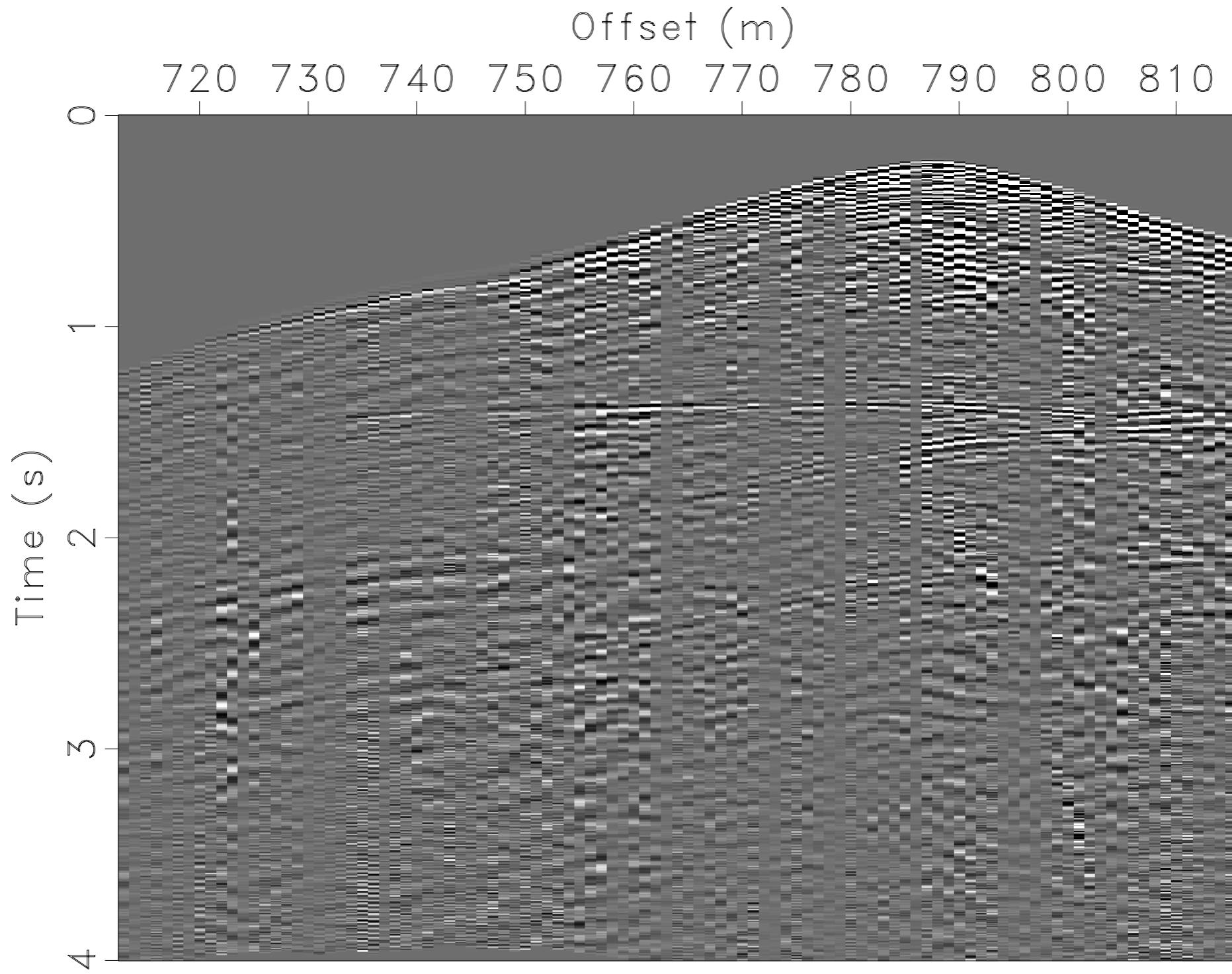
Real Data Example

Raw Data



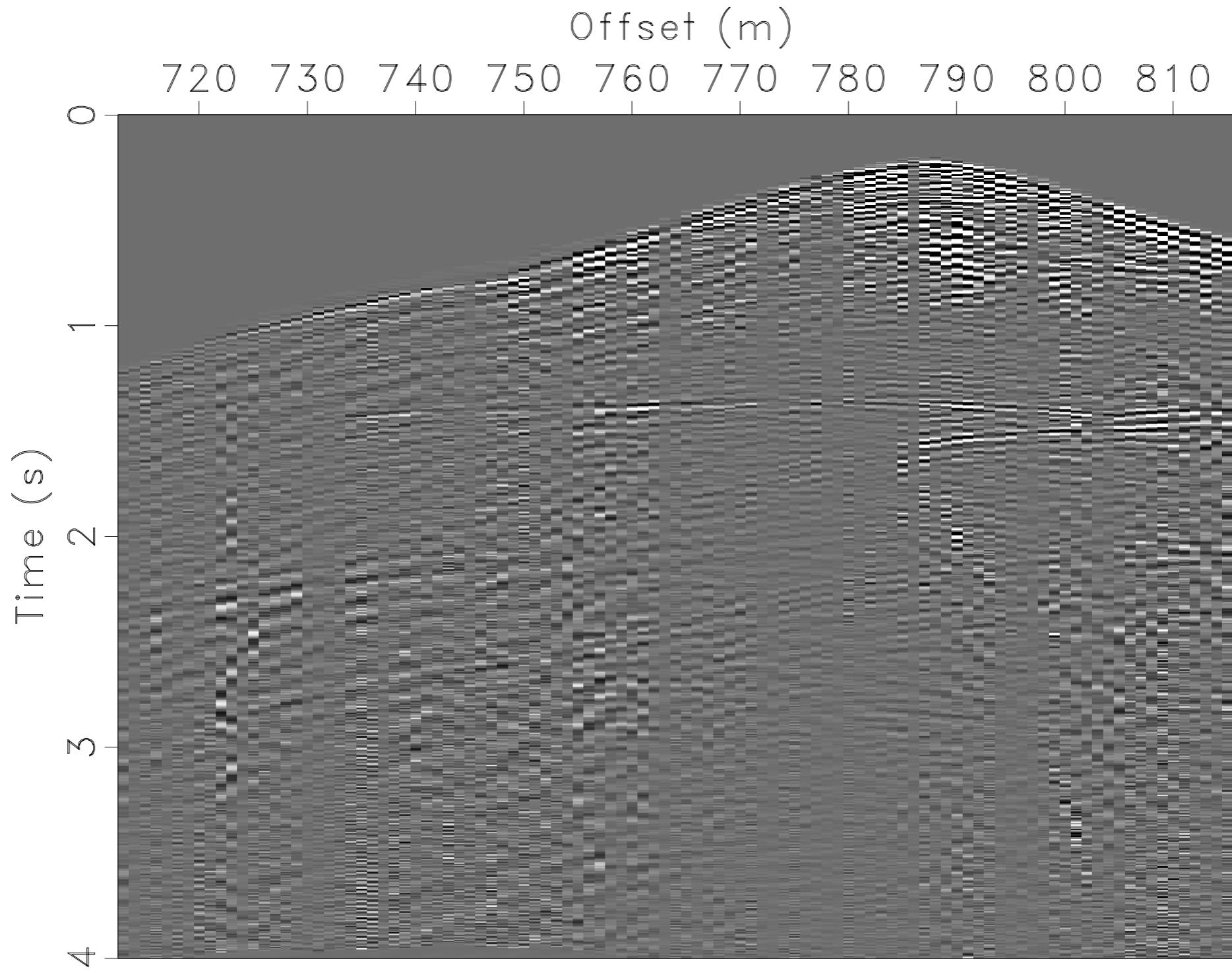
Real Data Example

Provided Reflectors



Real Data Example

Estimated Reflectors



Conclusions

- Two signal separation schemes for surface wave removal
 - Block coordinate relaxation
 - More sensitive parameters
 - Might degrade small amount of reflector information
 - Bayesian Formulation
 - Less sensitive
 - More control over separation
 - Less effect on reflector information than block coordinate relaxation scheme
- Both methods effective on synthetic data.
- Bayesian method shown on real data.
- SLIMpy user demos now contains a demo with the synthetic example and an example with the Oz25 data set.
- Future Work:
 - Full 3D data
 - Interferometric Predictions.

Acknowledgments

SLIM team members

S. Ross Ross, H. Modzelewski, and C. Brown for SLIMpy
(slim.eos.ubc.ca/SLIMpy)

Shell Canada for the real datasets

E. J. Candès, L. Demanet, D. L. Donoho, and L. Ying for CurveLab (www.curvelet.org)

S. Fomel, P. Sava, and the other developers of Madagascar (rsf.sourceforge.net)

This presentation was carried out as part of the SINBAD project with financial support, secured through ITF, from the following organizations: BG, BP, Chevron, ExxonMobil, and Shell. SINBAD is part of the collaborative research & development (CRD) grant number 334810-05 funded by the Natural Science and Engineering Research Council (NSERC).

