

# *AVA analysis and geological dip estimation via two-way wave-equation based extended images*

Rajiv Kumar, Tristan van Leeuwen and Felix J. Herrmann

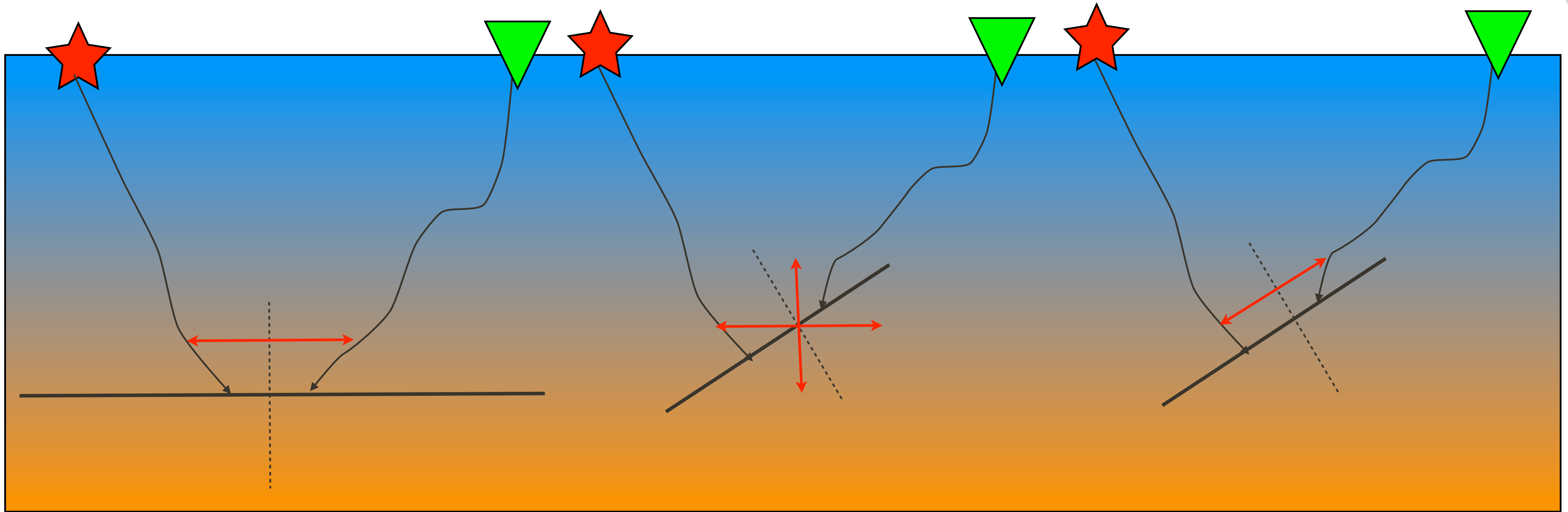
# Motivation

Computation of *full*-subsurface offset volumes is computationally *prohibitively* expensive  
(storage & computation time)

*Full*-subsurface *offset* volumes allow us to conduct

- ▶ AVA w/ geologic *dip* corrections
- ▶ MVA

using information from *all* directions.

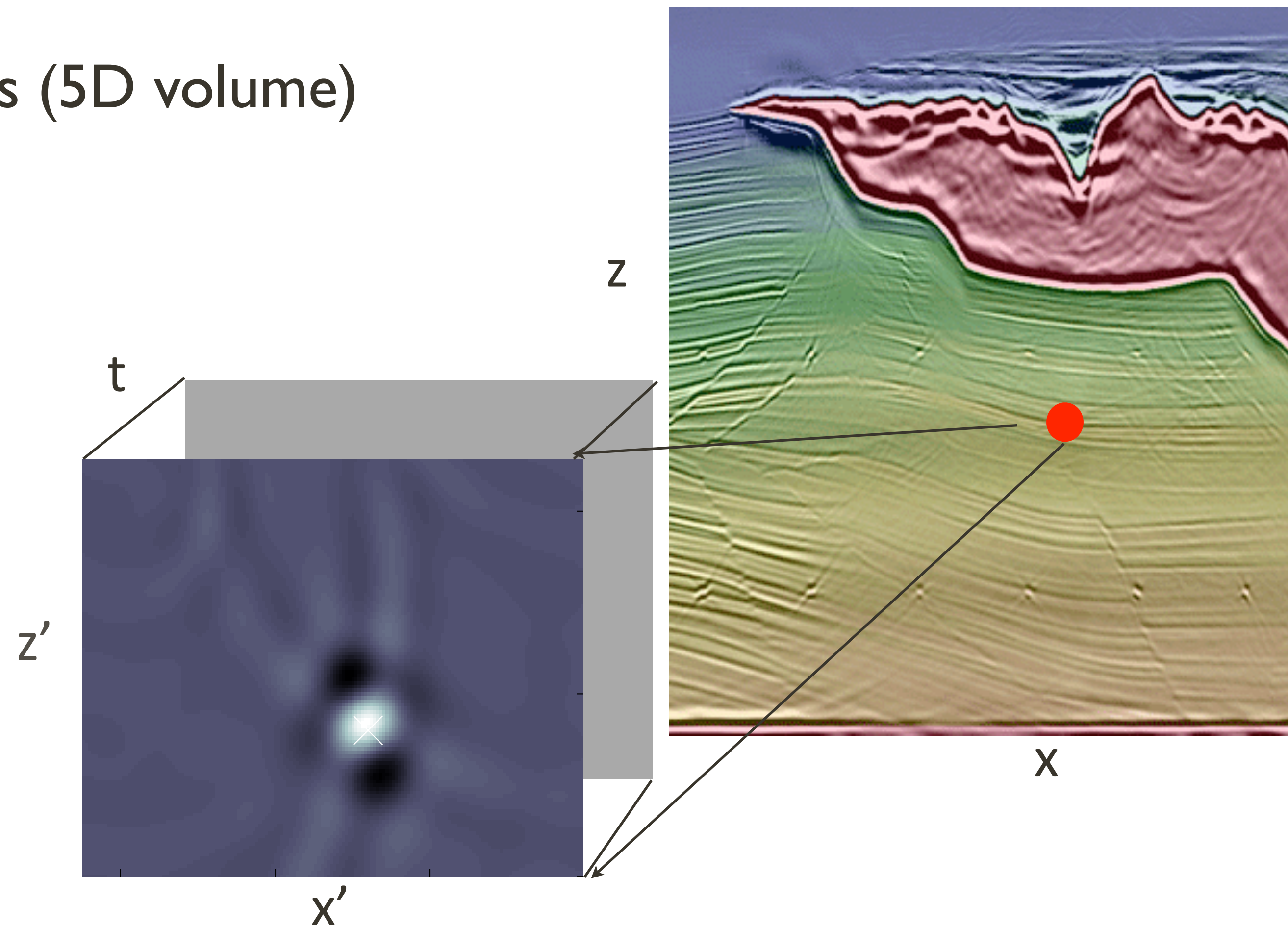


horizontal  
offset

horizontal  
+vertical  
offset

all offsets

- ▶ use *all* subsurface offsets (5D volume)
- ▶ 2-way wave-equation



but.... we can *never* hope to *compute* or *store* such an *extended* image volume!  
Can we work with the *extended* volume *implicitly* ?

# Outline

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- ▶ Anatomy
- ▶ Computation
- ▶ Dip Angle Gather
- ▶ Application
- ▶ Conclusions

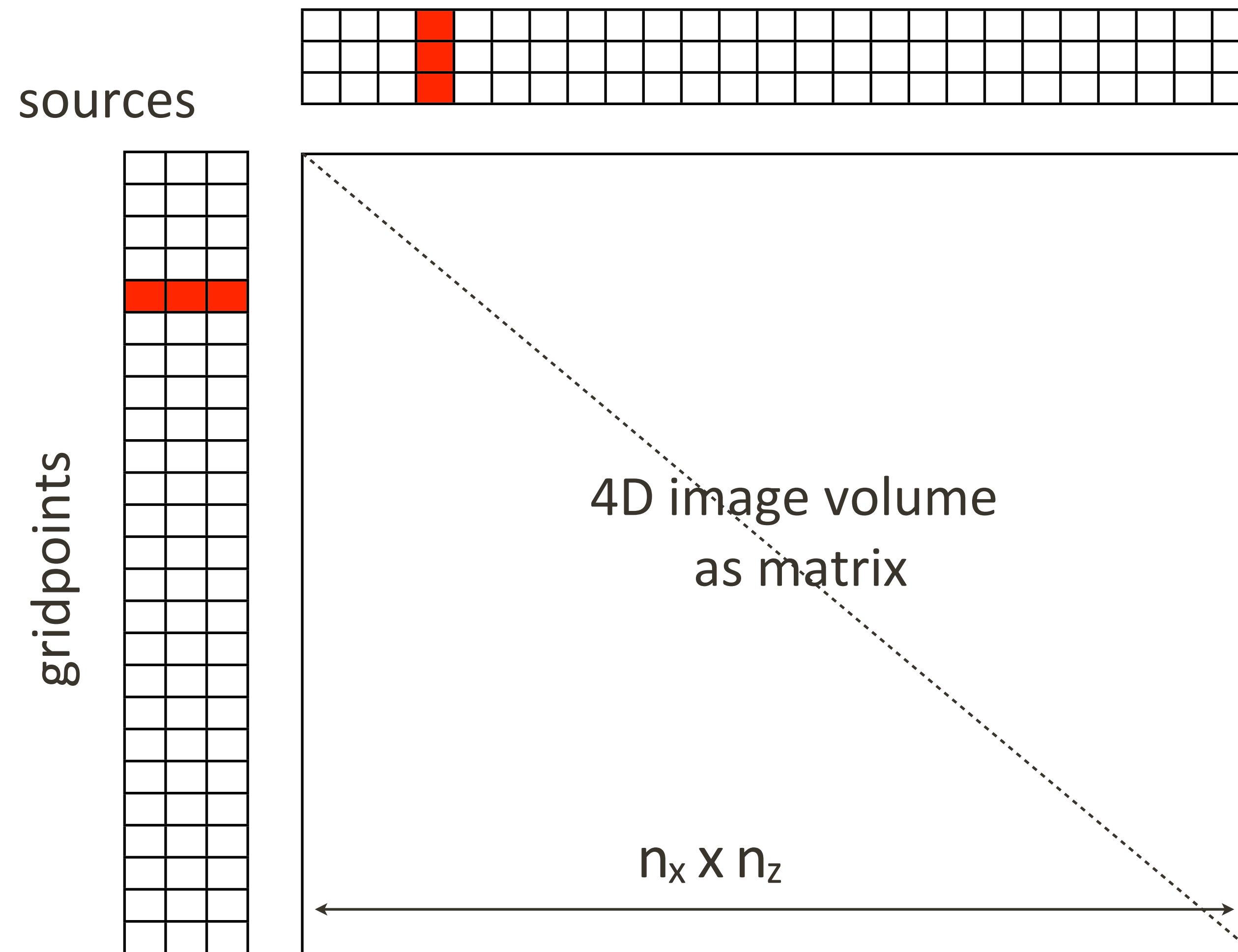
# Anatomy

$$e(\omega, \mathbf{x}, \mathbf{x}') = \sum_i u_i(\omega, \mathbf{x}) v_i(\omega, \mathbf{x}')^*$$

