


# Derisking Geological Storage w/ simulation-based seismic monitoring design & machine learning

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SLIM   
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ML4Seismic



Georgia Tech College of Computing  
School of Computational  
Science and Engineering



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School of Earth and  
Atmospheric Sciences



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# Derisking Geological Storage w/ simulation-based seismic monitoring design & machine learning

Huseyin Tuna Erdinc<sup>1</sup>, Abhinav Prakash Gahlot<sup>2</sup>, Ziyi Yin<sup>3</sup>, Mathias Louboutin<sup>2</sup>, Felix J. Herrmann<sup>1,2,3</sup>

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# Challenges

## monitoring Geological CO<sub>2</sub> Storage in Saline Aquifers

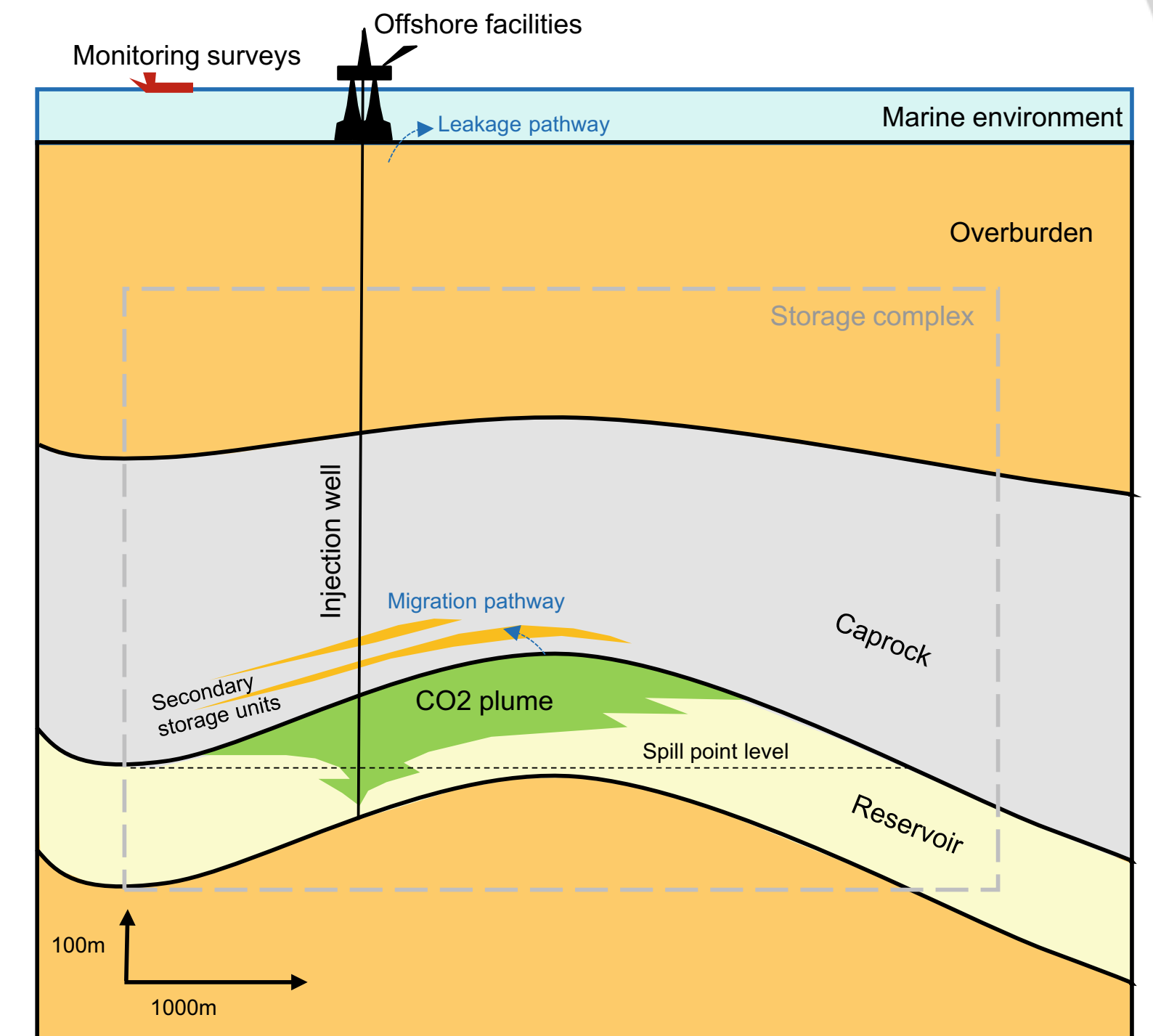
**Regulators & general public require transparency & assurances that *supercritical CO<sub>2</sub>* stays put in the *storage complex***

- ▶ *reservoir* simulations alone are *uncertain* due to large *variability* permeability
- ▶ risk profile storage & containment highest at start & at end
- ▶ there is a need for *reproducibility*

**Develop low-cost time-lapse seismic system to monitor CO<sub>2</sub> plumes**

- ▶ maximally captures information collected over many decades
- ▶ low-cost by being sparse w/o insisting on replication of surveys
- ▶ attains accuracy needed to detect early onset leakage *automatically*
- ▶ *collect 1–2 orders of magnitude cheaper over a century*

**Systematic assessment of risks using techniques from uncertainty quantification.**



from Ringrose

# Risk profiles

## Uncertainties & risk storage model

- ▶ *highest at start*
- ▶ diminish when *more* time-lapse data is *collected*

## Containment risk increases

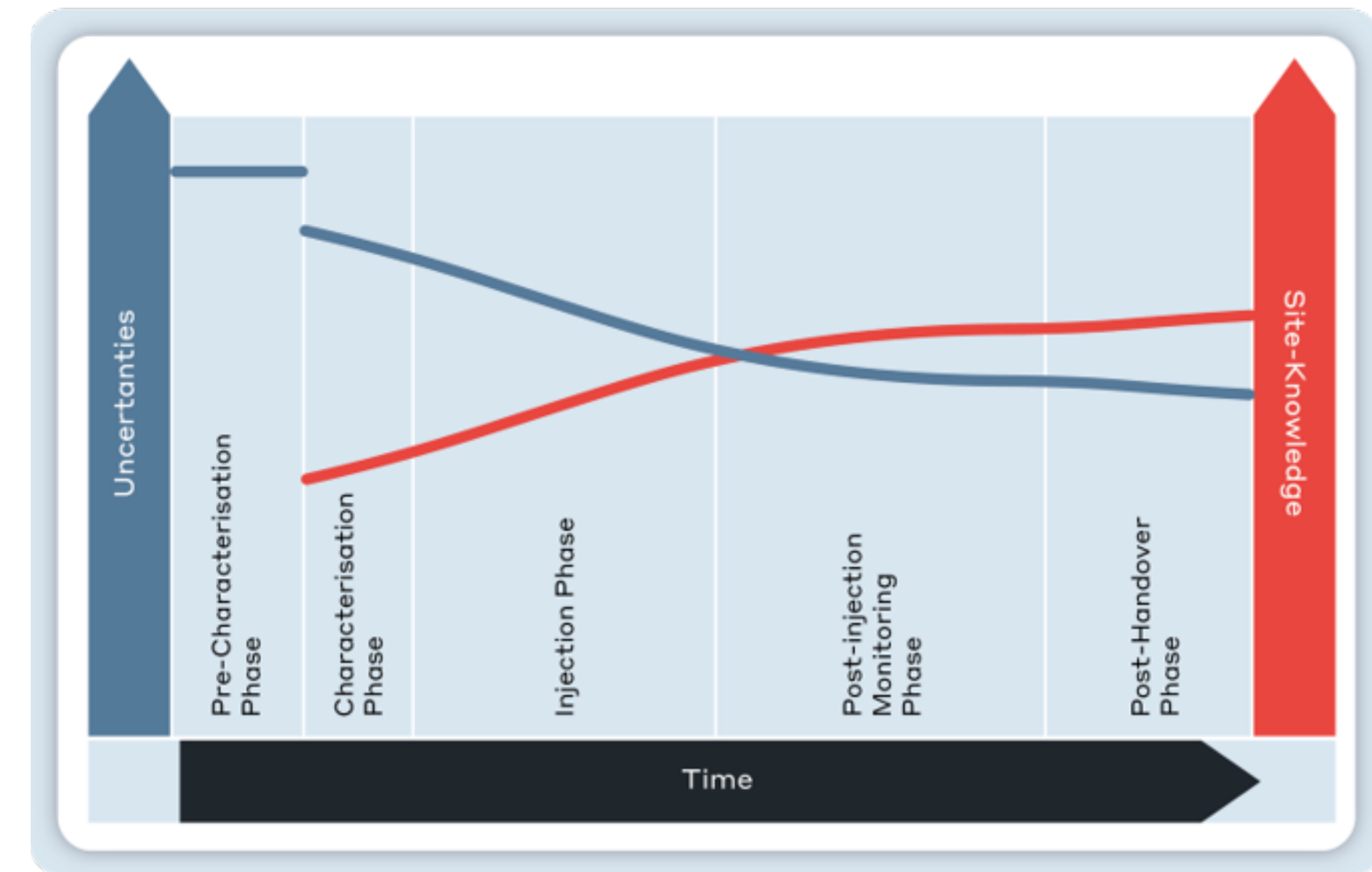
- ▶ *w/ amount* of CO<sub>2</sub> stored
- ▶ *w/ size area* undergoing *pressure* changes

There can be **NO** lapse in *monitoring* because

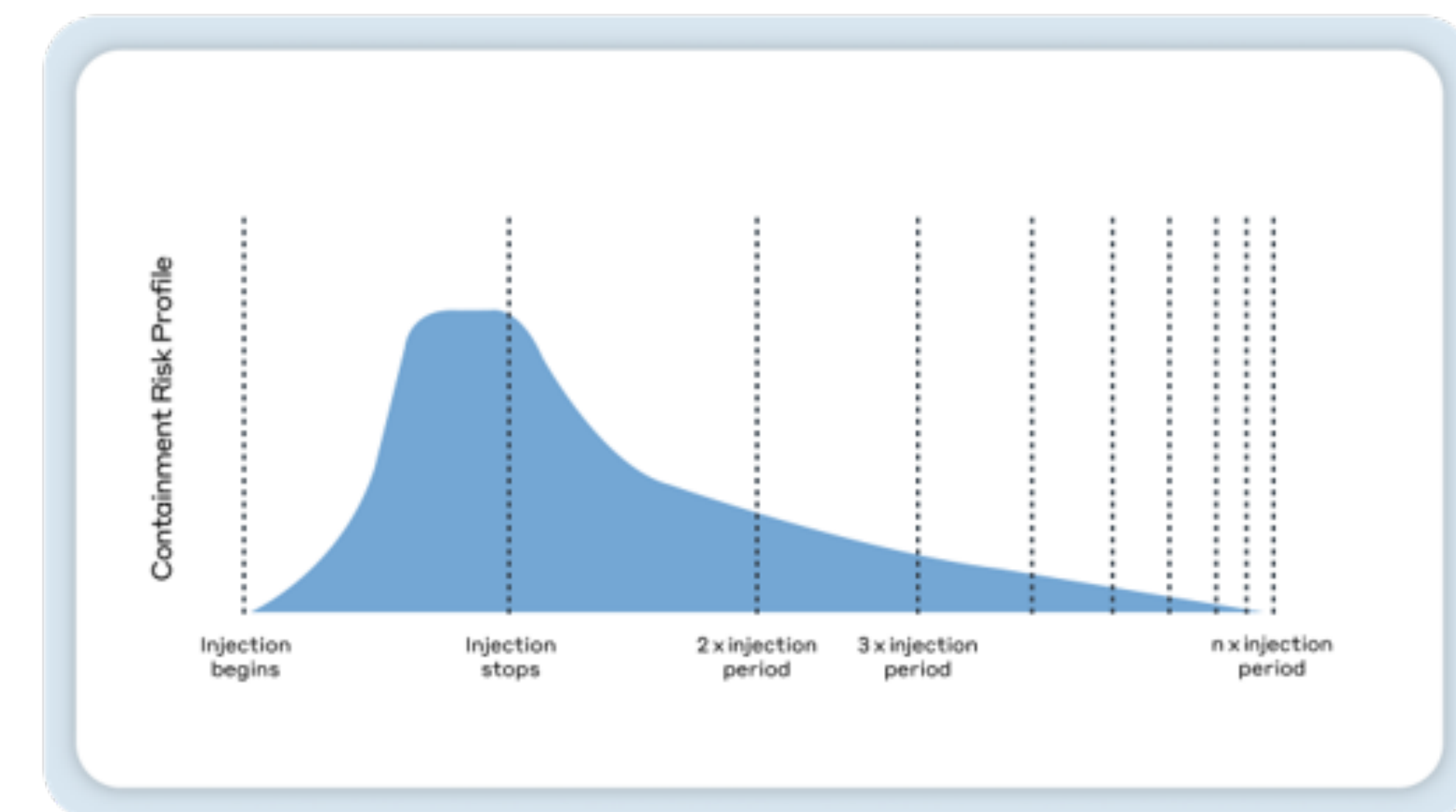
- ▶ any lack of *transparency* conformance
- ▶ will lead in loss in *confidence* by the *general* public

**High-fidelity time-lapse information needs to be collected regularly over long periods of time!**

## uncertainty profile



## containment risk profile



# Workflow simulation-based seismic monitoring design

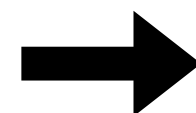
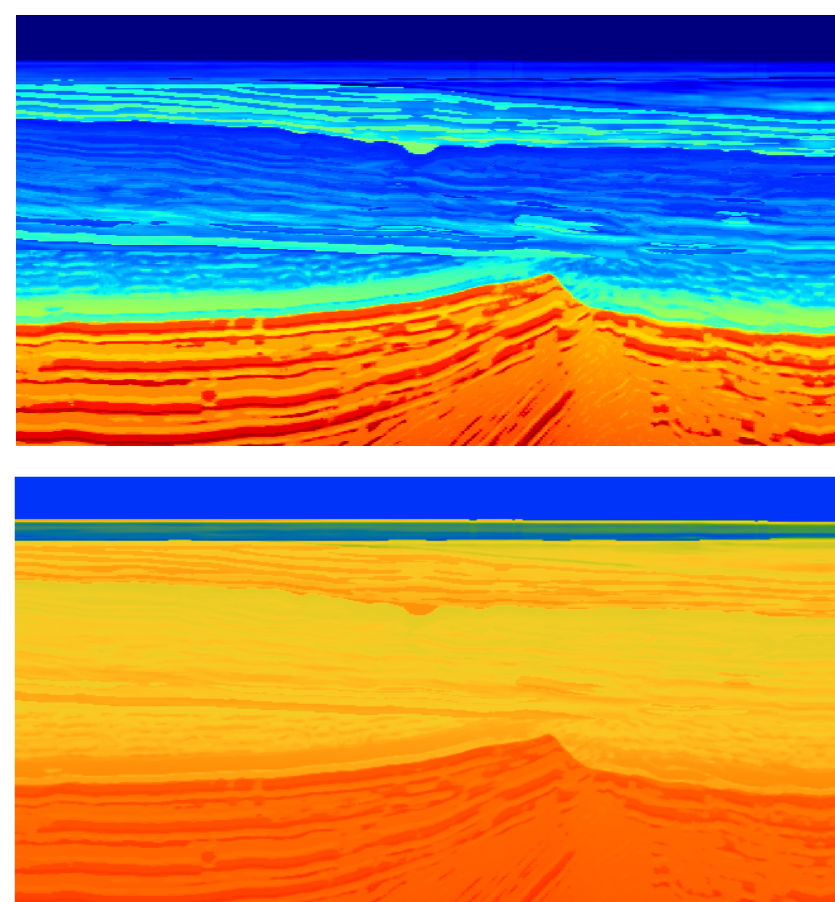
Ziyi Yin, Huseyin Tuna Erdinc, Abhinav Prakash Gahlot, Mathias Louboutin and F. Herrmann. “Derisking geological carbon storage from high-resolution time-lapse seismic to explainable leakage detection.” *The Leading Edge* (2023).



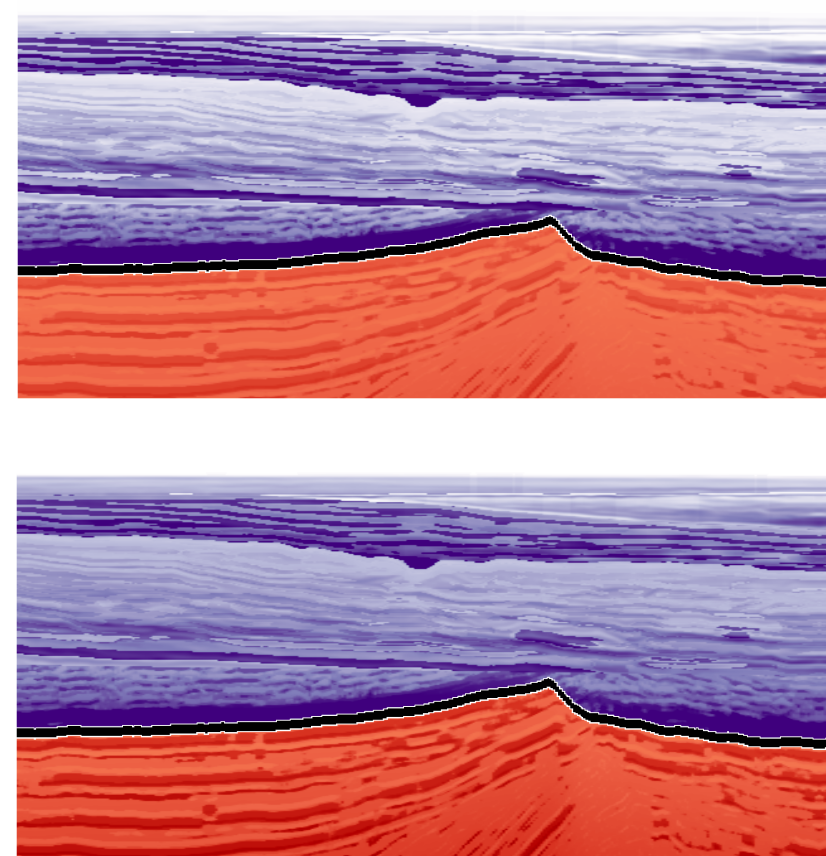
# Workflow

Ziyi Yin, Huseyin Tuna Erdinc, Abhinav Prakash Gahlot, Mathias Louboutin and F. Herrmann. "Derisking geological carbon storage from high-resolution time-lapse seismic to explainable leakage detection." The Leading Edge (2023).

proxy model  
wavespeed, density



reservoir model  
permeability, porosity



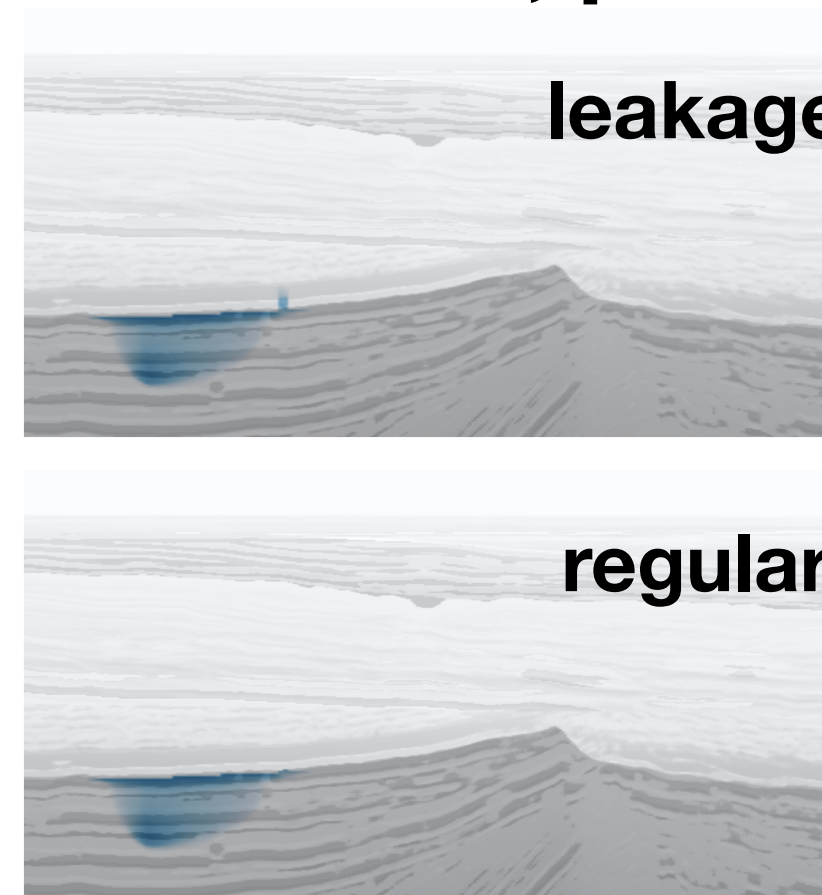
pressure  
induced  
fault



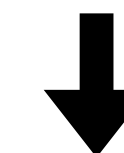
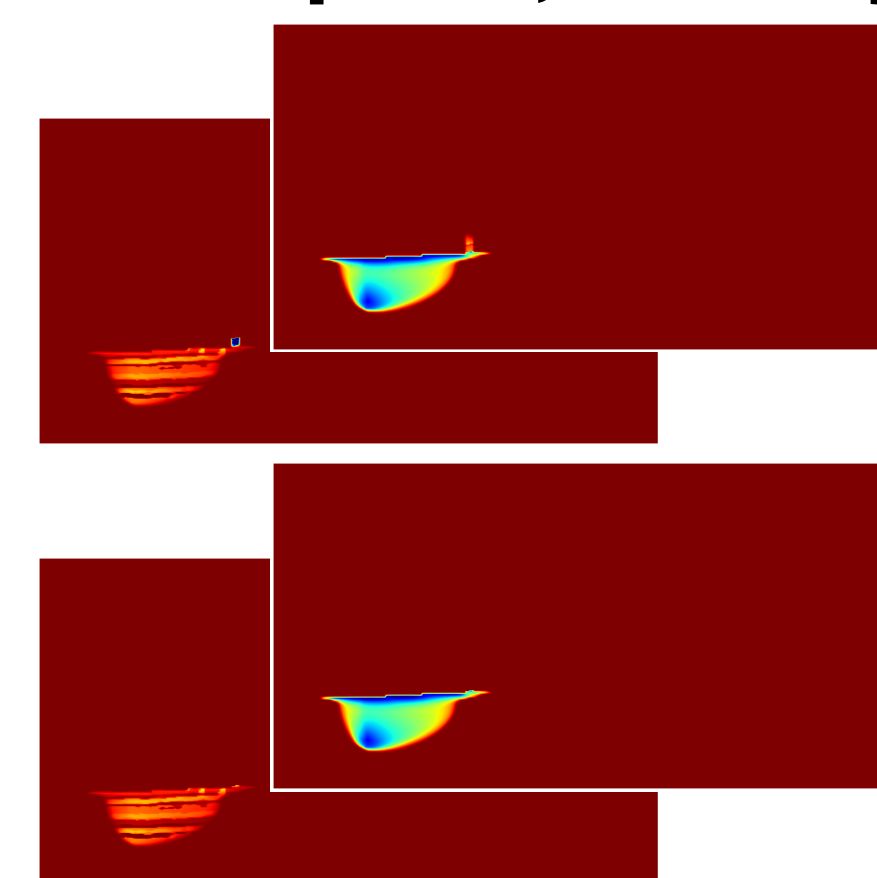
two-phase  
flow



CO<sub>2</sub> dynamics  
concentration, pressure



time-lapse models  
wavespeed, density



class activation mapping

deep neural classifier

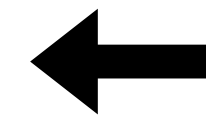
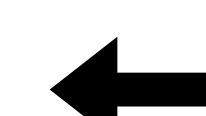
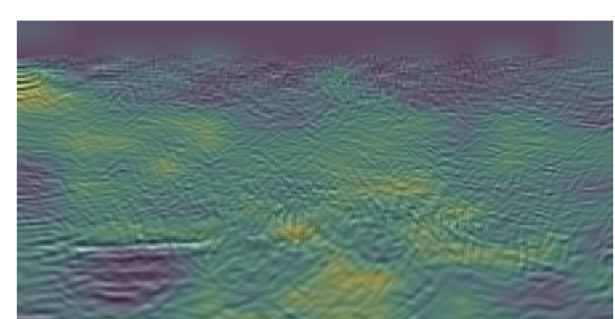
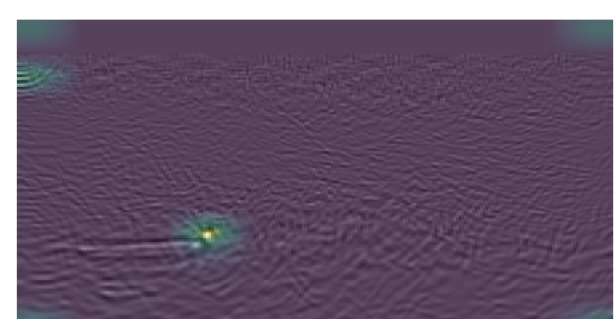
time-lapse imaging

time-lapse (diff) data

Confusion Matrix

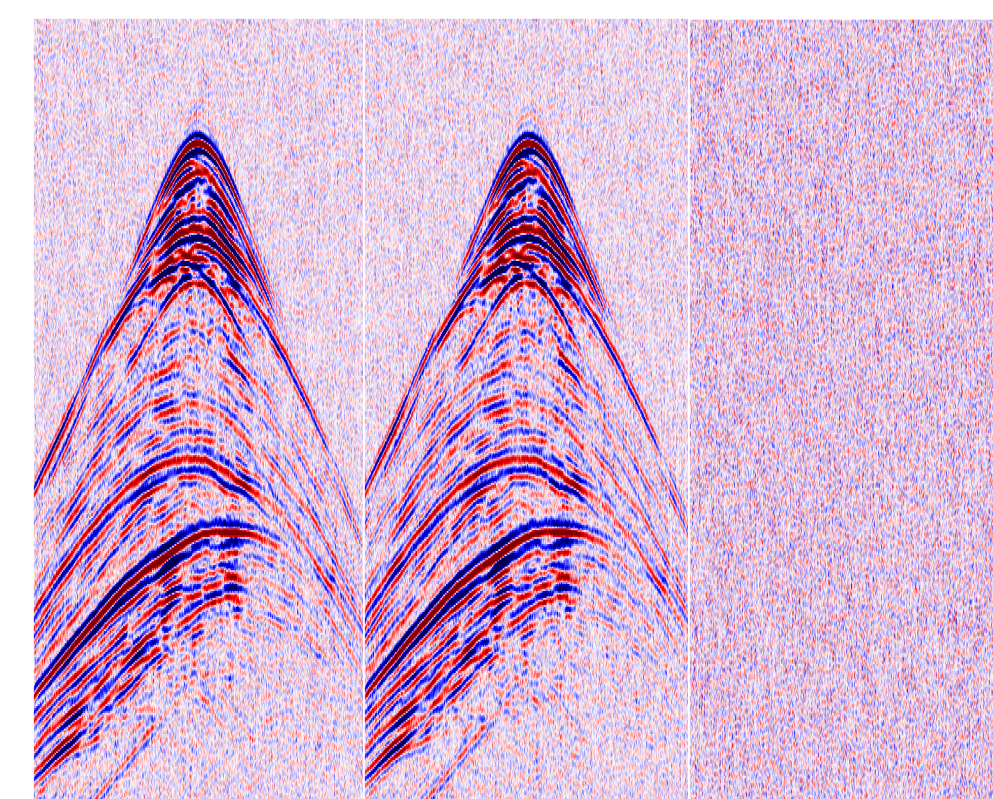
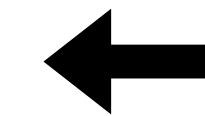
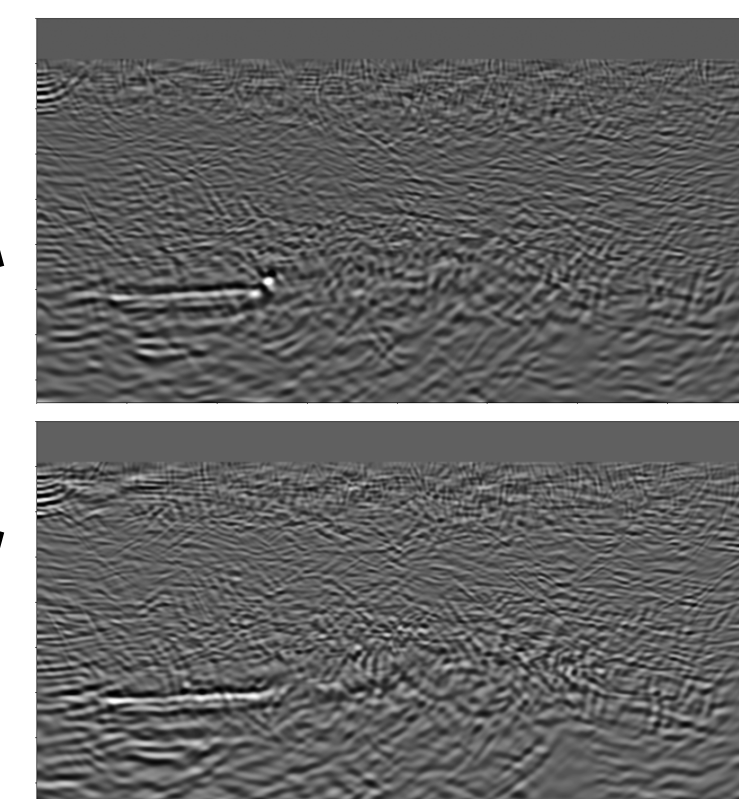
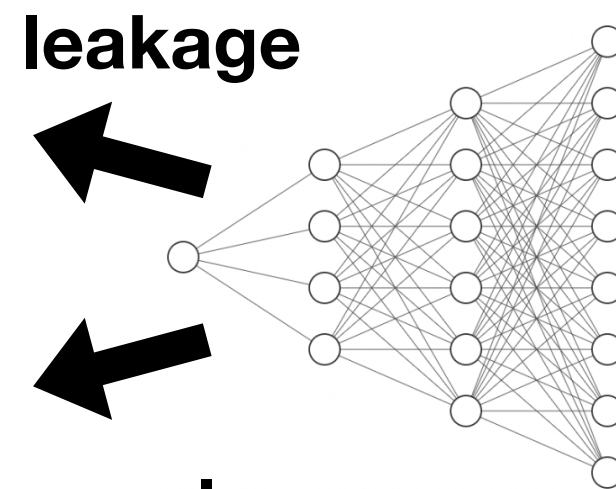
No Leakage	True Neg 193 48.98%	False Pos 13 3.30%
Leakage	False Neg 41 10.41%	True Pos 147 37.31%
	No Leakage	Leakage

