

## Motivation

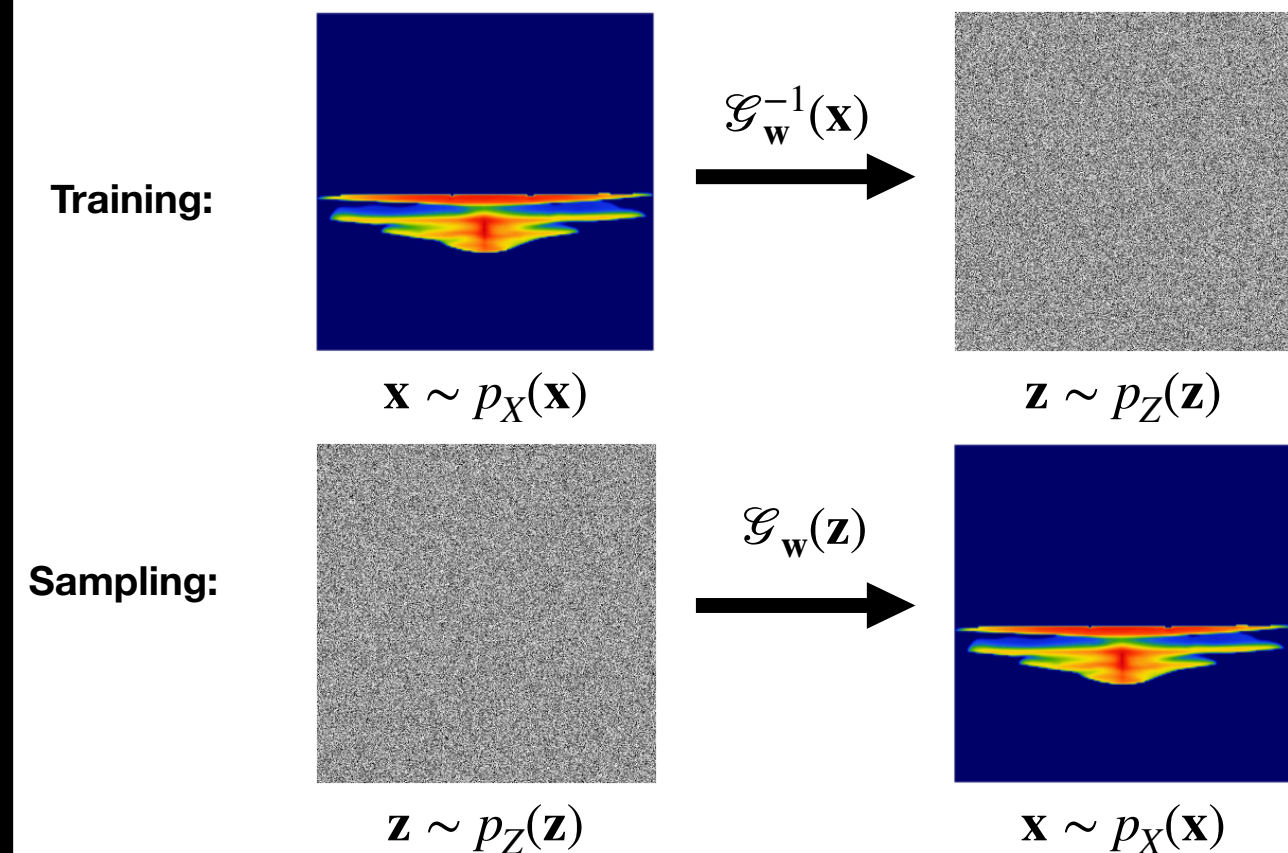
CO<sub>2</sub> plume forecasts with fluid-flow simulations alone are uncertain

- ▶ can **not** expect precise predictions of regular & irregular flow
- ▶ need to *condition* CO<sub>2</sub> plumes on observed monitoring data
- ▶ combine monitoring data w/ multiphase flow models

Calls for principled approach using ML & data assimilation to

- ▶ incorporate time-lapse well & seismic data *jointly*
- ▶ assess uncertainty in CO<sub>2</sub> plumes to *inform* policy decisions

## Conditional Normalizing Flows (CNF)



Train CNF on  $N$  training pairs  $\{\mathbf{x}^{(n)}, \mathbf{y}^{(n)}\}_{n=1}^N$  with