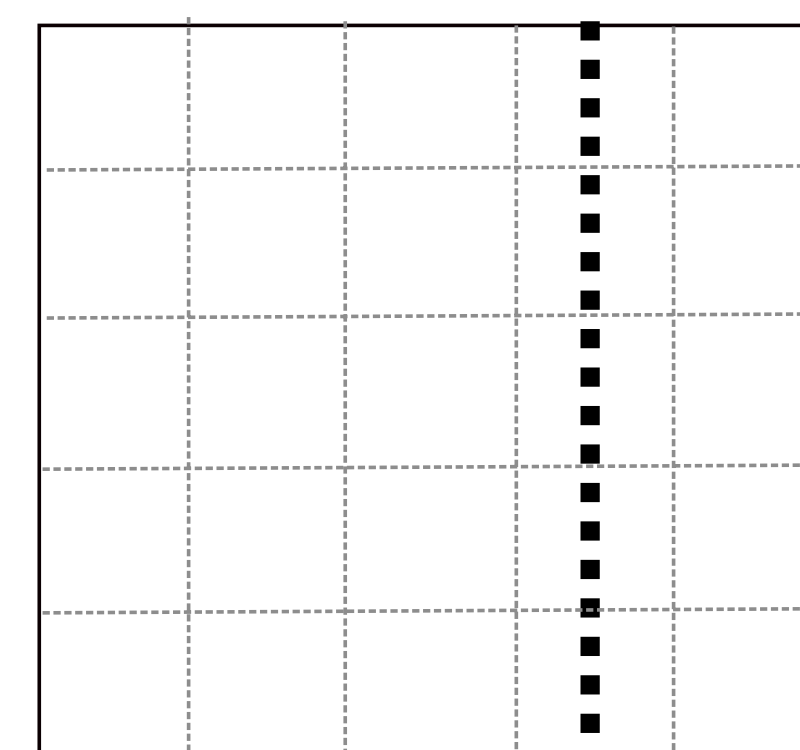
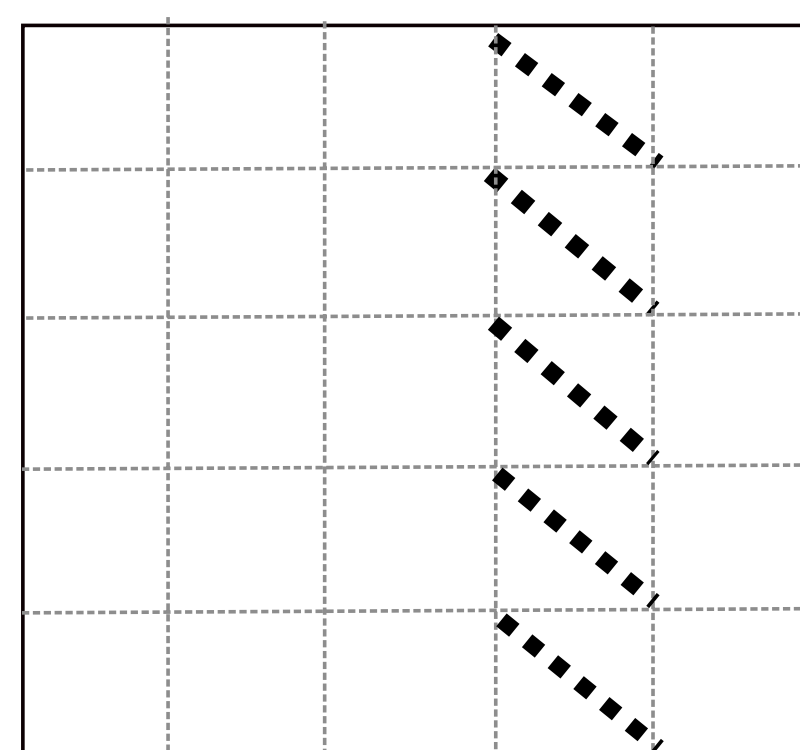
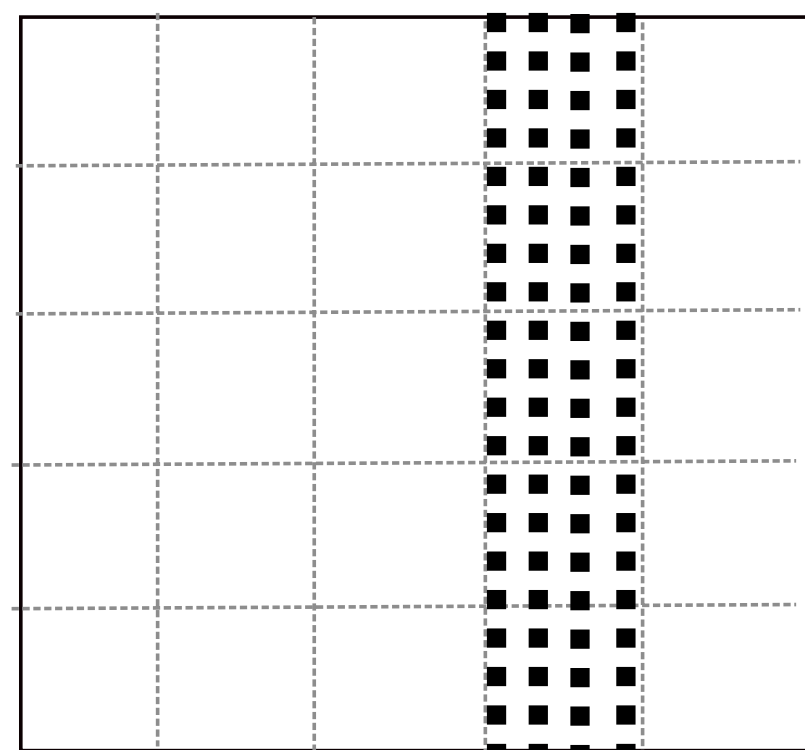
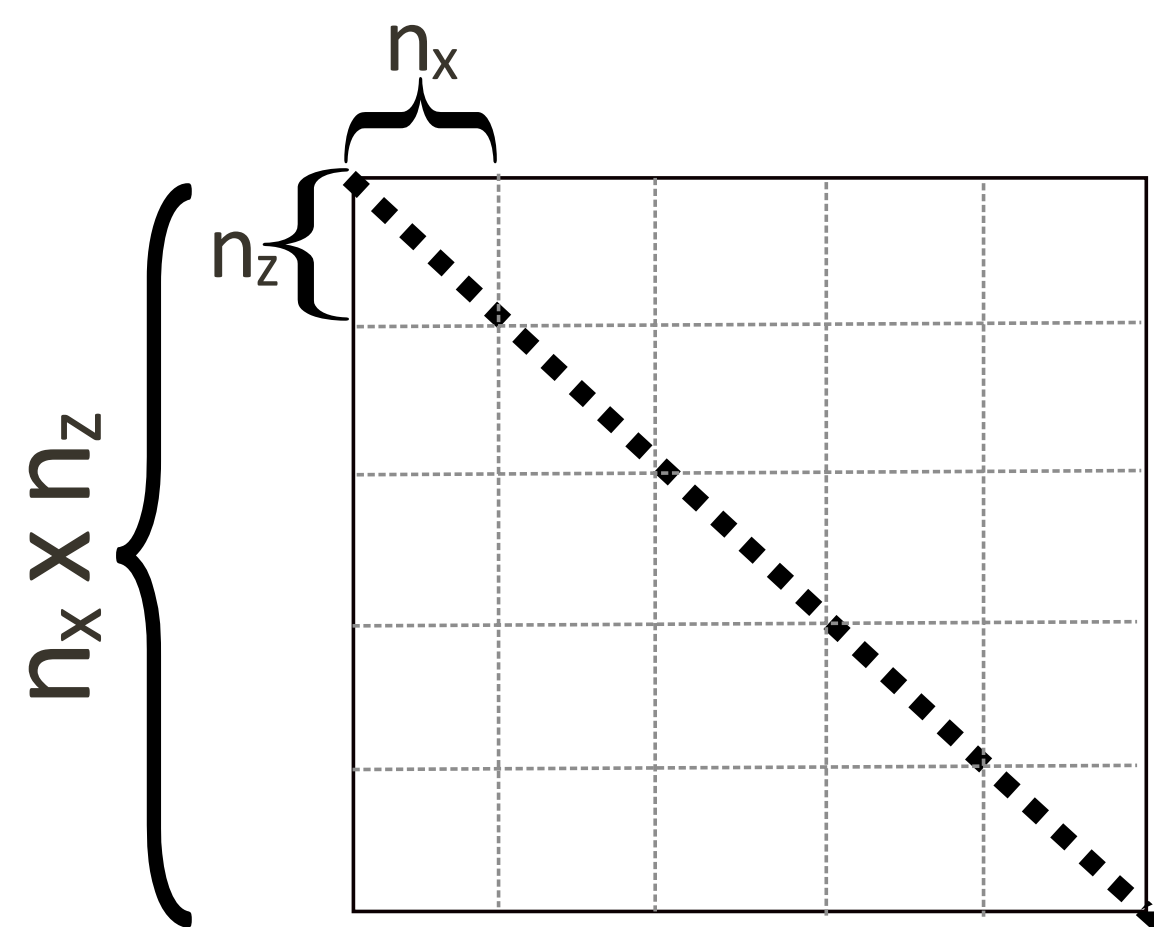
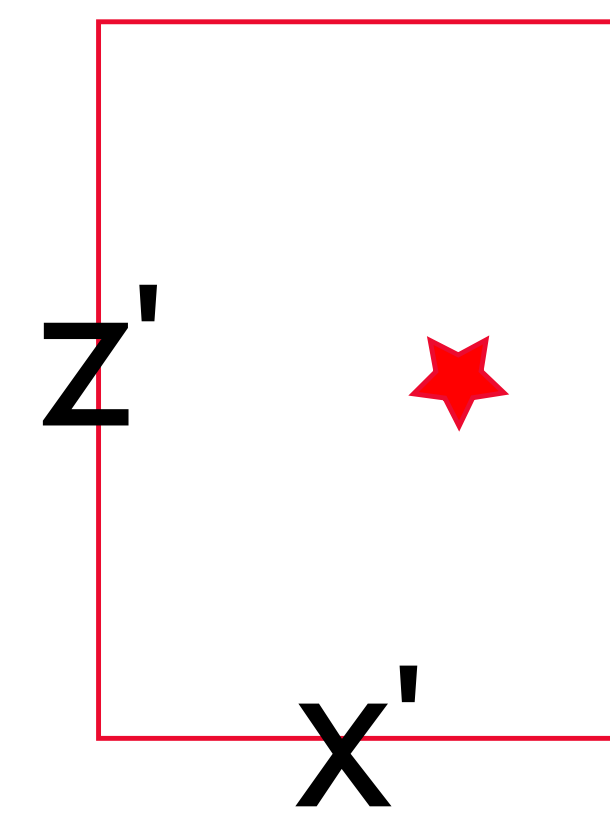
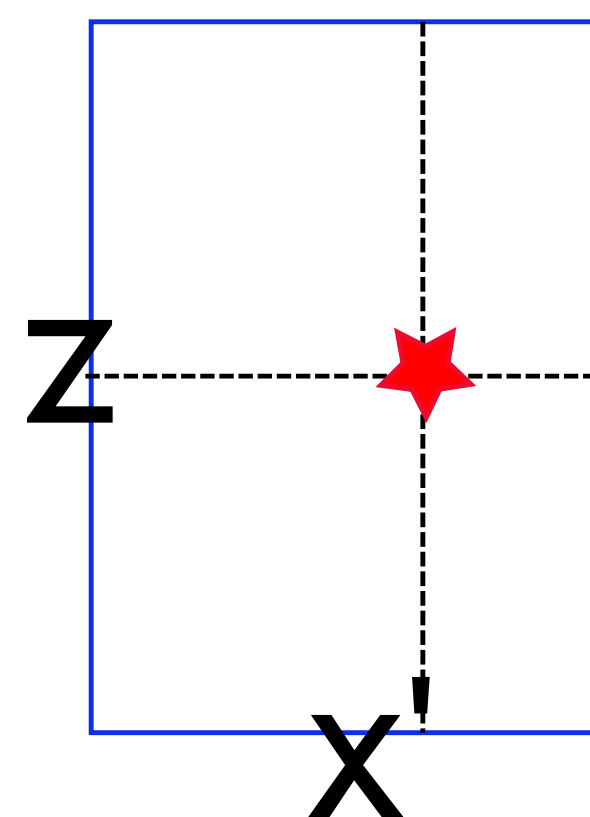
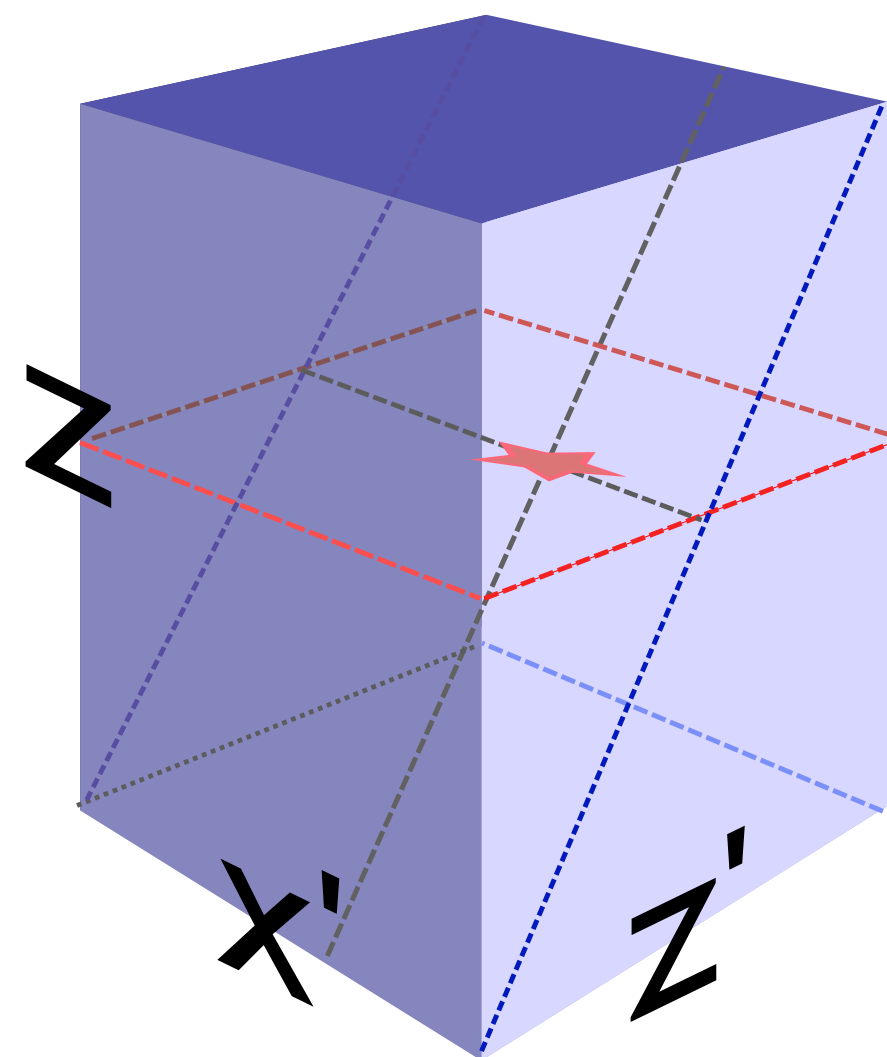
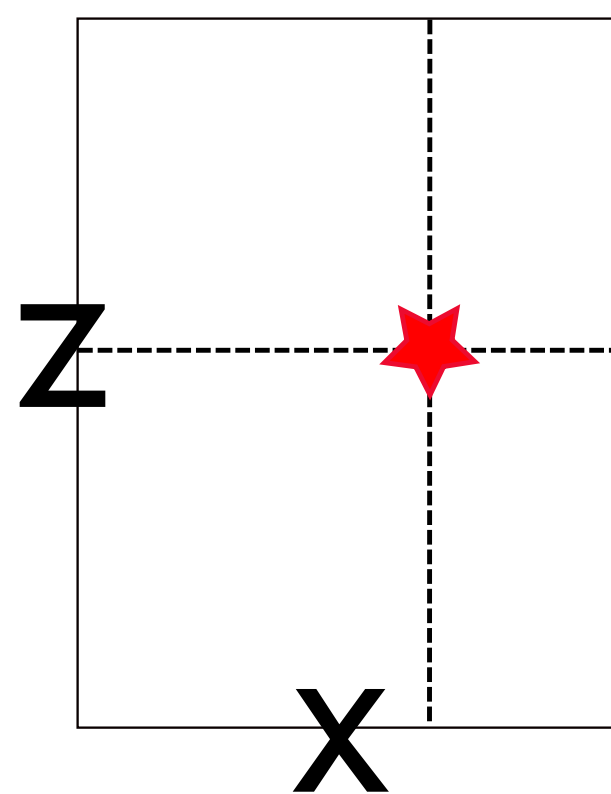
- ▶ Organize wavefields in monochromatic *data matrices* [\[Berkhout, 84\]](#)
- ▶ Express image volume *tensor as matrix*