accuracy = 86.29%



leakage

regular



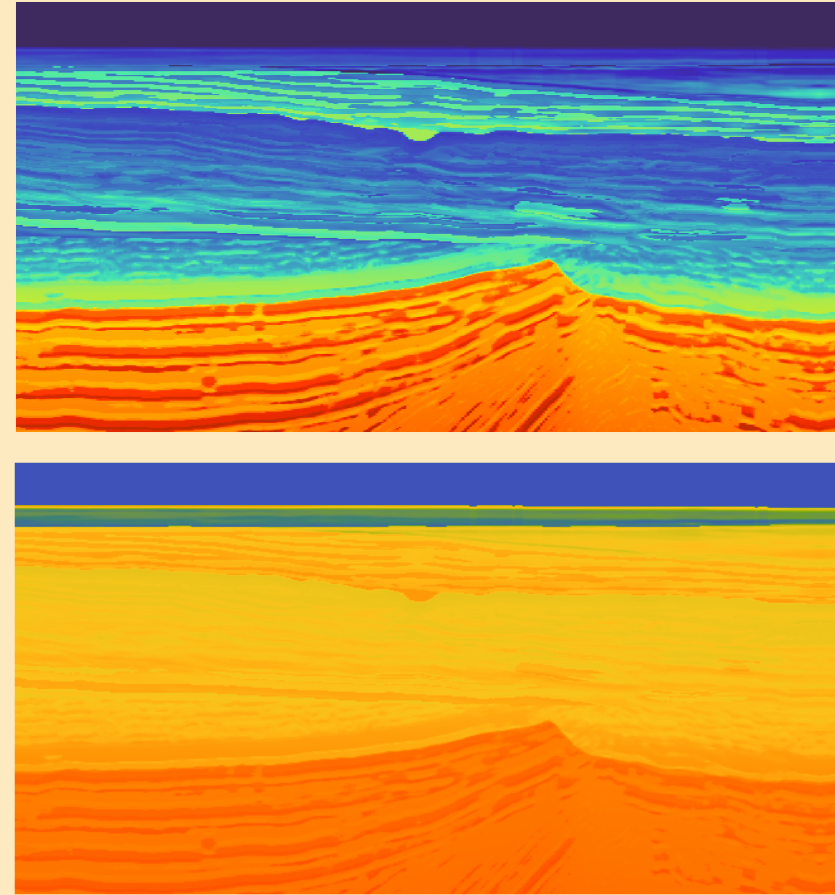


# Rock property conversion

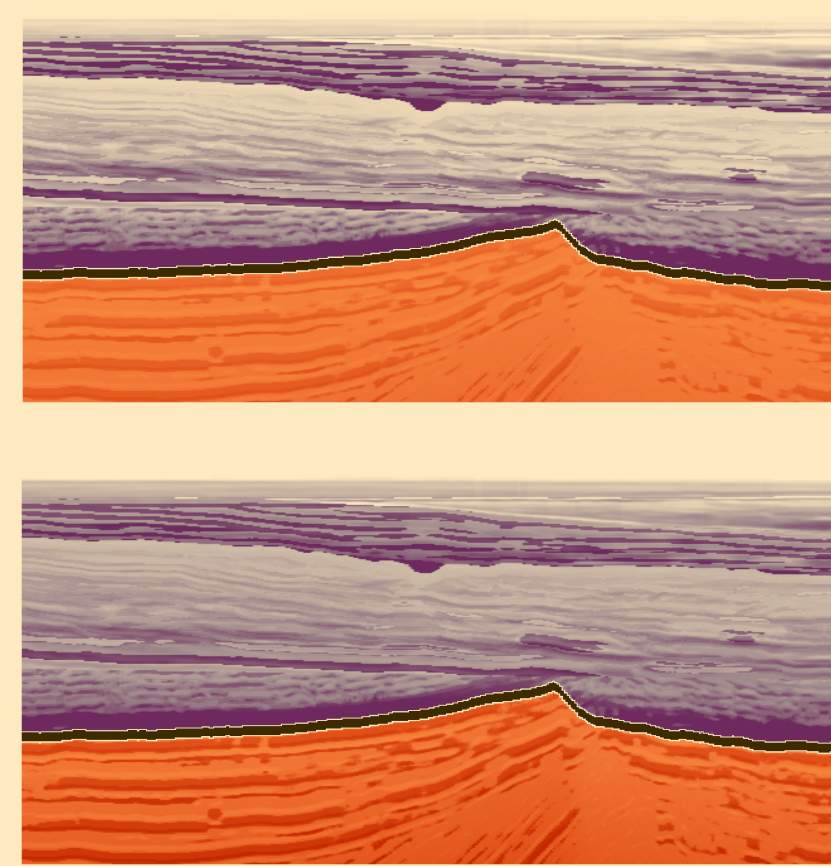


# Workflow

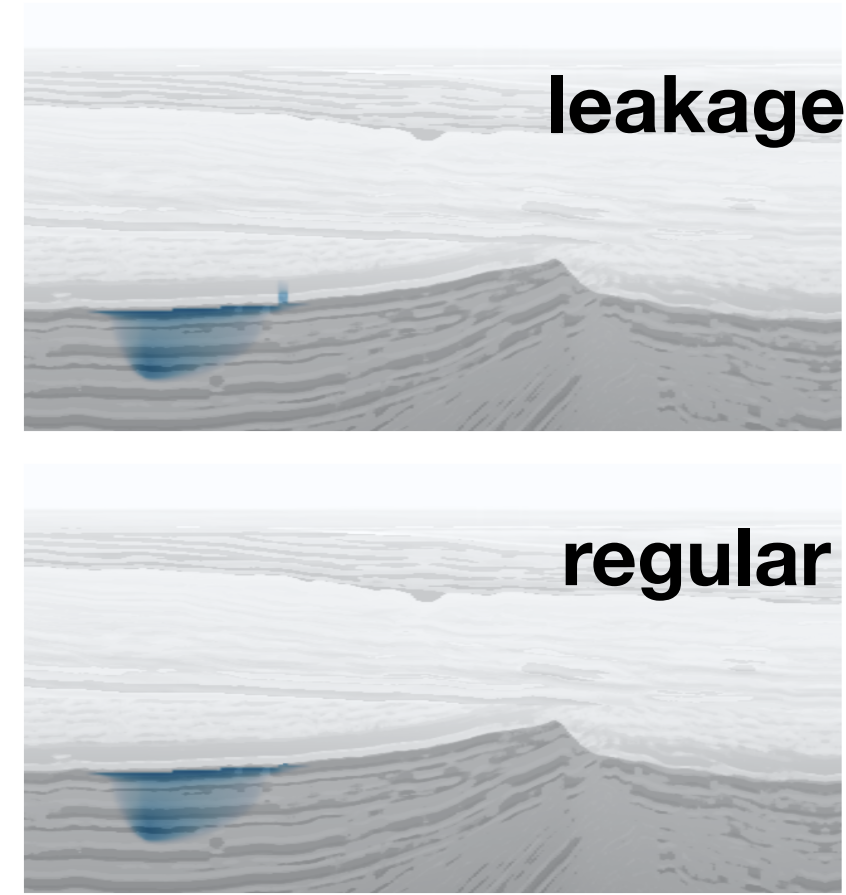
proxy model  
wavespeed, density



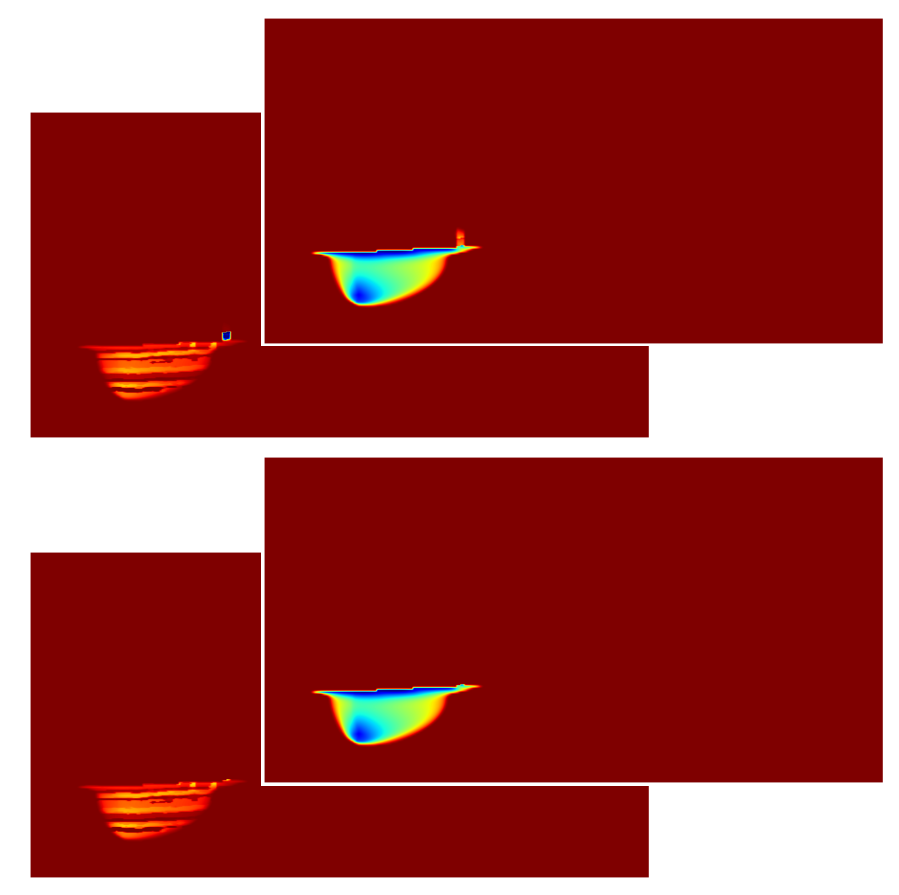
reservoir model  
permeability, porosity



CO<sub>2</sub> dynamics  
concentration, pressure



time-lapse models  
wavespeed, density



pressure induced fault  
two-phase flow

class activation mapping

deep neural classifier

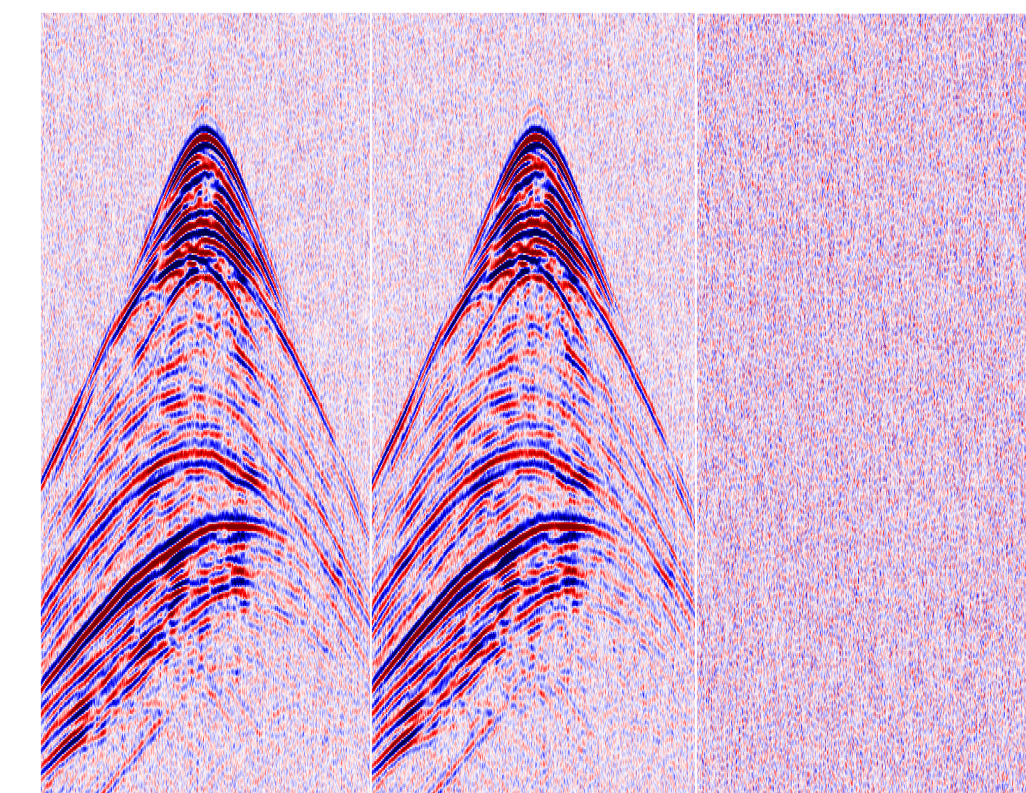
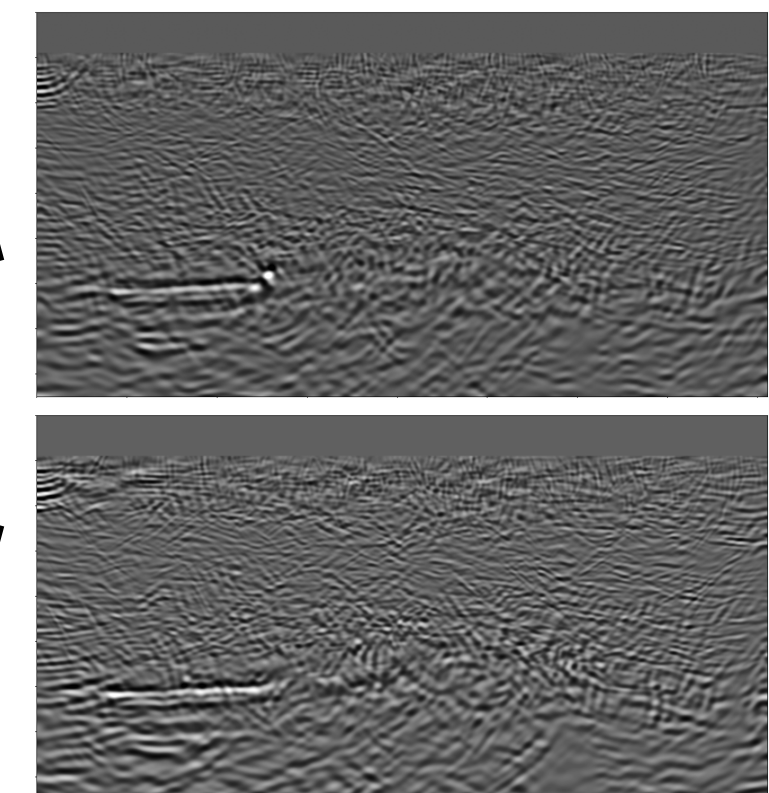
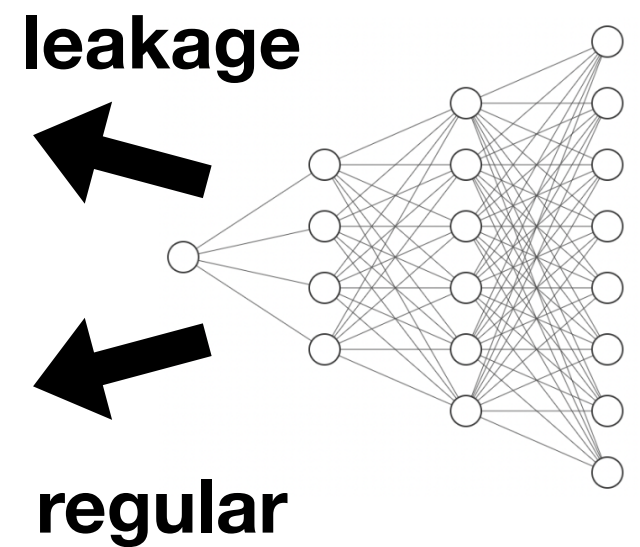
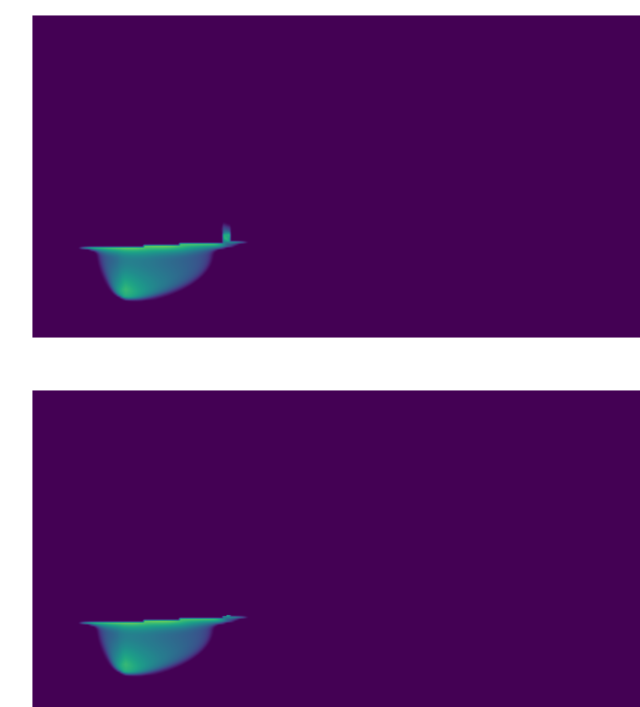
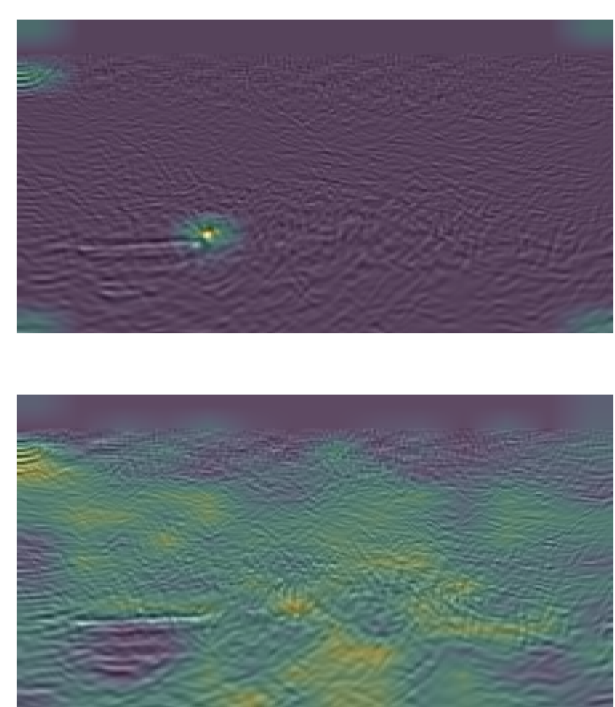
time-lapse imaging

time-lapse (diff) data

Confusion Matrix

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	No Leakage	Leakage

accuracy = 86.29%





# Conversion velocity $\Rightarrow$ permeability

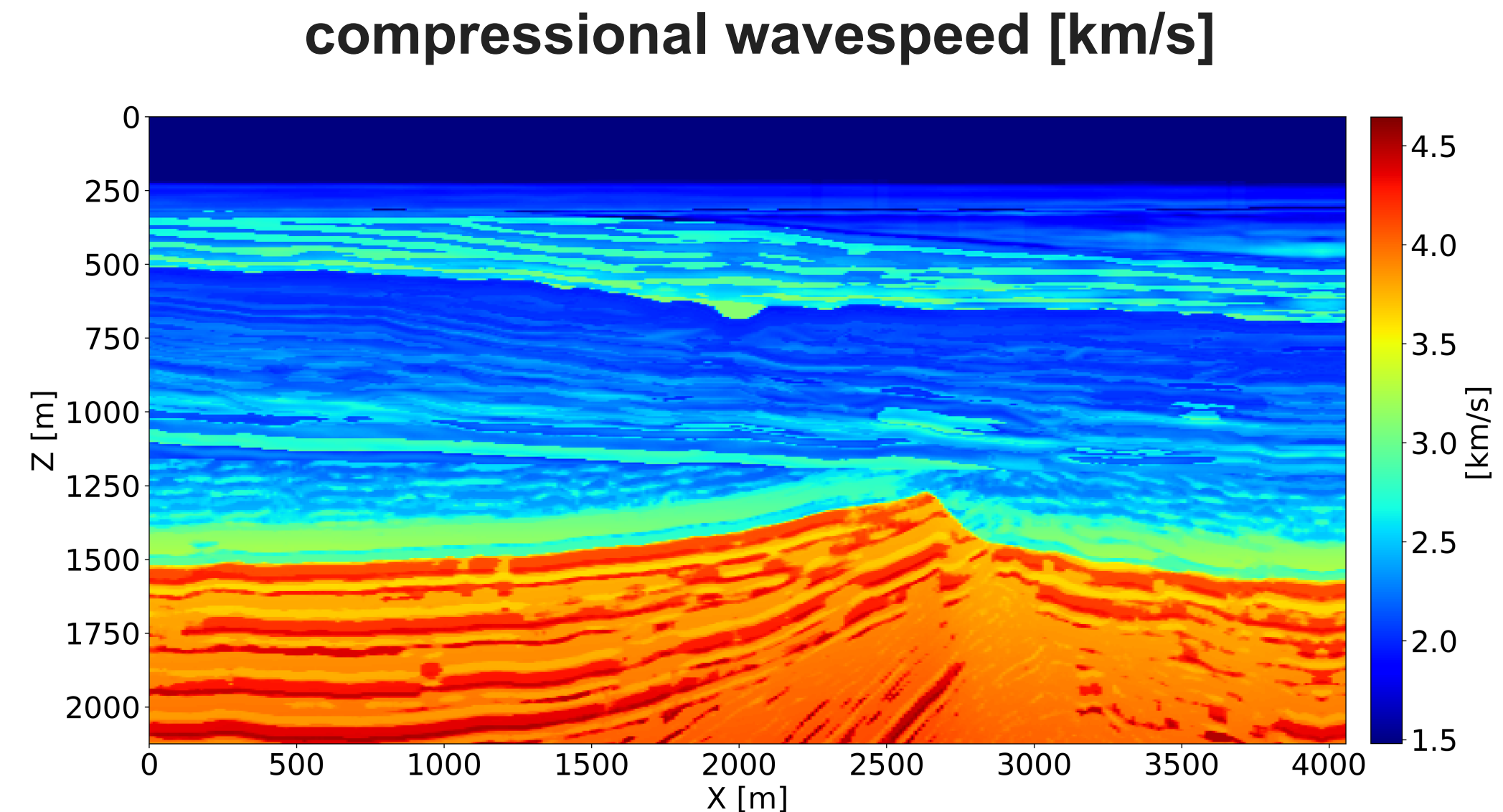
Converted with  $v_p$  1km/s  $\uparrow \Rightarrow K$  1.63mD  $\uparrow$

- ▶  $K$  permeability
- ▶  $v_p$  compressional wavespeed

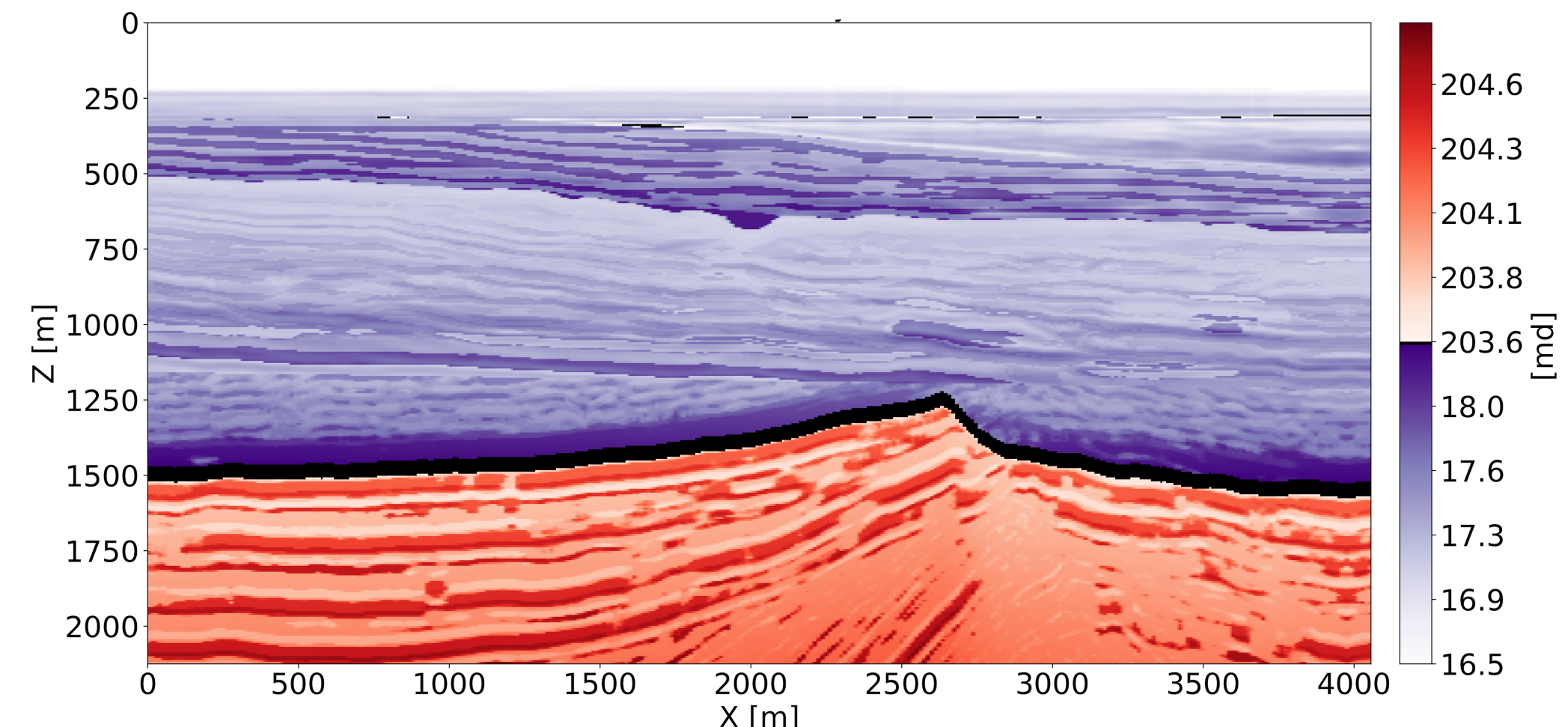
Three main geologic sections:

- ▶ secondary seal – Haisborough group  
(blue, > 300m, permeability 15 – 18mD)
- ▶ primary seal – Rote Halite member  
(black, 50m, permeability  $10^{-4} - 10^{-2}$ mD)
- ▶ saline aquifer – Bunter sandstone  
(red, 300 – 500m, permeability > 200mD)

Values taken from Strategic UK CCS Storage  
Appraisal Project



permeability [mD]





# Conversion

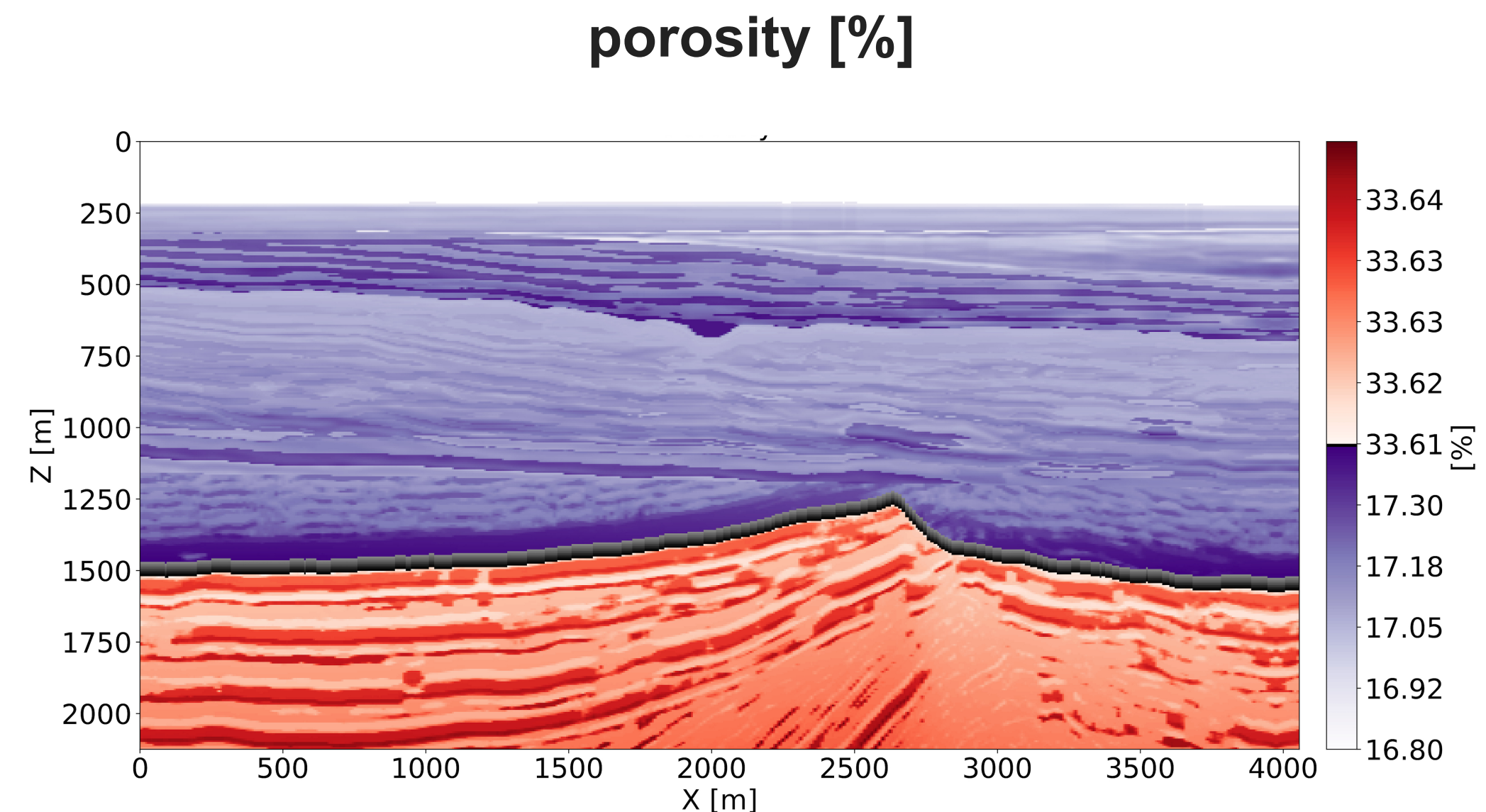
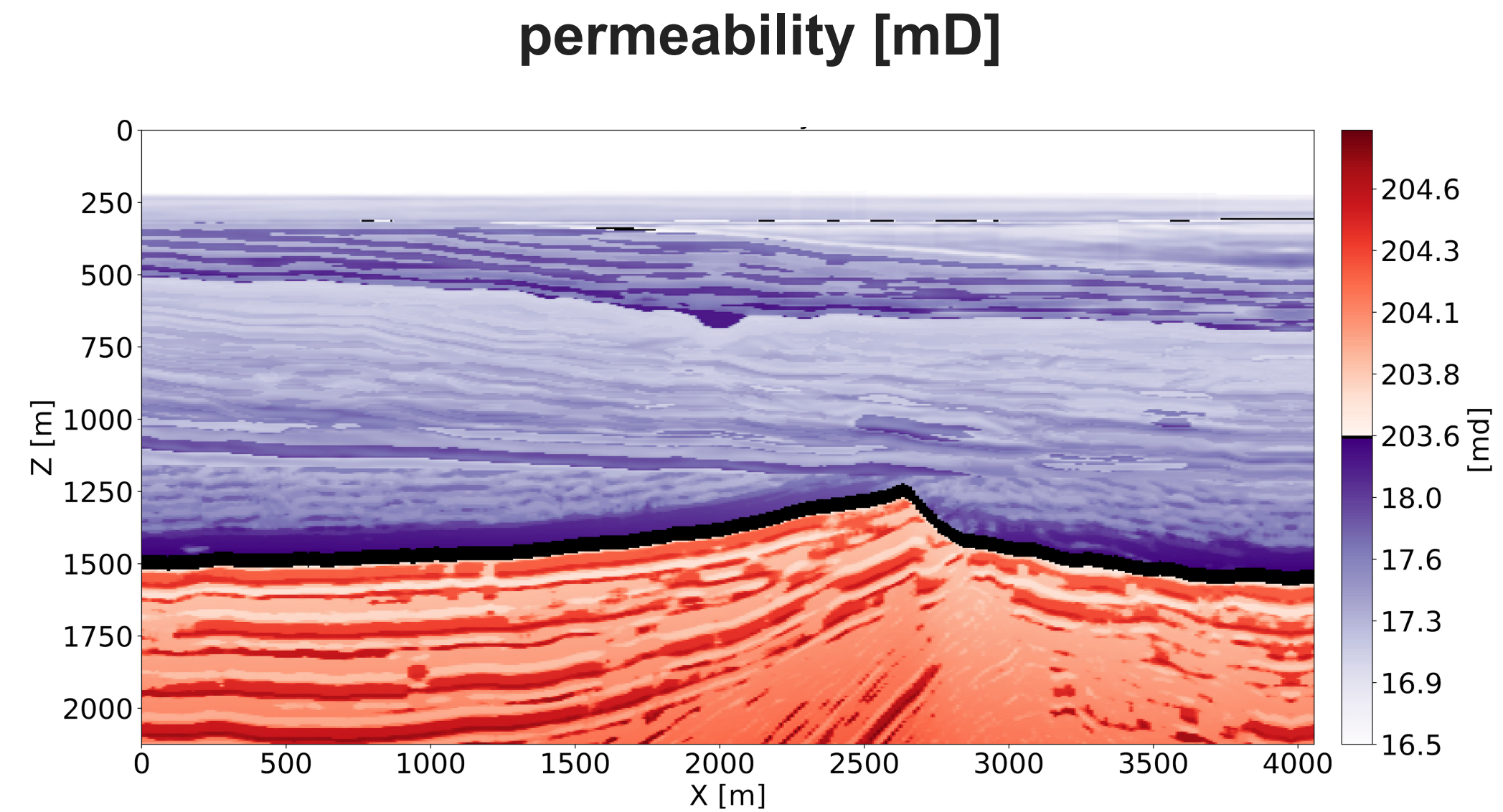
permeability  $\implies$  porosity