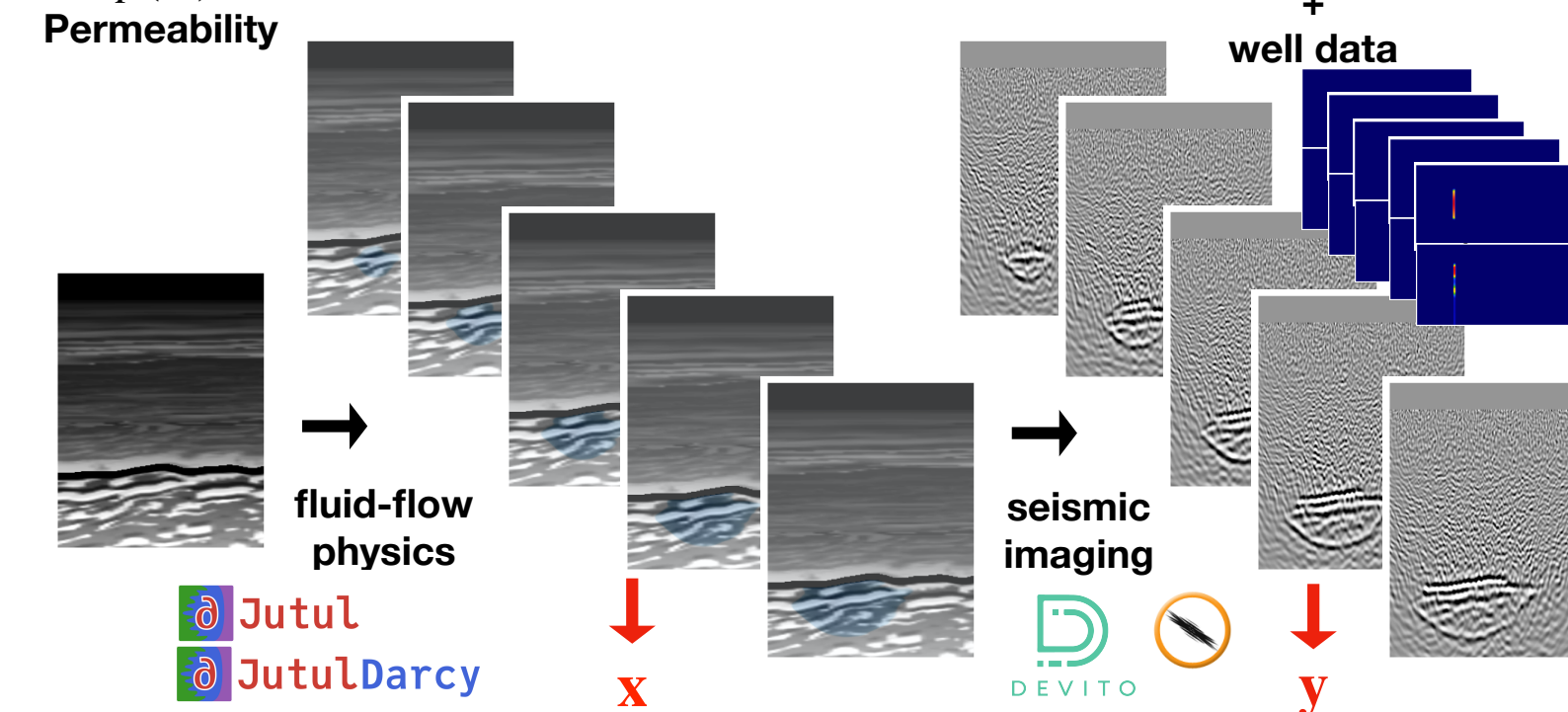
$$\hat{\theta} = \arg \min_{\theta} \frac{1}{N} \sum_{n=1}^N \left( \|f_{\theta}(\mathbf{x}^{(n)}; \mathbf{y}^{(n)})\|_2^2 - \log |\det \mathbf{J}_{f_{\theta}}| \right)$$

Trained invertible network  $p_{\hat{\theta}}(\mathbf{x} | \mathbf{y}) \approx p(\mathbf{x} | \mathbf{y})$  and turn, conditioned on any  $\mathbf{y}$ ,

- ▶ samples of  $\mathbf{x}$  into noise – i.e.,  $f_{\hat{\theta}}(\mathbf{x}; \mathbf{y}) \sim N(0, I)$
- ▶ noise samples  $\mathbf{z} \sim N(0, I)$  into samples  $\mathbf{x} \sim p_{\hat{\theta}}(\mathbf{x} | \mathbf{y}^{\text{obs}})$  where  $\mathbf{x} = f_{\hat{\theta}}^{-1}(\mathbf{z}; \mathbf{y}^{\text{obs}})$