$$E = UV^*$$

# Extended images



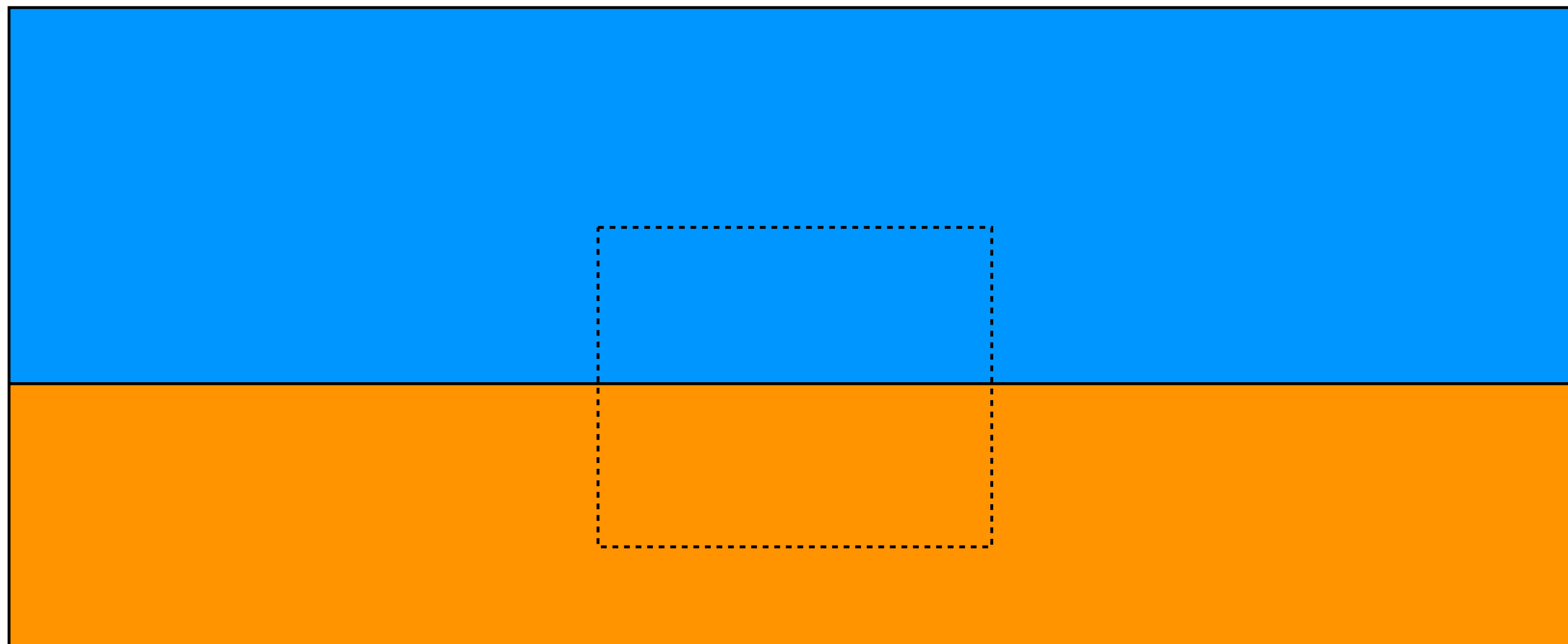
# Extended images





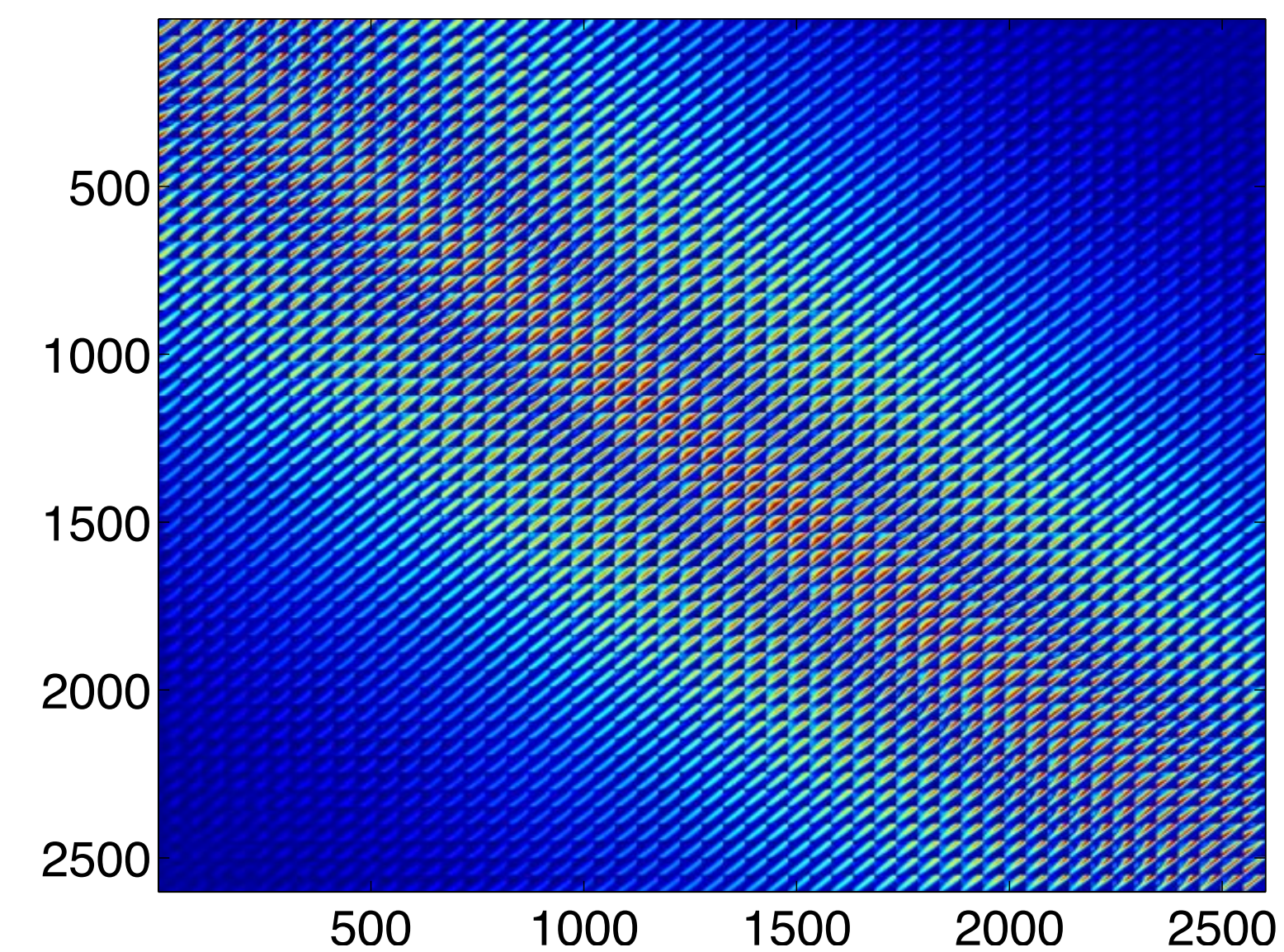
# Extended images

example for *one* layer

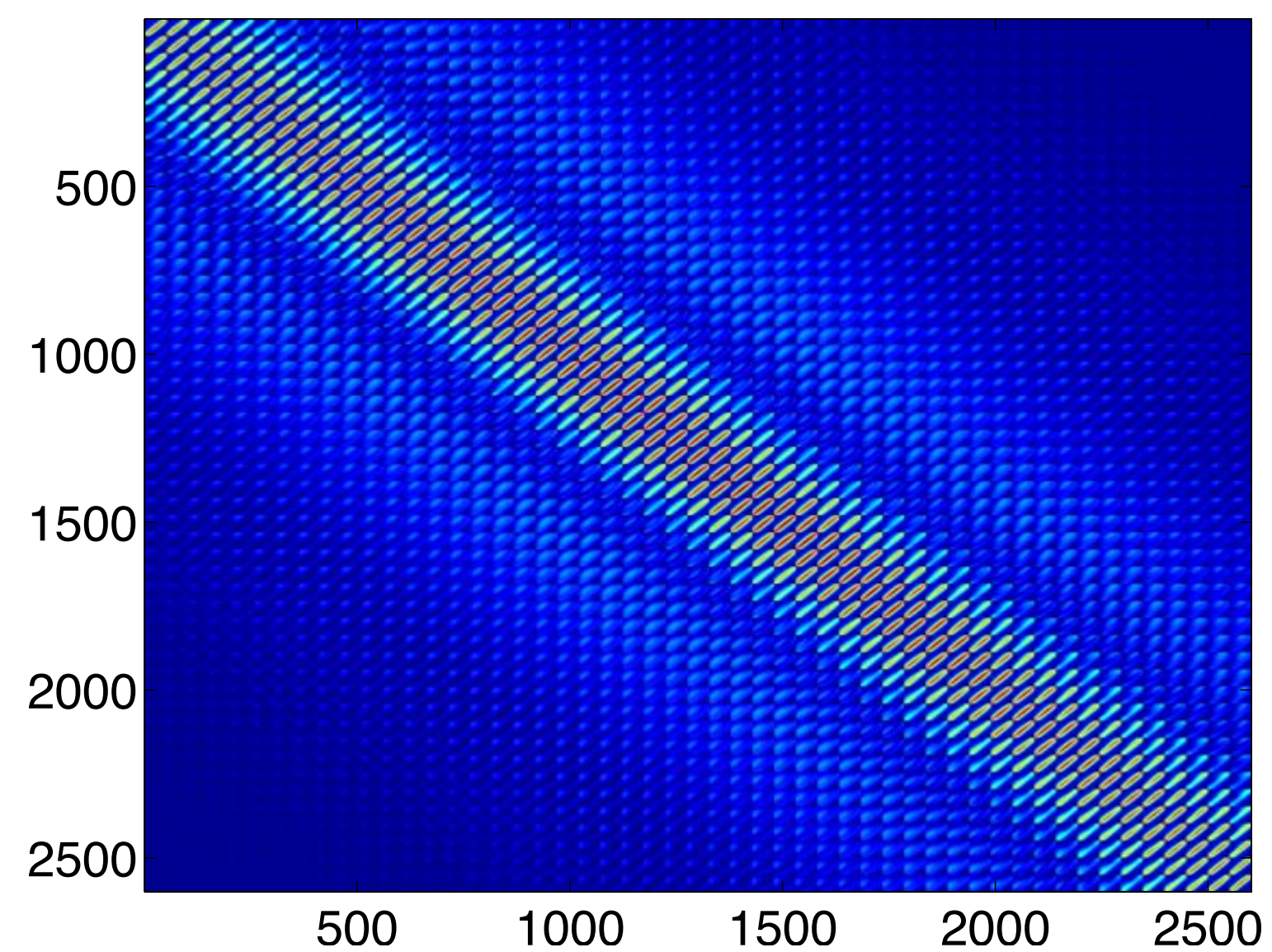


# Extended images

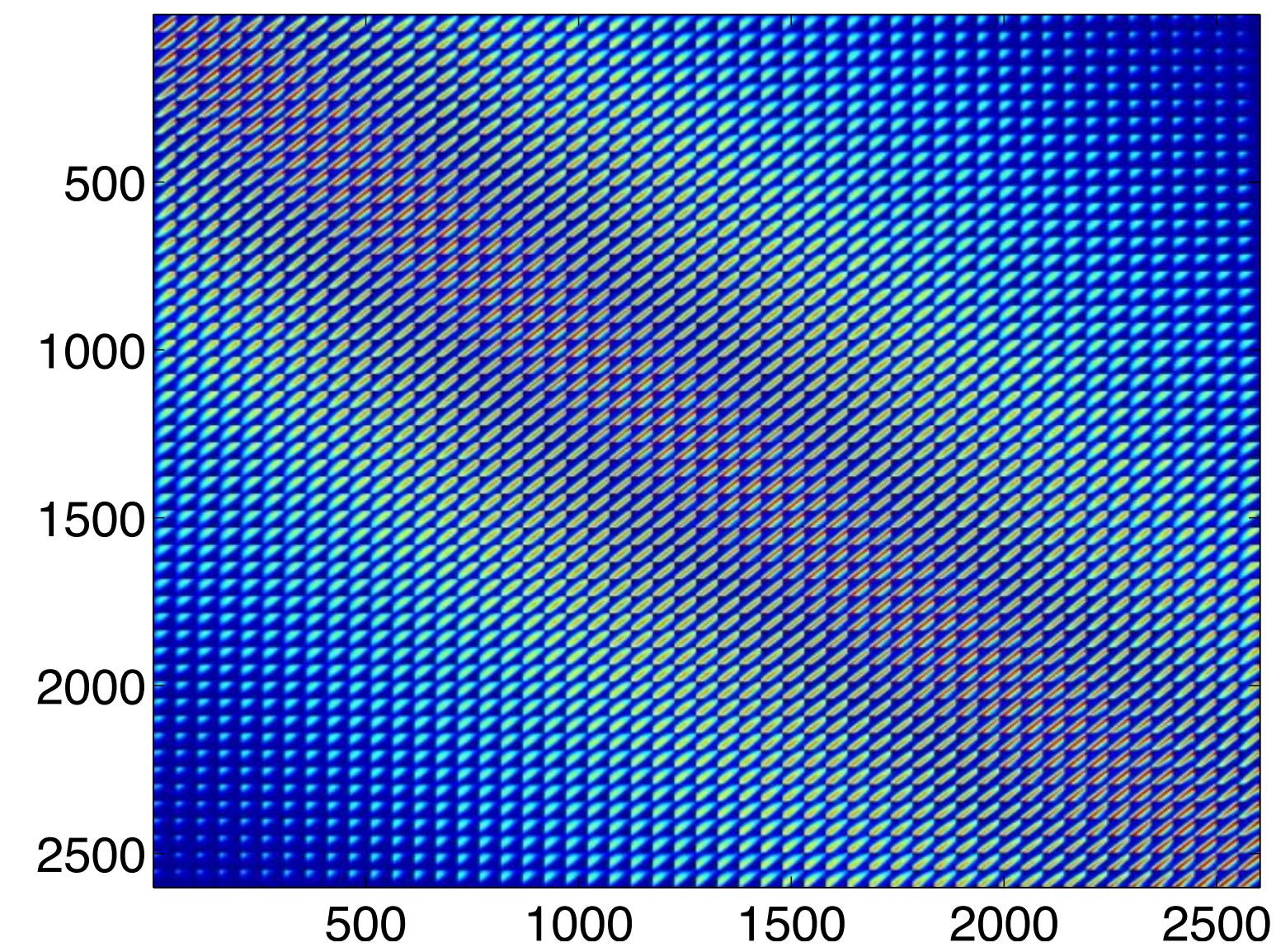
full matrix



low  
velocity



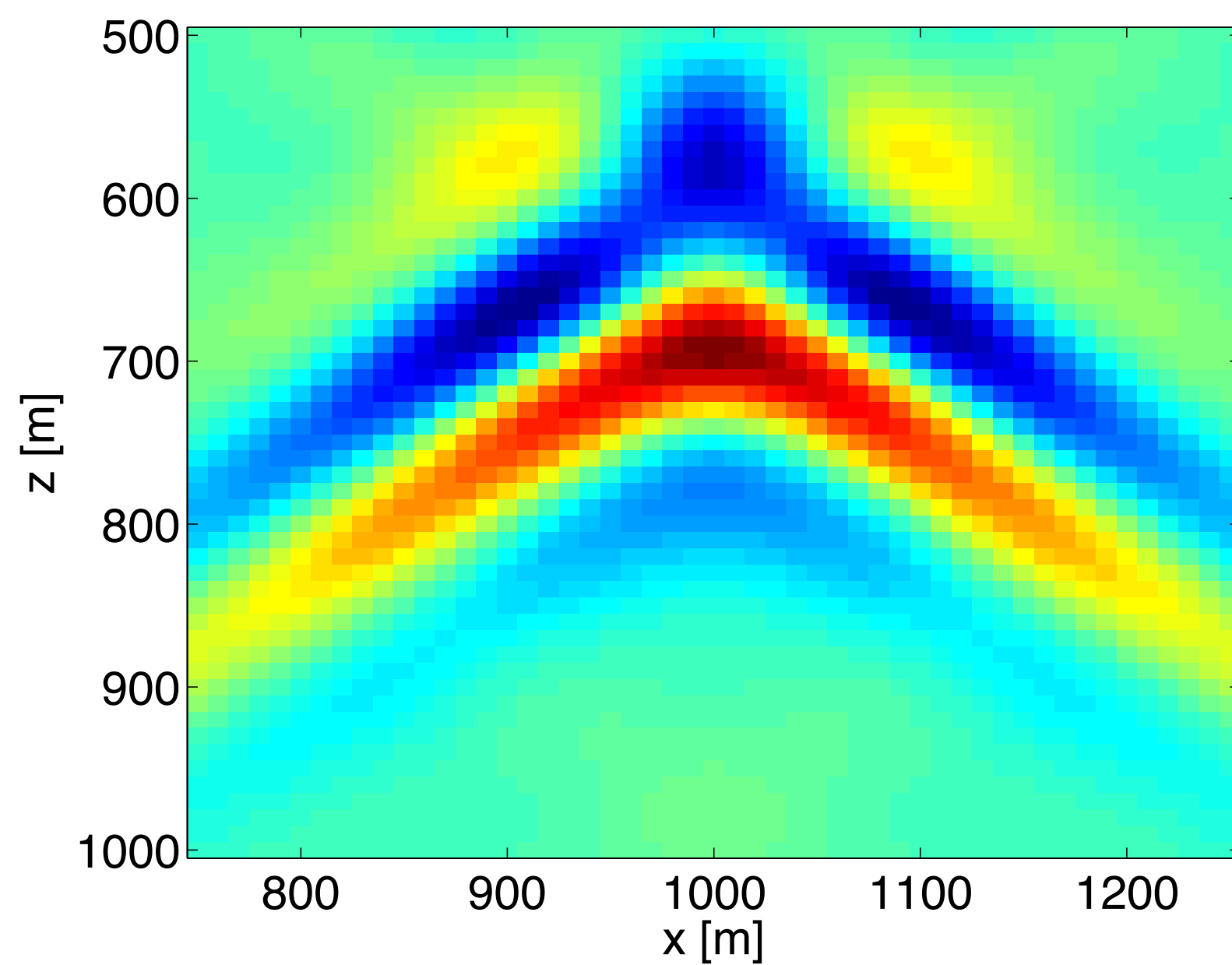
correct  
velocity



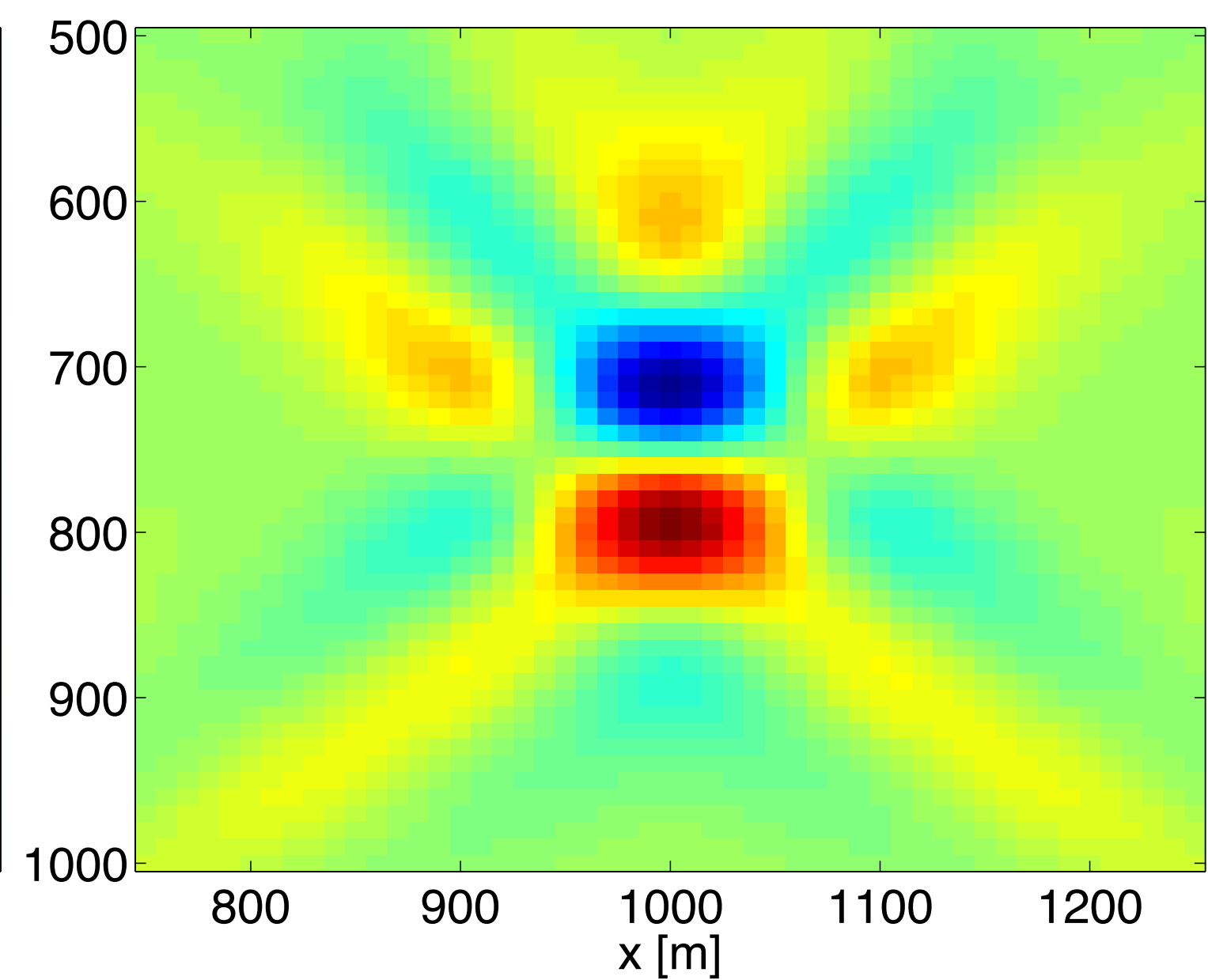
high  
velocity

# Extended images

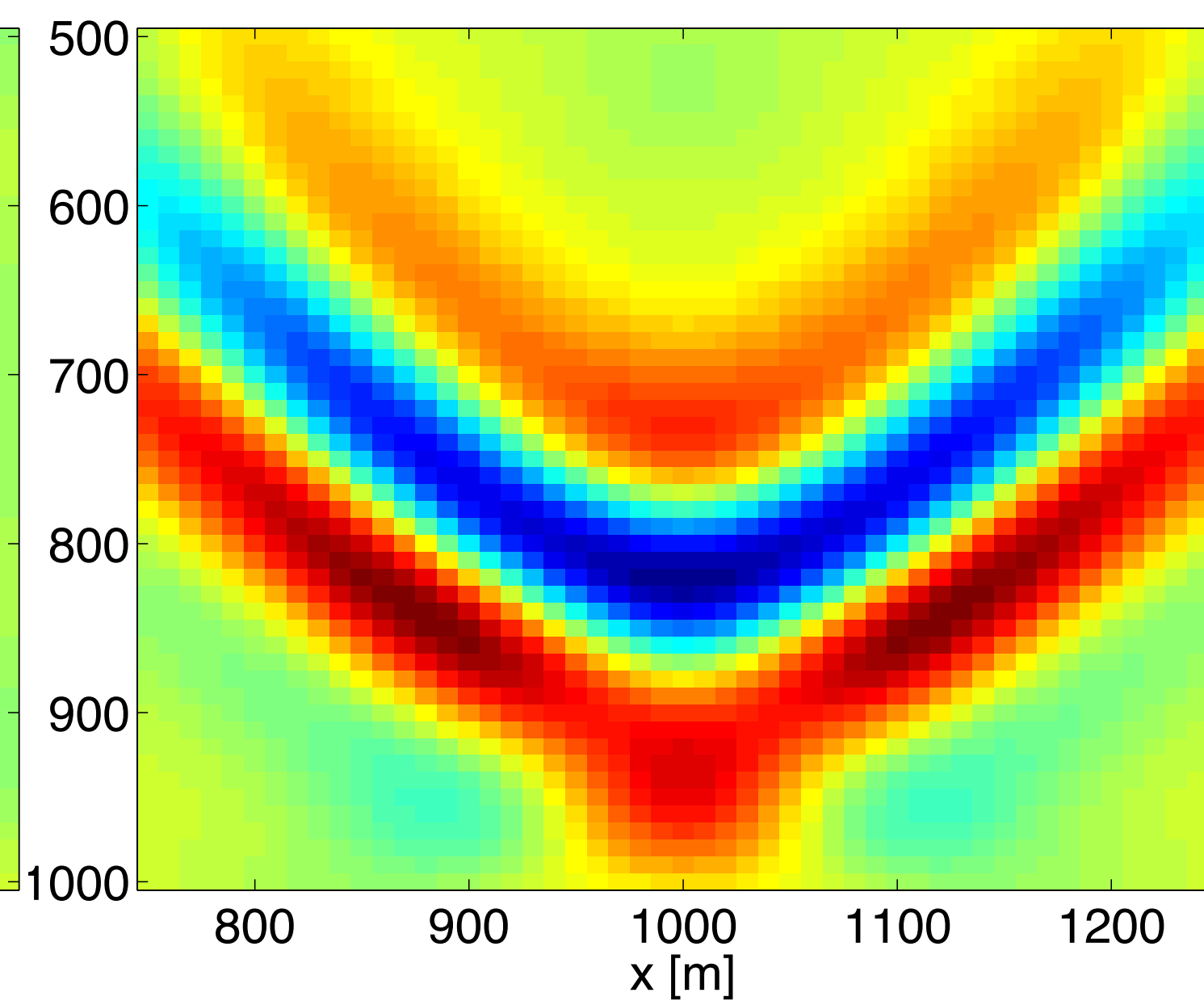
one column



low  
velocity



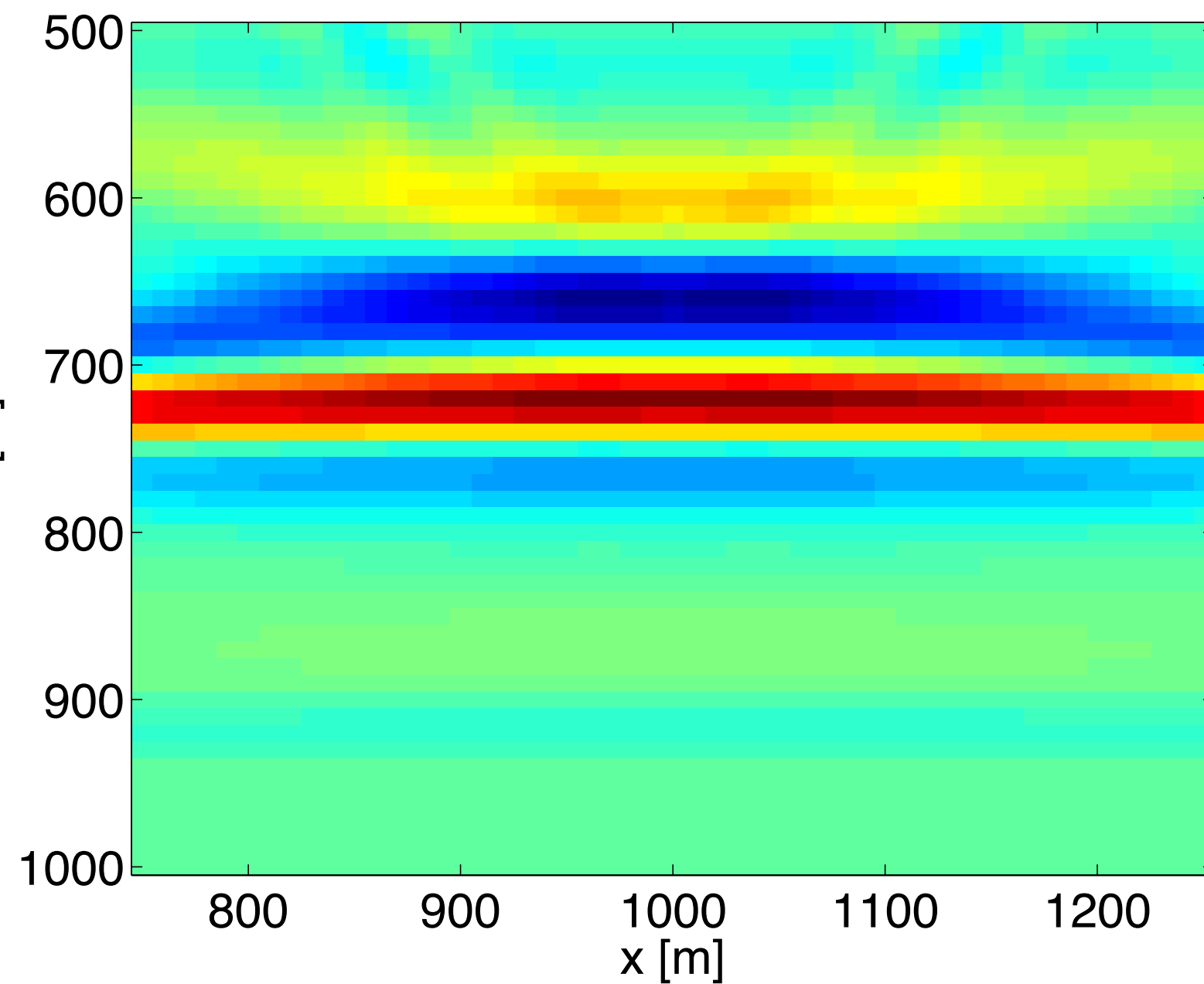
correct  
velocity



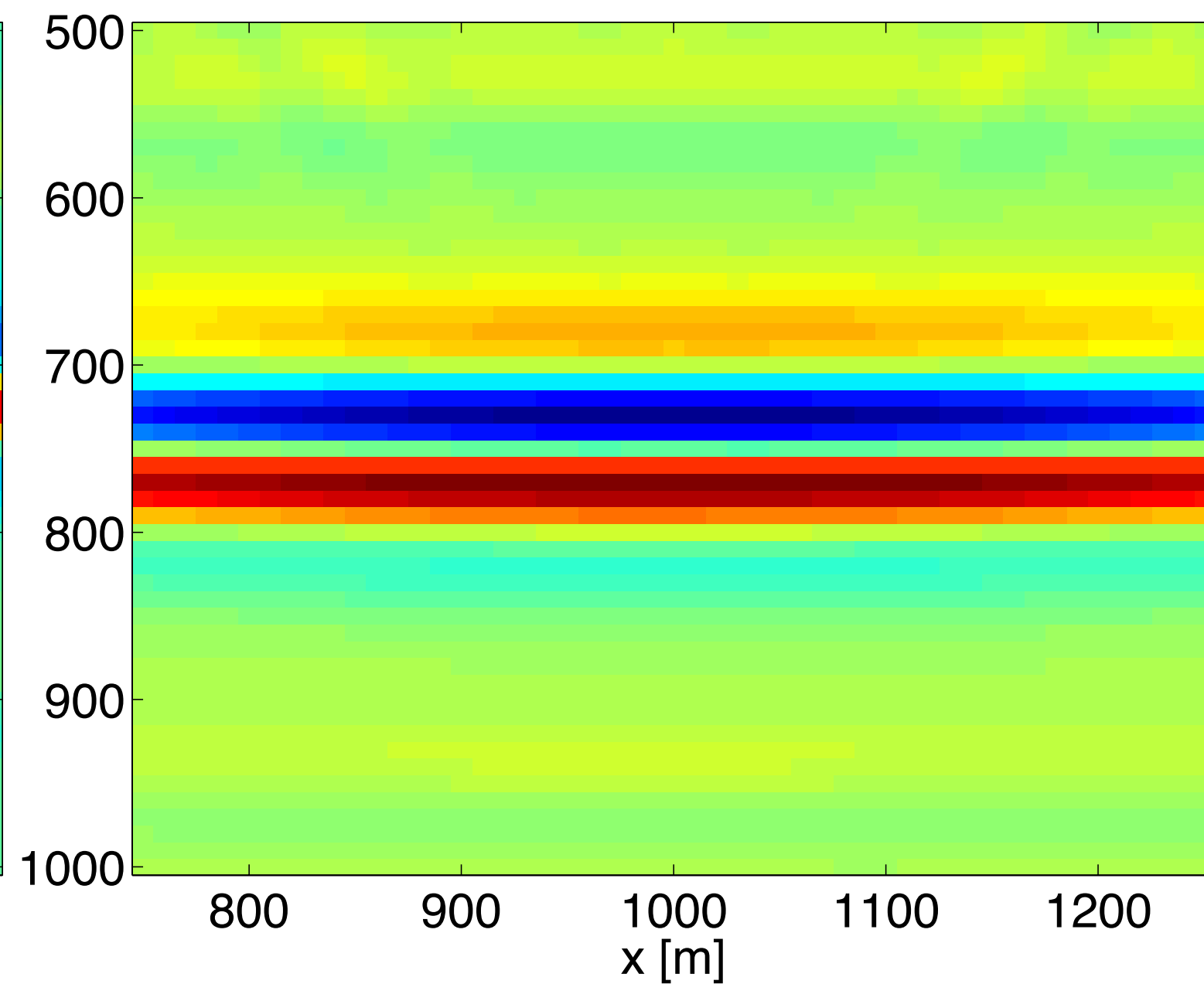
high  
velocity

# Extended images

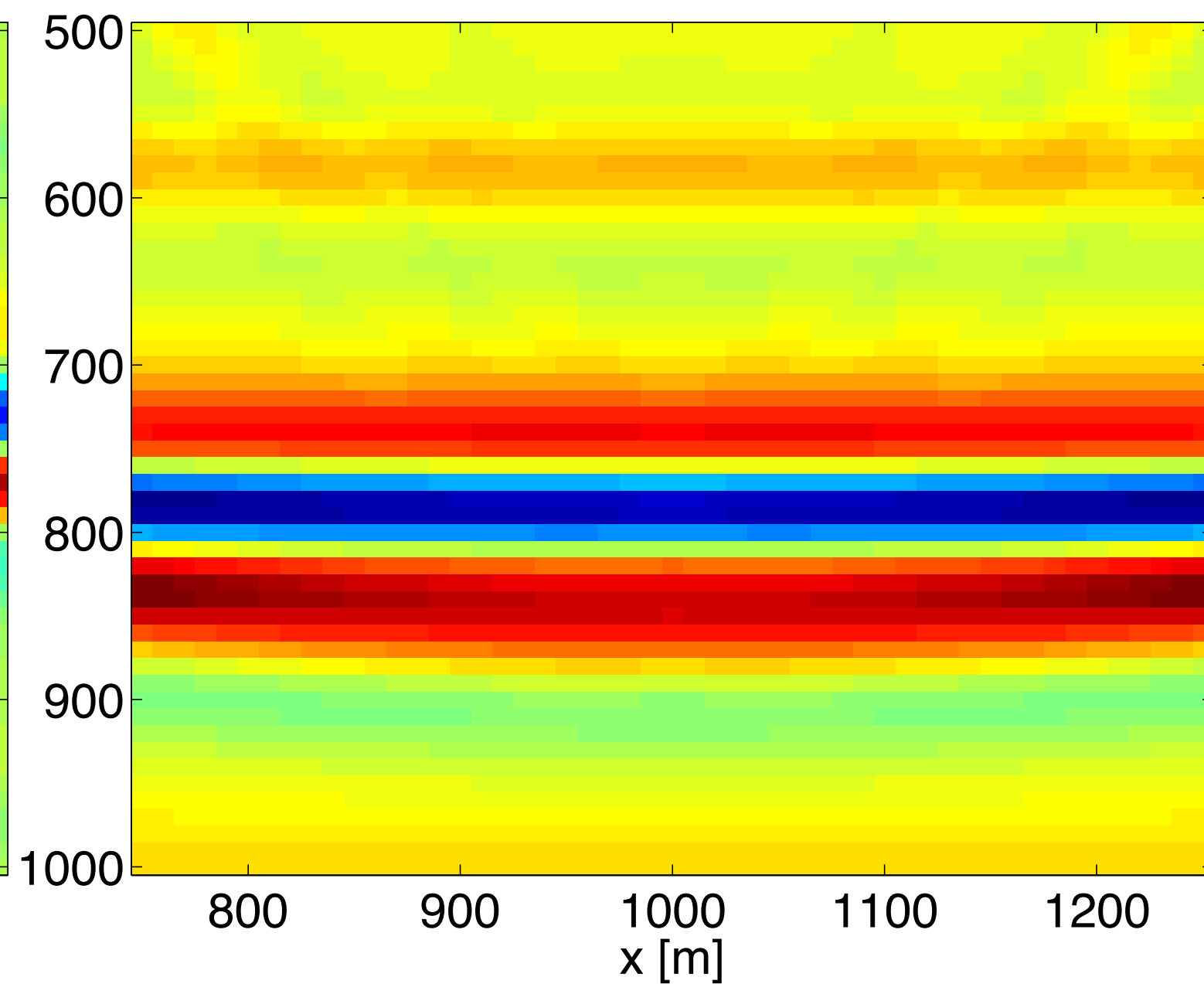
diagonal



low  
velocity



correct  
velocity



high  
velocity

# Computation

- ▶ *complete* image volume too *large* to form:  $(n_x \times n_z)^2$
- ▶ instead, *probe* volume for information via *mat-vecs*  $E\mathbf{y}$  [van Leeuwen and Herrmann, 12]
- ▶  $\mathbf{y}$  can be interpreted as subsurface (sim.) *source* function

# Computation

*mat-vec with extended image:*

$$\mathbf{e} = E\mathbf{y} = H^{-1}P_s^T Q D^* P_r H^{-1}\mathbf{y}$$

- ▶  $\tilde{\mathbf{d}} = P_r H^{-1}\mathbf{y}$  (one subsurface source)
- ▶  $\tilde{\mathbf{w}} = D^* \tilde{\mathbf{d}}$  (source weights)
- ▶  $\mathbf{e} = H^{-1}P_s^T Q \tilde{\mathbf{w}}$  (one source)

# Computation

Are able to compute *full*-subsurface image gathers

- ▶ *w/o looping over all sources*
- ▶ probe image space w/ arbitrary *test functions*
  - *point scatterers (one at location of subsurface point)*
  - *Gaussian weights (simultaneous source)*