Kozeny-Carman relationship:

$$K = \phi^3 \left( \frac{1.527}{0.0314(1 - \phi)} \right)^2$$

- ▶  $K$  permeability
- ▶  $\phi$  porosity
- ▶ values taken from Strategic UK CCS Storage Appraisal Project

**Permeability & porosity models serve as input for two-phase fluid flow simulations.**

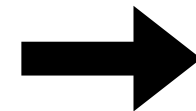
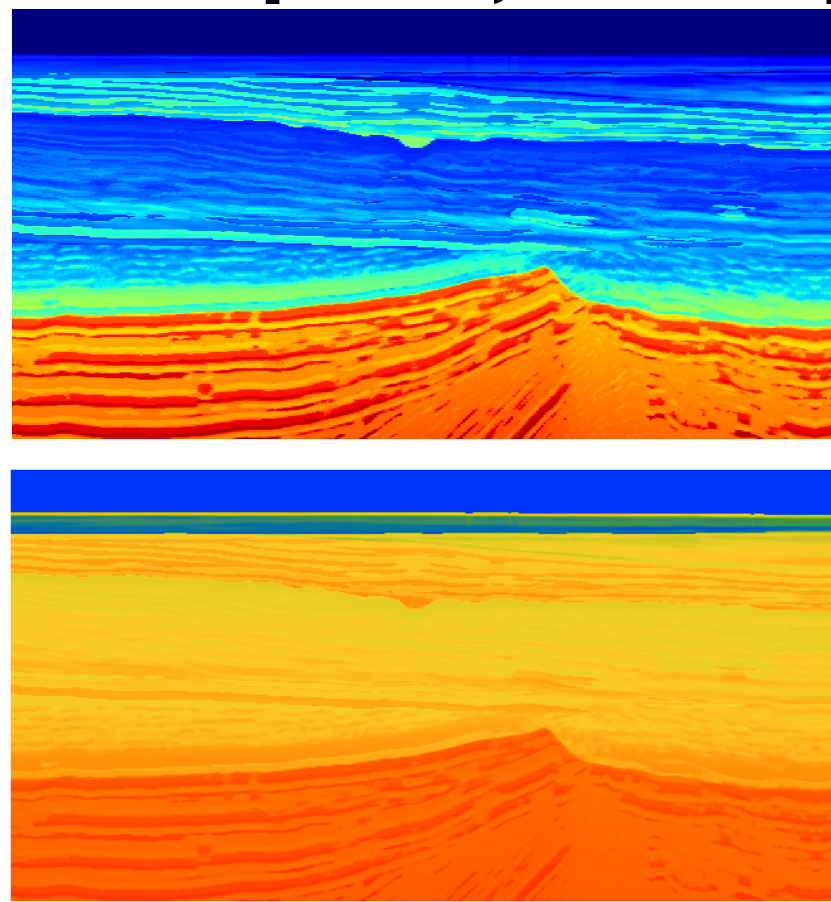


# Fluid-flow modeling

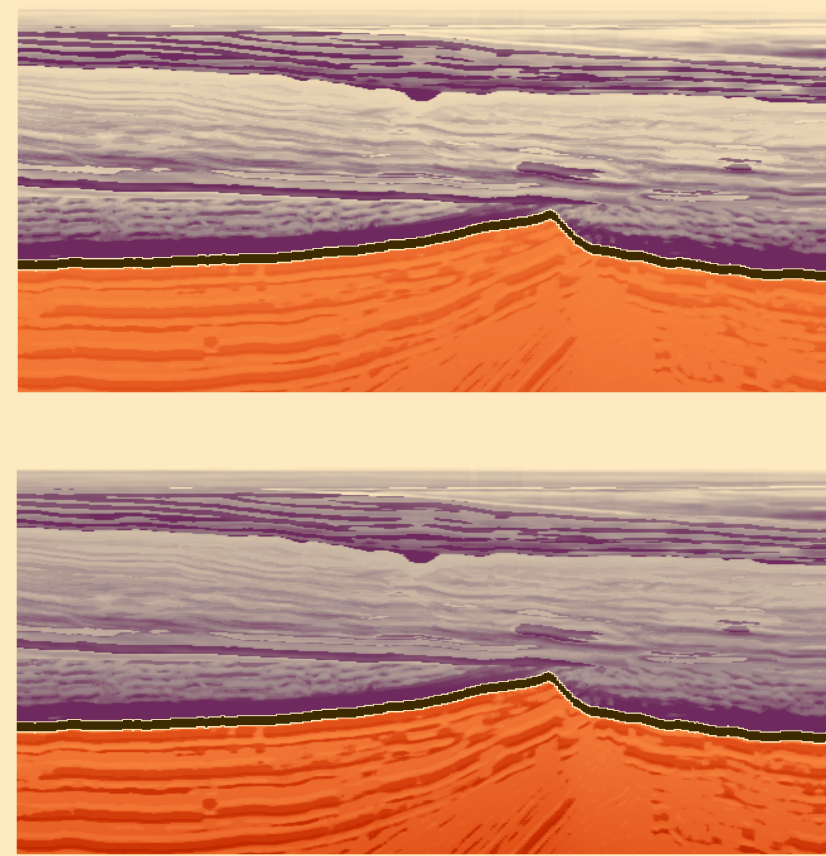


# Workflow

proxy model  
wavespeed, density

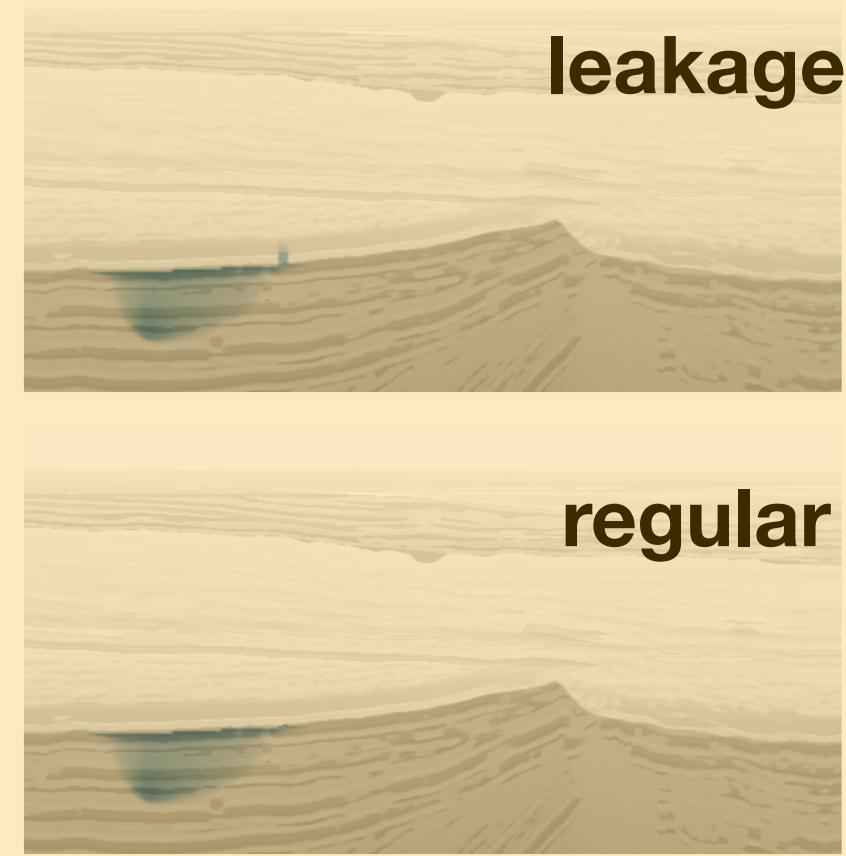


reservoir model  
permeability, porosity

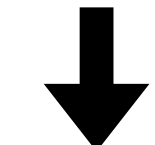
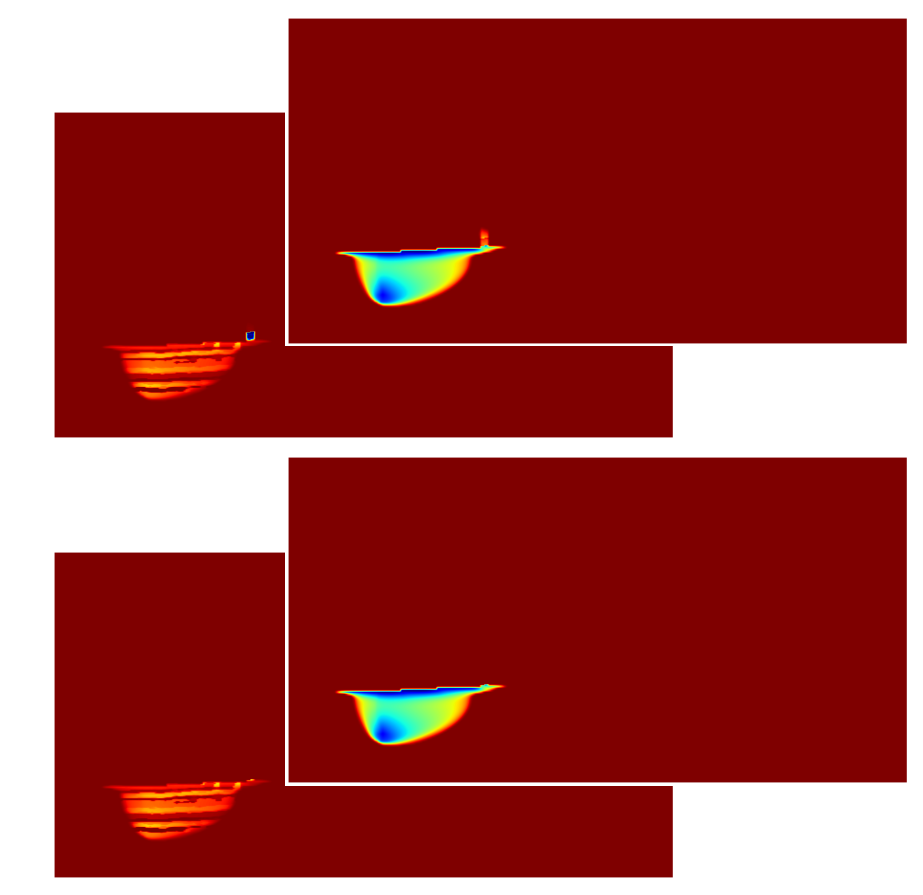


pressure induced fault  
two-phase flow

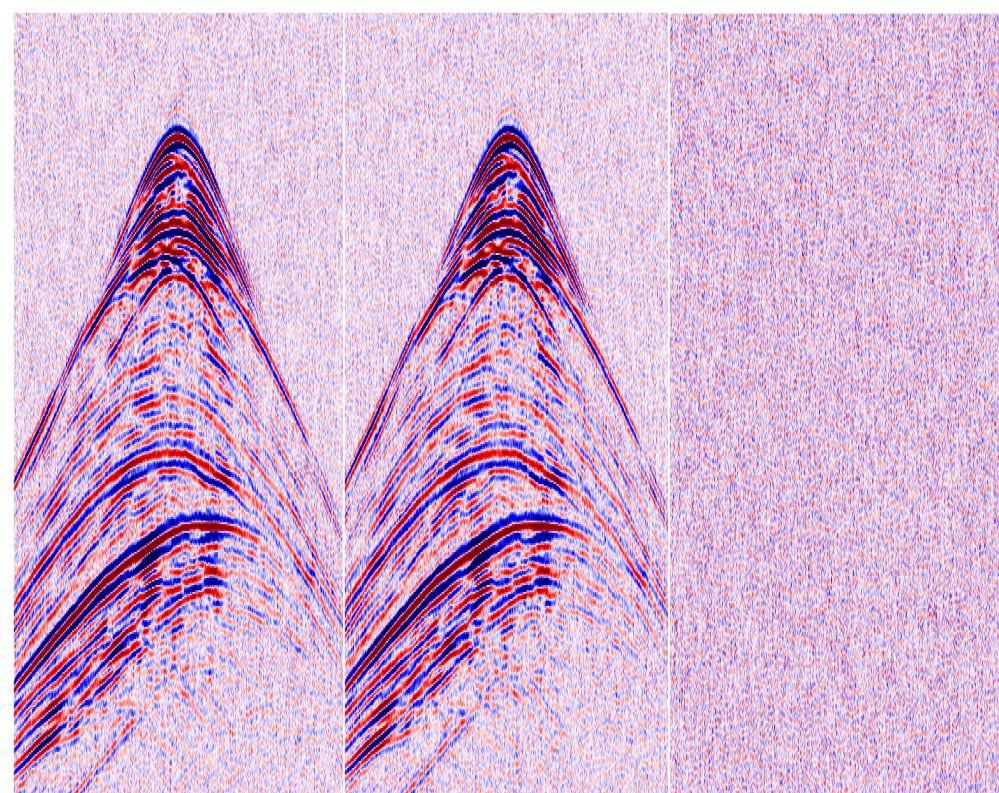
CO<sub>2</sub> dynamics  
concentration, pressure



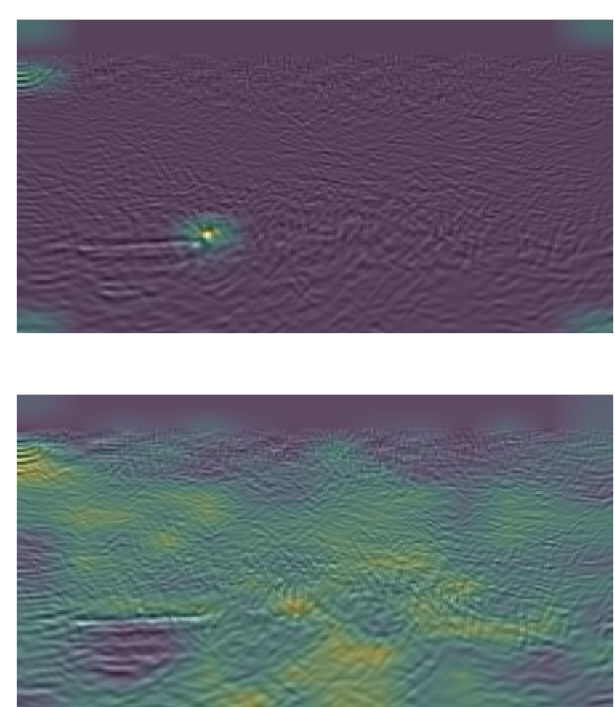
time-lapse models  
wavespeed, density



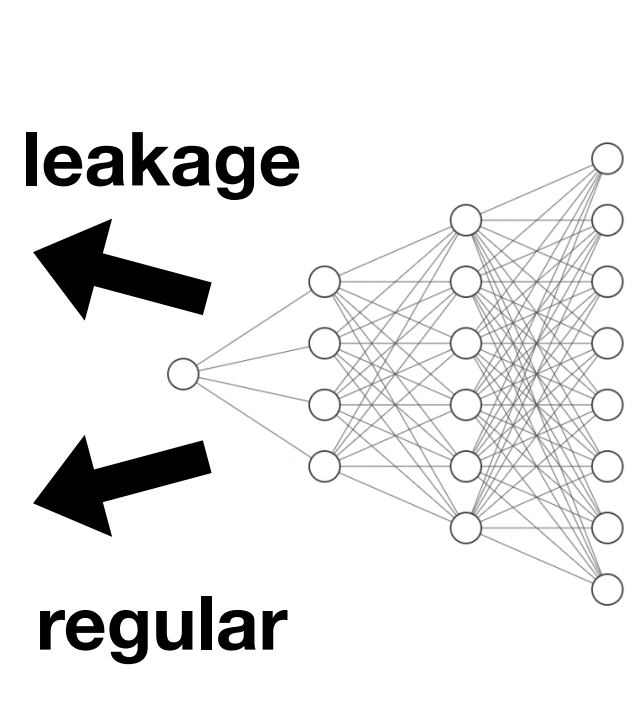
time-lapse (diff) data



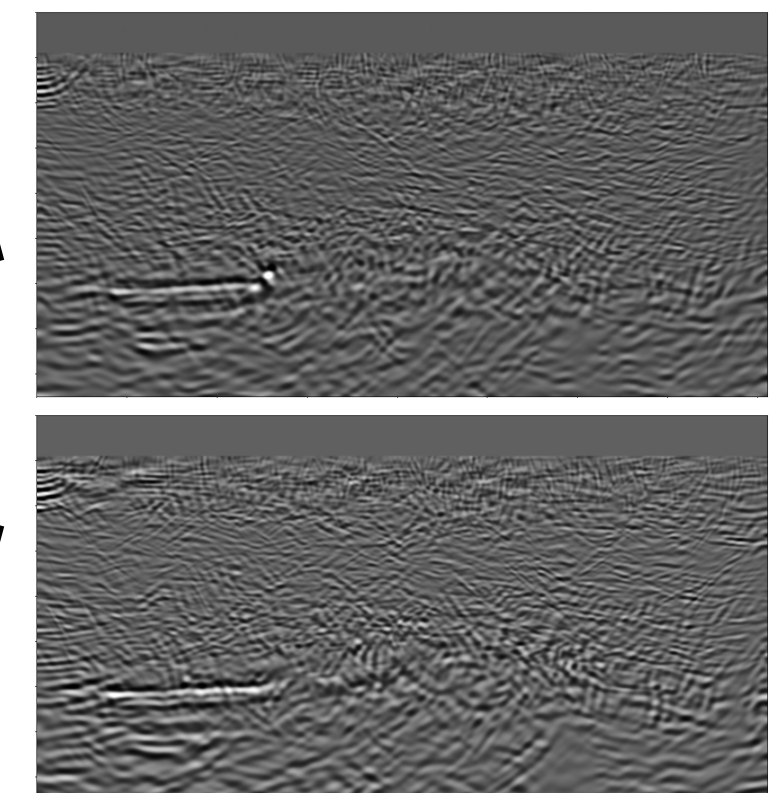
class activation mapping



deep neural classifier



time-lapse imaging



Confusion Matrix

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Leakage	False Neg 41 10.41%	True Pos 147 37.31%
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accuracy = 86.29%



# CO<sub>2</sub> dynamics

## two-phase flow equations

**mass balance equation:**

$$\frac{\partial}{\partial t}(\phi S_i \rho_i) + \nabla \cdot (\rho_i \mathbf{v}_i) = \rho_i q_i, \quad i = 1, 2$$

inject CO<sub>2</sub> to replace water

$$S_1 + S_2 = 1$$

**Darcy's law:**

$$\mathbf{v}_i = -\frac{K k_{ri}}{\tilde{\mu}_i} (\nabla P_i - g \rho_i \nabla Z), \quad i = 1, 2$$

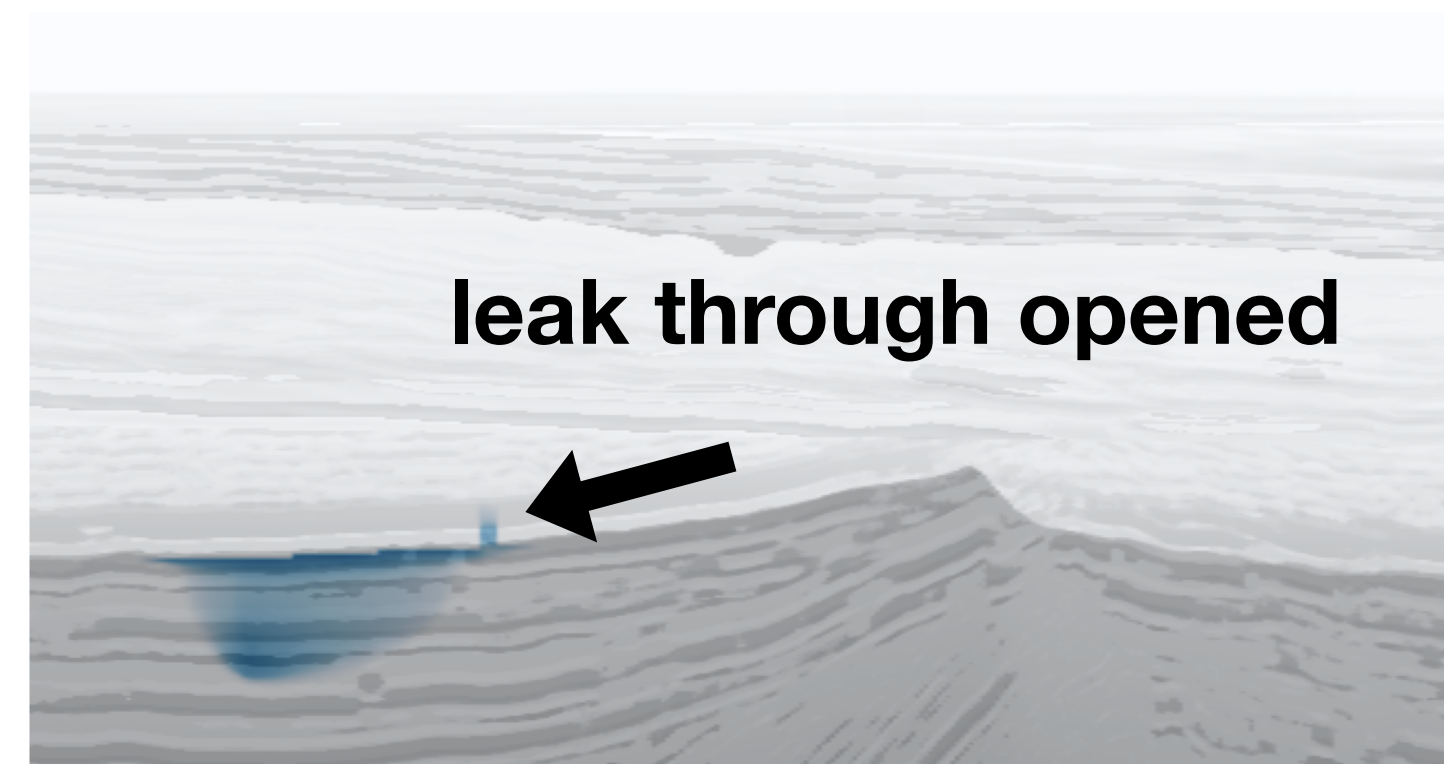
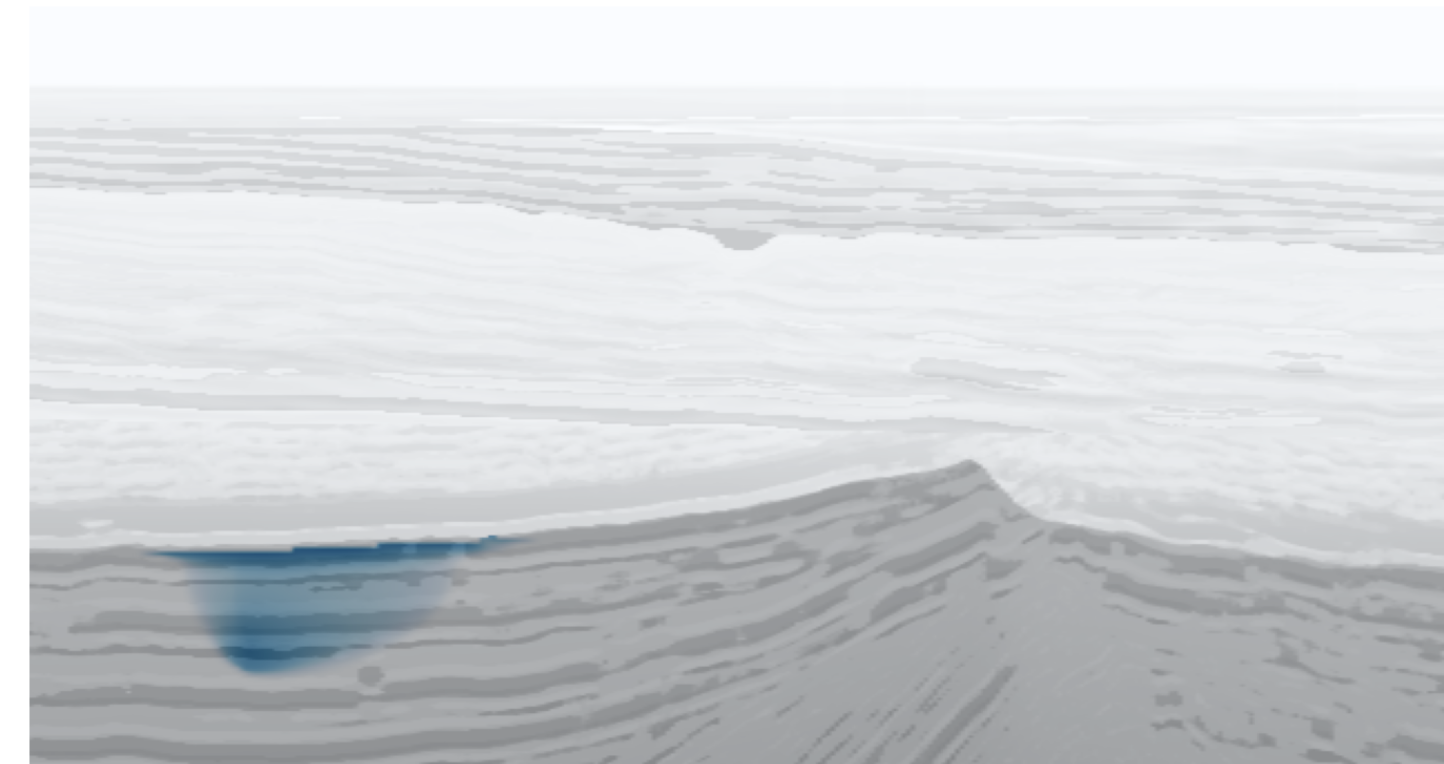
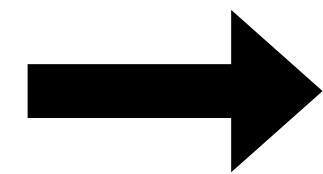
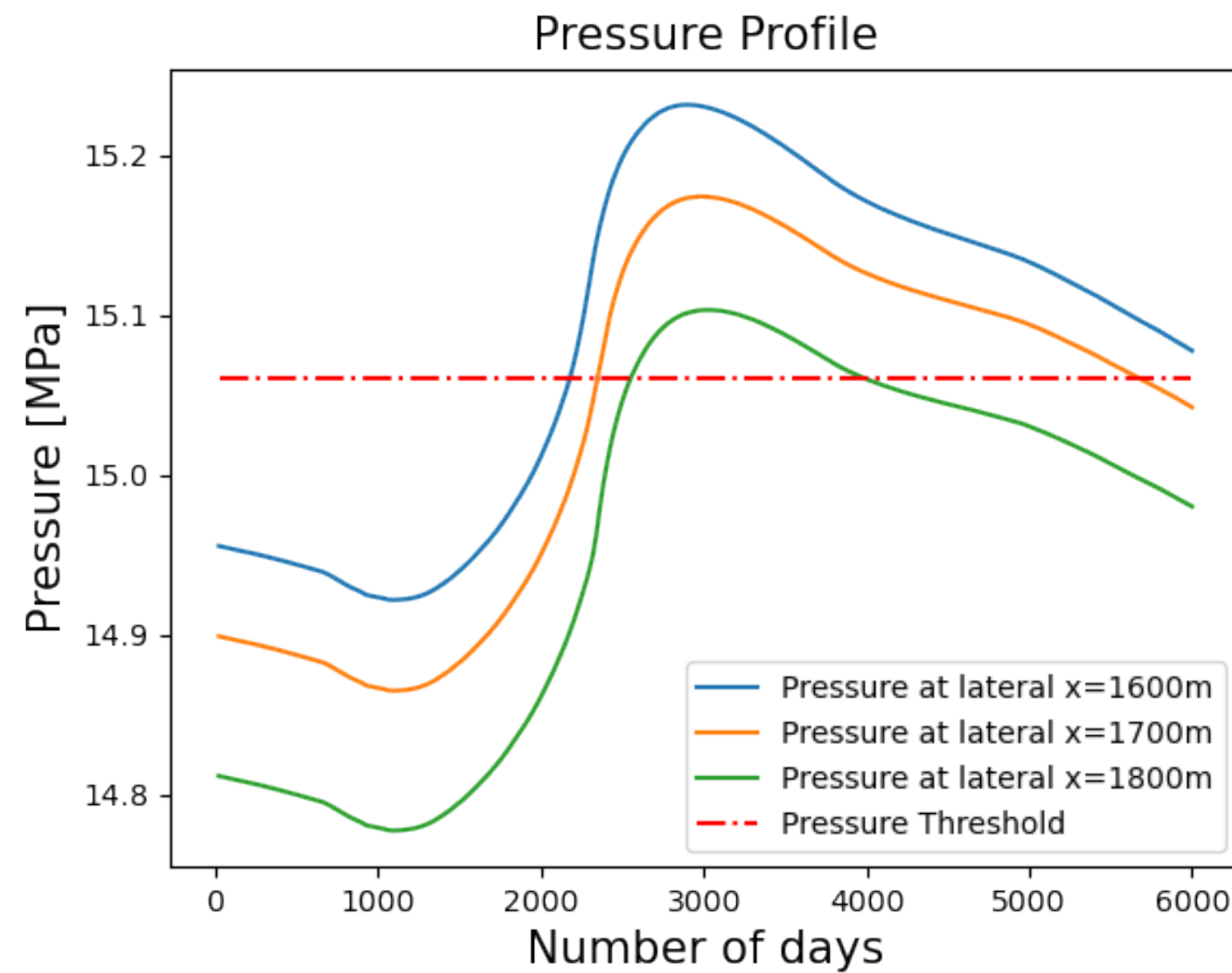
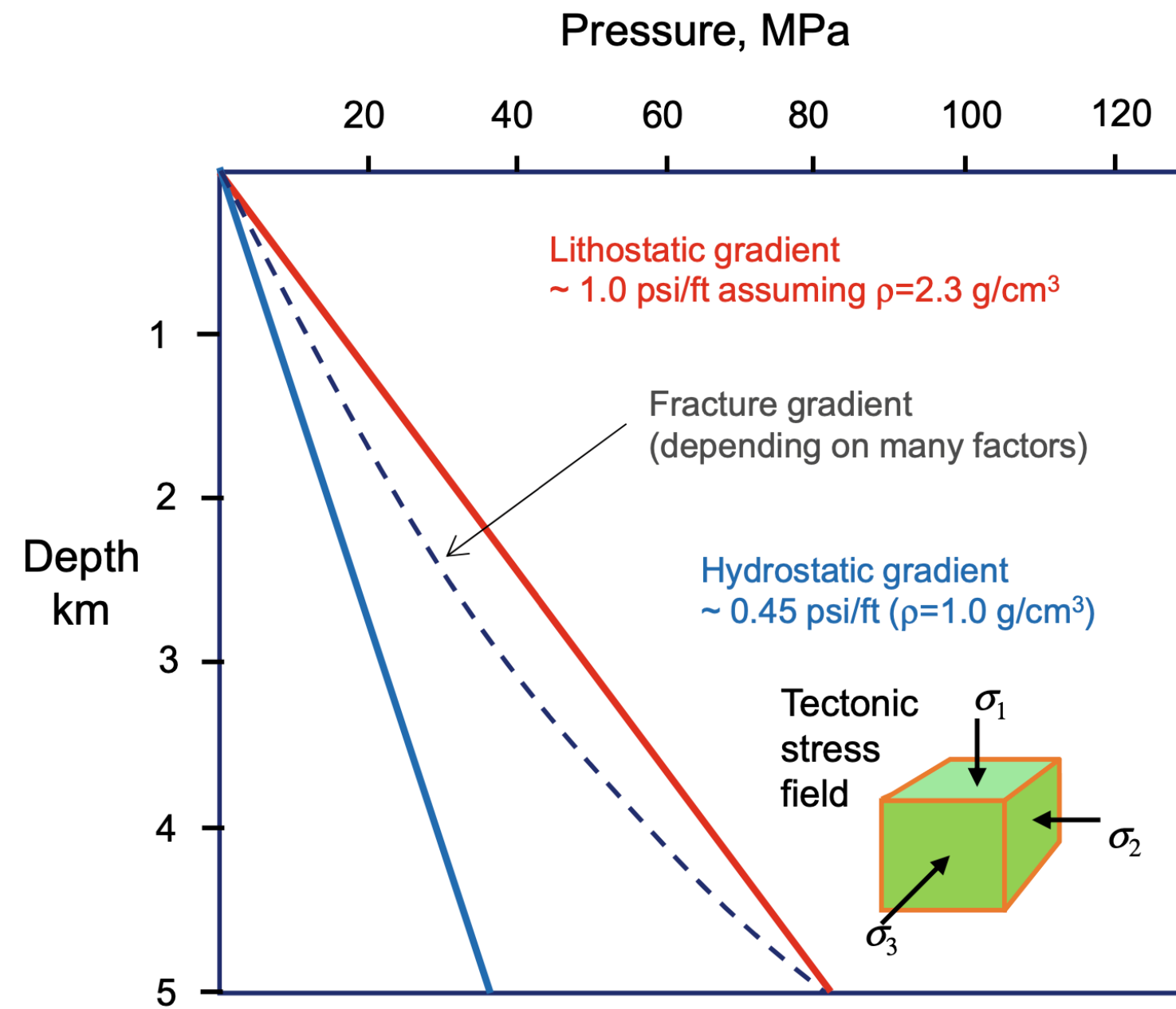
**fluid pressure:**

$$P_2 = P_1 - P_c(S_2)$$

Symbol	Meaning
$K$	permeability
$\phi$	porosity
$k_{ri}$	relative permeability
$S_i$	fluid saturation
$P_i$	fluid pressure
$P_c$	capillary pressure
$\mathbf{v}_i$	Darcy's velocity
$\rho_i$	fluid density
$\tilde{\mu}_i$	fluid viscosity
$q_i$	injection/production rate
$g$	gravity constant
$Z$	vector of vertical direction

# Pressure-induced fractures

Philip Ringrose. How to Store CO2 Underground: insights from early-mover CCS Projects. Springer, 2020. URL: <https://link.springer.com/book/10.1007/978-3-030-33113-9>.