## Dataset Simulation

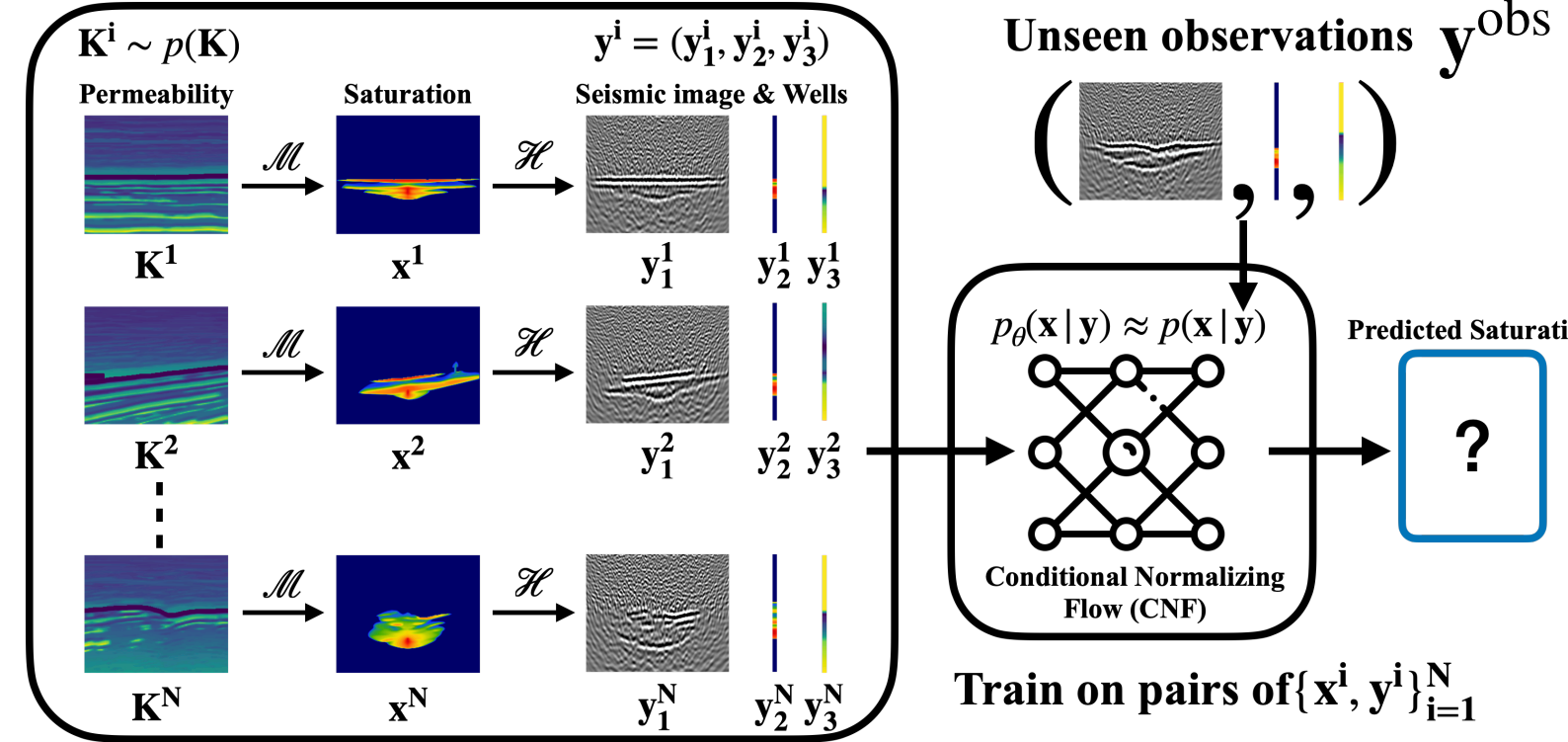


**CO<sub>2</sub> plume simulations:**

- ▶ draw permeability realization  $\mathbf{K} \sim p(\mathbf{K})$
- ▶ inject 1.2 MT CO<sub>2</sub> annually
- ▶ simulations output every 80 days

**Monitoring:**

- ▶ saturation & pressure data collected at injection & production wells
- ▶ time-lapse seismic images from 200 receivers (20m) & 8 sources (500m)