# Computation

computation of an *image point gather*

	# of PDE solves	“flops for correlations”
conventional	$2N_s$	$N_s \times N_h$
mat-vecs	$2N_x$	$N_s \times N_r$

$N_s$  - # of sources

$N_r$  - # of receivers

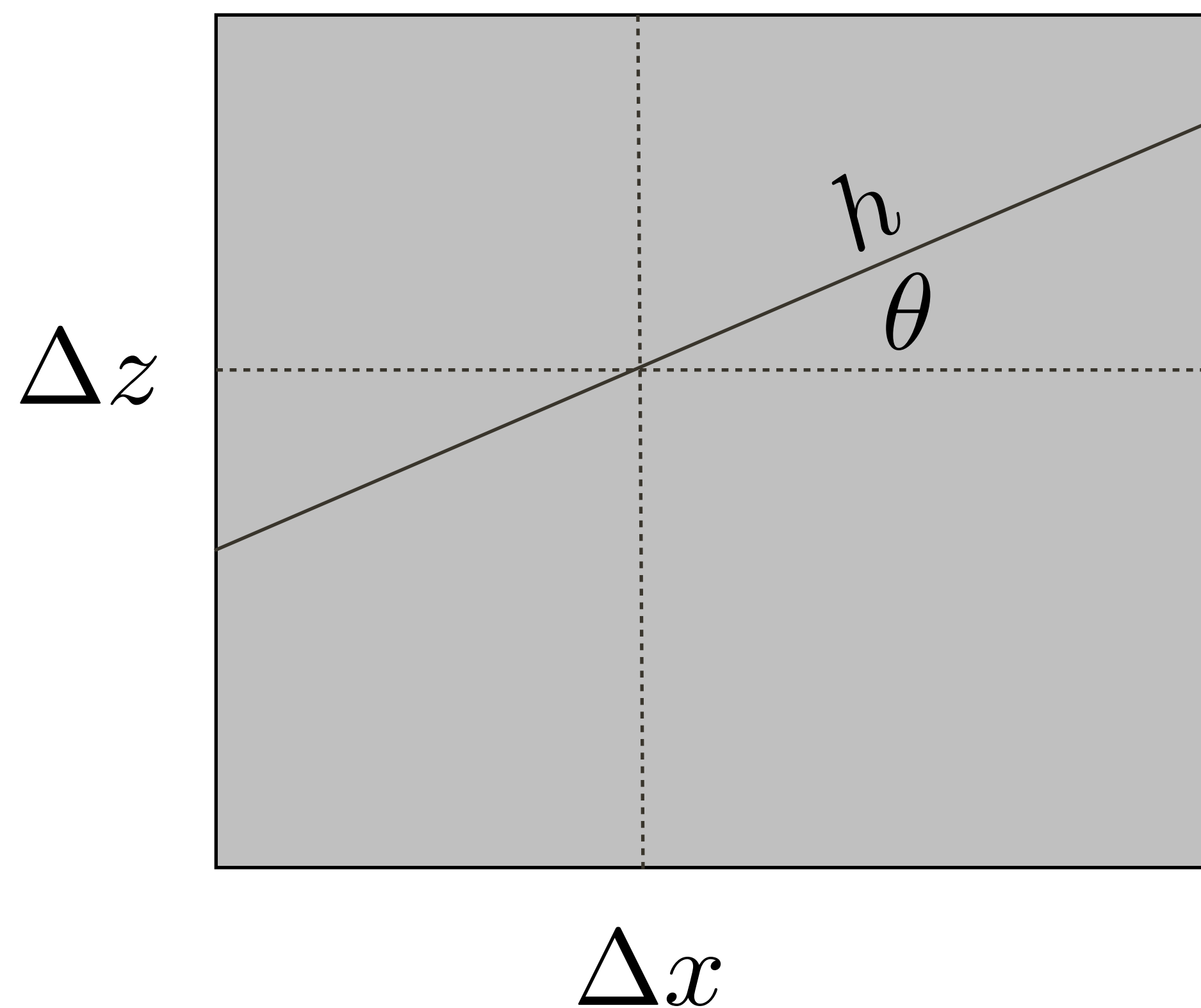
$N_h$  - # of subsurface offsets

$N_x$  - # of sample points



# Dip-angle gathers

*align subsurface offset with local dip*



# Dip-angle gathers

1. compute *image-point* gather

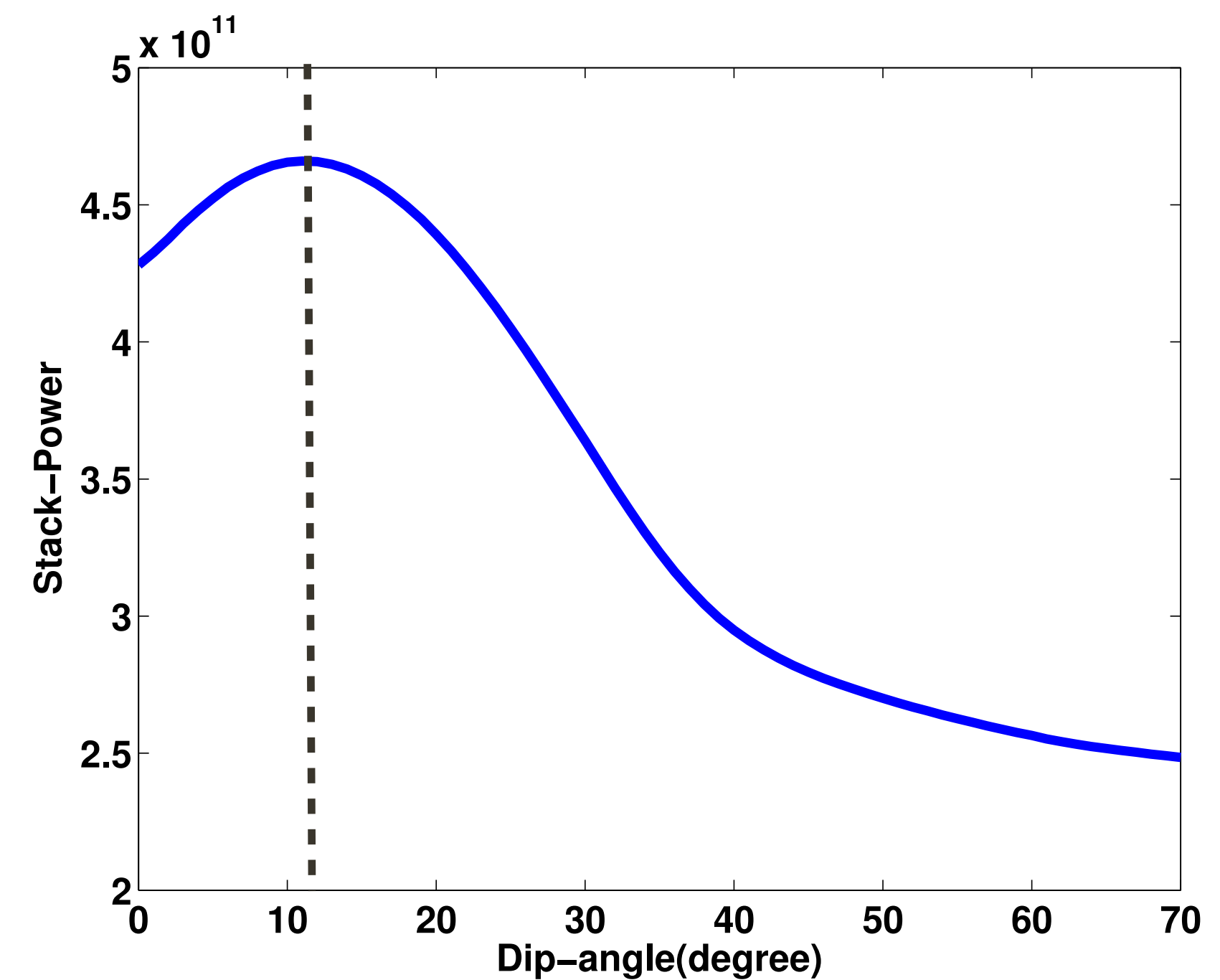
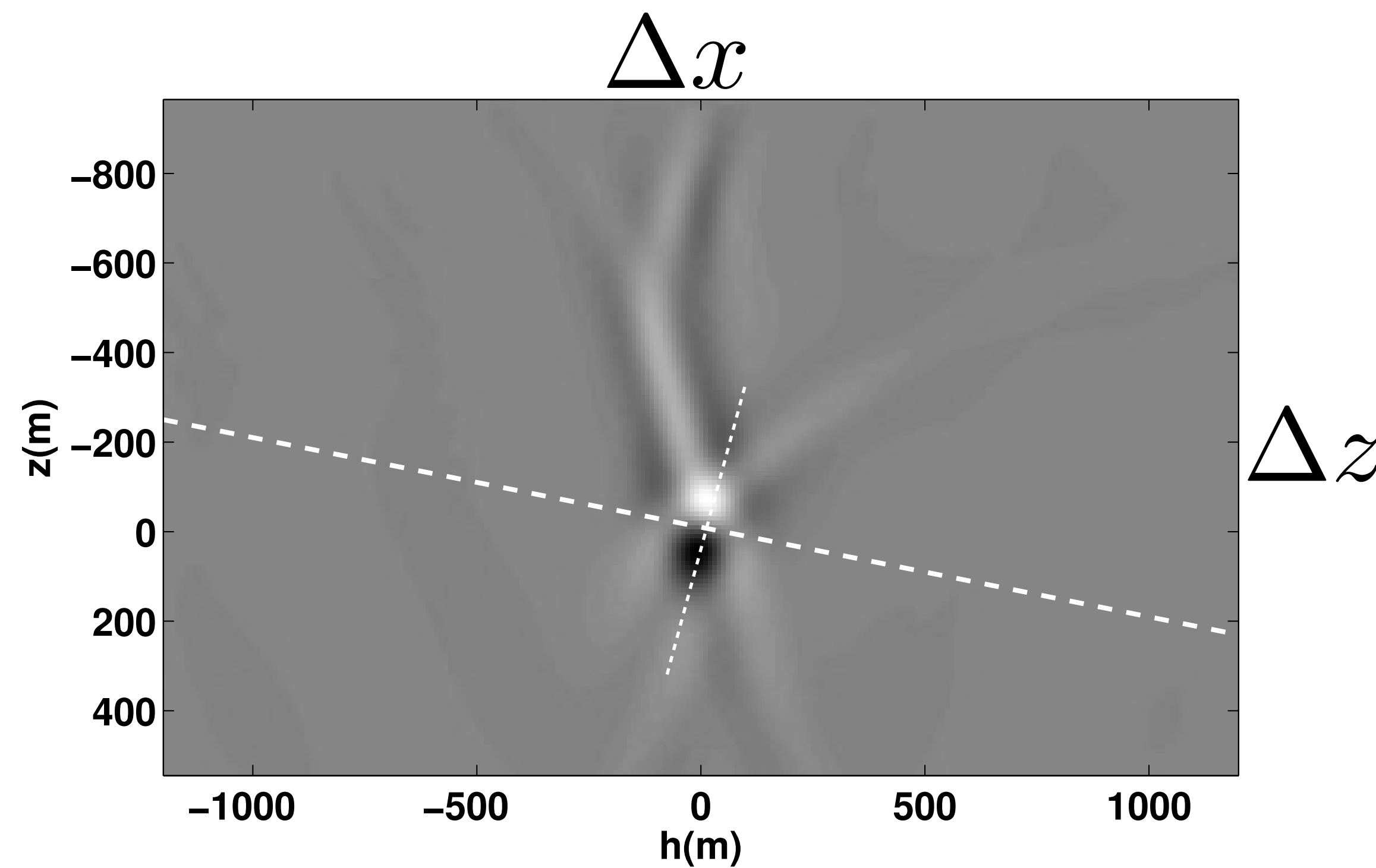
2. determine dip

$$\tilde{\theta} = \arg \max_{\theta} \sum_h \left| \sum_{\omega} e(\omega, \mathbf{x}_i, \mathbf{x}(h, \theta + \pi/2)) \right|$$

3. extract *offset* along *dip*

# Dip-angle gathers

the *dip* can be *detected* by measuring the *stackpower* normal to the *dip*



# Dip-angle gathers

Radon transform to compute *angle* gather

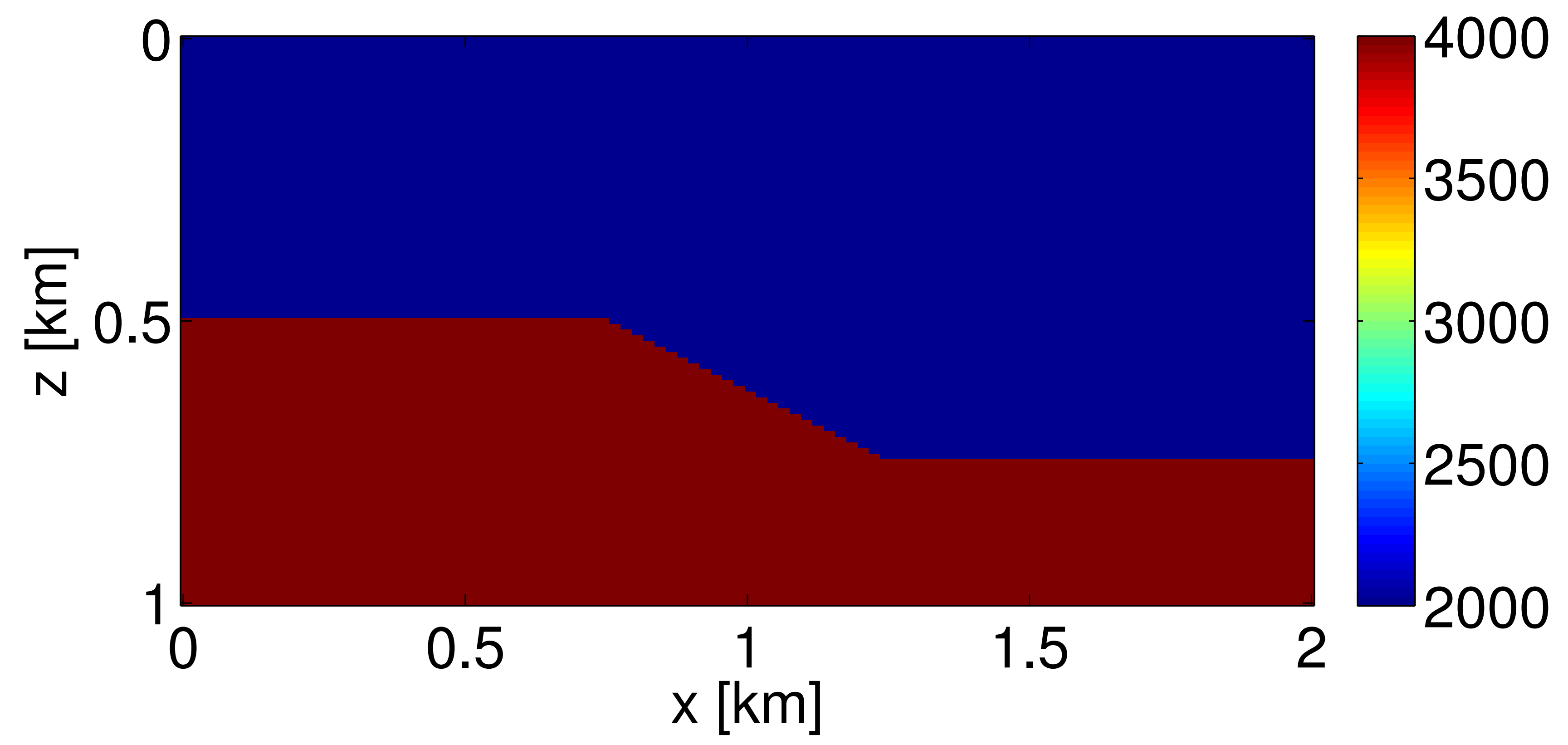
$$I(\mathbf{x}_i, p, \theta) = \sum_{\omega} \sum_h e(\omega, \mathbf{x}_i, \mathbf{x}(h, \theta)) e^{i\omega p h}$$

where

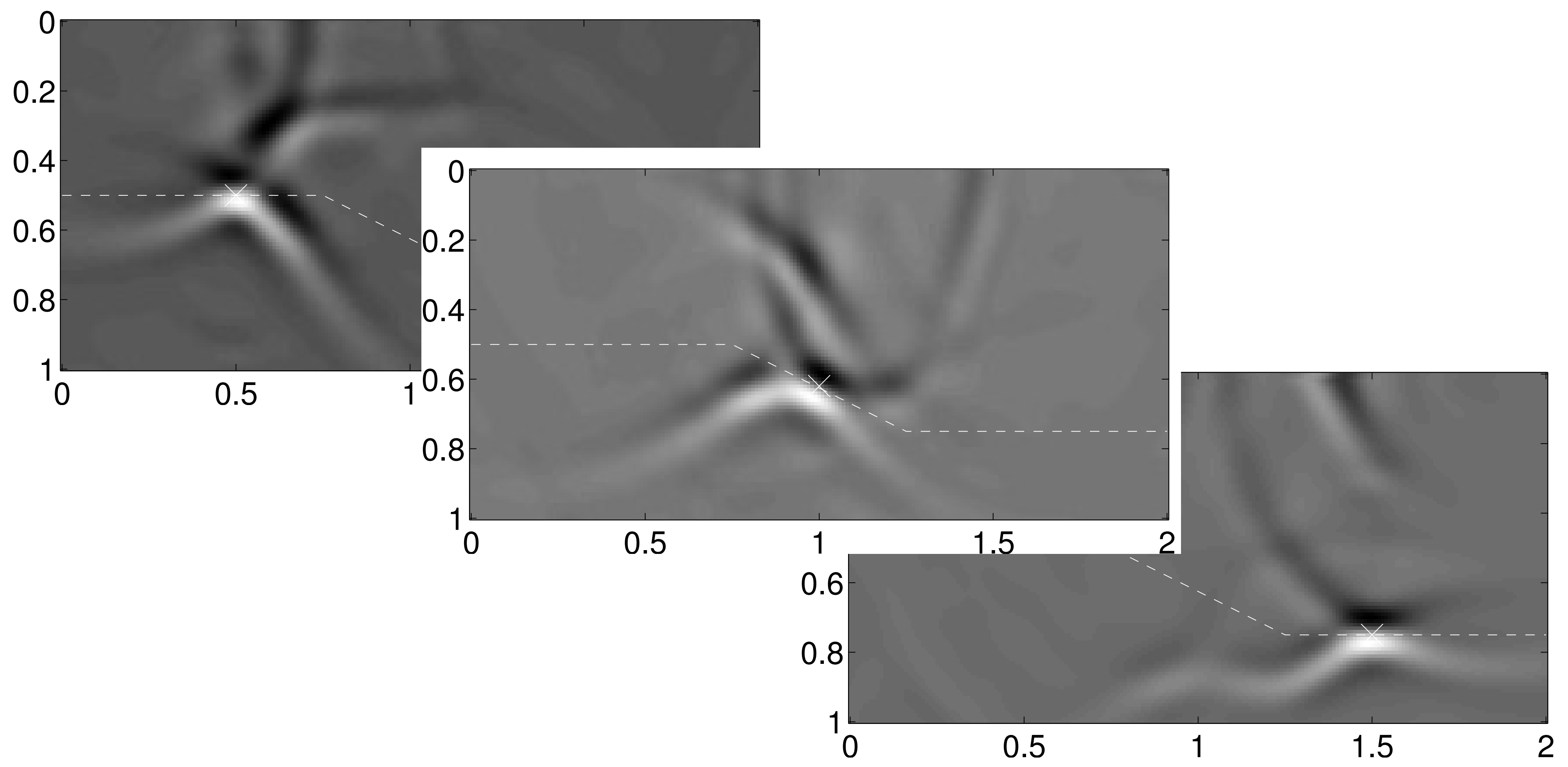
$$p = \frac{k_x}{\omega} = \frac{\sin(\alpha)}{v}$$