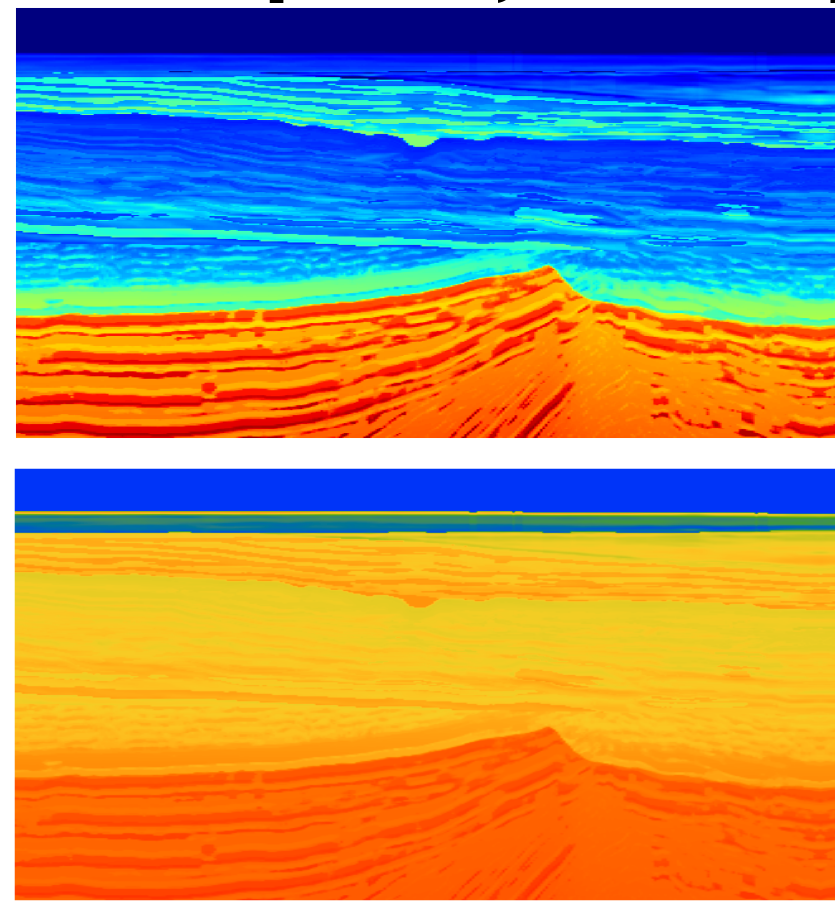


# Rock-physics modeling

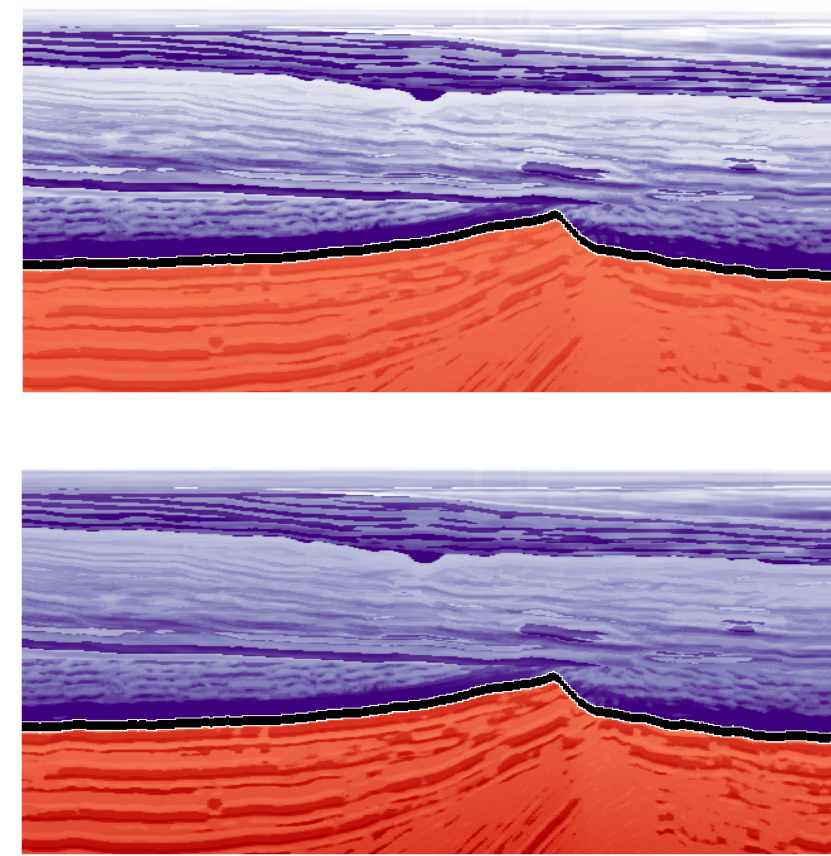


# Workflow

proxy model  
wavespeed, density

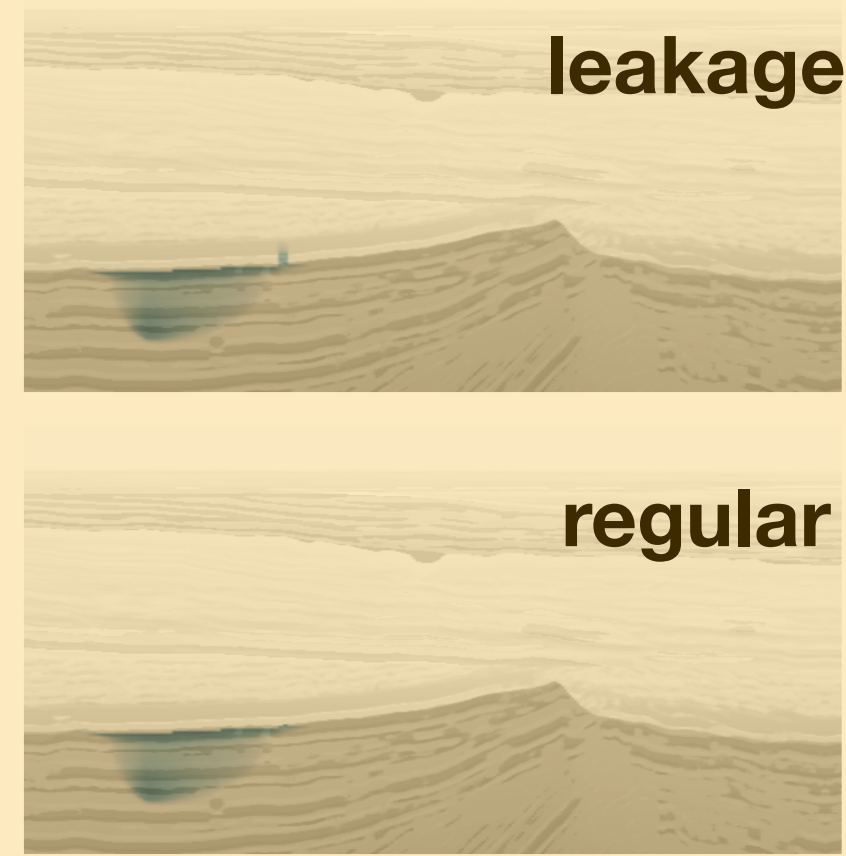


reservoir model  
permeability, porosity

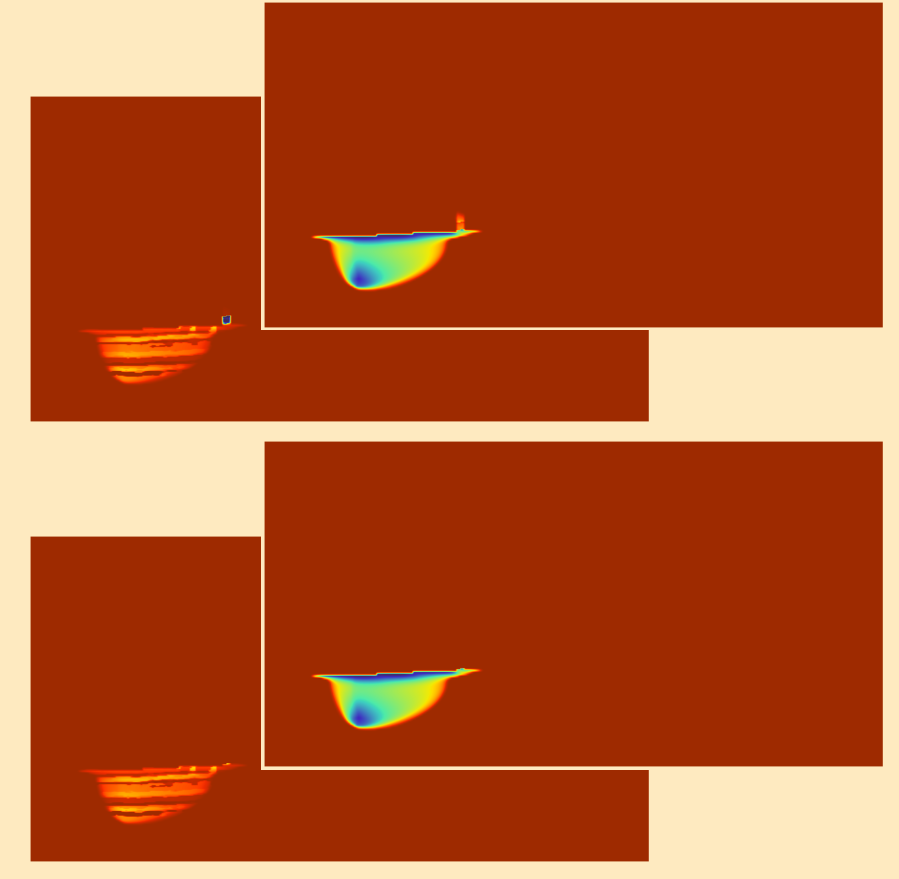


pressure induced fault  
two-phase flow

CO<sub>2</sub> dynamics  
concentration, pressure



time-lapse models  
wavespeed, density

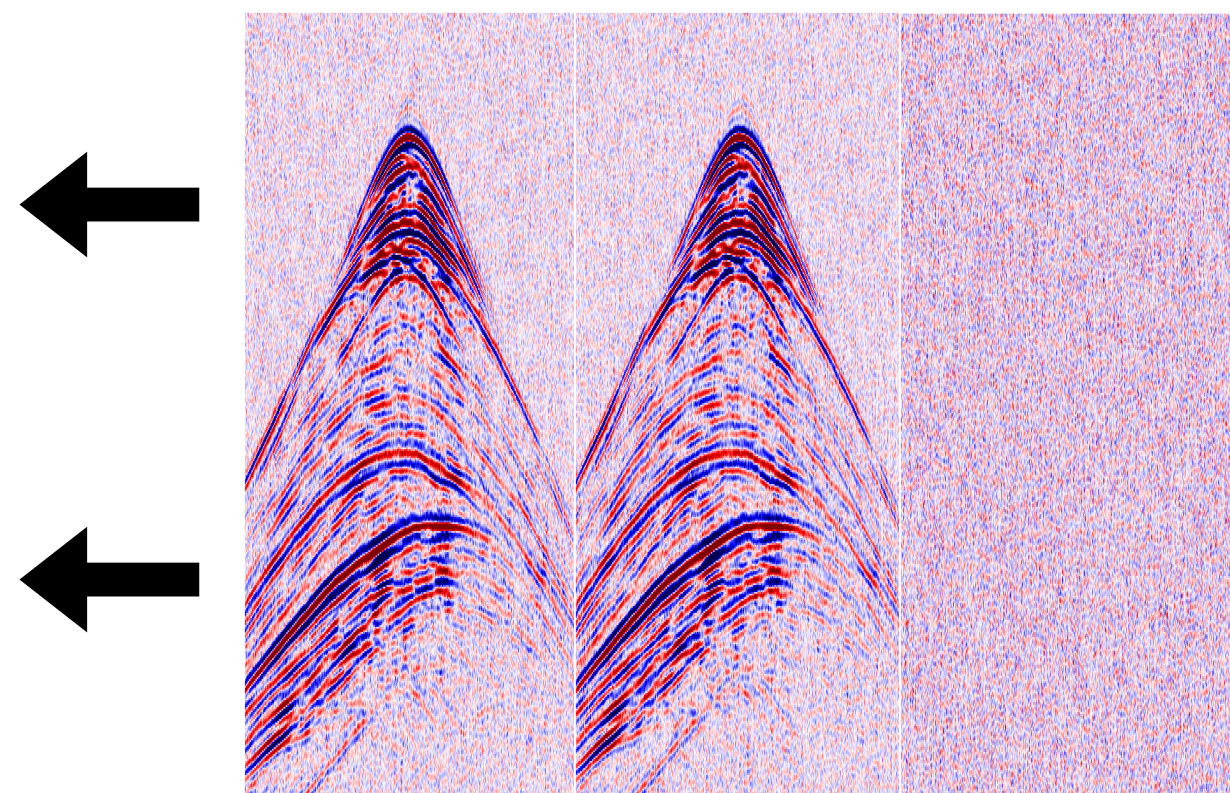
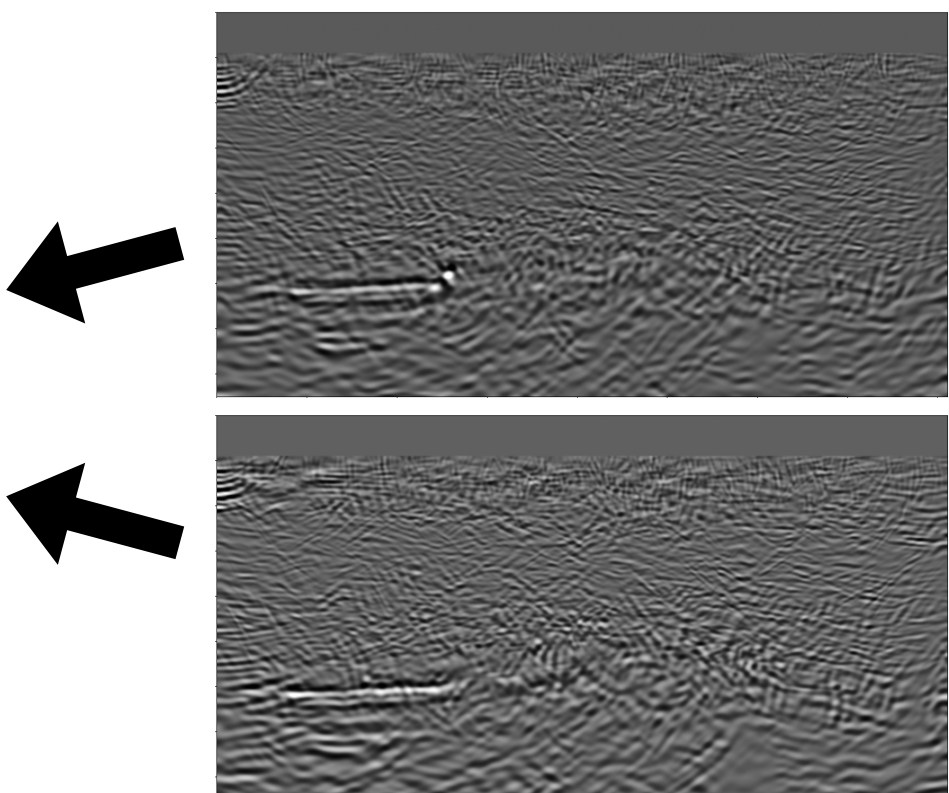
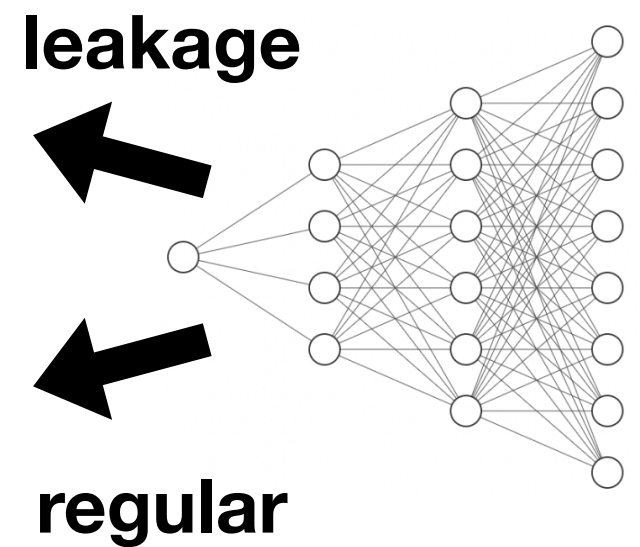
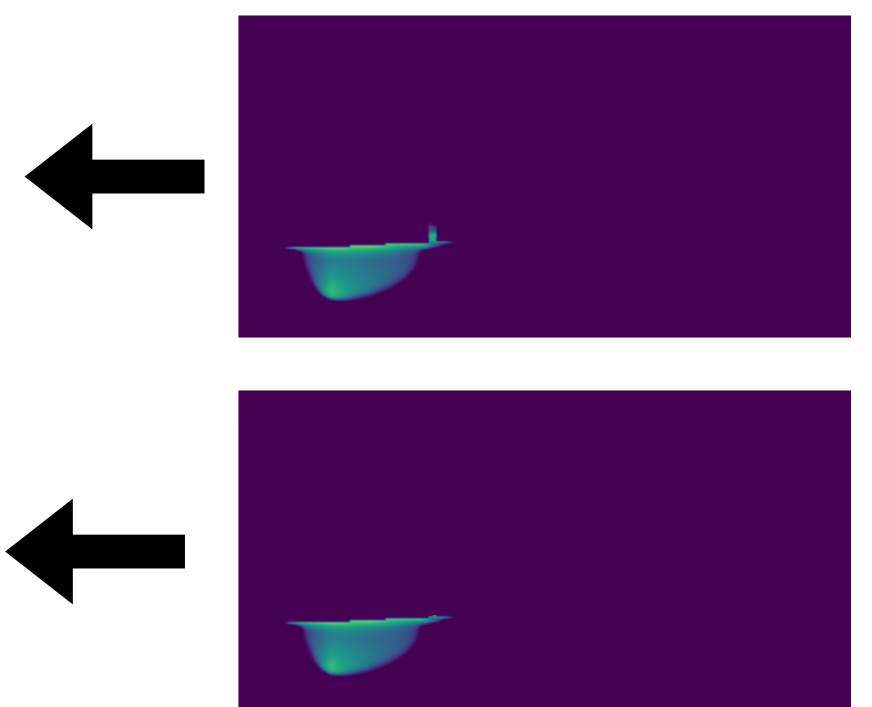
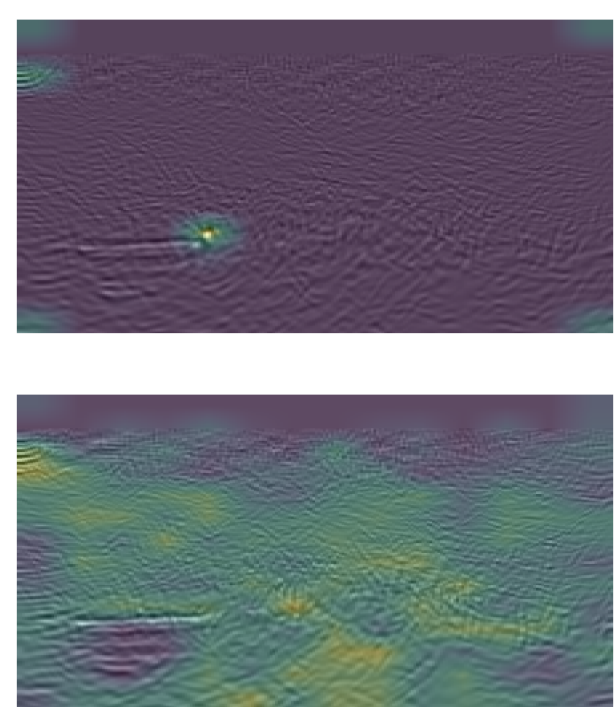
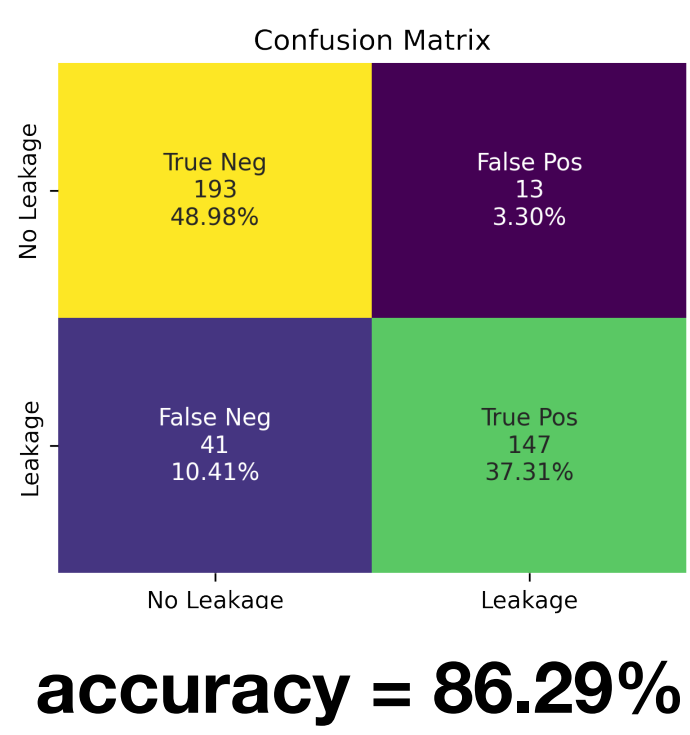


class activation mapping

deep neural classifier

time-lapse imaging

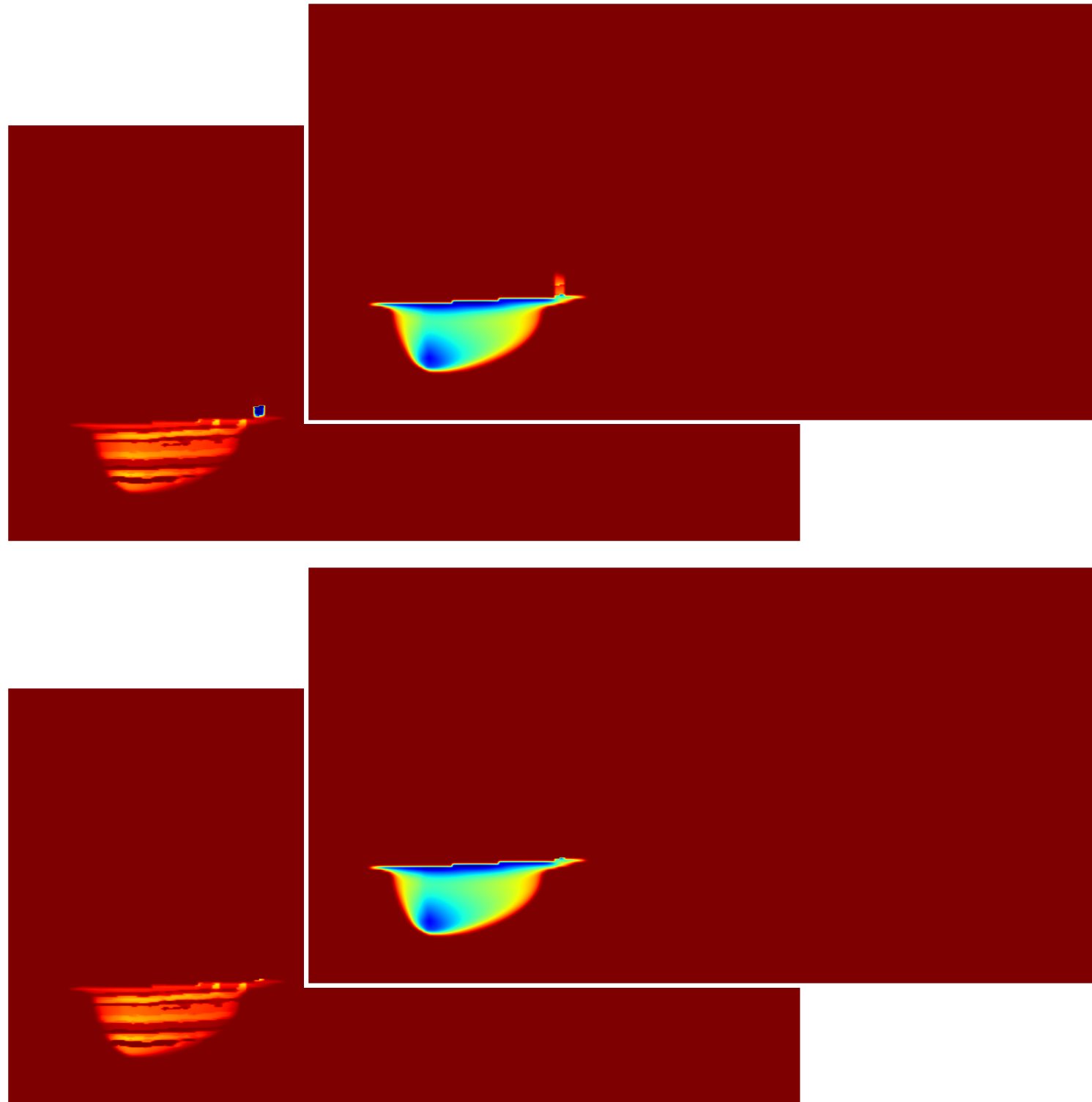
time-lapse (diff) data





# Rock physics

## patchy saturation model



CO<sub>2</sub> concentration ↑ →  $v_p$  &  $\rho$  ↓

$v_p$  decrease by 0-300 m/s

localized time-lapse changes

1.68% change in acoustic impedance

Symbol	Meaning
$B_{r1}/B_{r2}$	bulk modulus of rock fully saturated with fluid 1/2
$B_{f1}/B_{f2}$	fluid bulk modulus
$\rho_{f1}/\rho_{f2}$	fluid density
$\mu_r$	rock shear modulus
$v_p/v_s$	rock P/S-wave velocity
$B_o$	bulk modulus of rock grains
$\rho_r$	rock density
$\phi$	rock porosity
$S$	CO <sub>2</sub> saturation

$$B_{r1} = \rho_r (v_p^2 - \frac{4}{3} v_s^2)$$

$$\mu_r = \rho_r v_s^2$$

$$\frac{B_{r2}}{B_o - B_{r2}} = \frac{B_{r1}}{B_o - B_{r1}} - \frac{B_{f1}}{\phi(B_o - B_{f1})} + \frac{B_{f2}}{\phi(B_o - B_{f2})}$$

$$\hat{B}_r = [(1 - S)(B_{r1} + \frac{4}{3}\mu_r)^{-1} + S(B_{r2} + \frac{4}{3}\mu_r)^{-1}]^{-1} - \frac{4}{3}\mu_r$$

$$\hat{\rho}_r = \rho_r + \phi S (\rho_{f2} - \rho_{f1})$$

$$\hat{v}_p = \sqrt{\frac{\hat{B}_r + \frac{4}{3}\mu_r}{\hat{\rho}_r}}$$

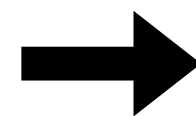
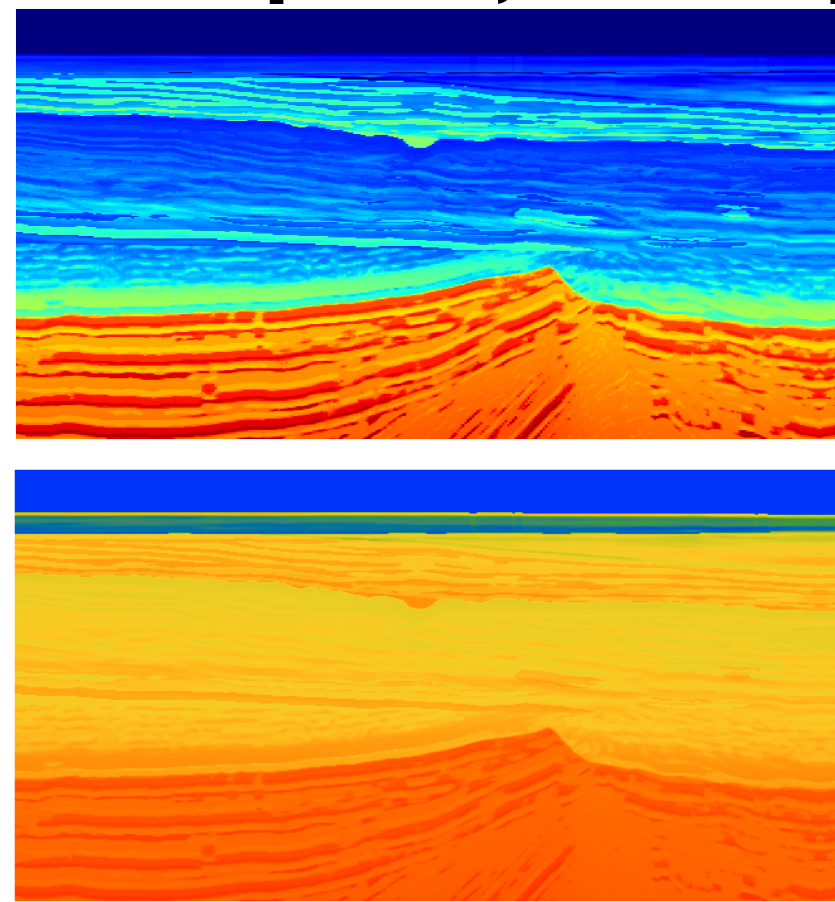


