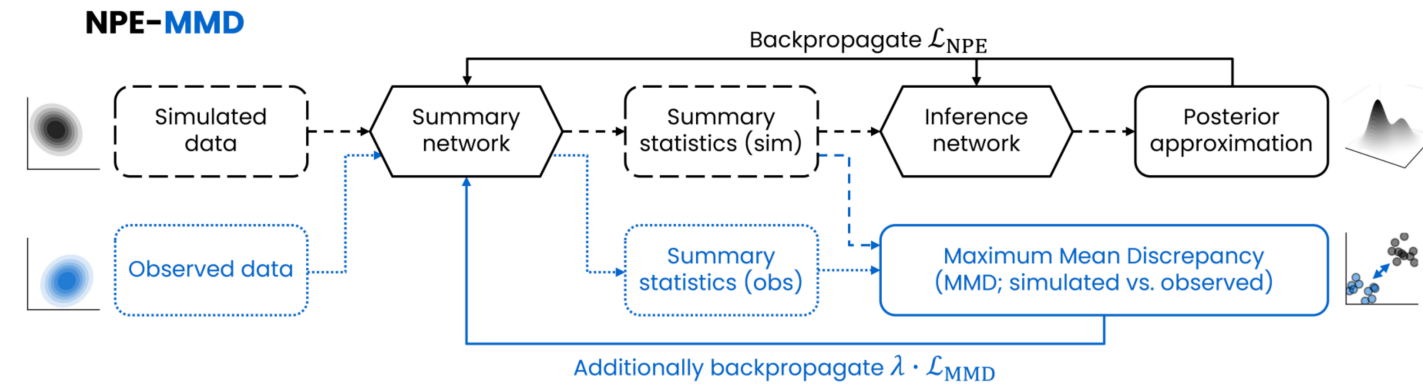


Motivation

- Simulation-based inference (SBI) delivers full posteriors for seismic inversion, but relies on an accurate simulator, noise model, and prior.
- Real seismic data involve elastic wave propagation; large-scale training simulations are often acoustic because of computational constraints.
- This acoustic–elastic mismatch is a form of model misspecification: posteriors become biased and uncertainty is underestimated.

Goal: develop robust SBI that remains reliable under the acoustic–elastic gap — learning from abundant acoustic simulations plus a few unpaired elastic observations.

ElasNet: MMD-Regularized Neural Posterior Estimation



- Acoustically* imaged common-image gathers (CIGs) act as physics-informed summary statistics; a learned summary network h_ψ further compresses them.
- Maximum mean discrepancy (MMD)** aligns summary features of simulated (acoustic) and observed (elastic) CIGs — *unpaired* data, no adversarial training.
- A **conditional normalizing flow** f_θ learns the posterior of velocity models; λ balances the flow loss and the MMD alignment.

