

Learned one-shot imaging

Mathias Louboutin², Rafael Orozco¹, Ali Siahkoobi³, and Felix J. Herrmann¹
¹Georgia Institute of Technology, ²Devito Codes Ltd, ³Rice University



Introduction

Seismic imaging's main limiting factor is the scale of the involved dataset and the number of independent wave-equation solves required to migrate thousands of shots. To tackle this dimensionality curse, we introduce a learned framework that extends the conventional computationally reductive linear source superposition (e.g., via random simultaneous-source encoding) to a nonlinear learned source superposition and its corresponding learned supershot. With this method, we can image the subsurface at the cost of a one-shot migration by learning the most informative superposition of shots.

Methodology

Objectives:

- Learn non-linear supershot
- Learn corresponding simultaneous source
- Maximally inform subsurface reflectivity

Simultaneous learning of two networks.

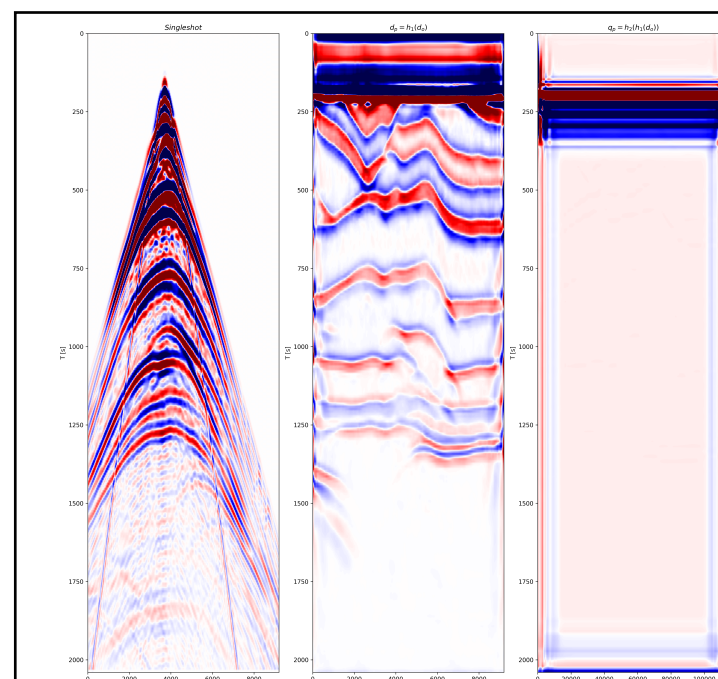
Supervised learning trains on pairs of known subsurface image (synthetics or legacy images) and corresponding data.

$$\min_{\theta, \phi} \mathbb{E}_{(\mathbf{d}, \delta \mathbf{m}) \sim p(\mathbf{d}, \delta \mathbf{m})} \left[\frac{1}{2} \left\| \mathbf{J}(\mathcal{H}_{\phi} \circ \mathcal{G}_{\theta}(\mathbf{d}))^{\top} \mathcal{G}_{\theta}(\mathbf{d}) - \delta \mathbf{m} \right\|_2^2 \right]$$

Unsupervised learning trains on data only through migration-demigration. **Only requires data and a subsurface background model.**

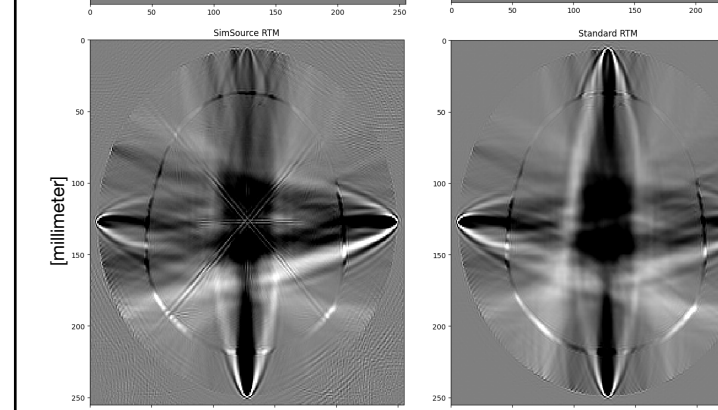
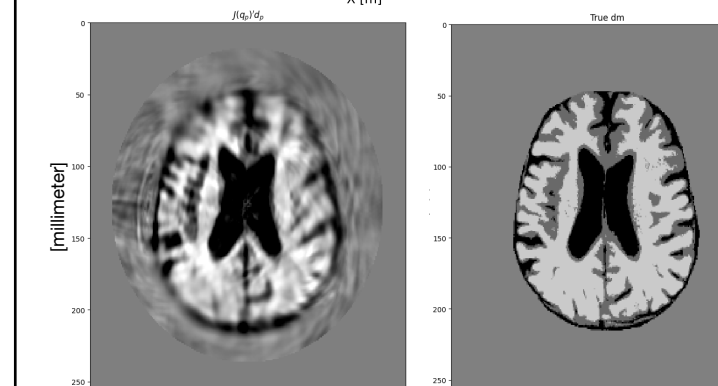
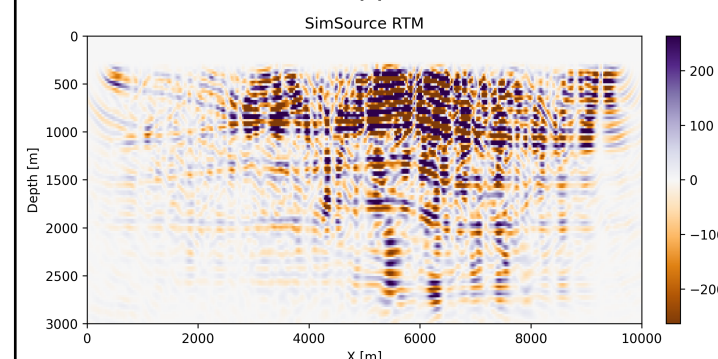
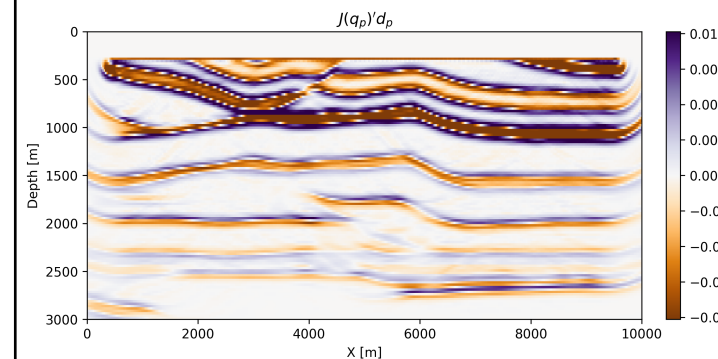
$$\min_{\theta, \phi} \mathbb{E}_{\mathbf{d} \sim p(\mathbf{d})} \left[\frac{1}{2} \left\| \tilde{\mathbf{J}} \mathbf{J}(\mathcal{H}_{\phi} \circ \mathcal{G}_{\theta}(\mathbf{d}))^{\top} \mathcal{G}_{\theta}(\mathbf{d}) - \tilde{\mathbf{d}} \right\|_2^2 \right],$$