# Seismic modeling

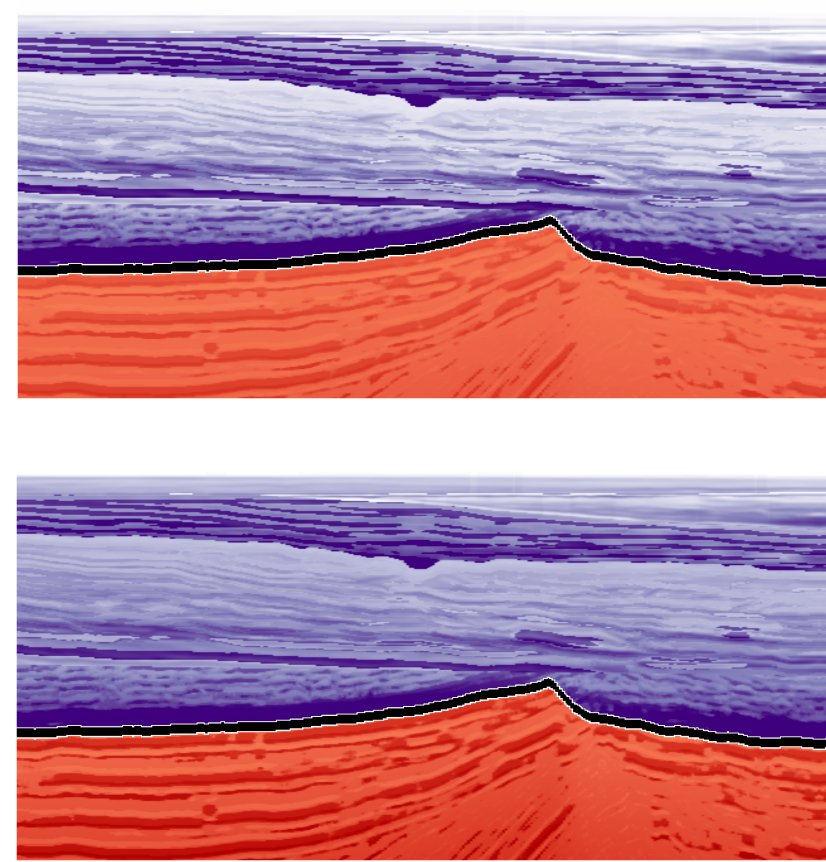


# Workflow

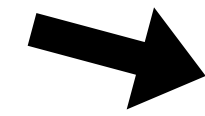
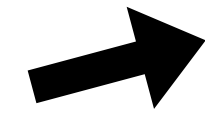
proxy model  
wavespeed, density



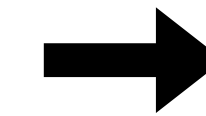
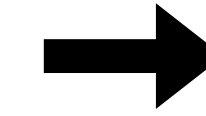
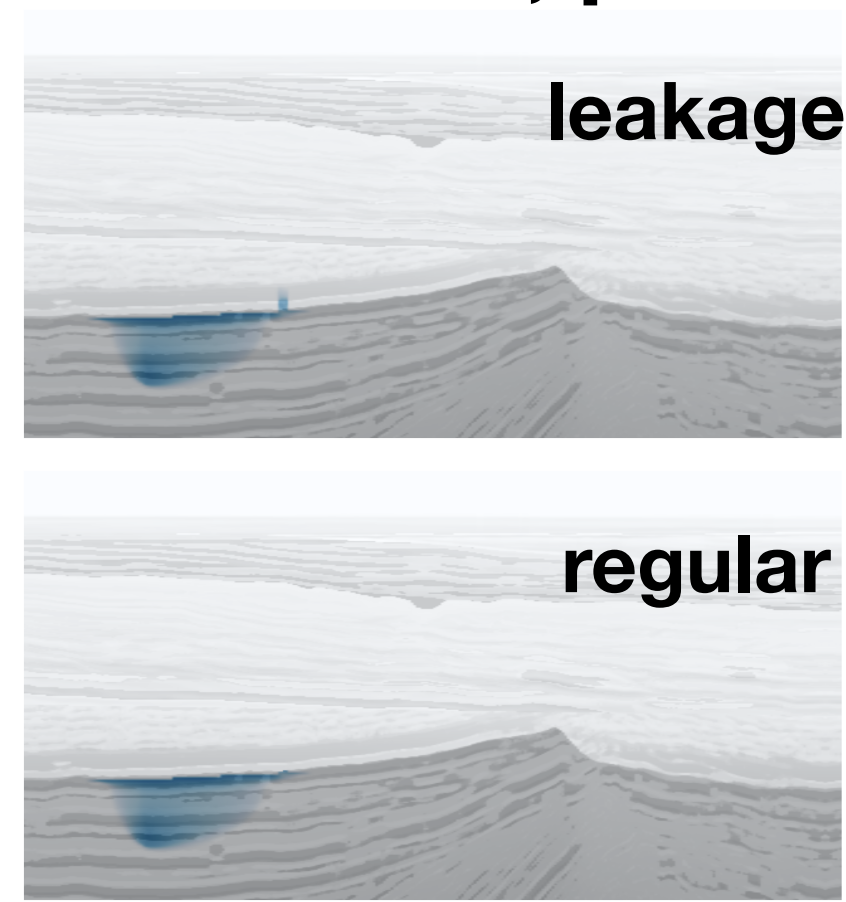
reservoir model  
permeability, porosity



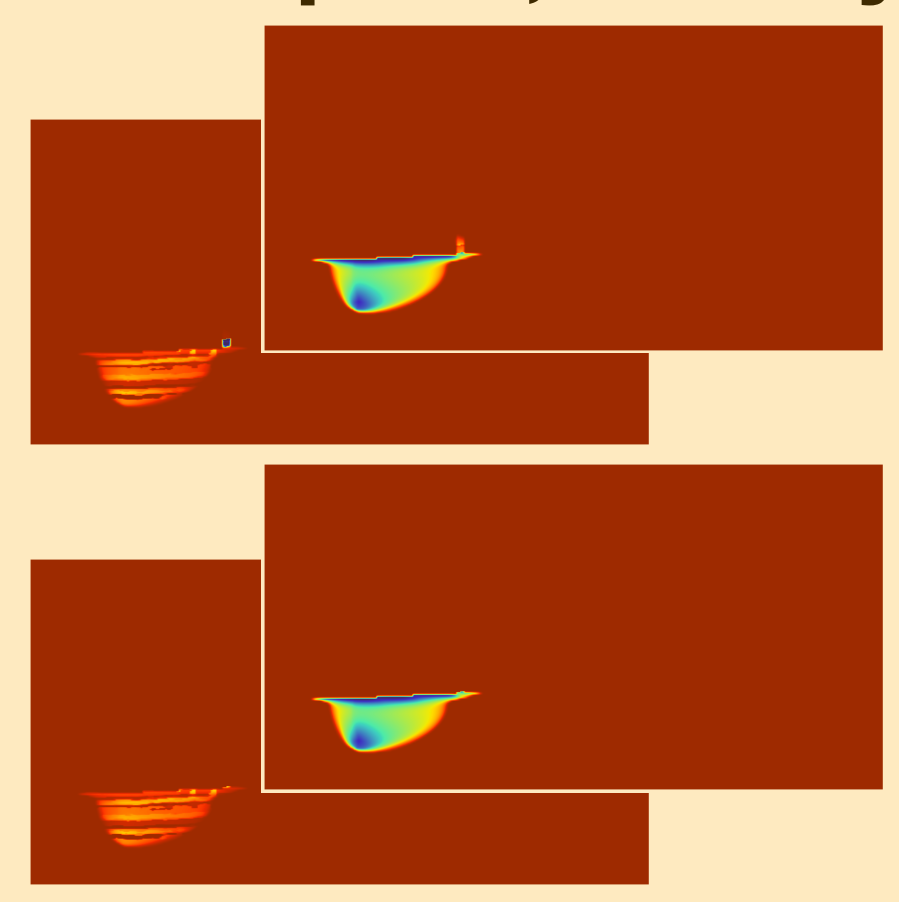
pressure induced fault  
two-phase flow



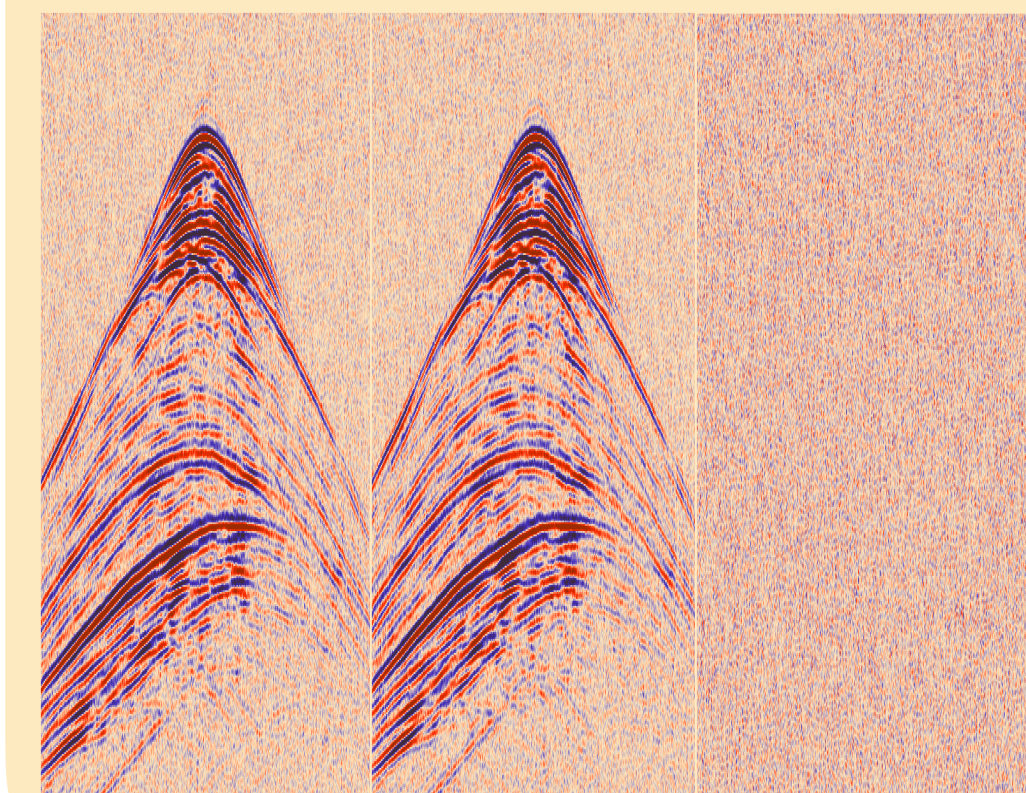
CO<sub>2</sub> dynamics  
concentration, pressure



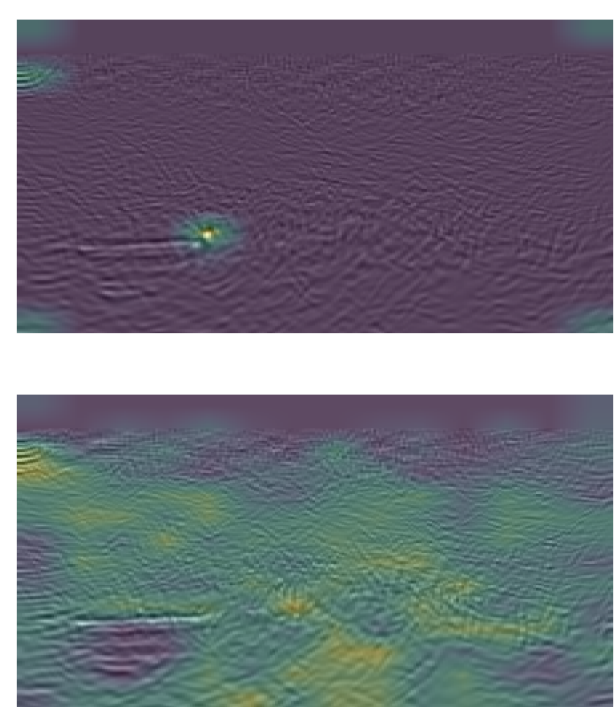
time-lapse models  
wavespeed, density



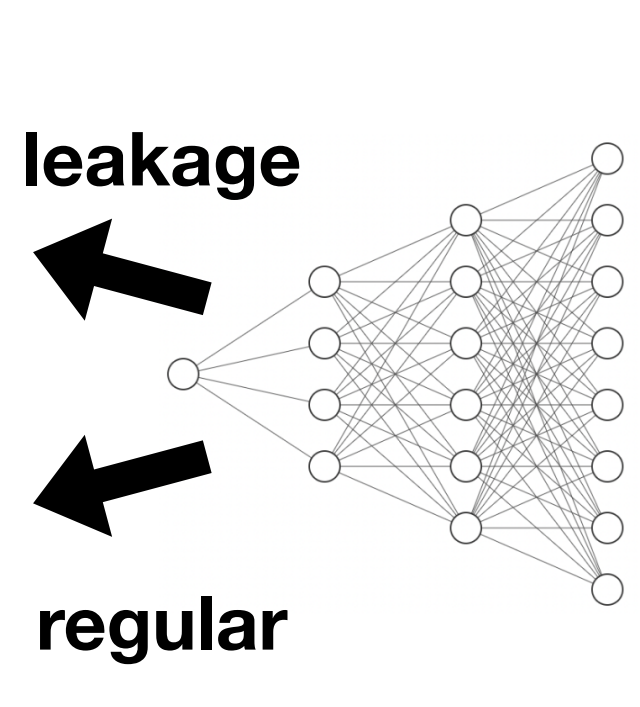
time-lapse (diff) data



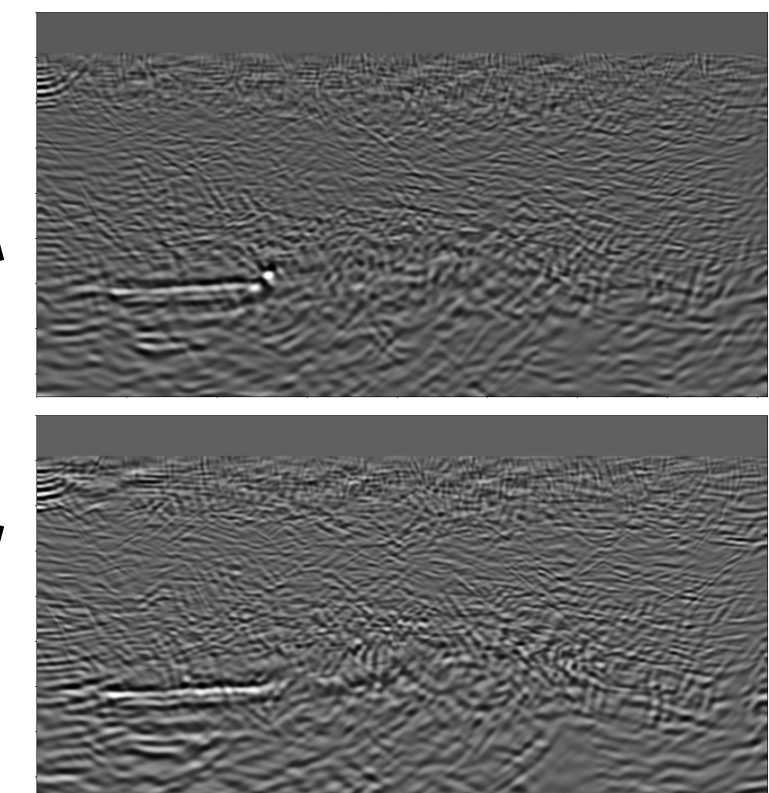
class activation mapping



deep neural classifier



time-lapse imaging



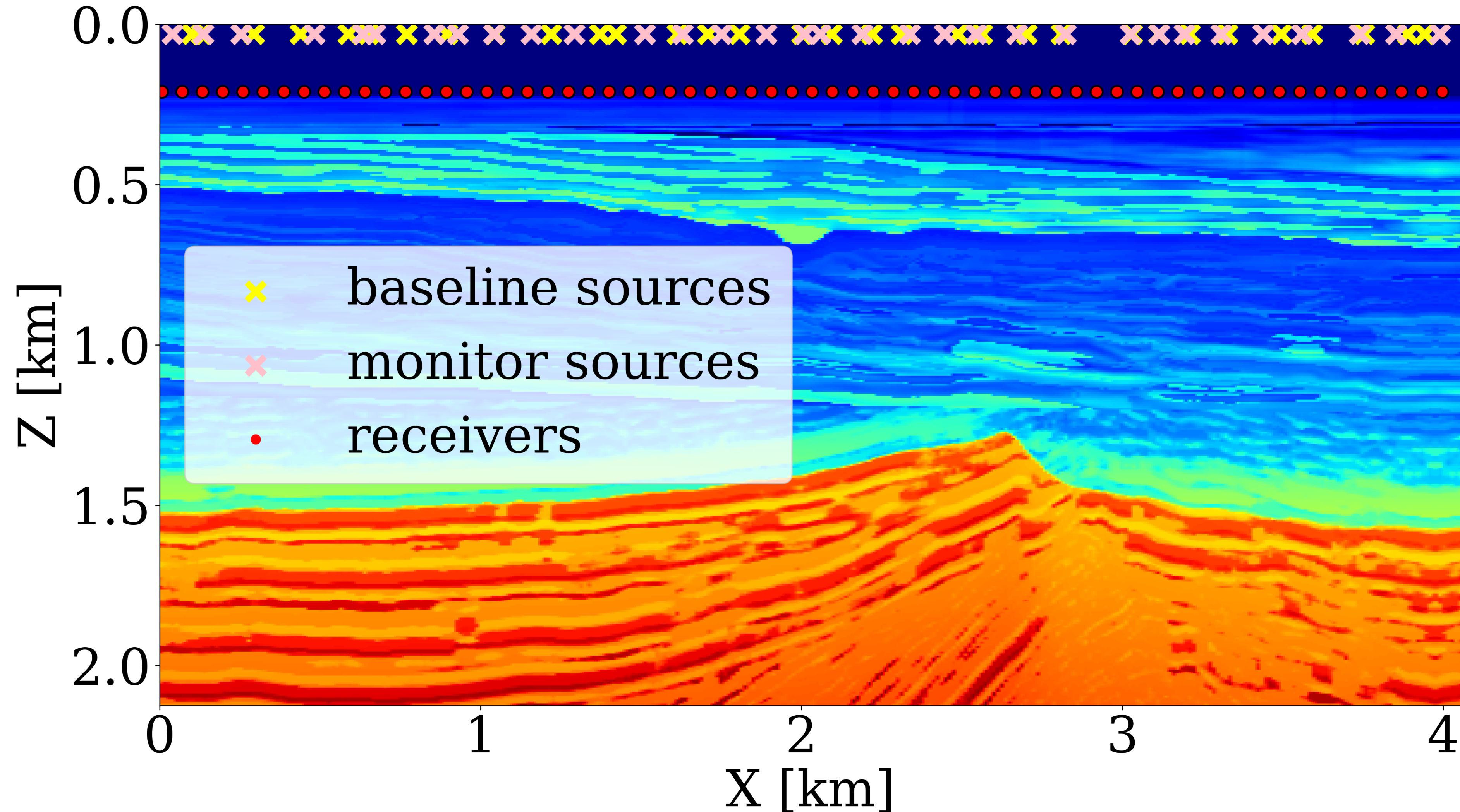
Confusion Matrix

No Leakage	True Neg 193 48.98%	False Pos 13 3.30%
Leakage	False Neg 41 10.41%	True Pos 147 37.31%
	No Leakage	Leakage

accuracy = 86.29%



# Setup



- ▶ 32 non-replicated source locations (average source sampling 125m)
- ▶ 162 hydrophones 2m above ocean bottom (average receiver sampling 25m)
- ▶ Ricker wavelet w/ central frequency 25 Hz

# Seismic time-lapse simulations

```
# Generate nv vintages of linear data
F0 = [Pr*judiModeling(model0)*Ps[i]' for I=1:nv]           # forward modeling
J   = [judiJacobian(F0[i], q[i]) for i=1:nv]             # linearized born modeling
dlin = J .* dimp                                         # generate linear data
# add band-limited noise
noise = deepcopy(dlin)
for k = 1:nv
    for l = 1:nsrc
        # filter white noise by source wavelet
        noise[k].data[l] = real.(ifft(fft(randn(Float32, size(dlin[k].data[l]))).*fft(q[k].data[1])))
    end
end
snr    = 8.0f0
noise = noise/norm(noise) * norm(dlin) * 10f0^(-snr/20f0)
dlin  = dlin + noise                                     # 8 dB additive noise
```

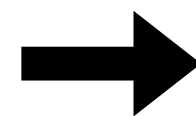
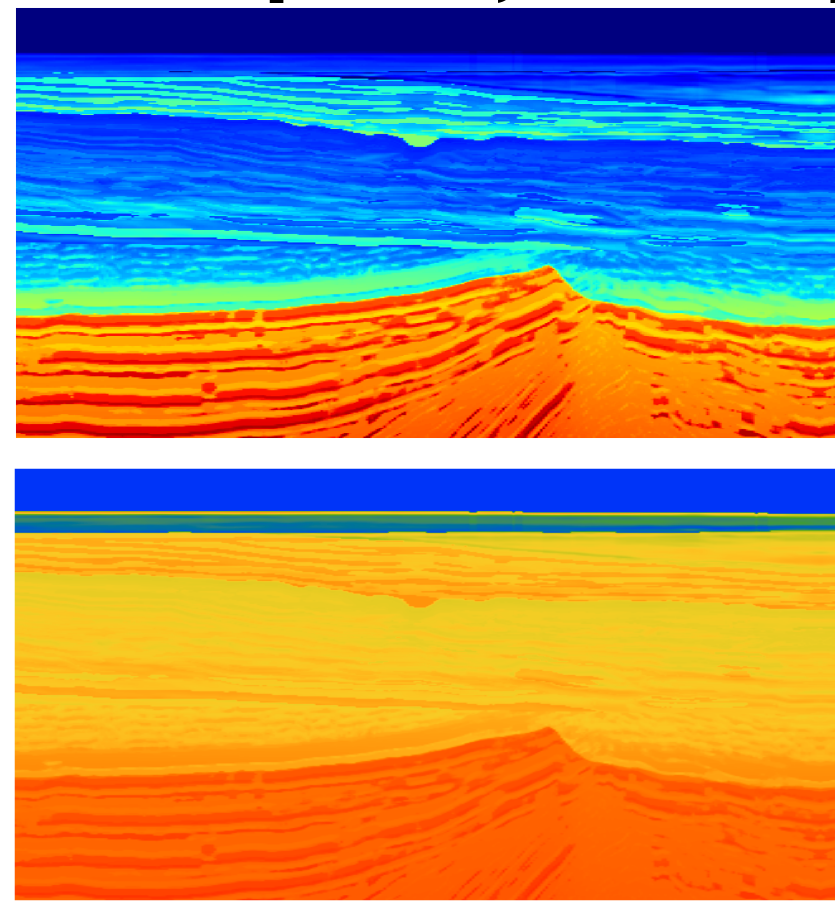
- ▶ linearized Born modeling (demigration)
- ▶ SNR 8 dB by adding white noise filtered w/ source wavelet

# Time-lapse imaging

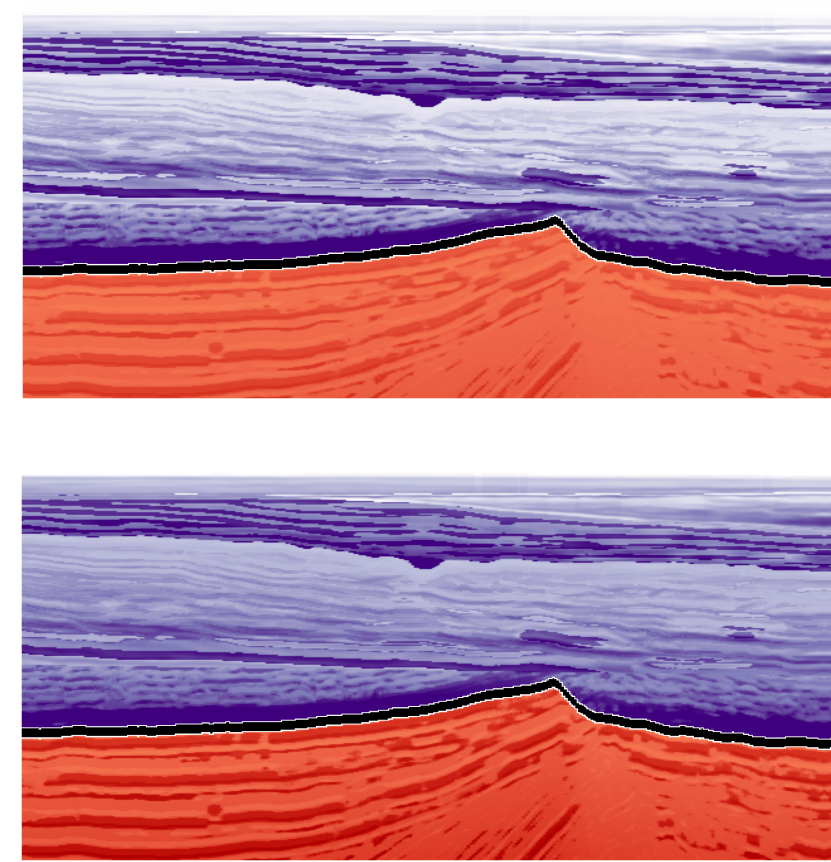


# Workflow

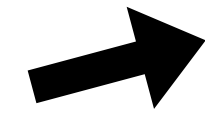
proxy model  
wavespeed, density



reservoir model  
permeability, porosity

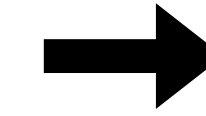
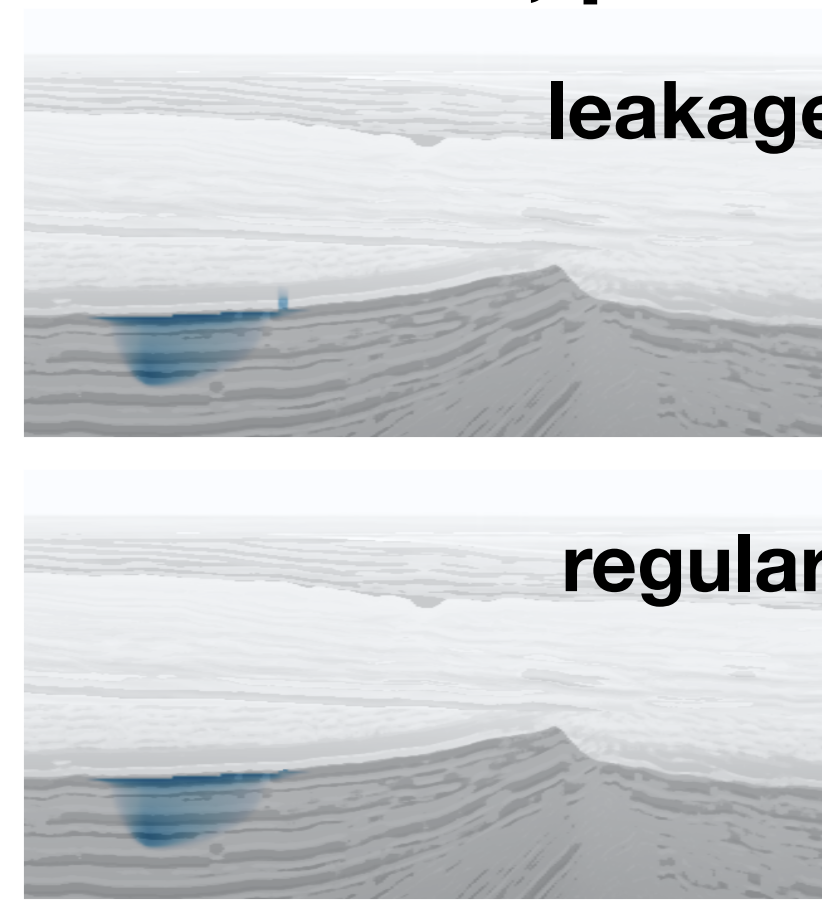


pressure  
induced  
fault

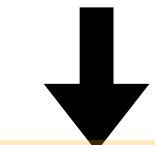
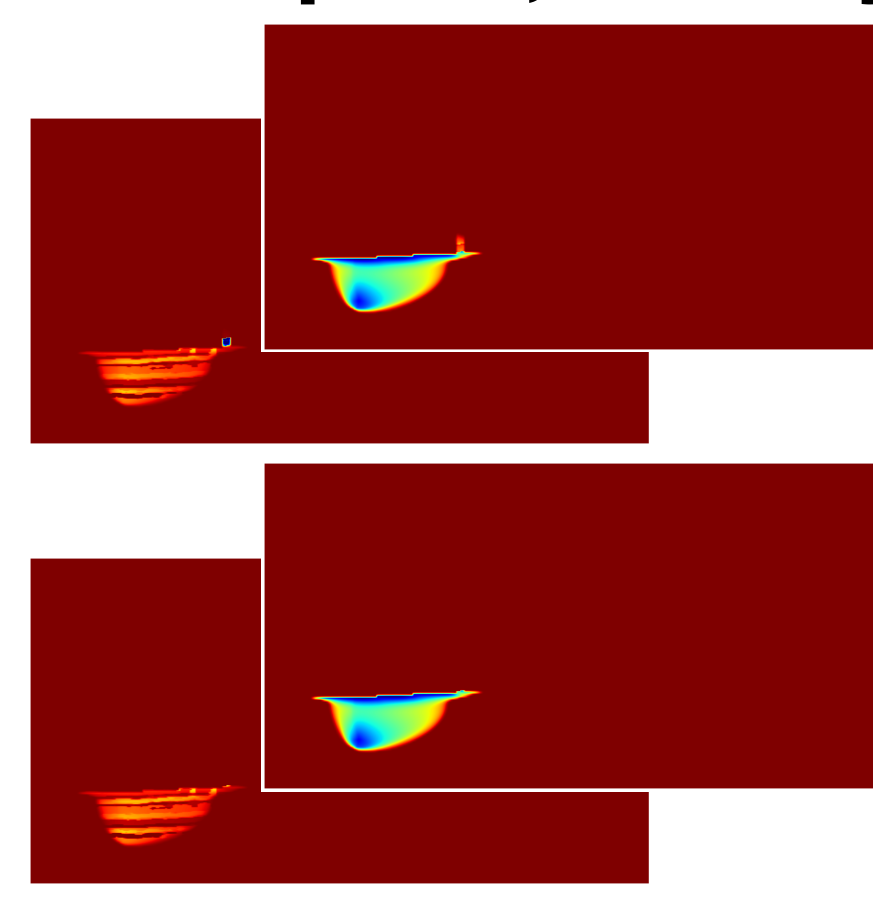