[de Bruin, 90]

# Dip-angle gathers

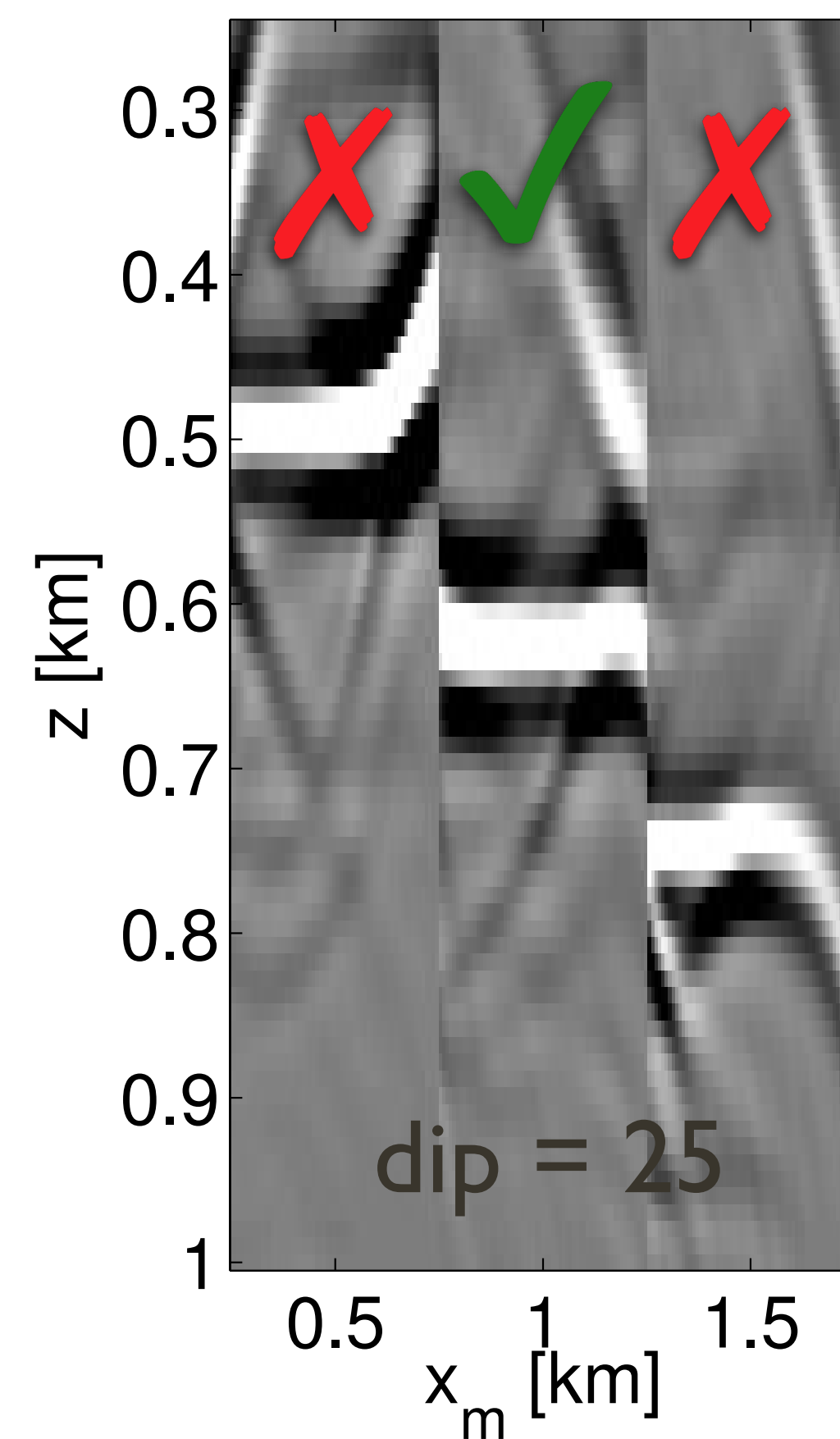
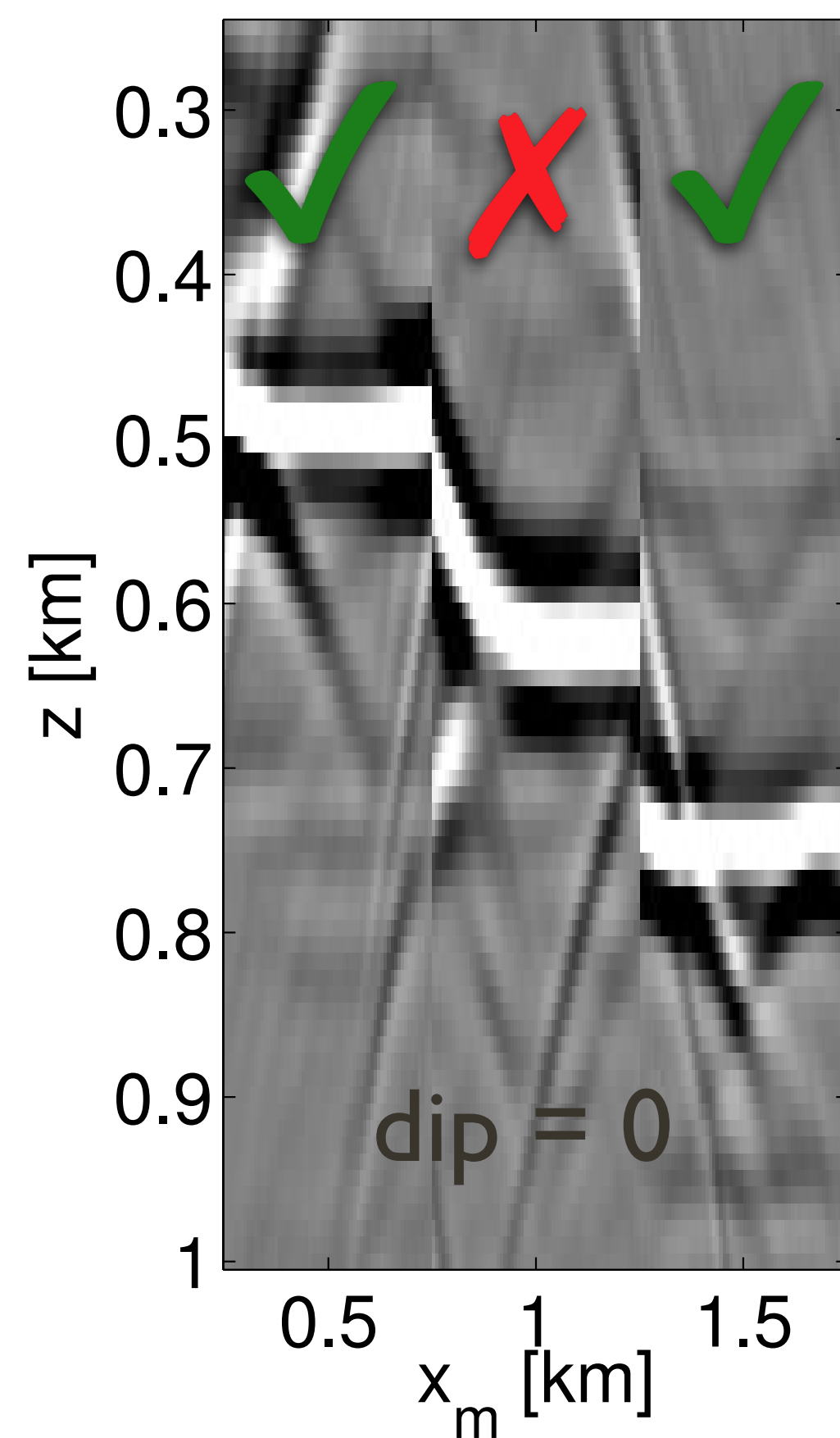


# Dip-angle gathers



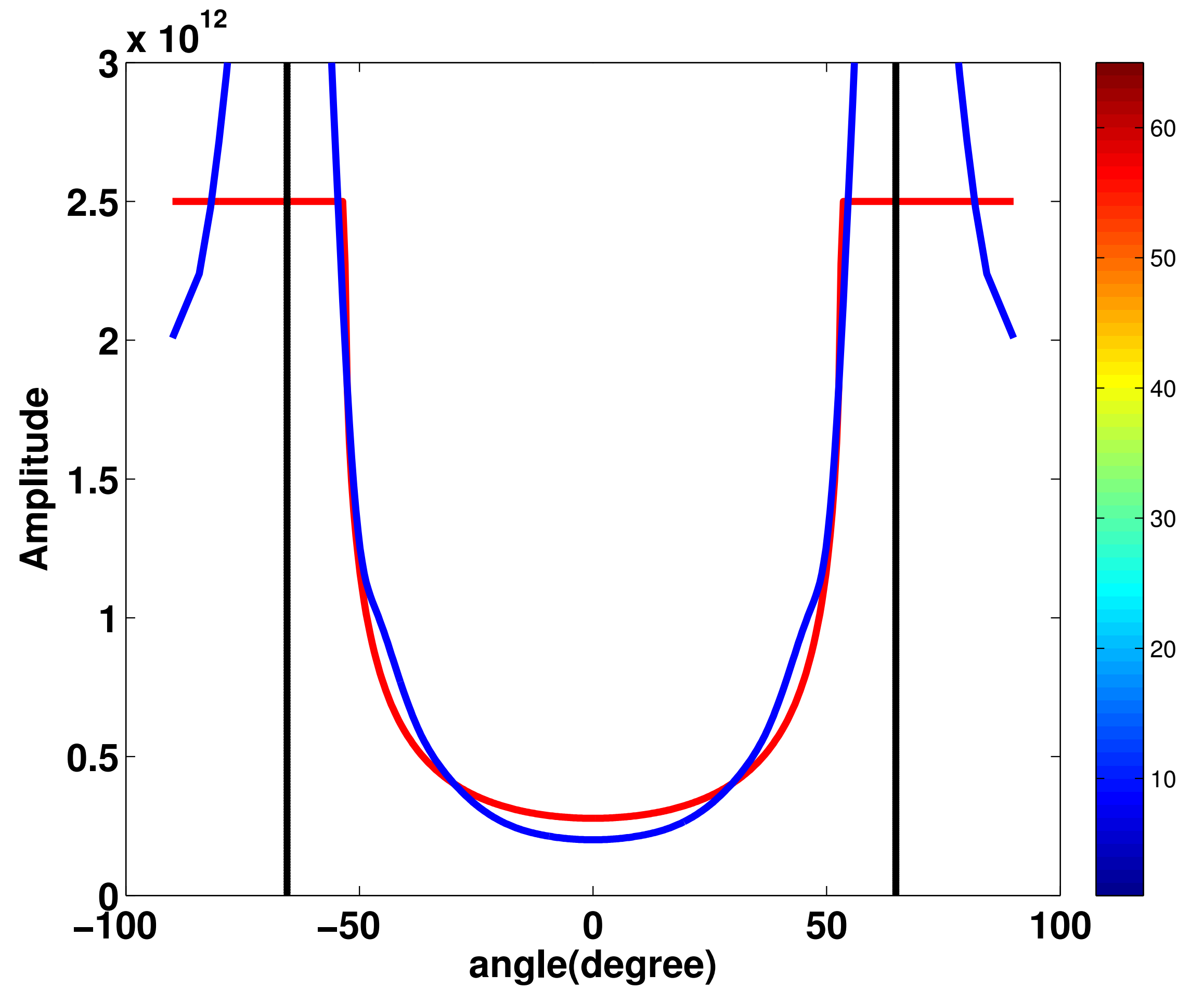
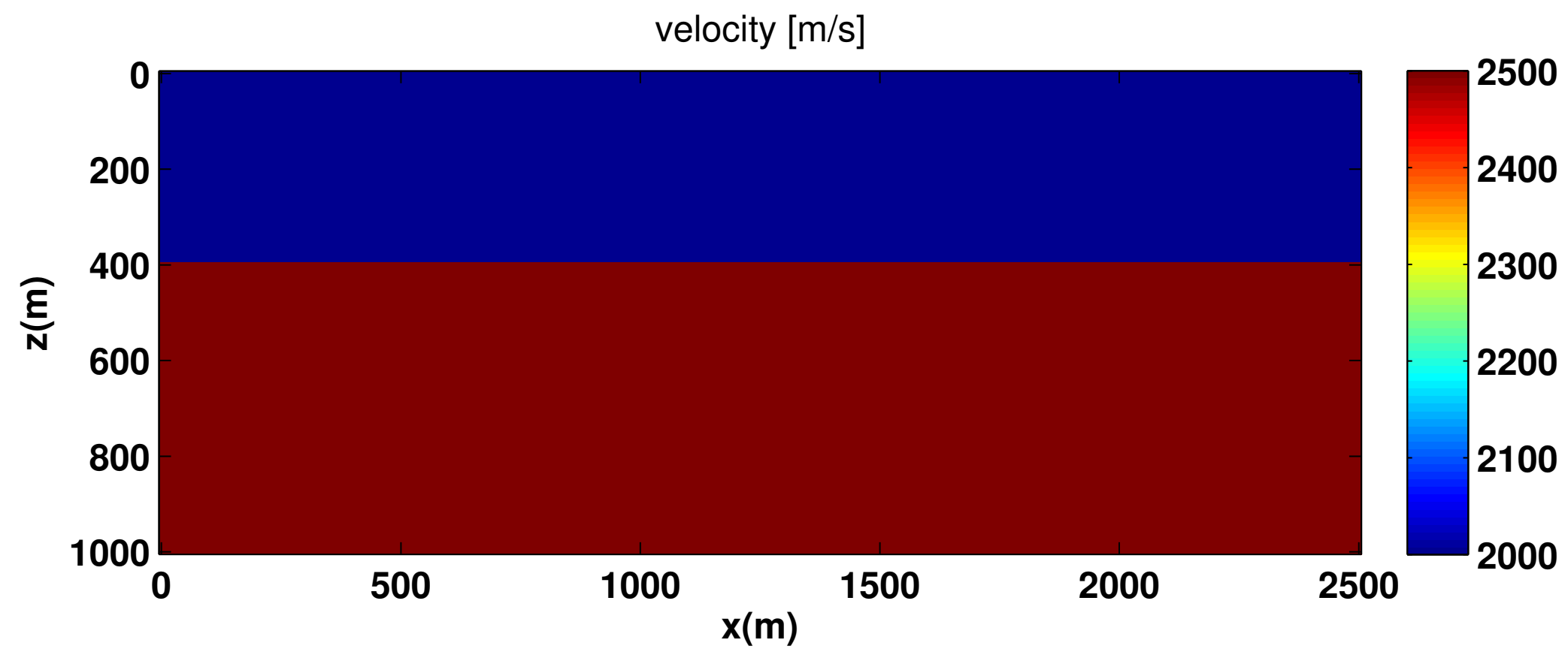
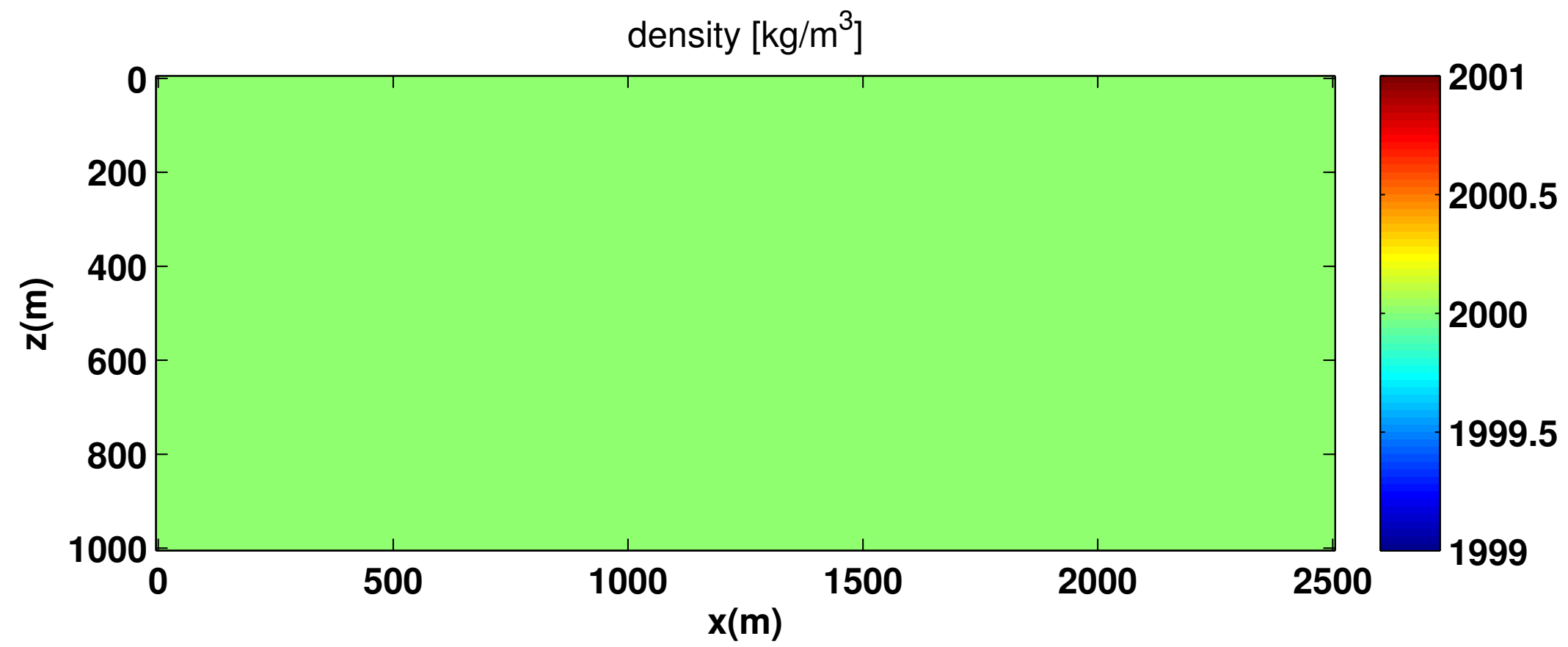
# Dip-angle gathers