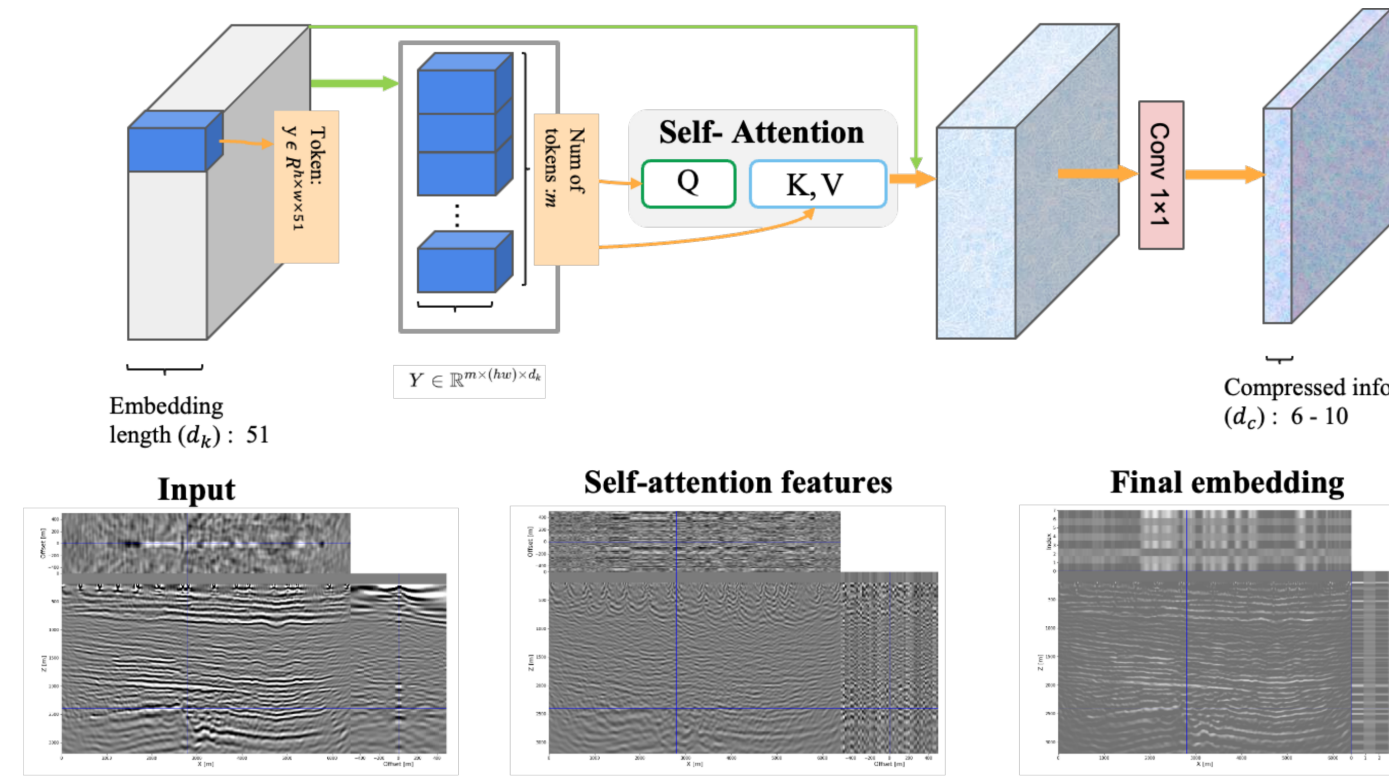
$$\mathcal{L}_{\text{total}} = \underbrace{-\mathbb{E}_{(\mathbf{x}, \mathbf{y}_{\text{sim}})} \left[\log p_Z(f_\theta(\mathbf{x}; h_\psi(\mathbf{y}_{\text{sim}}))) + \log \left| \det \frac{\partial f_\theta}{\partial \mathbf{x}}(\mathbf{x}; h_\psi(\mathbf{y}_{\text{sim}})) \right| \right]}_{\text{Conditional normalizing flow loss}} + \underbrace{\lambda \cdot \text{MMD}^2[h_\psi(\mathbf{y}_{\text{sim}}) \parallel h_\psi(\mathbf{y}_{\text{obs}})]}_{\text{MMD loss}}$$

Total training objective: conditional normalizing-flow loss + $\lambda \cdot \text{MMD}^2$ between acoustic and elastic summary features.

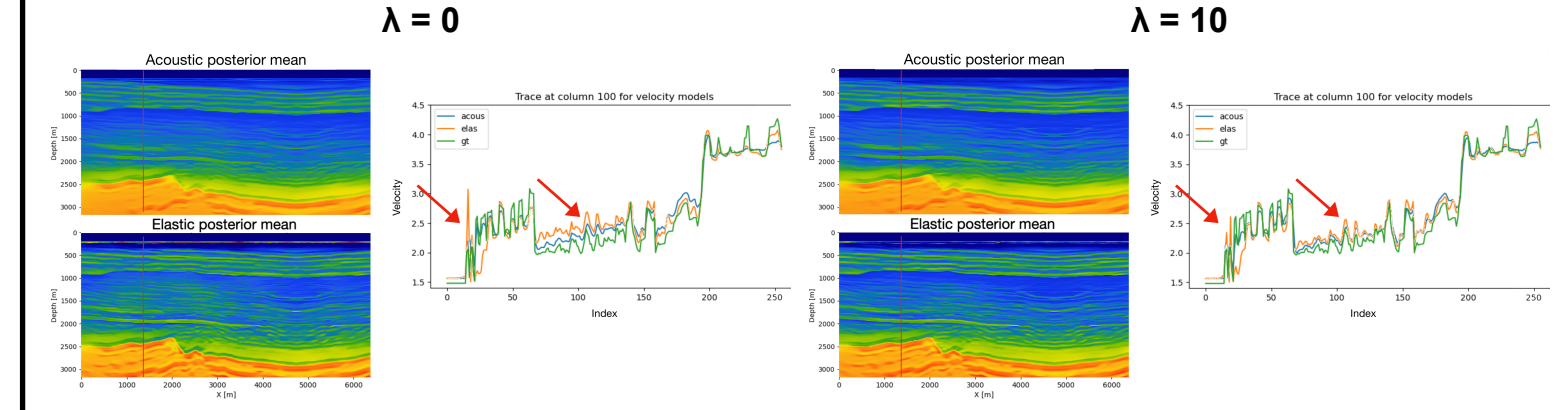
Note: The observed field data does not need to be paired with the simulated data during training.

Attention-Based Summary Network h_ψ

Offset responses at each spatial location of a CIG (51 subsurface offsets) are treated as tokens. Self-attention within local 8×8 windows aggregates offset-dependent focusing information; a 1×1 convolution compresses features to $d_c \in [6, 10]$ channels.



Traces at $x = 1.4$ km



Arrows: water-bottom contrast (≈ 200 m) and central region. With $\lambda = 10$ the elastic trace aligns with the acoustic one and approaches the ground truth.