two-phase  
flow

CO<sub>2</sub> dynamics  
concentration, pressure



time-lapse models  
wavespeed, density



class activation mapping

deep neural classifier

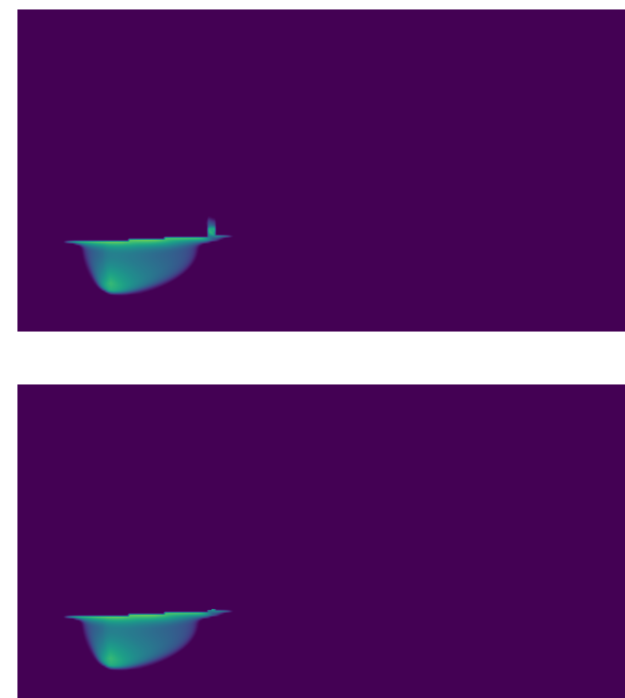
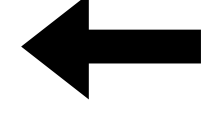
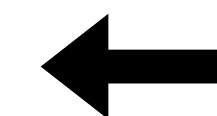
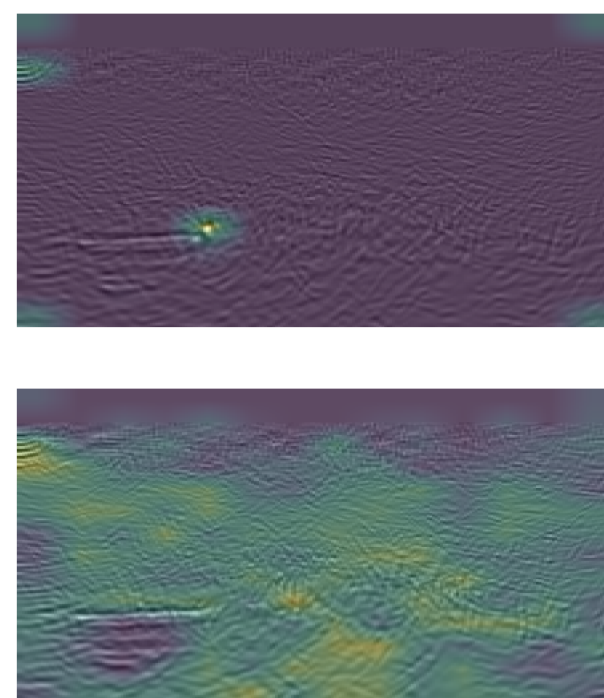
time-lapse imaging

time-lapse (diff) data

Confusion Matrix

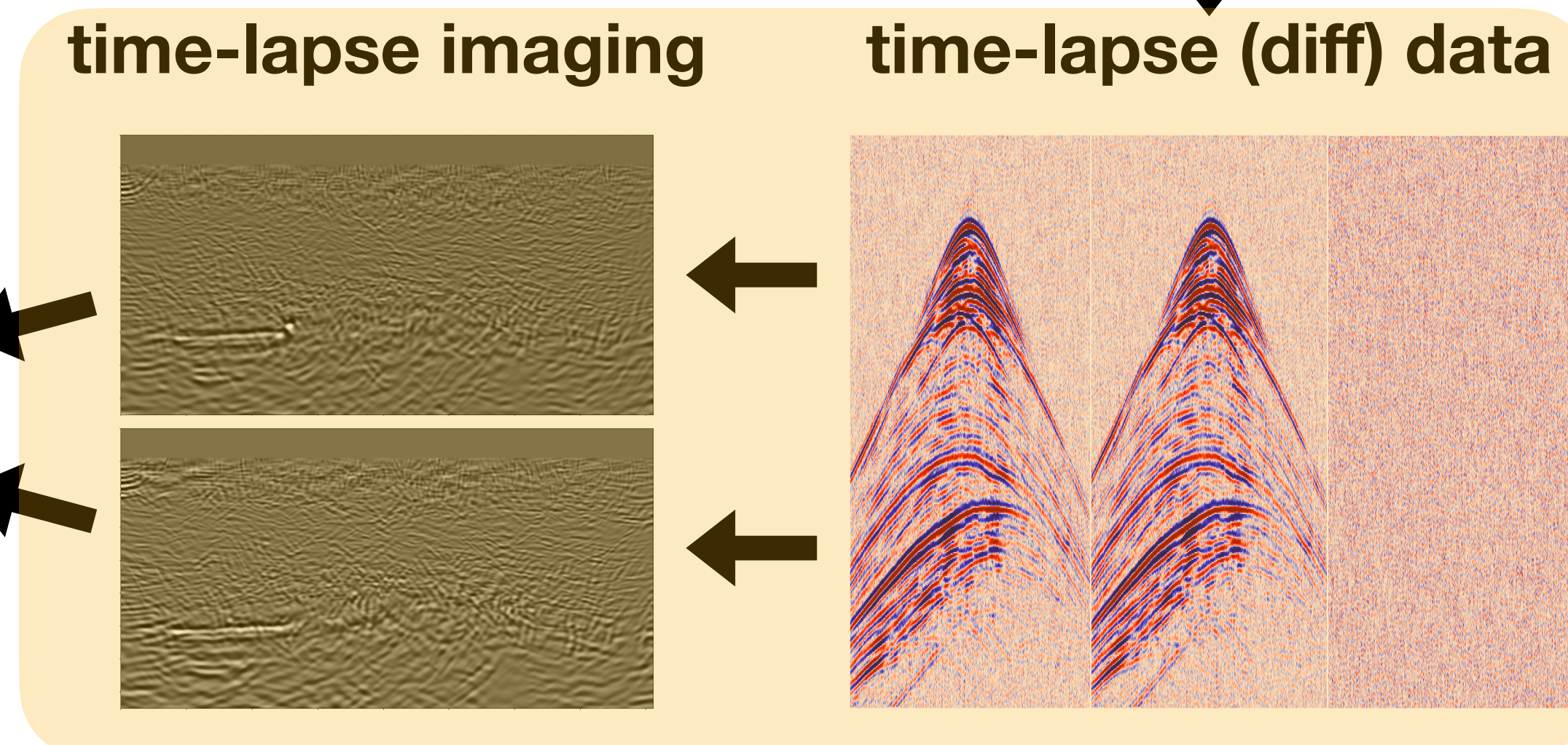
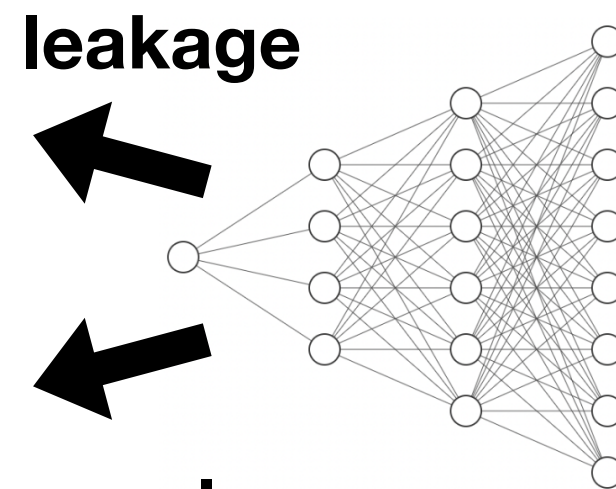
No Leakage	True Neg 193 48.98%	False Pos 13 3.30%
Leakage	False Neg 41 10.41%	True Pos 147 37.31%
	No Leakage	Leakage

accuracy = 86.29%



leakage

regular





# Joint imaging joint recovery model

Invert  $\mathbf{Az} = \mathbf{b}$  where

$$\mathbf{A} = \begin{bmatrix} \frac{1}{\gamma} \mathbf{A}_1 & \mathbf{A}_1 & & & \\ \frac{1}{\gamma} \mathbf{A}_2 & & \mathbf{A}_2 & & \\ \dots & & & \dots & \\ \frac{1}{\gamma} \mathbf{A}_{n_v} & & & & \mathbf{A}_{n_v} \end{bmatrix} \quad \mathbf{z} = \begin{bmatrix} \mathbf{z}_0^\top & \mathbf{z}_1^\top & \dots & \mathbf{z}_{n_v}^\top \end{bmatrix}^\top$$

common component      innovation components

$\gamma$  ( $0 < \gamma < n_v$ ) controls weight on *common* component

1st column adds complementary info when  $\mathbf{A}_i \neq \mathbf{A}_j$

exploit shared information

**No need to *replicate* to get high degrees of repeatability**



# Optimization

## linearized Bregman Iterations

Solve via curvelet-domain sparsity promotion:

$$\begin{aligned} \min_{\mathbf{x}} \quad & \lambda \|\mathbf{C}\mathbf{x}\|_1 + \frac{1}{2} \|\mathbf{C}\mathbf{x}\|_2^2 \\ \text{subject to} \quad & \|\mathbf{b} - \mathbf{A}\mathbf{x}\|_2^2 \leq \sigma^2 \end{aligned}$$

for  $k = 1, 2, \dots$

$$\mathbf{u}^{k+1} = \mathbf{u}^k - t^k \mathbf{A}^{(k)\top} (\mathbf{A}^{(k)} \mathbf{x}^k - \mathbf{b}^{(k)})$$

$$\mathbf{x}^{k+1} = \mathbf{C}^\top S(\mathbf{C}\mathbf{u}^{k+1}, \lambda)$$

$\mathbf{C}$  – curvelet transform

$\mathbf{A}^{(k)}, \mathbf{b}^{(k)}$  – the demigration operator for randomly (w/ replacement) selected shots

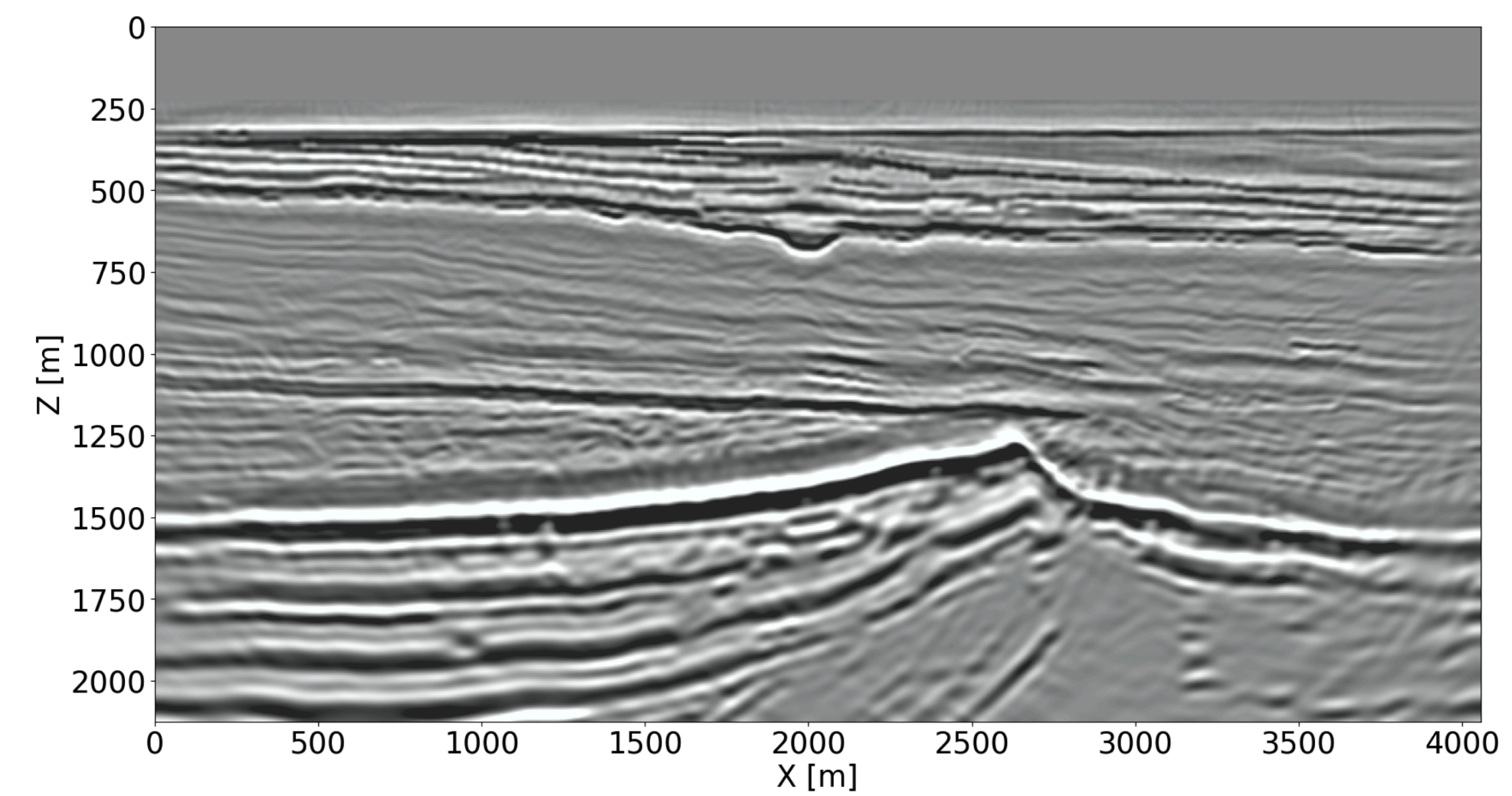
$S(t, \lambda) = \max\{|t| - \lambda, 0\} \text{sign}(t)$  – soft thresholding w/ threshold  $\lambda$



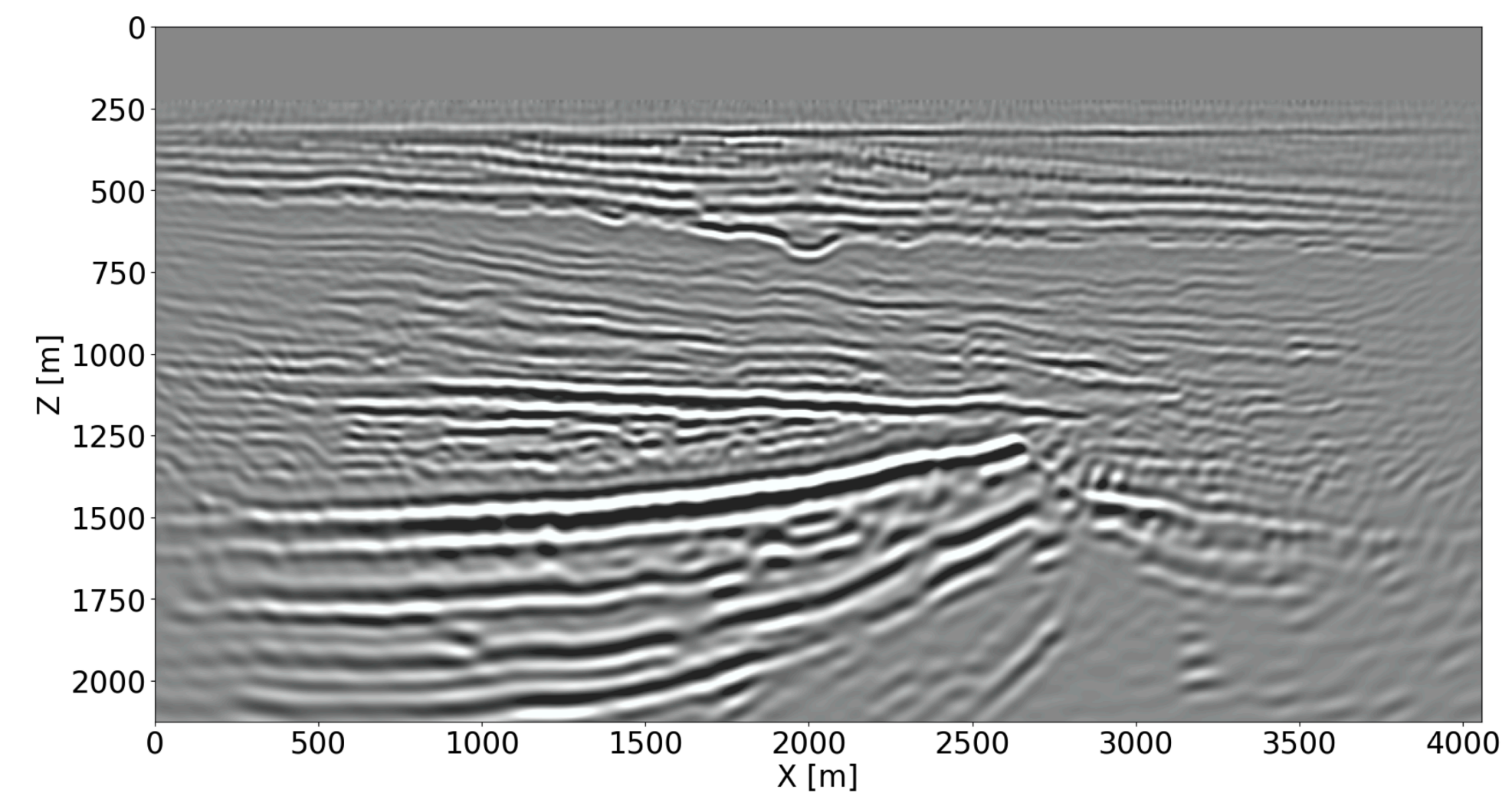
# Seismic imaging

## JRM vs RTM

### JRM



### RTM



Number of iterations: 22

Batch size: 4

Number of sources: 32

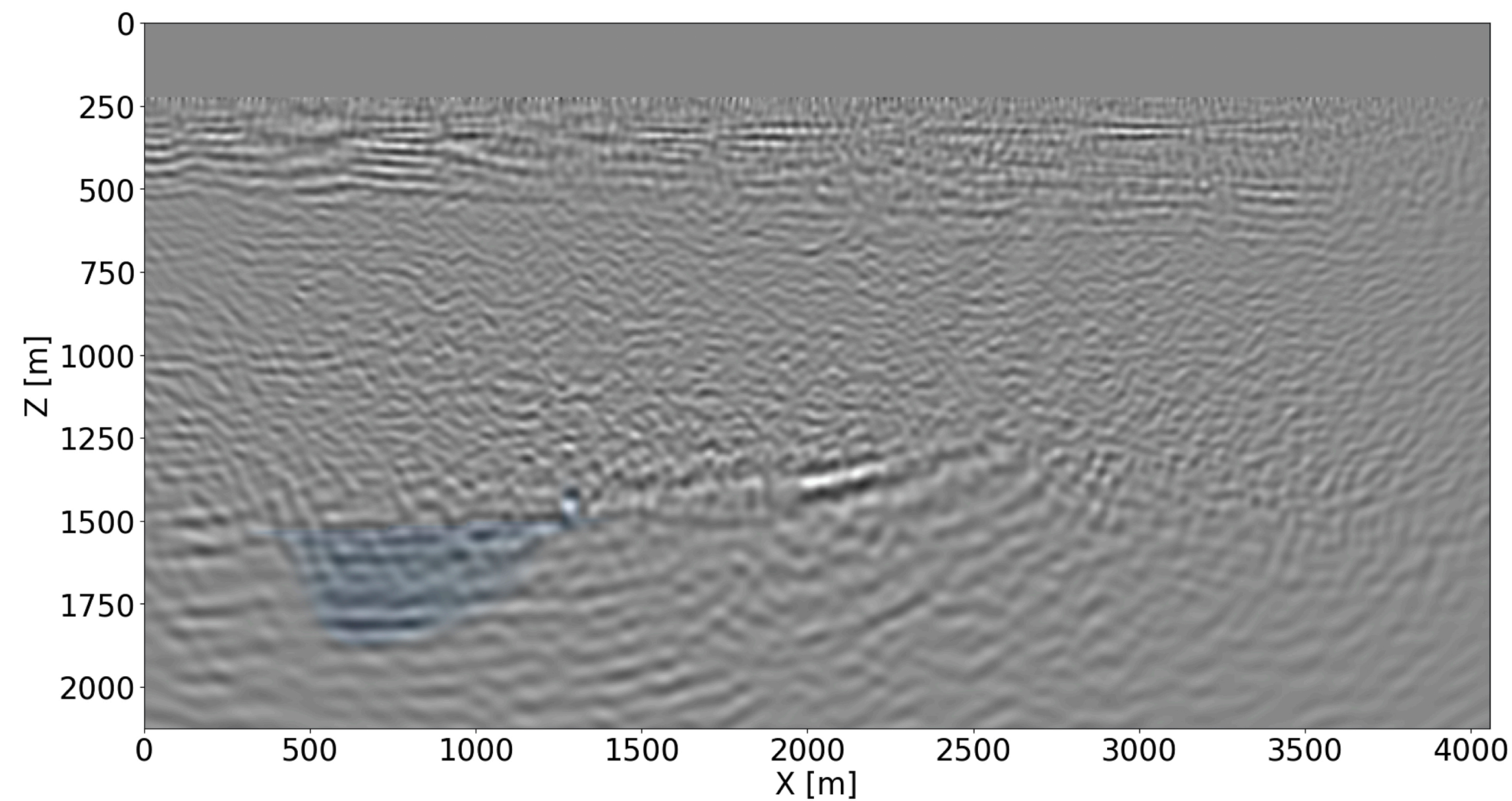
Number of data passes: 3



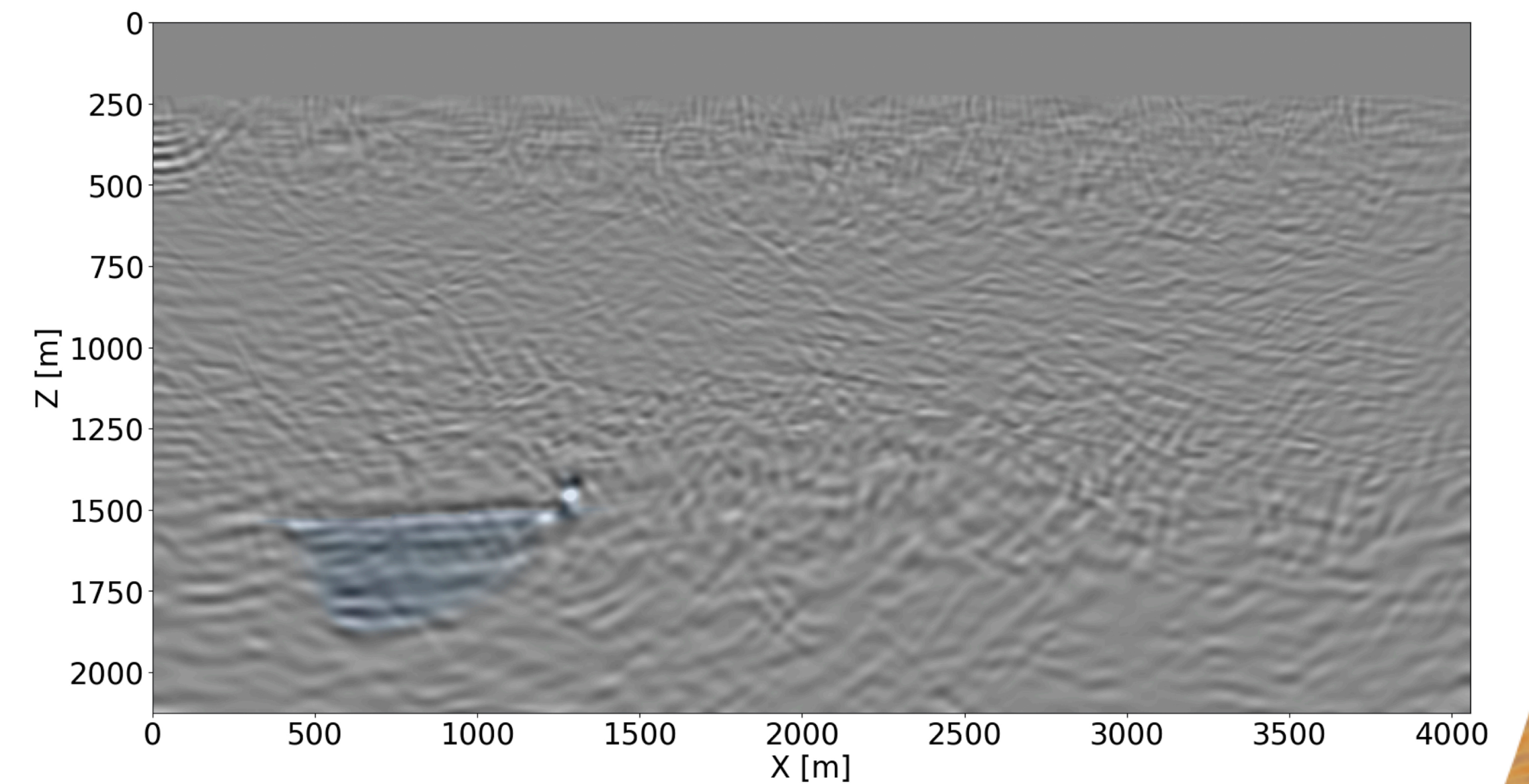
# Time-lapse differences

$$\text{NRMS} = 200\% \times \frac{\|\mathbf{x}_1 - \mathbf{x}_2\|}{\|\mathbf{x}_1\| + \|\mathbf{x}_2\|}$$

**Independent  
RTMs**  
NRMS = 8.48%



**JRM**  
NRMS = 3.20%





# Automatic leakage detection w/ explainable ML

Ziyi Yin, Huseyin Tuna Erdinc, Abhinav Prakash Gahlot, Mathias Louboutin and F. Herrmann. “Derisking geological carbon storage from high-resolution time-lapse seismic to explainable leakage detection.” *The Leading Edge* (2023).

Erdinc, H. T., Gahlot, A. P., Yin, Z., Louboutin, M., & Herrmann, F. J. De-risking Carbon Capture and Sequestration with Explainable CO<sub>2</sub> Leakage Detection in Time-lapse Seismic Monitoring Images. *AAAI Symposium* (2022)

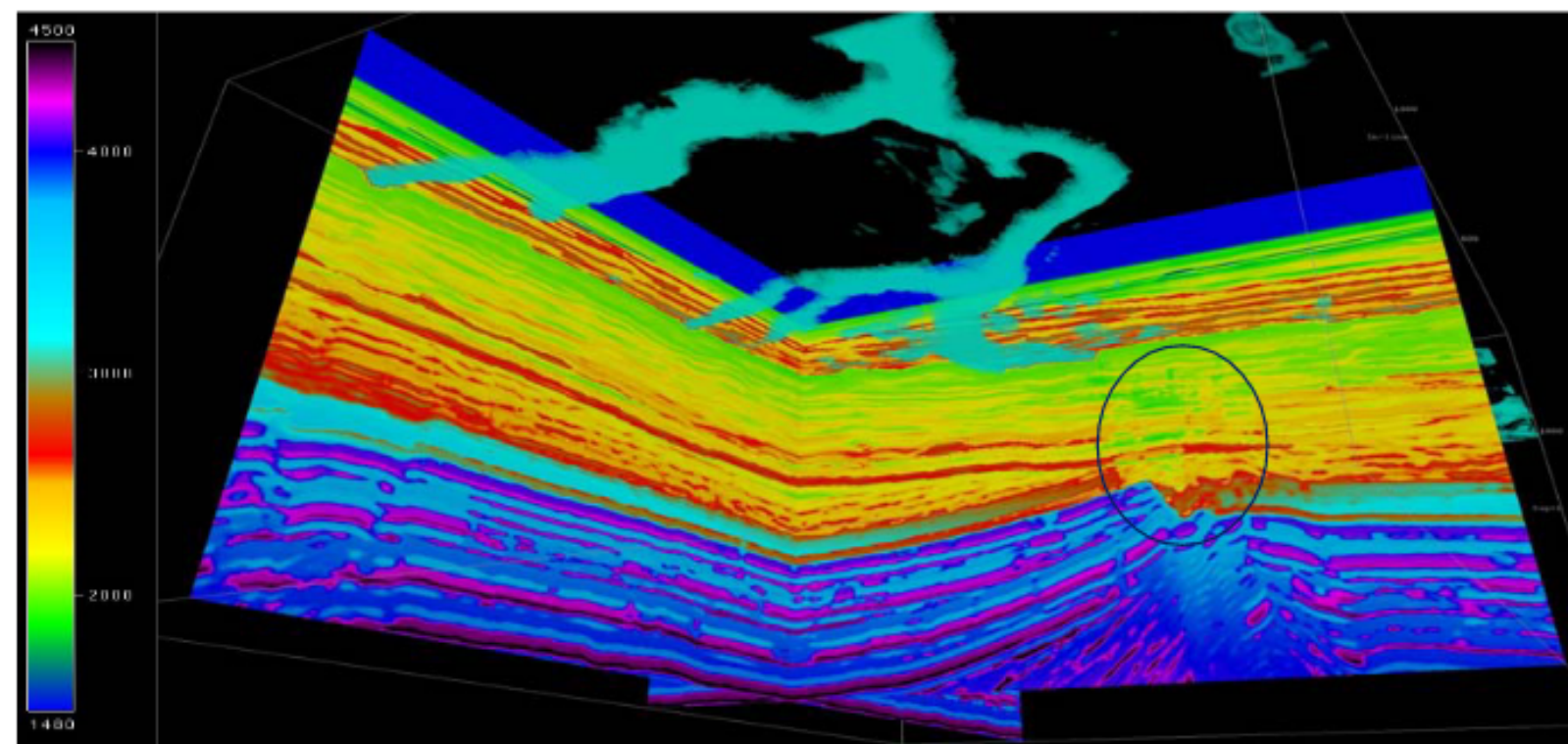


# Training set

## Compass model

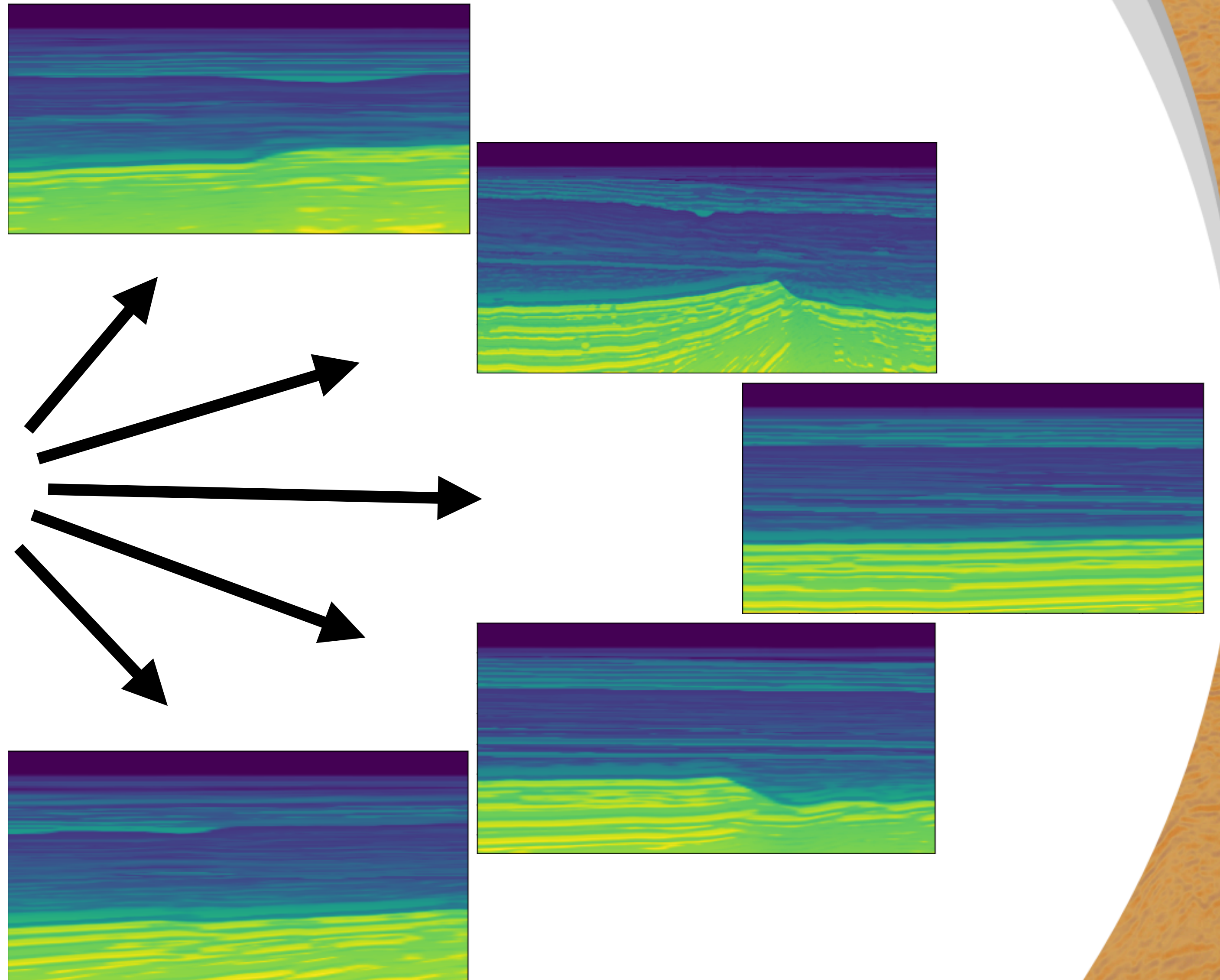
Five different 2D velocity slices

1000 leak/no leak scenarios



Retrieved from Jones (2008)