angle gathers for *correct* velocity, should all be *flat*



# AVA

## [I-layer]

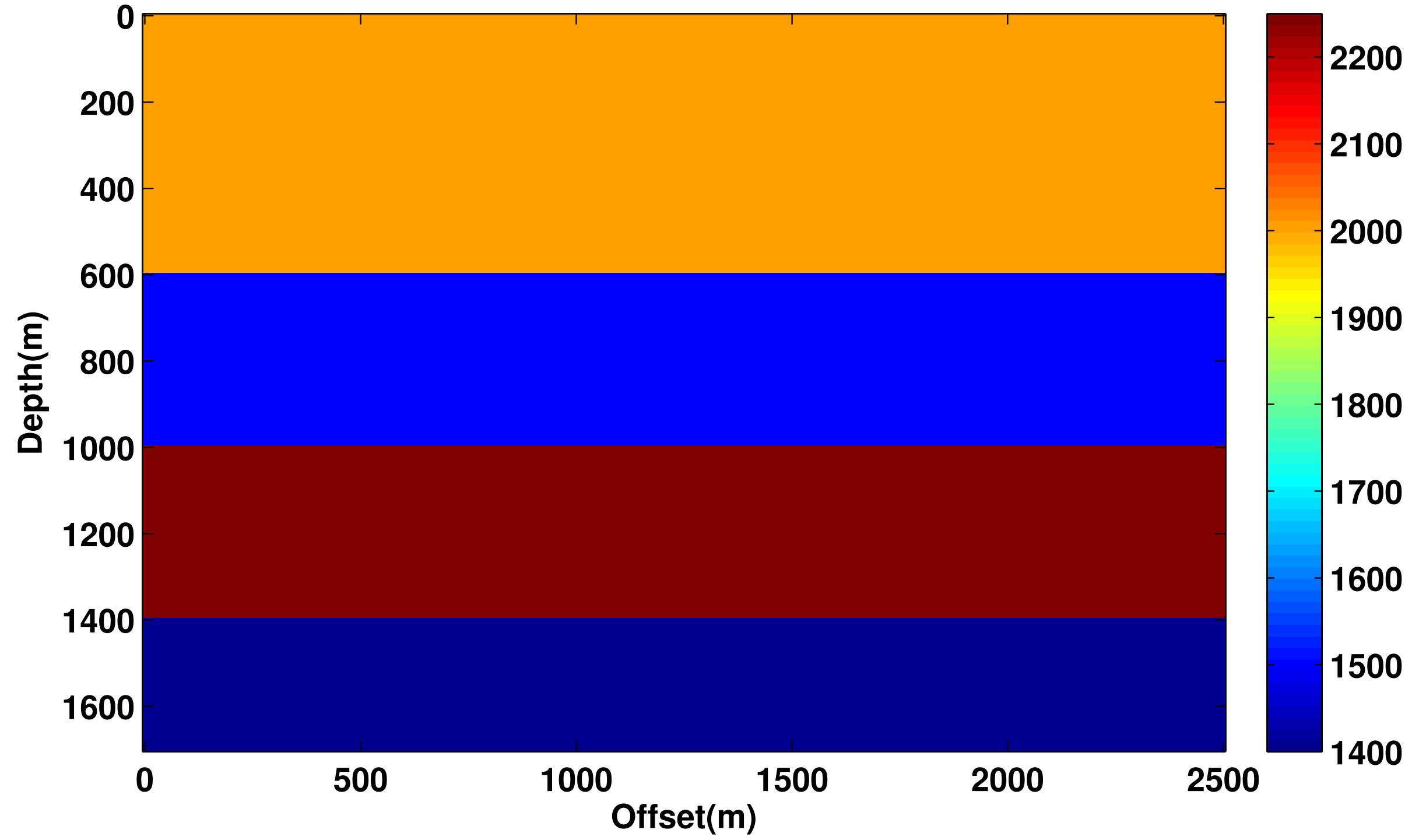




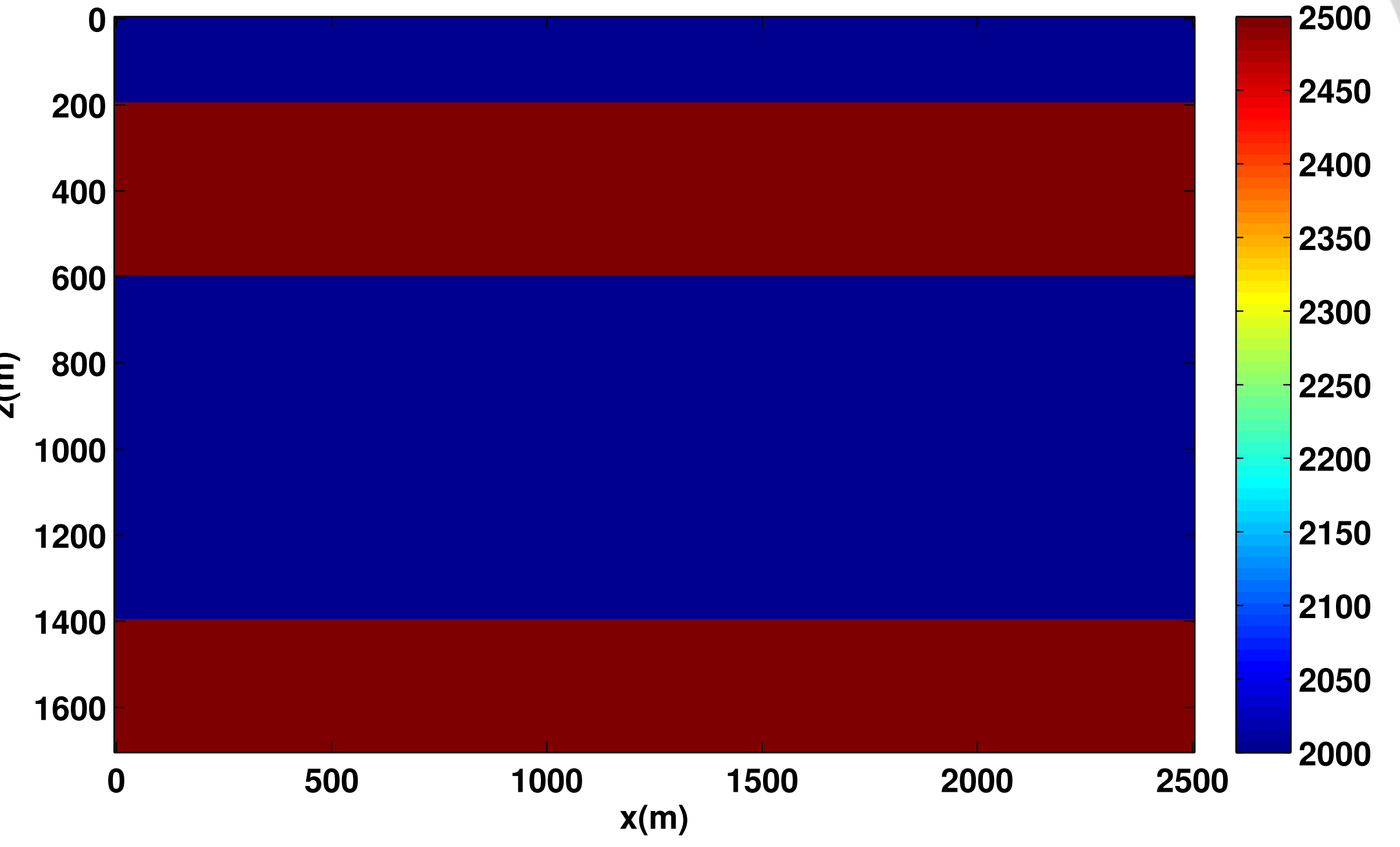
# AVA

## [4-layer]

density [kg/m<sup>3</sup>]

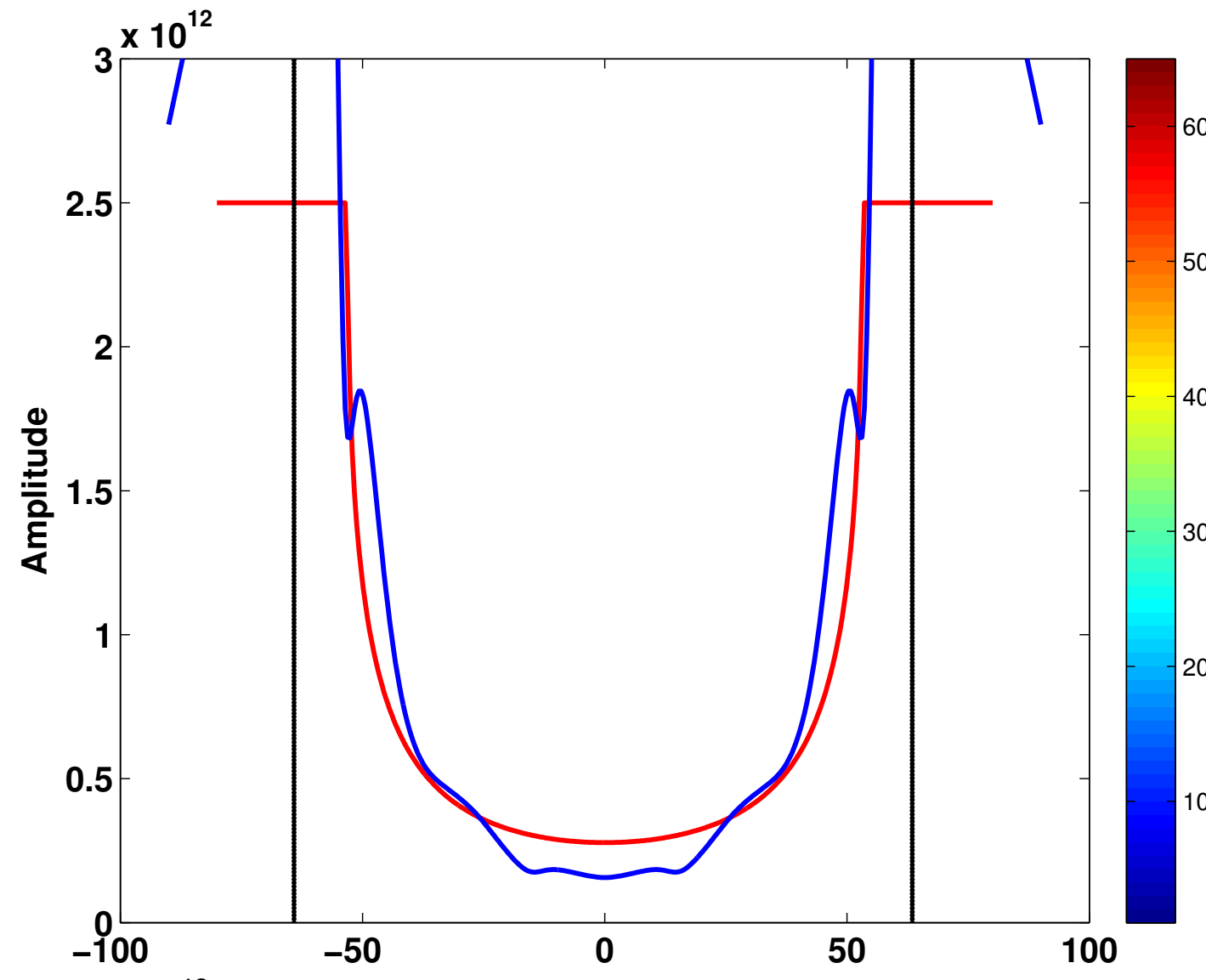


velocity [m/s]