Observations

- Acoustic and elastic posterior means both preserve the overall structure — the summary network captures the features needed to inform the posterior.
- Increasing the MMD weight pulls the elastic summary distribution closer to the acoustic one.
- The summary statistic learns to ignore elastic events that do not inform the posterior of acoustic properties.
- Elastic posterior means show finer details: PP-reflections carry contributions from both P- and S-wave velocities.

Conclusions

- ElasNet bridges acoustic simulations and elastic observations by combining robust CIG summaries with MMD distribution alignment.
- Trained almost entirely on inexpensive acoustic simulations; only ≈ 90 unpaired elastic examples are needed.
- Reduces acoustic–elastic posterior discrepancies and improves structural consistency and uncertainty calibration — a scalable path for SBI under realistic physics mismatch.

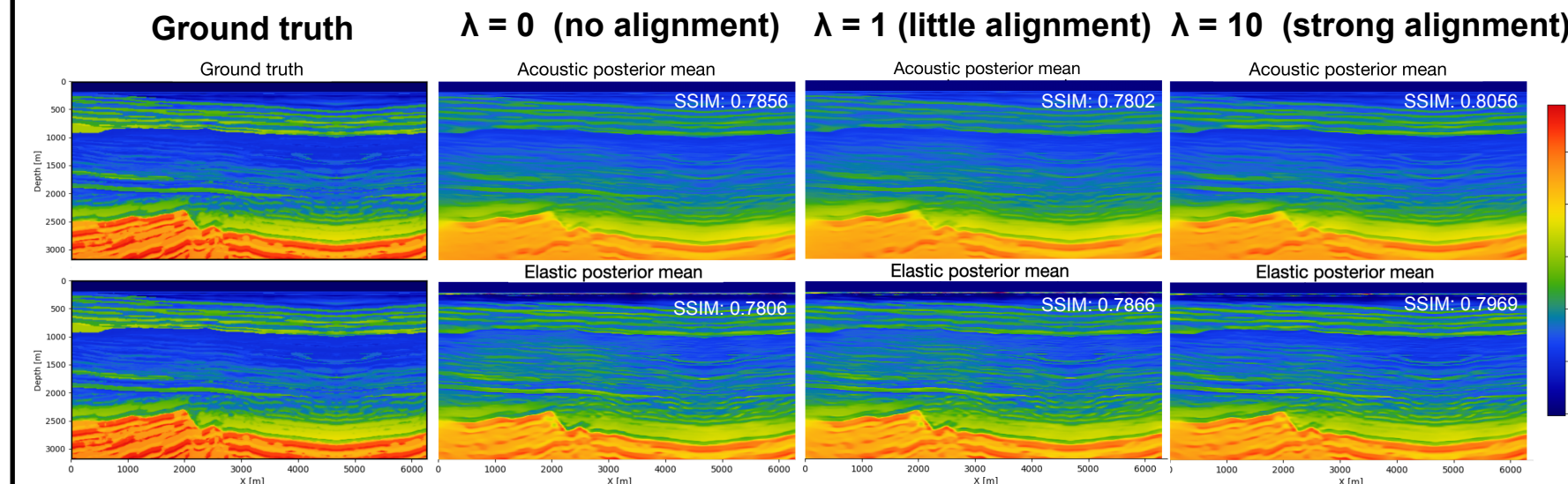
References

- Elsenhüller, Lasse, et al. "Does Unsupervised Domain Adaptation Improve the Robustness of Amortized Bayesian Inference? A Systematic Evaluation." arXiv preprint arXiv:2502.04949 (2025).
- Kelly, Ryan P., et al. "Simulation-based bayesian inference under model misspecification." arXiv preprint arXiv:2503.12315 (2025).
- Zeng, S., Orozco, R., Zeng, Y., Erdinc, H. T., Gahlot, A. P., & Herrmann, F. J. (2025, August). Attention please: Getting the most from CIGs with learned summary statistics. In International Meeting for Applied Geoscience and Energy. <https://slim.gatech.edu/Publications/Public/Conferences/SEG/2025/herrmann20205IMAGEapp>
- Arthur Gretton, Karsten M Borgwardt, Malte J Rasch, Bernhard Schölkopf, and Alexander Smola. A kernel two-sample test. Journal of Machine Learning Research, 13(Mar):723–773, 2012.

Acknowledgement

This research was carried out with the support of the Georgia Research Alliance and partners of the ML4Seismic Center.

Posterior Means: Effect of MMD Alignment



Ground truth (left column) vs. acoustic (top) and elastic (bottom) posterior means with increasing MMD alignment strength. Strong alignment ($\lambda = 10$) suppresses the spurious water-bottom contrast and mid-depth bias in the elastic posterior, producing better agreement with the ground truth and the highest SSIM for both acoustic and elastic cases.