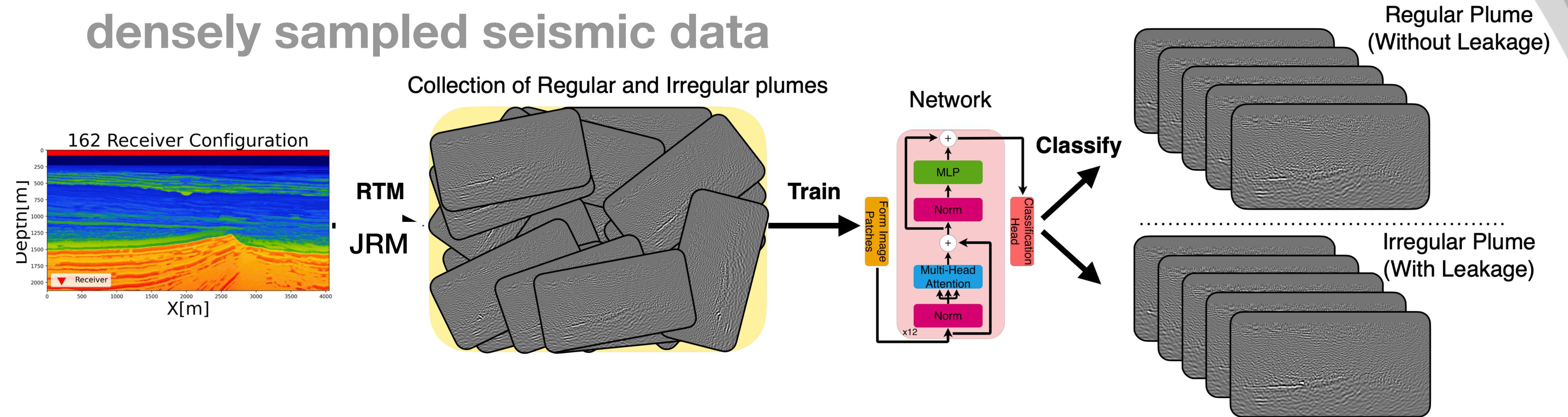
2D Velocity Slices





# Training dataset

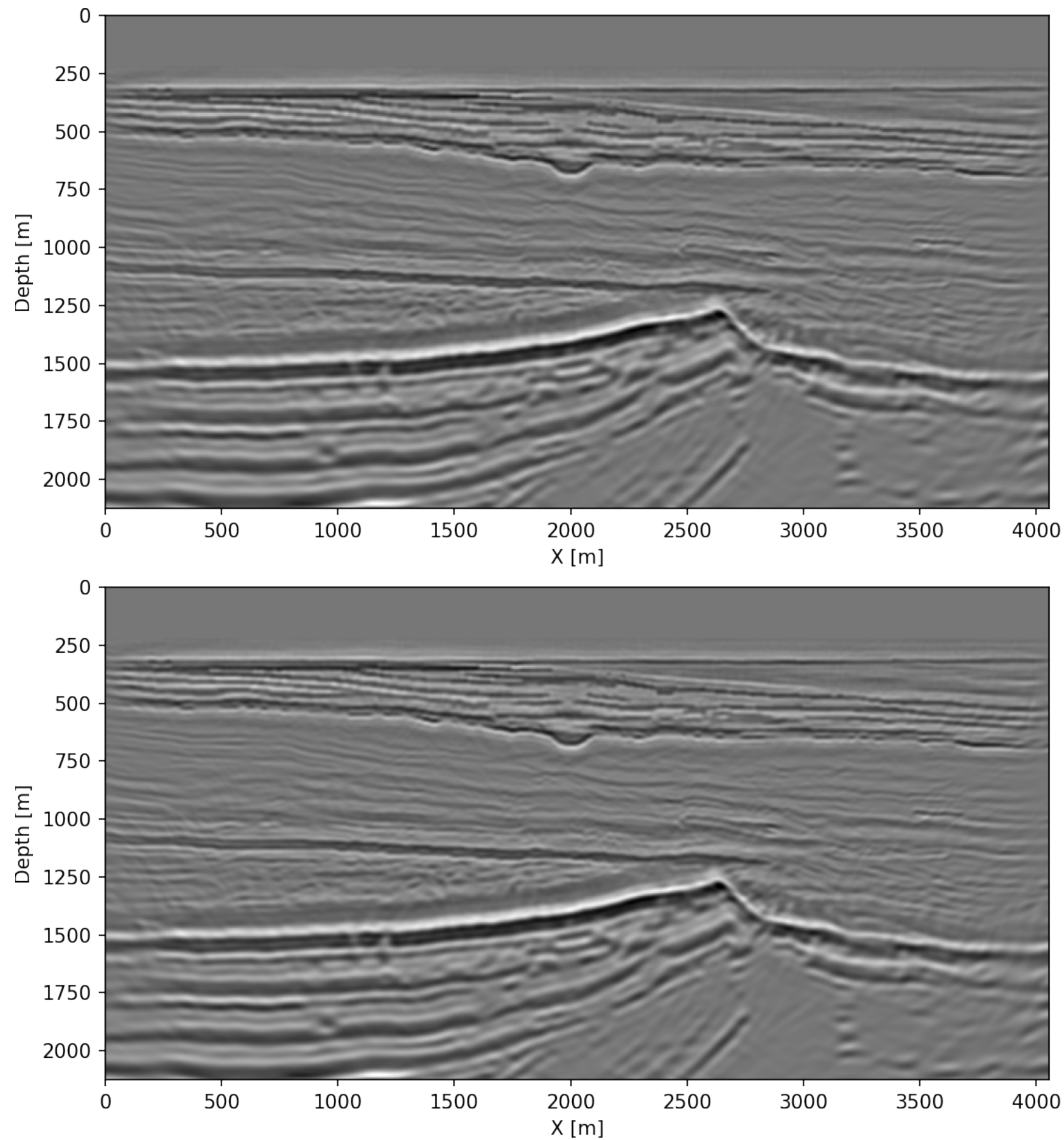
## densely sampled seismic data



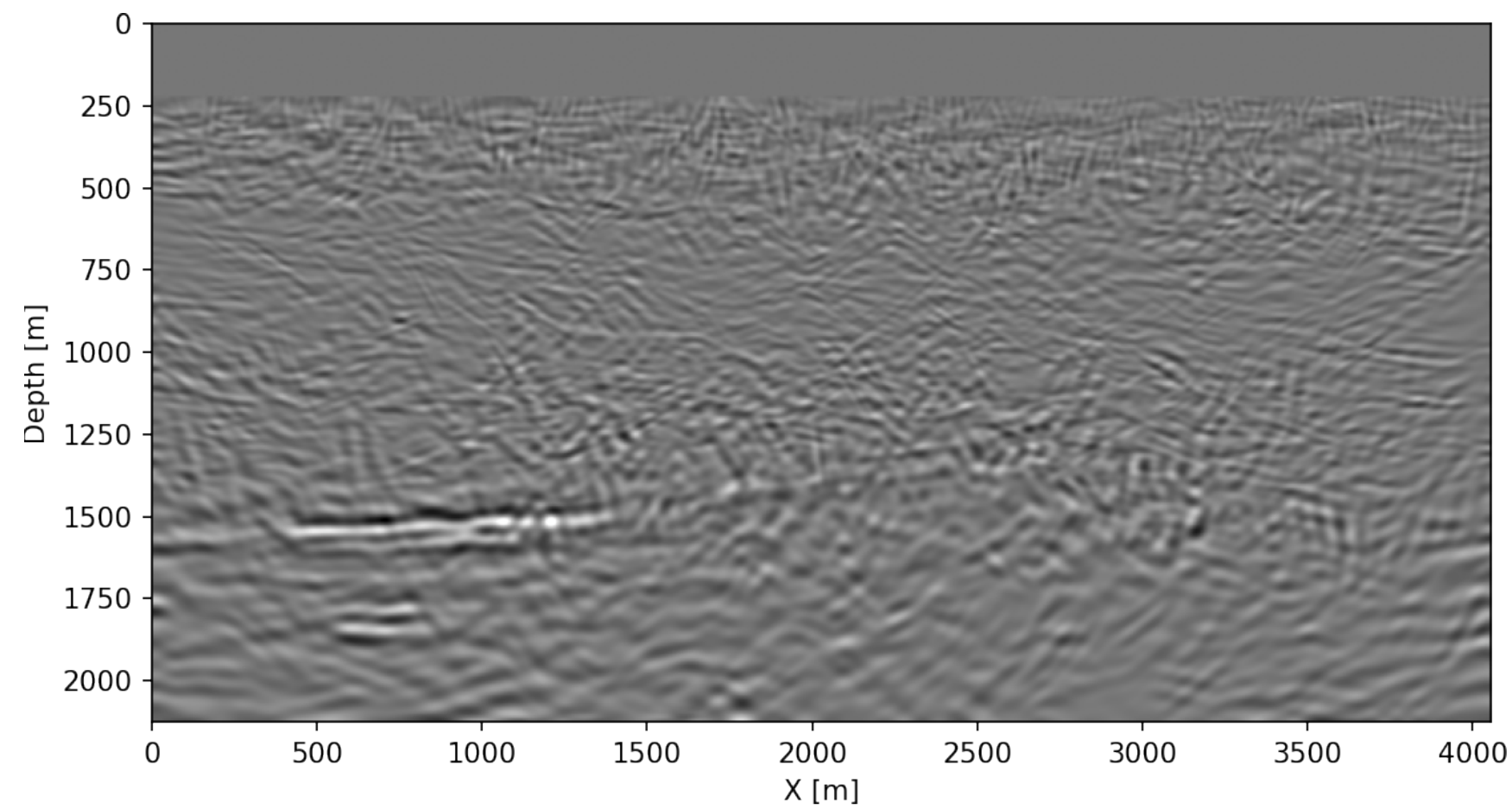
- ▶ pressure  $\geq 15\text{MPa}$  seal opens (12.5 m – 62.5 m) randomly
- ▶ permeability  $10^{-4}\text{ md} \rightarrow 500\text{ md}$
- ▶ linear time-lapse data generated w/ & w/o leakage
- ▶ time-lapse data inverted after 200 days w/ JRM  
<https://github.com/slimgroup/GCS-CAM/blob/main/scripts/JRM.jl>



# Seismic imaging no leakage



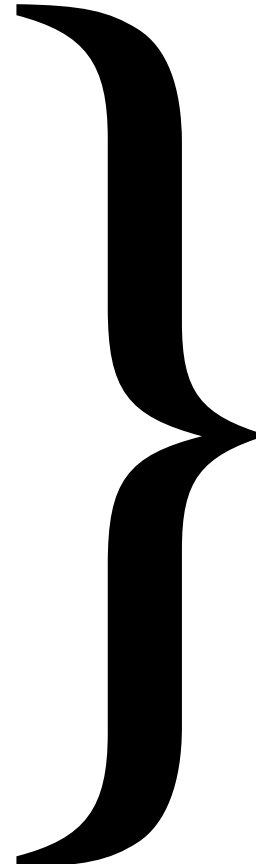
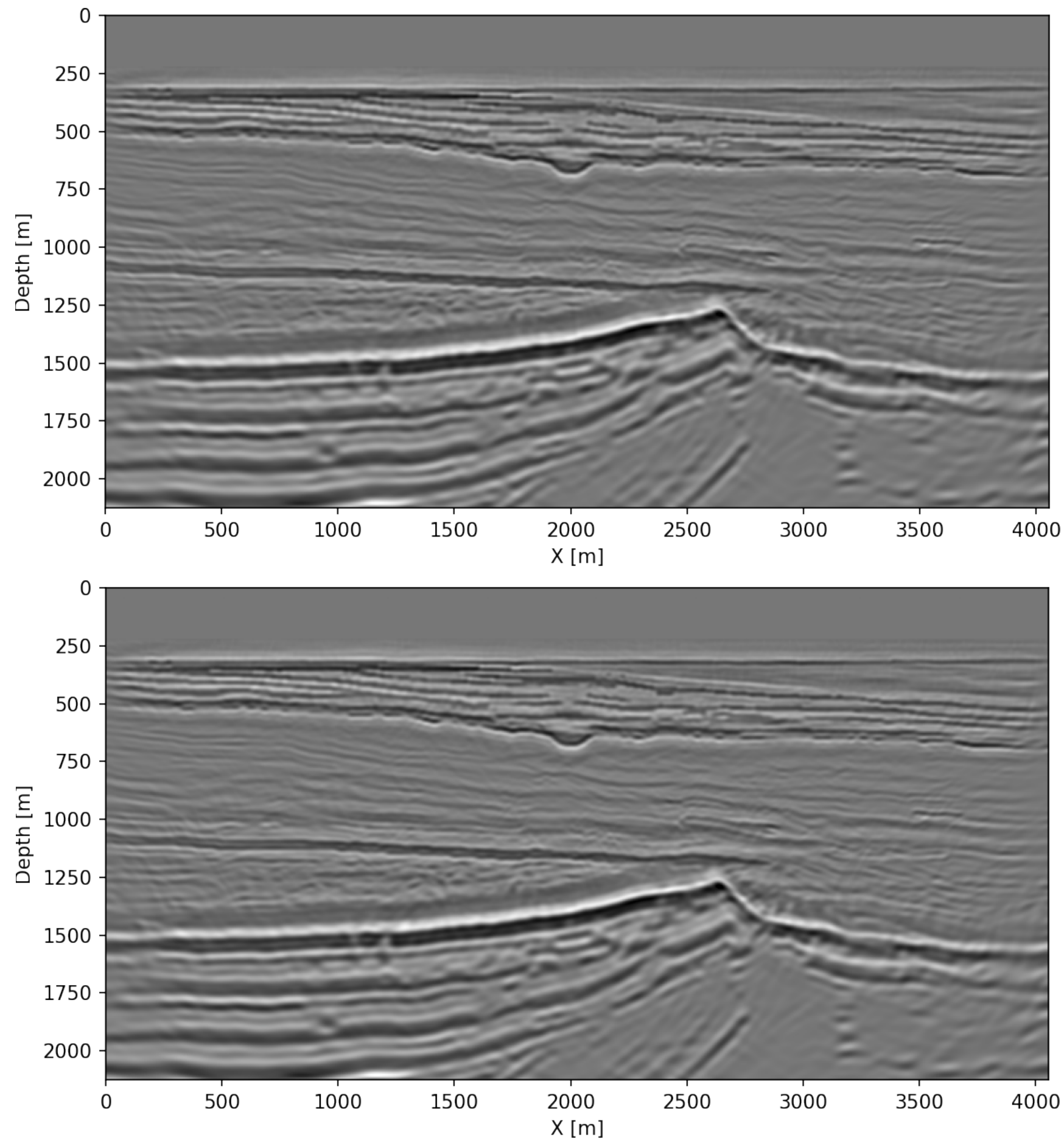
10X no leakage difference image



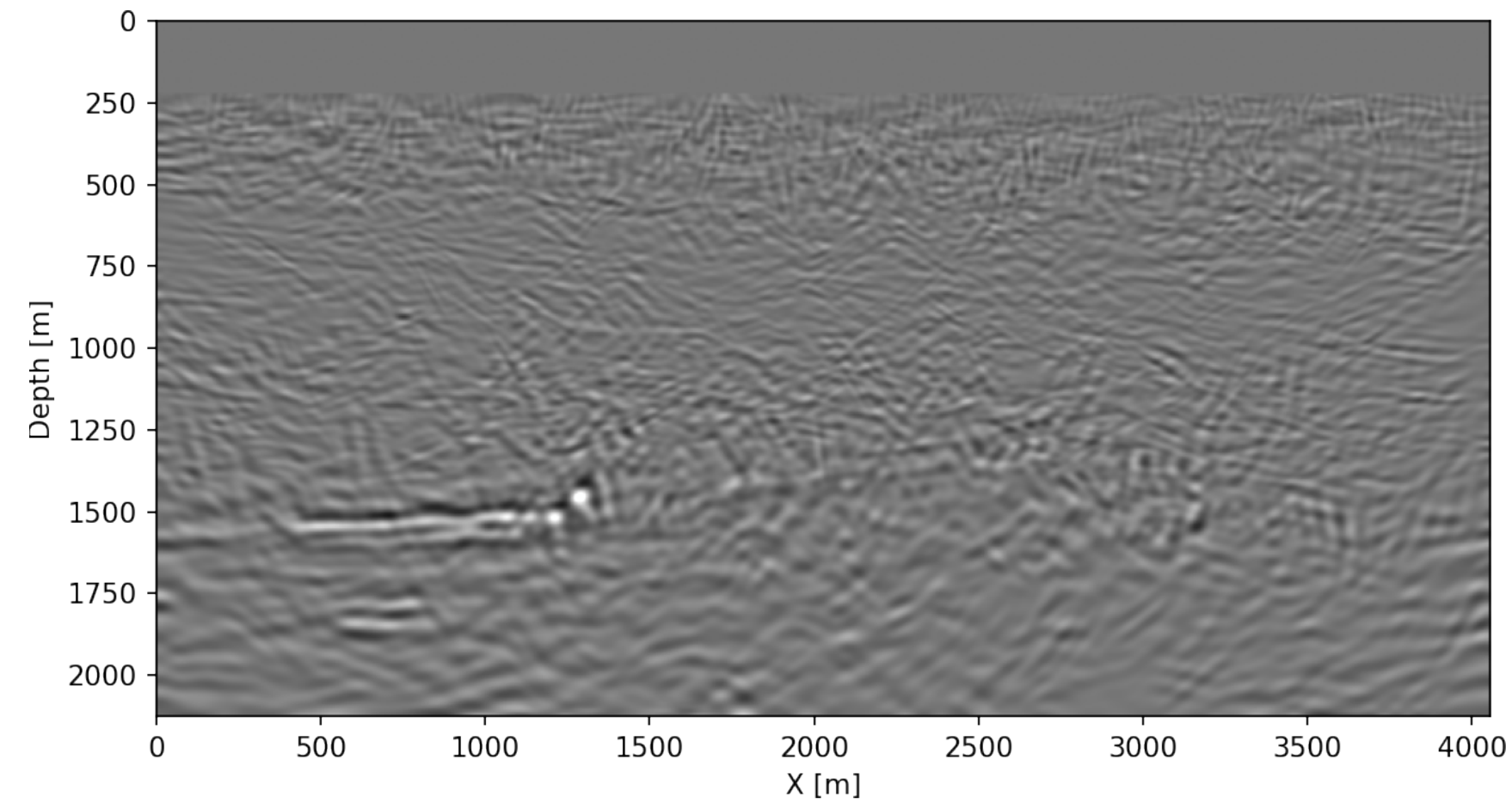
Difference images will be network input



# Seismic imaging leakage



## 10X leakage difference image



Difference images will be network input



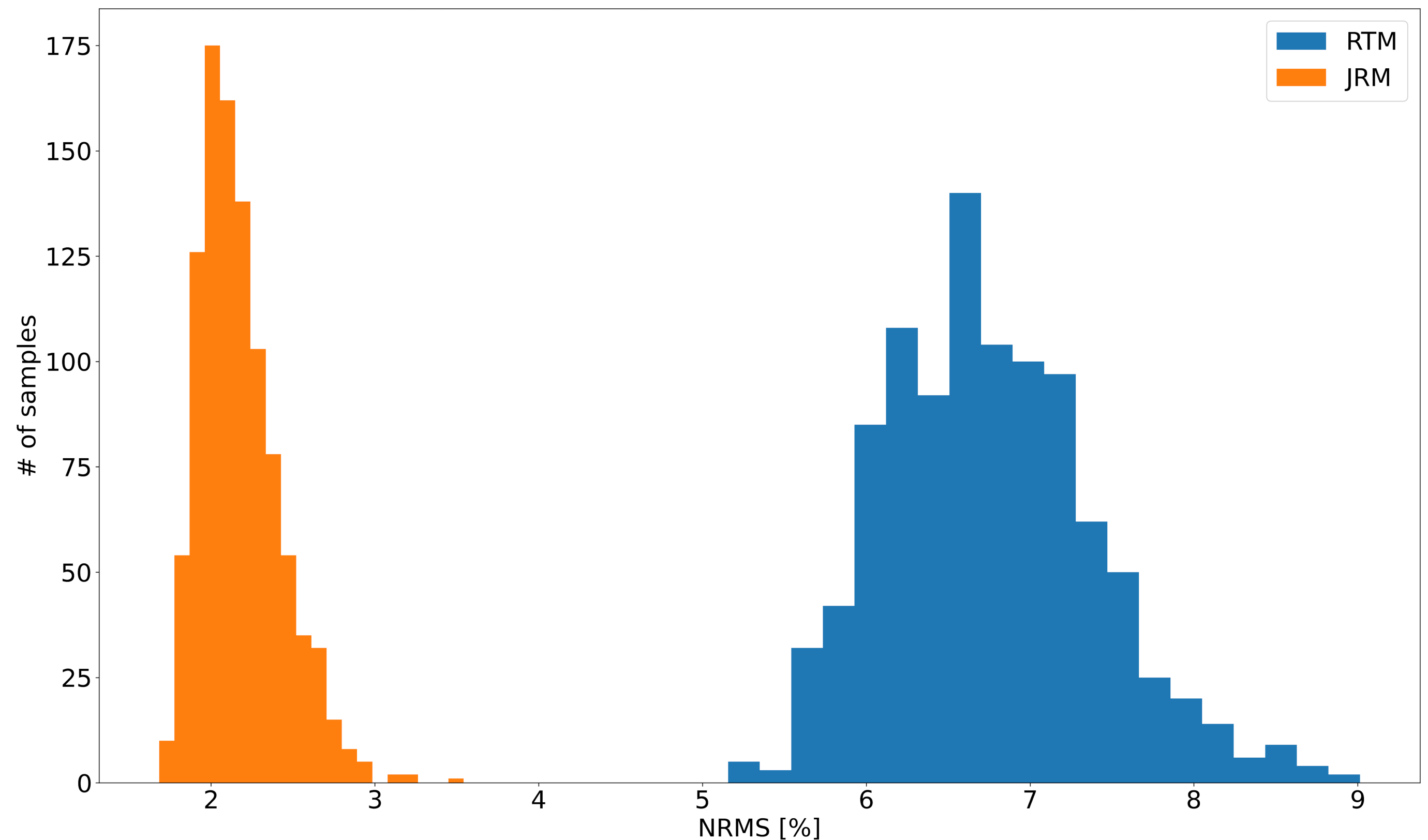
# JRM vs independent Imaging

## NRMS histogram

### JRM:

- ▶ lower NRMS
- ▶ narrower range
- ▶ **6~7% → 2~3%**
- ▶ more *repeatable* recovery

### NRMS statistics



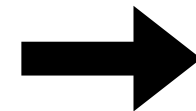
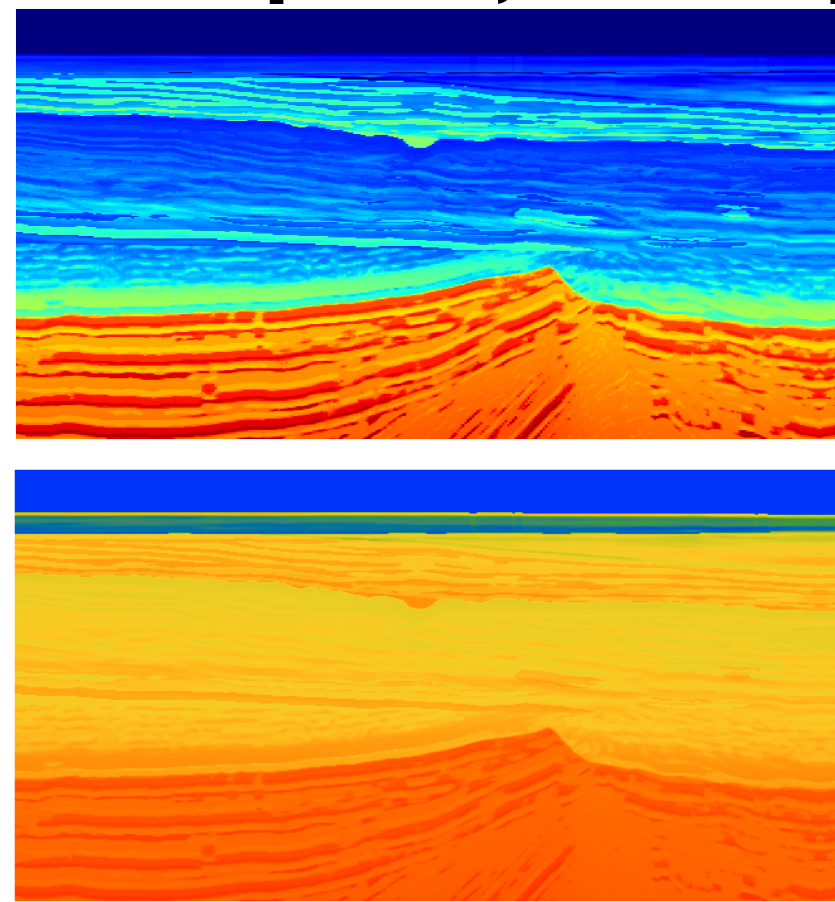


# Class activation mapping

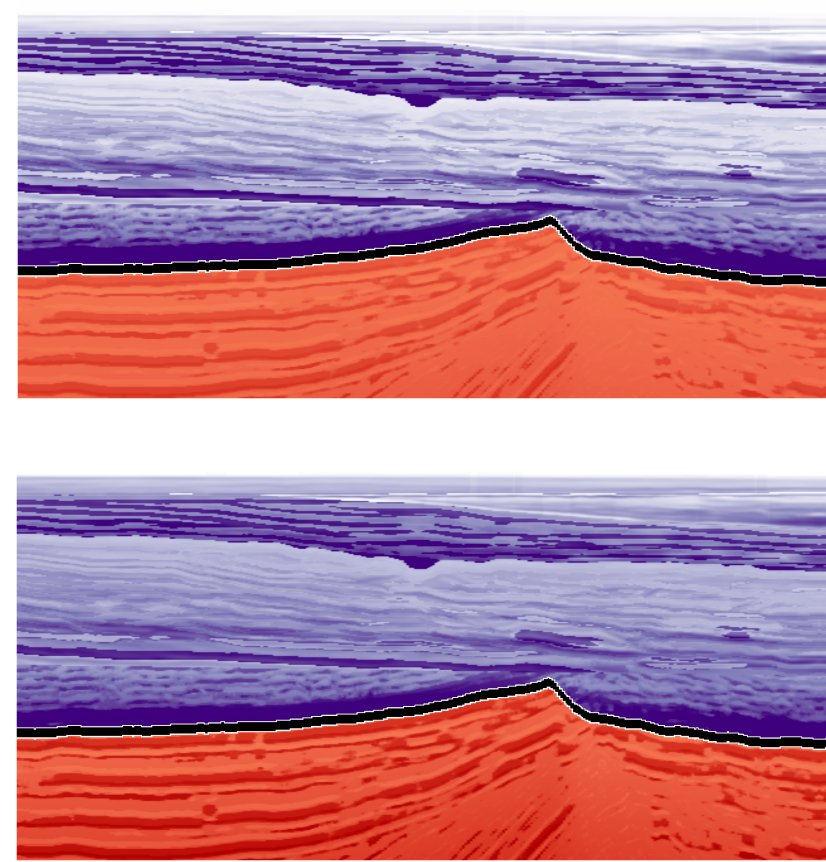


# Workflow

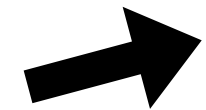
proxy model  
wavespeed, density



reservoir model  
permeability, porosity



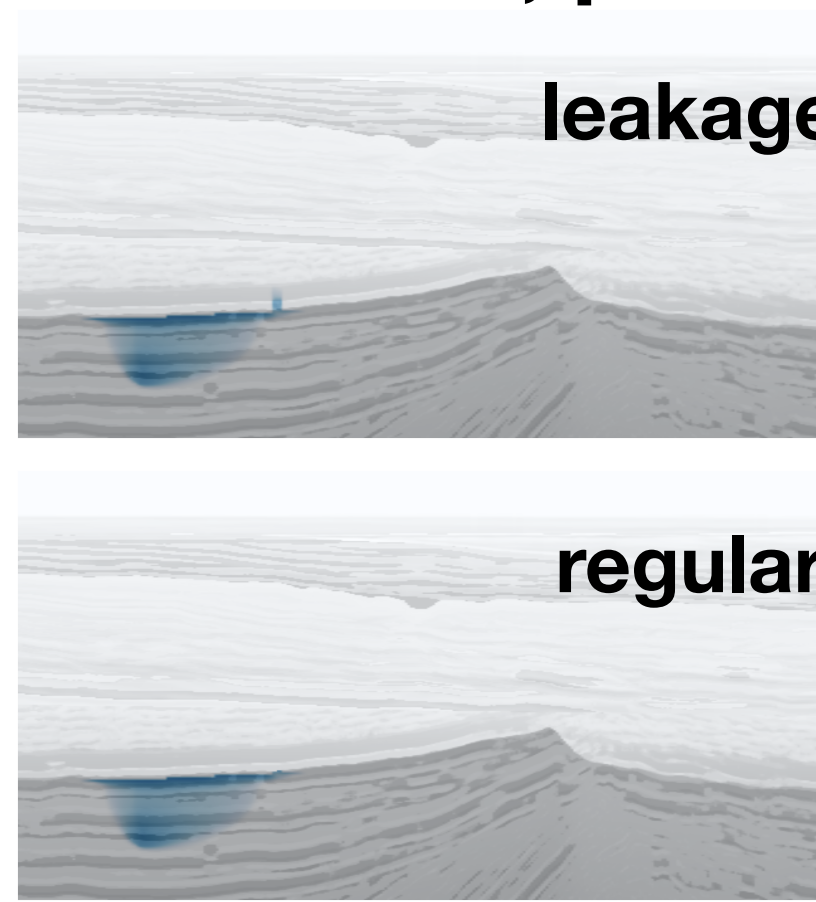
pressure  
induced  
fault



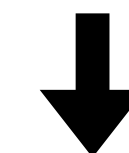
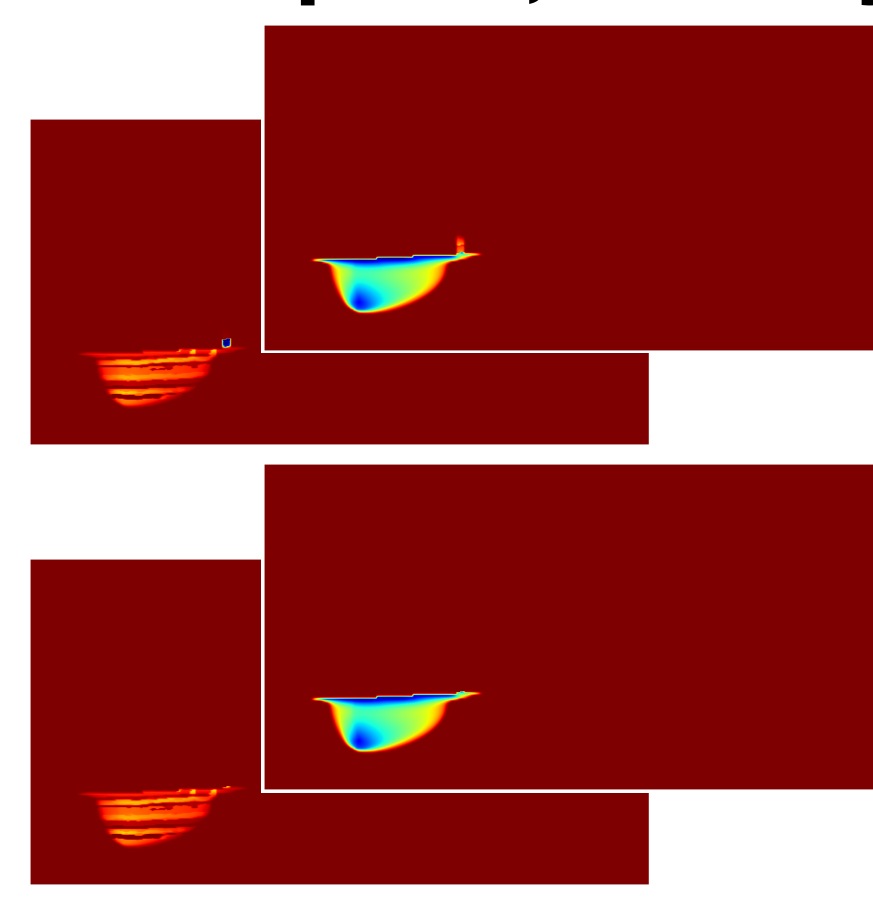
two-phase  
flow