References

- Saab, R., Wang, D., Yilmaz, O., Herrmann, F. 2007, Curvelet-based primary-multiple separation from a Bayesian perspective, SEG International Exposition and 77th Annual Meeting
- Londono, E., Lopez, L. and Kazmierczak, T., 2005, Using the karhunen-loeve transform to suppress ground roll in seismic data. *Earth Sci. Res. J.*, 9, 139-147
- Graves, R., 1996, Simulating seismic wave propagation in 3D elastic media using staggered-grid finite differences. *Bulletin of the Seismological Society of America*, 86, 1091-1106
- McMechan G.A. and Yedlin, M.J., 1981, Analysis of dispersive waves by wavefield transformations. *Geophysics*, 46, 869-874
- McKay, A.E., 1954, Review of pattern shooting. *Geophysics*, 19, 420-437
- Holzman, M., 1963, Chebysev optimized geophone arrays. *Geophysics*, 28, 145-155
- Coruh, C., Costain, J.K., 1983, Noise attenuation by Vibroseis whitening (VSW) processing. *Geophysics*, 48, 543-554
- Yilmaz, O., 2001, *Seismic Data Analysis*. Society of Exploration Geophysicists, Tulsa, USA.
- Galbraith, J. N., Wiggins, R. A., 1968, Characteristics of optimum multichannel stacking filters. *Geophysics*, 33, 36-48
- Embree, P., Burg, J. P., Backus, M. M., 1963, Wide band velocity filtering-the pie-slice process. *Geophysics*, 28, 948-974
- Fail, J. P., Grau, G., 1963. Les filters on eventail. *Geophys. Prospect.*, 11, 131-163
- Curtis, A., Gerstoft, P., Sato, H., Snieder, R., Wapenaar, K., 2006, Seismic interferometry - turning noise into signal. *The Leading Edge*, 25, 1082-1092

References

- Liu, X., 1999, Ground roll suppression using the Karhuren-Loeve transform. *Geophysics*, 64, 564-566
- Deighan, A., Watts, D., 1997, Ground-roll suppression using the wavelet transform. *Geophysics*, 62, 1896-1903
- Candès, E., Demanet, L., Donoho, D., and Ying, L., 2005, Fast discrete curvelet transforms. *Multiscale Model. Simul.*, 5 861-899.
- Candès, E., Romberg, J., and Tao, T., 2005, Stable signal recovery from incomplete and inaccurate measurements. *Comm. Pure Appl. Math.*, 59 1207-1223.
- Starck, J. L., Candès, E., and Donoho, D., 2000, The curvelet transform for image denoising. *IEEE Transactions on Image Processing*, 11 670--684.
- Donoho, D., Elad, M., and Temlyakov, V., 2006, Stable recovery of sparse overcomplete representations in the presence of noise. *IEEE Trans. Inform. Theory*. 52, 6-18
- Elad, M., Starck, J.L., Querre, P., and D.L. Donoho, D., Simultaneous Cartoon and Texture Image Inpainting Using Morphological Component Analysis (MCA), *Journal on Applied and Computational Harmonic Analysis*, Vol. 19, pp. 340-358, November 2005.
- Mallat, S. G., *A wavelet tour of signal processing*, 1997, Academic Press
- Figueiredo, M., and Nowak, R., 2003, An EM algorithm for wavelet-based image restoration, *IEEE Trans. Image Processing*, 8, 906-916
- Claerbout, J., 1968, Synthesis of a layered medium from it's acoustic transmission response. *Geophysics*, 33, 264-269

References

- Gelisli, K., Karsli, H., 1988, F-k filtering using the Hartley transform. *J. Seism. Explor.*, 7, 101-108
- Karsli, H., Bayrak, Y., 2004, Using the Wiener-Levinson algorithm to suppress ground-roll, *Journal of Applied Geophysics*, 55, 187-197
- McMechan, G. A., Sun, R., 1991, Depth filtering of first breaks and ground roll. *Geophysics*, 56, 390-396
- Donoho, D., 1995, De-noising by soft thresholding. *IEEE Trans. Inform. Theory*. 41, 613-627
- Starck, J.L., Elad, M., and Donoho, D., 2004, Redundant multiscale transforms and their applications to morphological component separation. *Advances in Imaging and Electron Physics*, 132
- Chen, S., Donoho D., and Saunders, M., 2001, Atomic decomposition by basis pursuit. *SIAM J. Sci. Comp.*, 43, 129-159
- Do, M.N.; Vetterli, M., 2001, Pyramidal directional filter banks and curvelets. *Image Processing, 2001. Proceedings. 2001 International Conference on*, 3, 158-161
- Herrmann, F., Boeniger, U., and Verschuur, E., 2007, Nonlinear primary-multiple separation with directional curvelet frames. *Geoph. J. Int.* to appear
- Hennenfent, G., and Herrmann, F. J., 2007, Curvelet reconstruction with sparsity-promoting inversion: successes and challenges, Submitted to EAGE 2007 69th Conference, London
- Demanet, L., Ying, L., 2006, Wave Atoms and Sparsity of Oscillatory Patterns, submitted
- Dong, S., Reiqing, H., Shuster, G., 2006, Interferometric prediction and least squares subtraction of surface waves. *SEG 76th Conference*, New Orleans