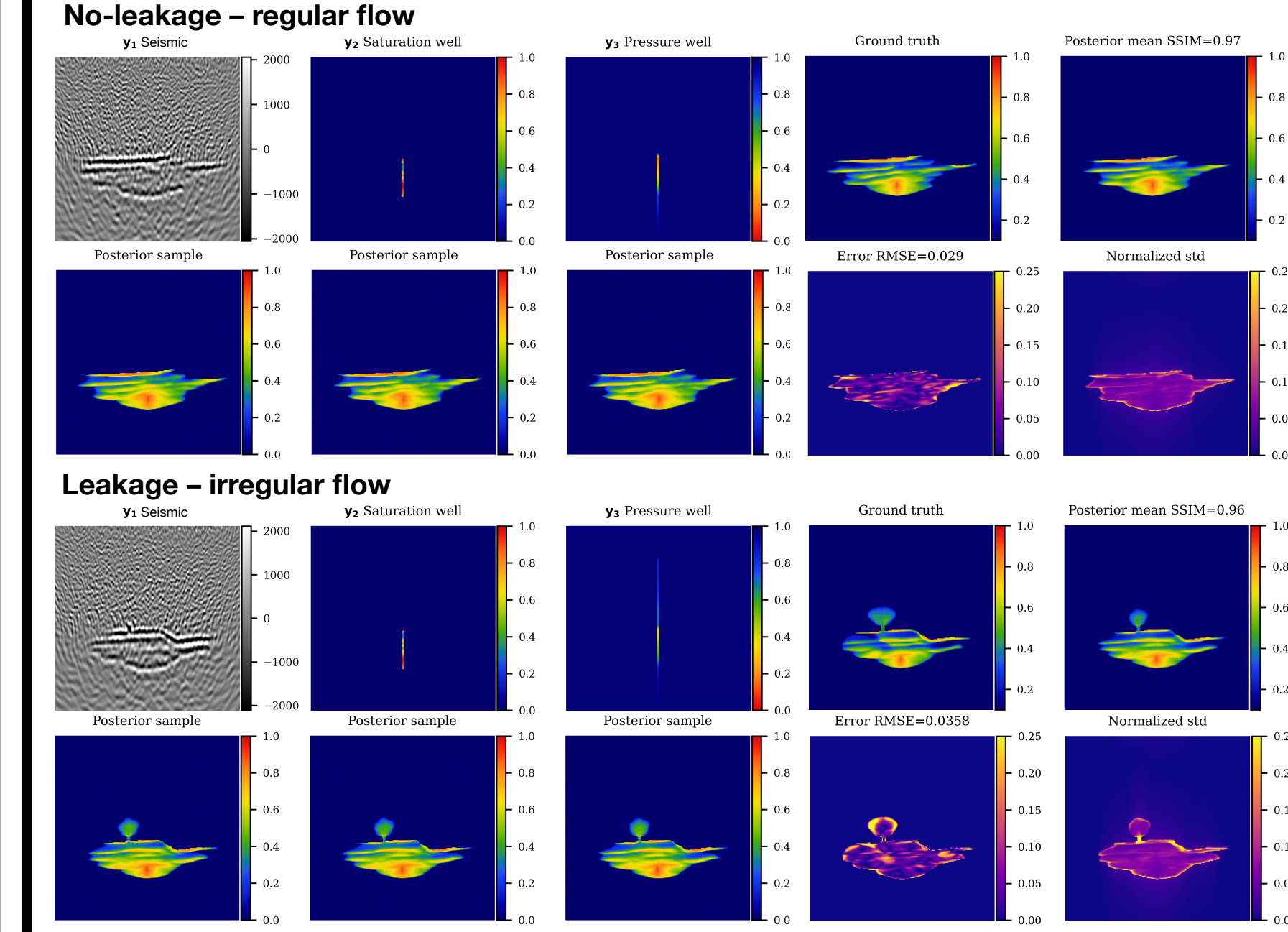


$\mathcal{M}$  – dynamics operator  $\mathcal{H}$  – observation operator  $\mathbf{K}$ – permeability model  $\mathbf{y}^{\text{obs}}$  – time-lapse observations

**Training & inference:**

- ▶ CNF is trained on simulated pairs CO<sub>2</sub> saturation  $\mathbf{x}$  & time-lapse data  $\mathbf{y}$
- ▶  $\mathbf{y} = (y_1, y_3, y_3)$  w/ seismic surface & saturation/pressure data at well
- ▶ At inference, CNF generates CO<sub>2</sub> plume predictions  $\mathbf{x} \sim p(\cdot | \mathbf{y}^{\text{obs}})$

## Results



**Observations:**

- ▶ conditional mean remains close to ground truth – high SSIM & low RMSE
- ▶ uncertainty (normalized std) is higher in geologically complex areas – top of the plume – fracture zone where CO<sub>2</sub> leaks
- ▶ uncertainty correlates well w/ errors compared to ground truth

## Conclusions

**Inference framework:**

- ▶ robust w.r.t to noise & uncertainties in permeability
- ▶ capable of predicting leakage w/ observed time-lapse data

**Future work:**

- ▶ perform sequential Bayesian inference
- ▶ assimilate time-lapse observations & monitor for early leakage

## References

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