Only migrate supershots. Training us cheaper than standard migration of all shots.



Supervised

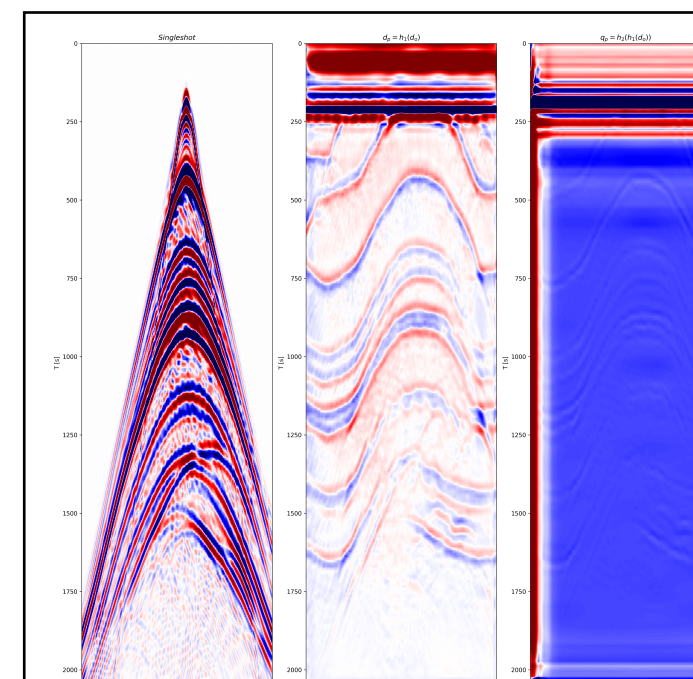
- Learned source similar to plane wave source
- Learned supershot reflects subsurface
- One-shot image very accurate



Medical ultrasound

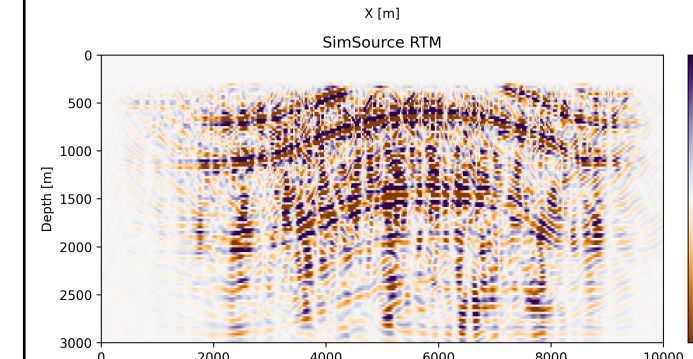
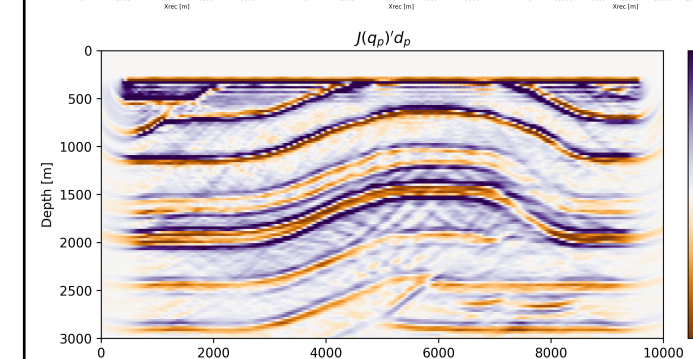
Acoustic values of brain tissue can diagnose

- Tumors
- Hemorrhage
- Air bubbles associated with plaque growth



Unsupervised

- Similar learned data
- More noise in the image
- Still very accurate



Conclusions

- Data-domain learning method that provides high accuracy images
- Subsurface through one-shot imaging
- Supervised and unsupervised methods
- Reduced crosstalk

References

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 Radev, Stefan T, Ulf K Mertens, Andreas Voss, Lynton Ardizzone, and Ullrich Köthe. 2020. "BayesFlow: Learning Complex Stochastic Models with Invertible Neural Networks." *IEEE Transactions on Neural Networks and Learning Systems*.