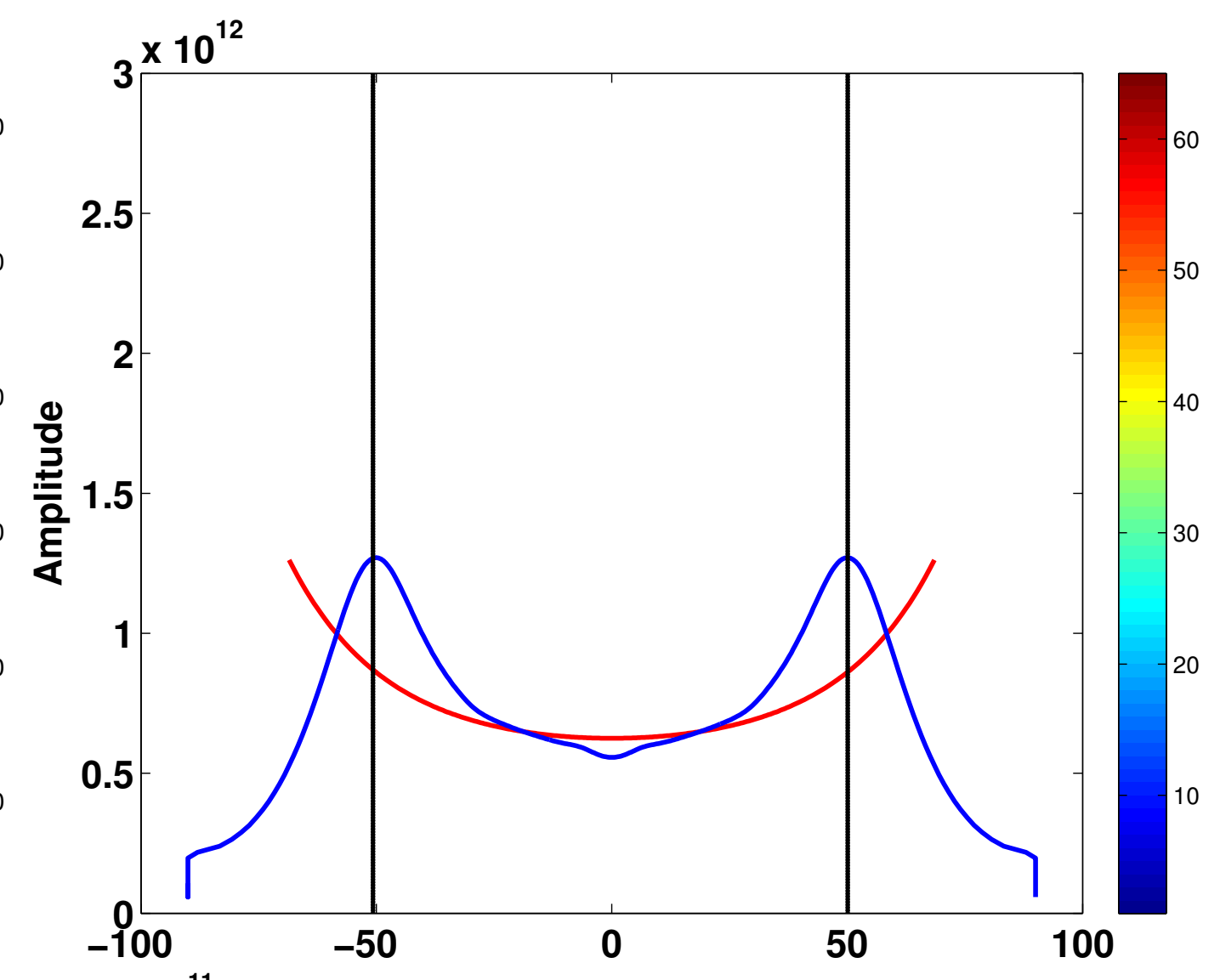


# AVA [4-layer]

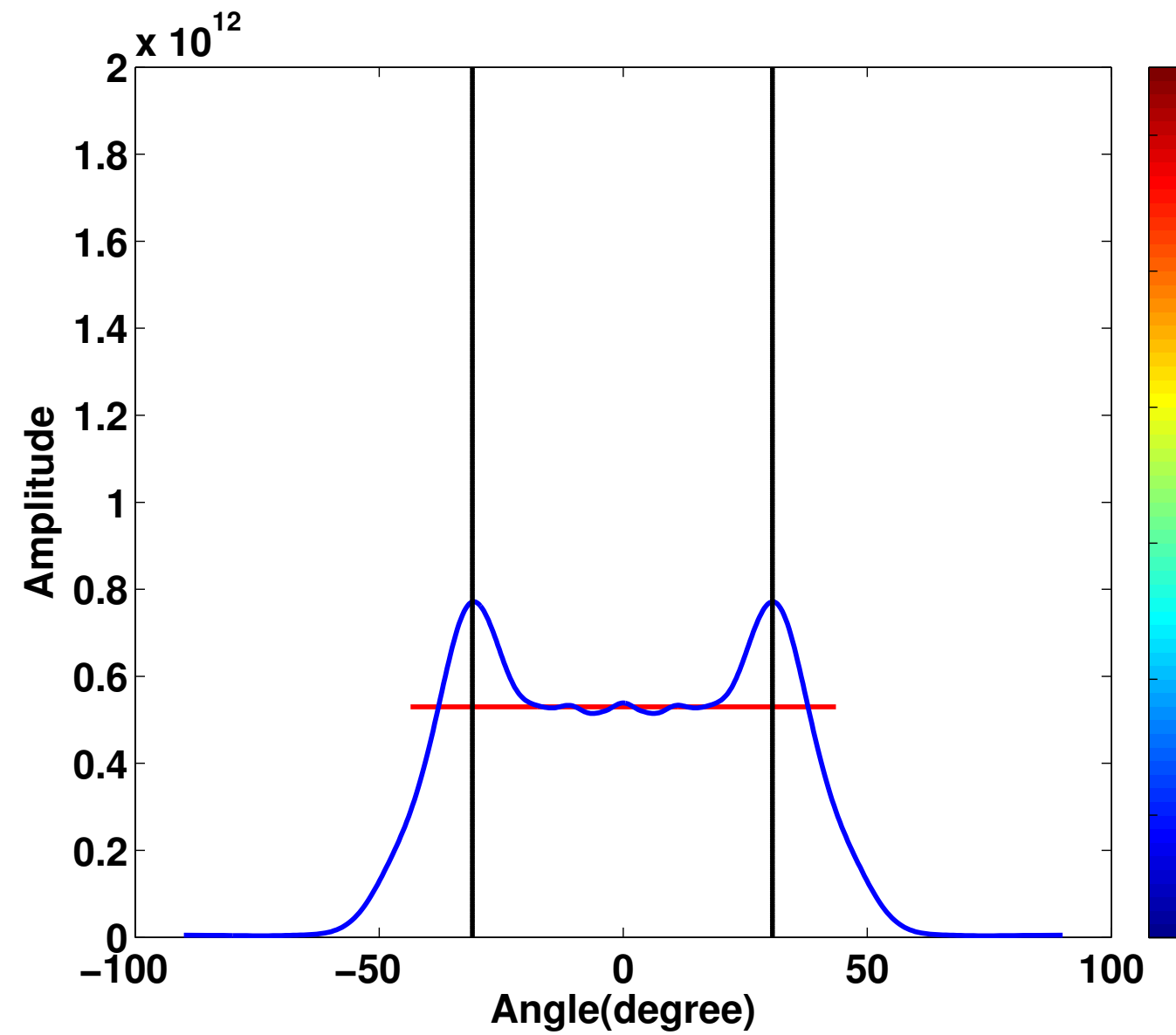
1st layer



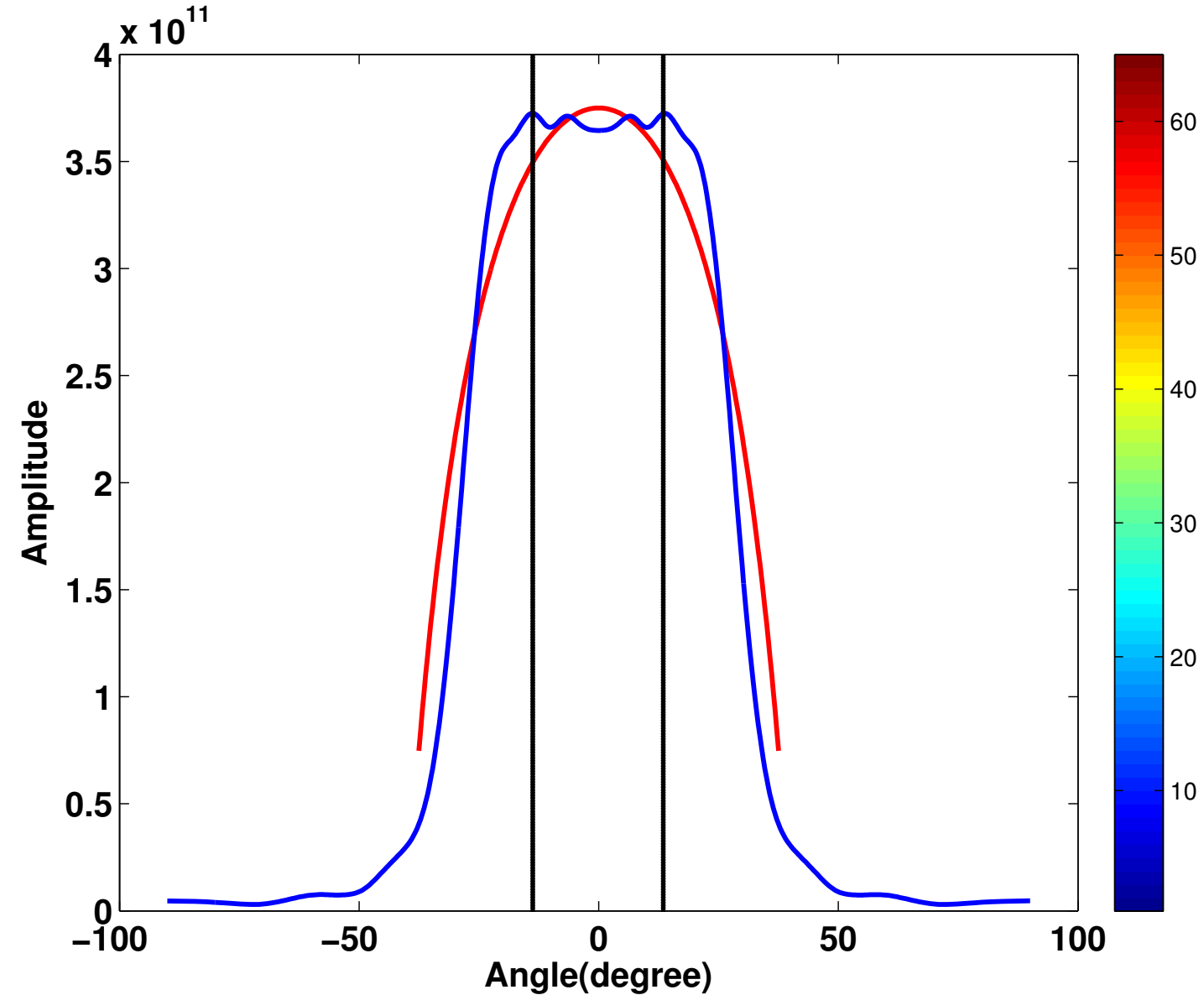
2nd layer



3rd layer

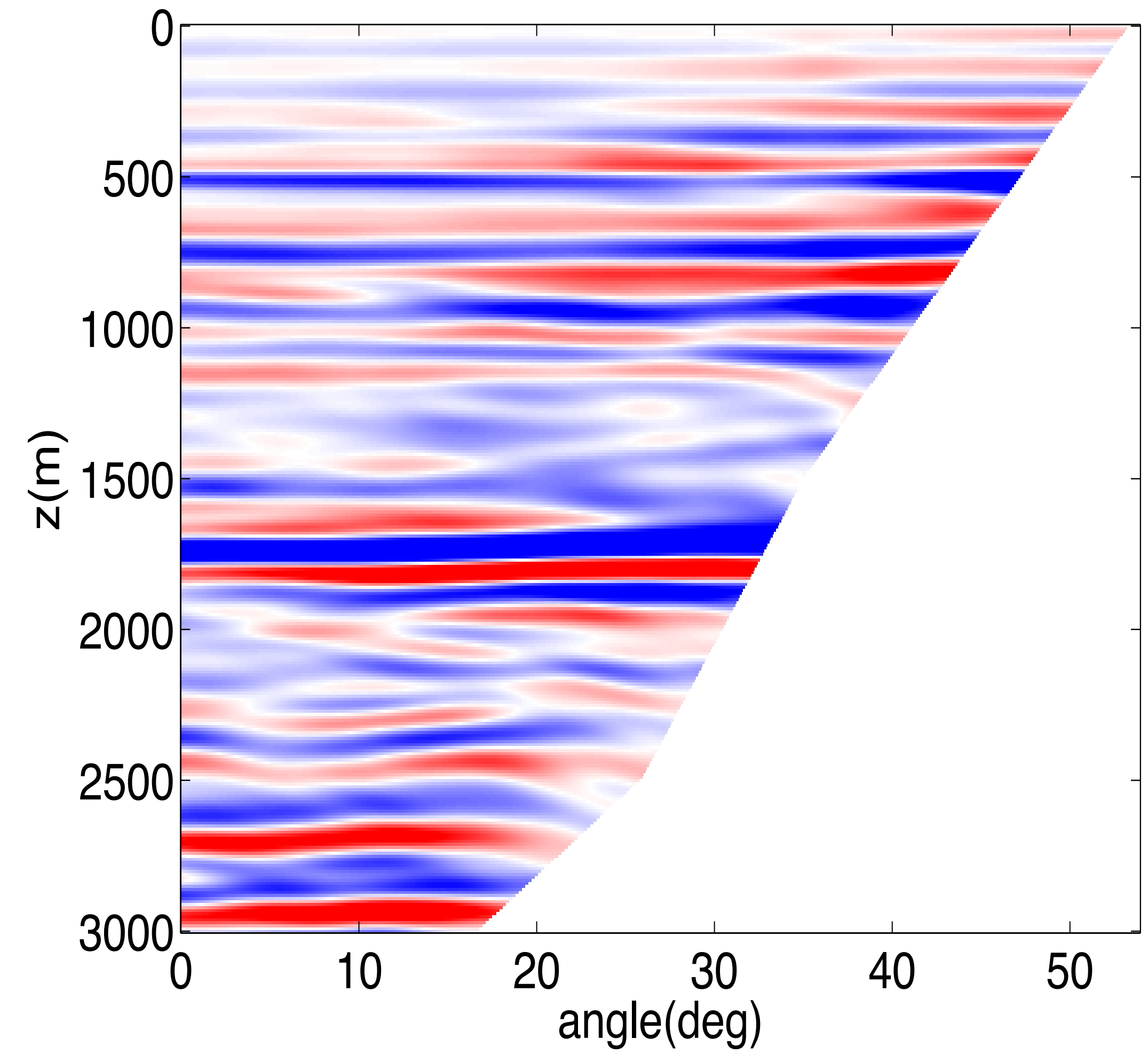
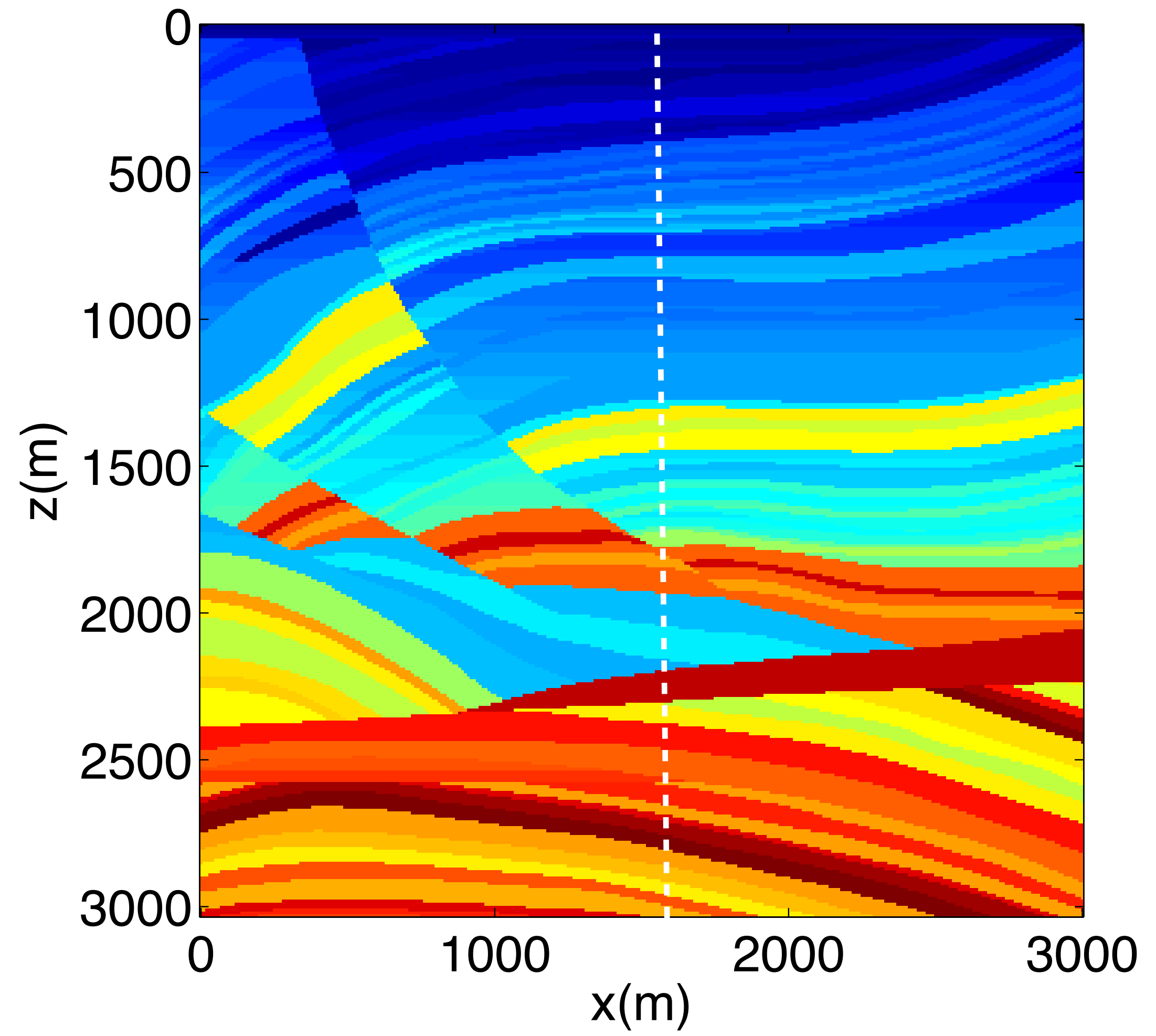


4th layer



# AVA

[marmousi model]



# Conclusion

- ▶ *Probe* image volume with *mat-vecs*
- ▶ Use *full* subsurface offsets, no need to estimate *dips a priori*
- ▶ *Suitable* for AVA at targeted regions
- ▶ estimate dip *automatically*

## Acknowledgements

Thank you for your attention !  
<https://www.slim.eos.ubc.ca/>



**W-11: Advances in Model Building, Imaging, and FWI,  
Friday, 27 September**

**Title : Efficient WEMVA using extended images**



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