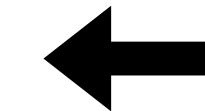
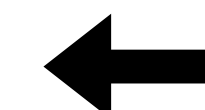
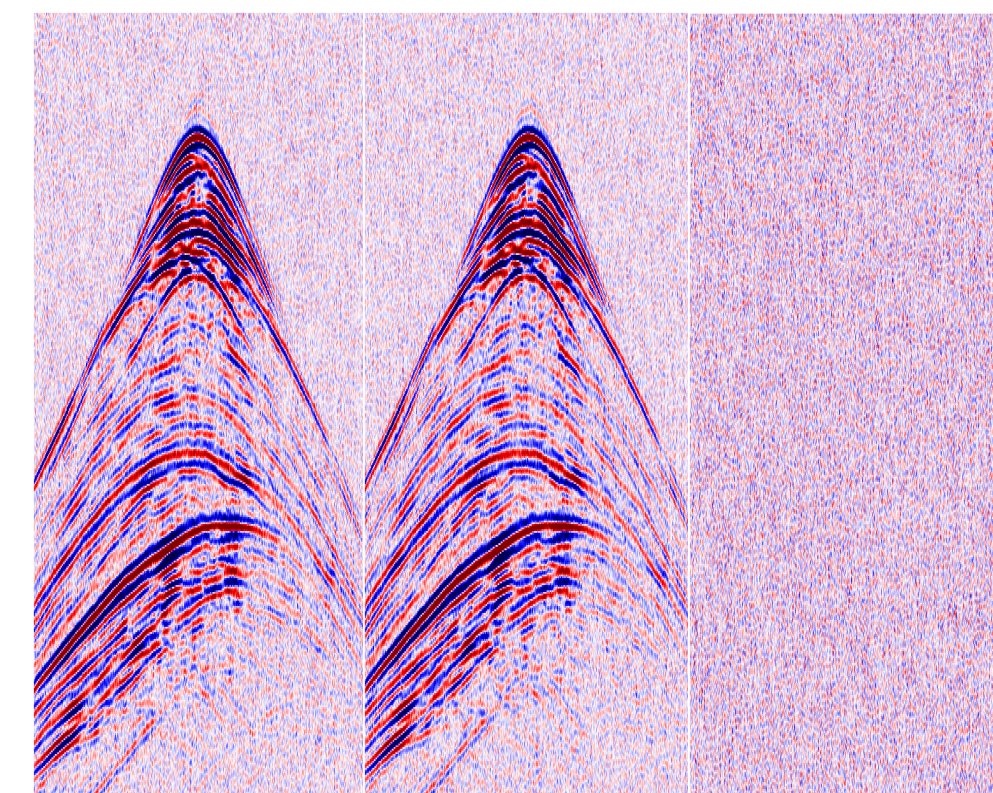
CO<sub>2</sub> dynamics  
concentration, pressure



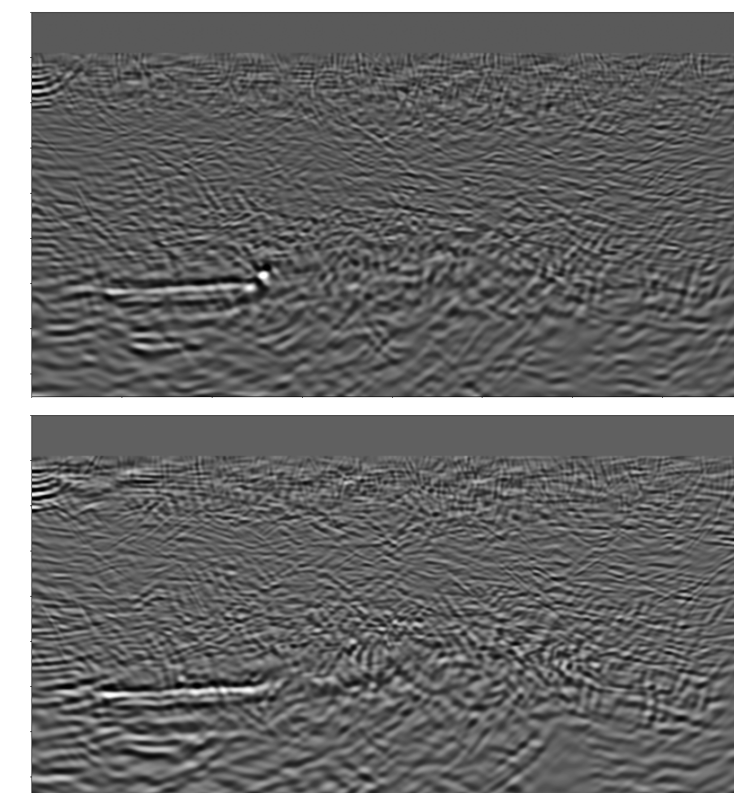
time-lapse models  
wavespeed, density



time-lapse (diff) data



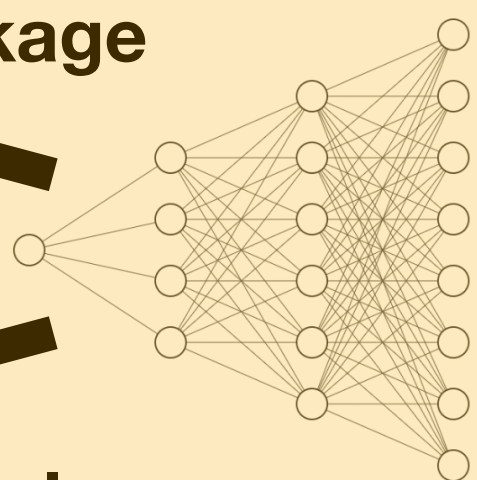
time-lapse imaging



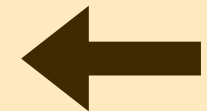
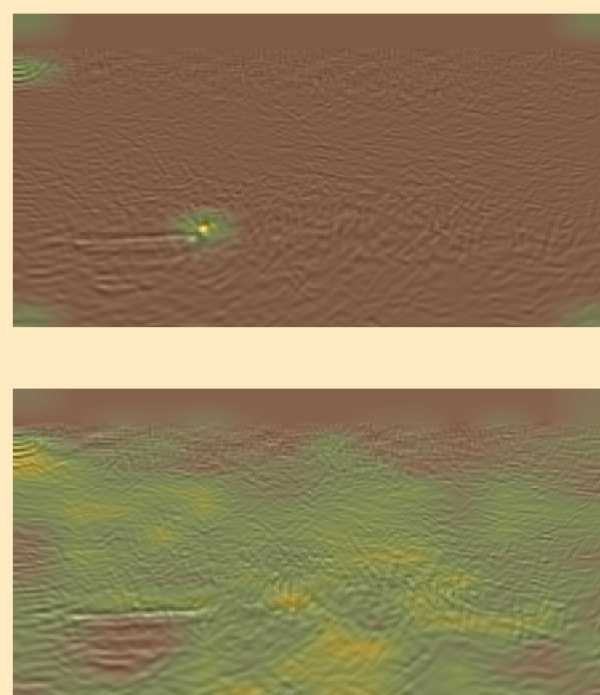
deep neural classifier

leakage

regular



class activation mapping



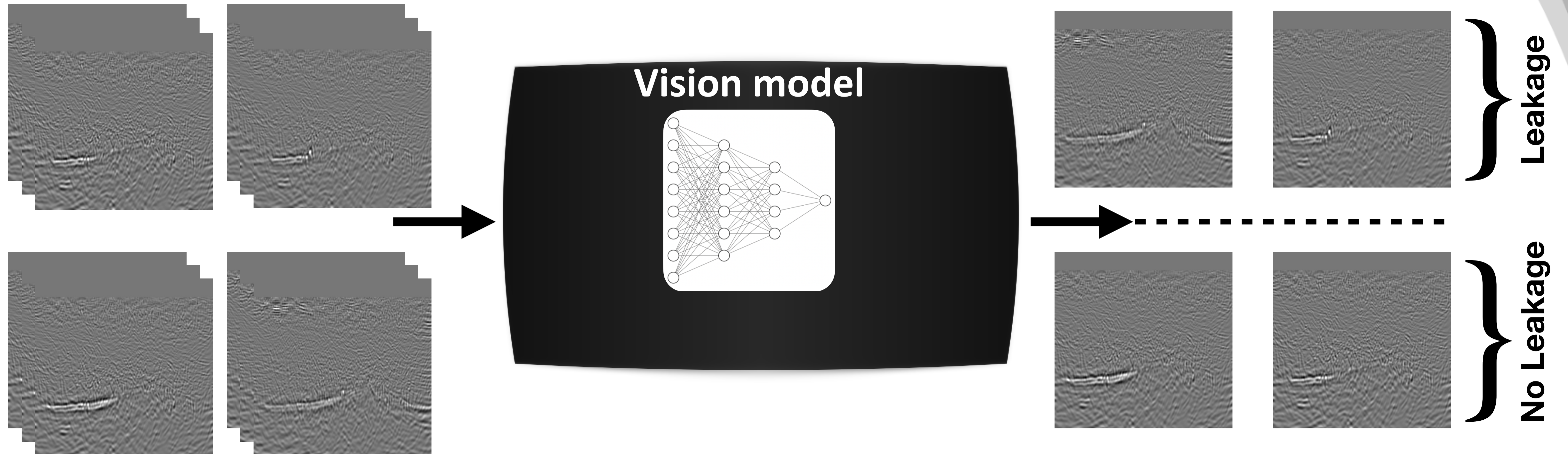
Confusion Matrix

No Leakage	True Neg 193 48.98%	False Pos 13 3.30%
Leakage	False Neg 41 10.41%	True Pos 147 37.31%
	No Leakage	Leakage

accuracy = 86.29%



# Classification network training



Convert time-lapse difference images to 224x224 size w/ 3 channels

Use state-of-the-art pre-trained vision transformer



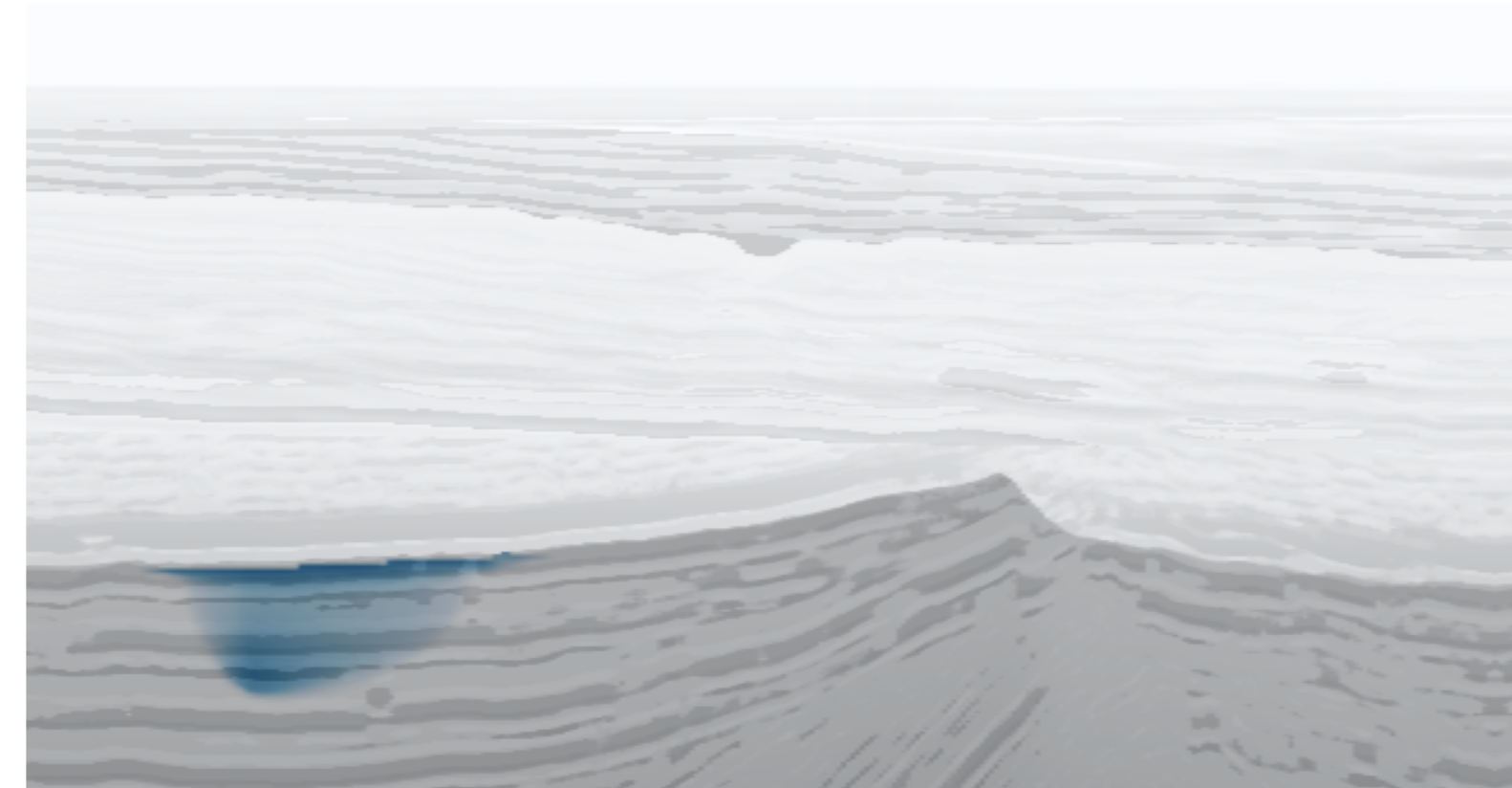
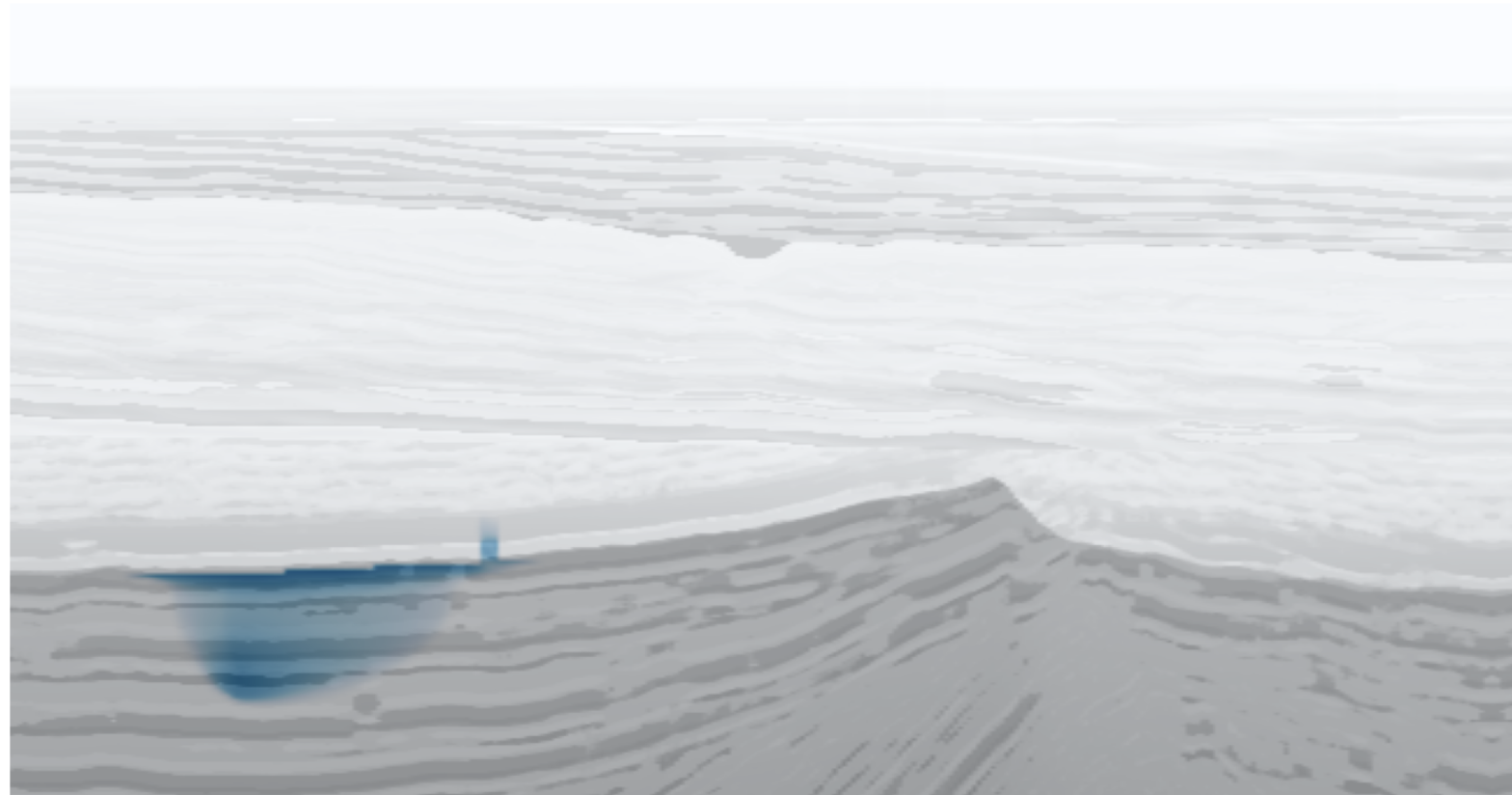
# Results

## Class Activation Mapping

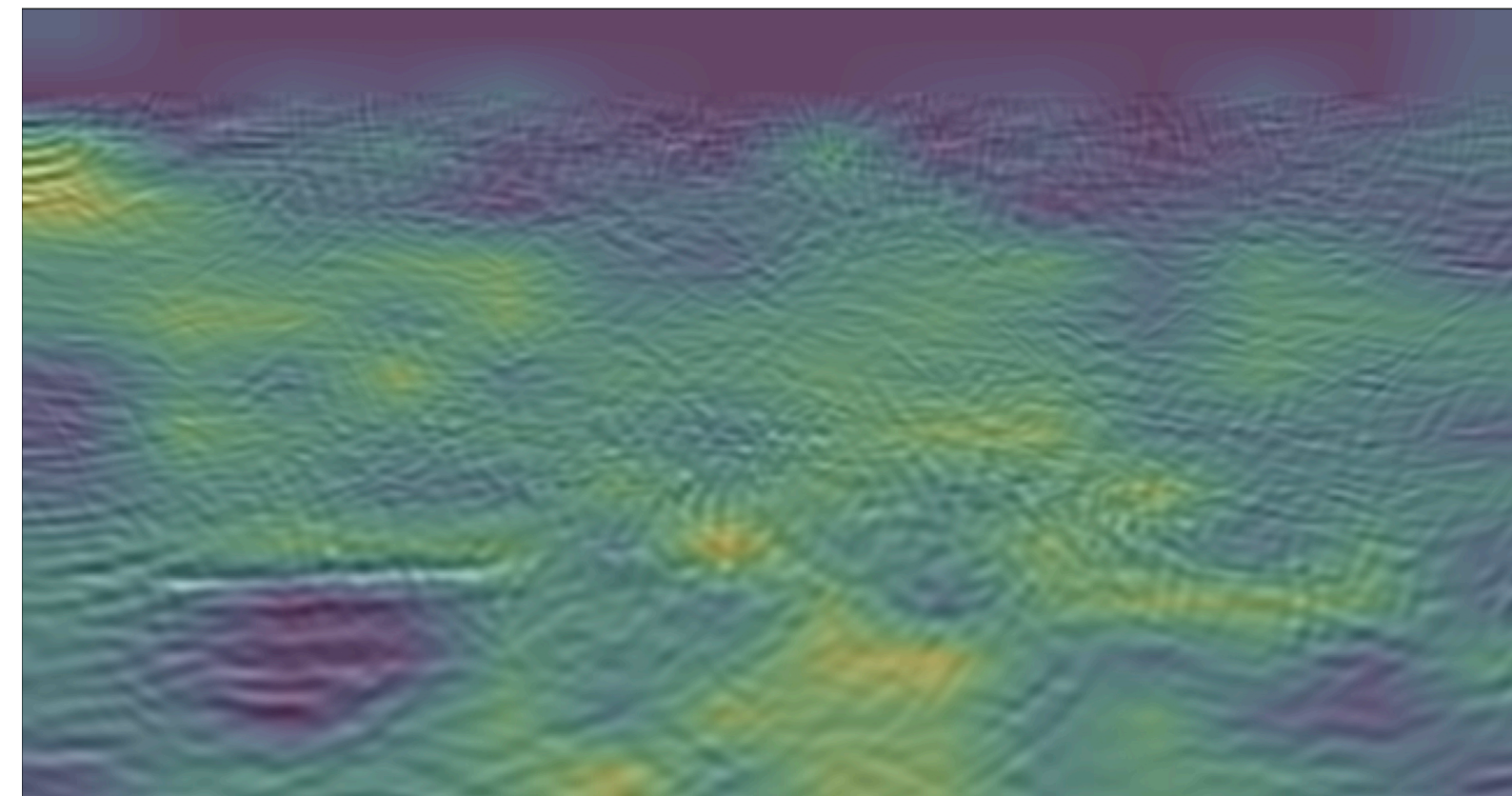
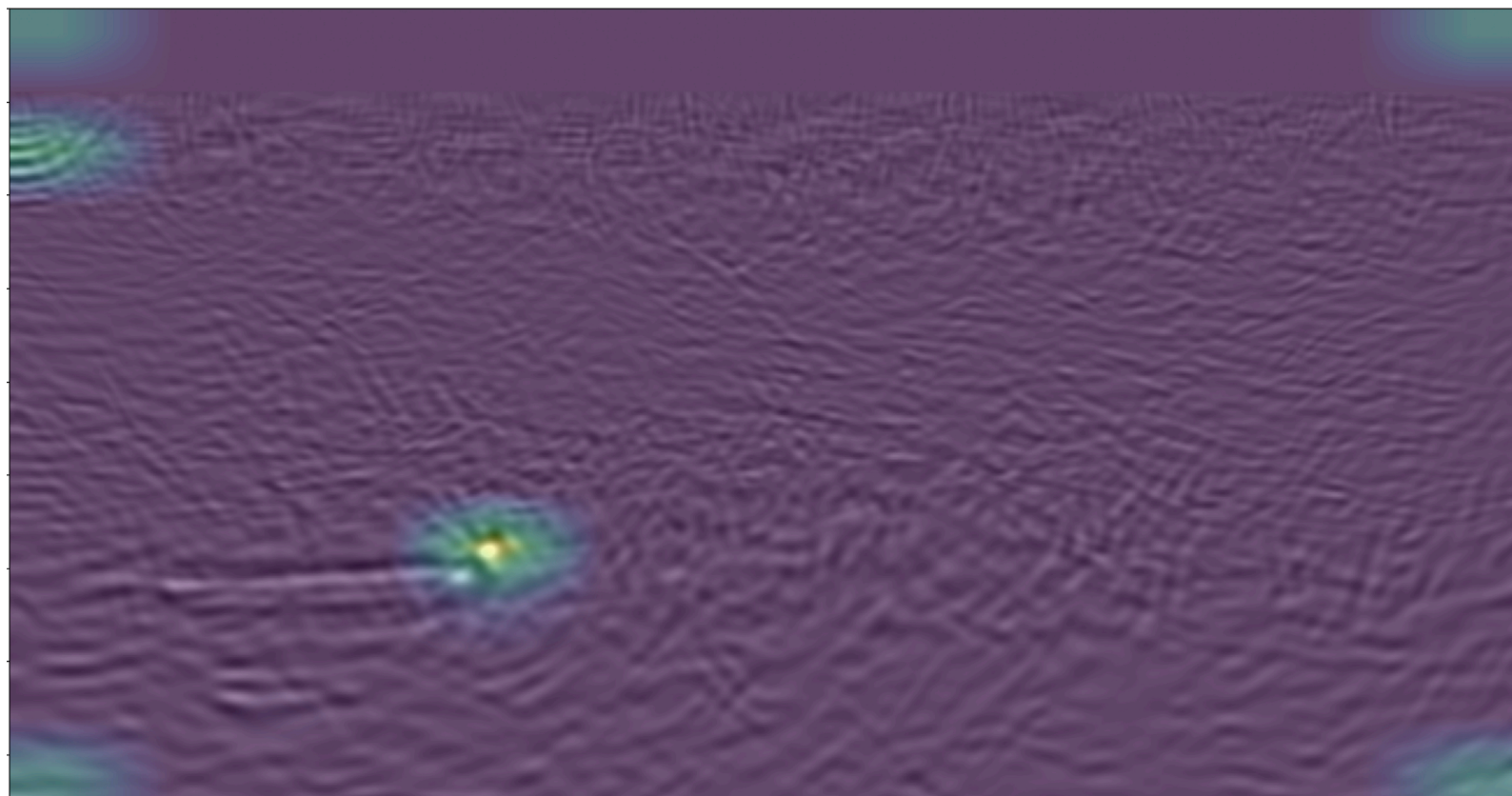
**leakage**

**regular**

**plume**



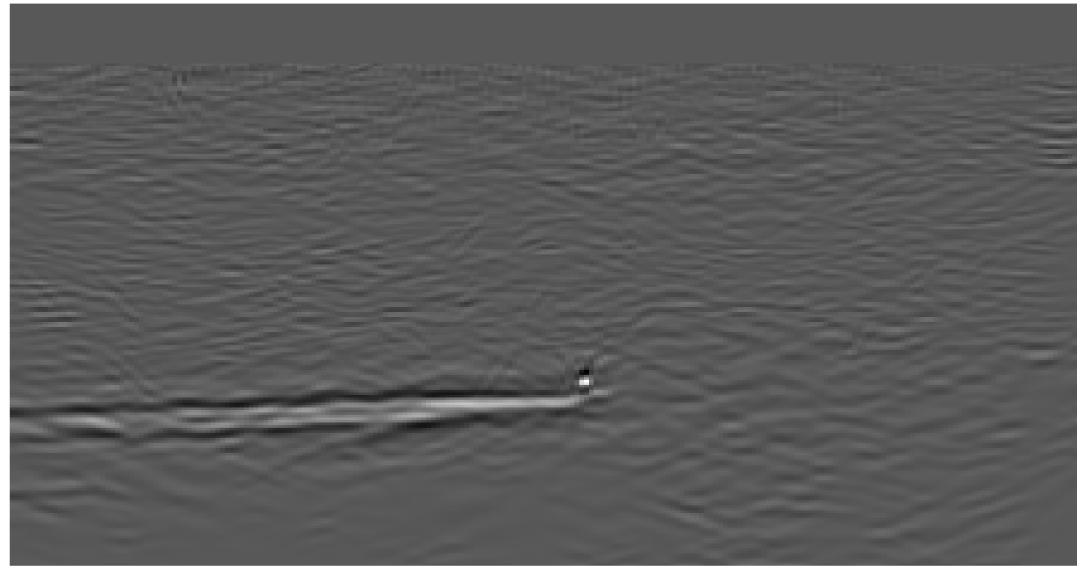
**CAM**



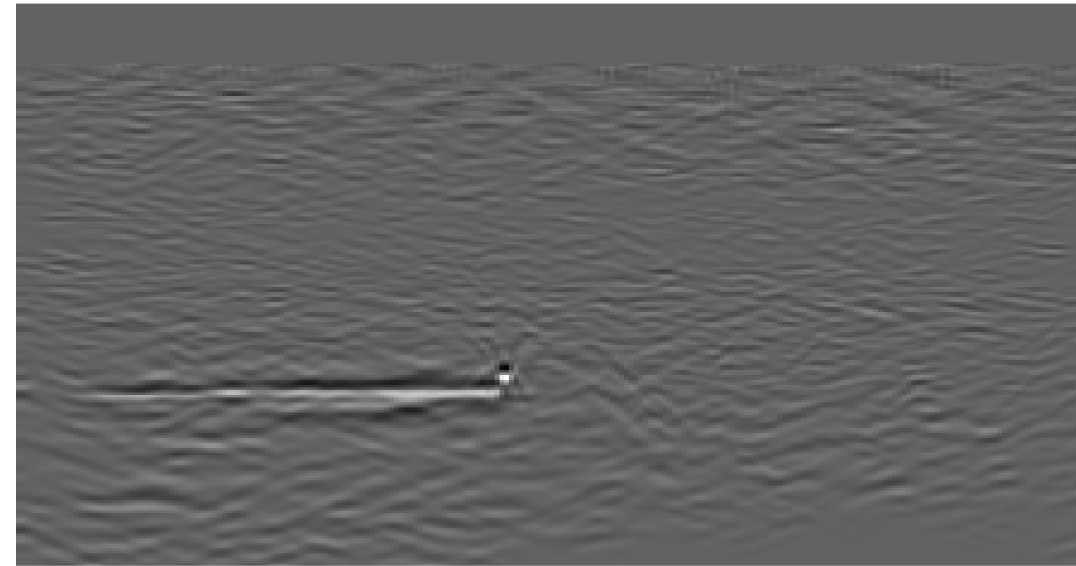


# Examples

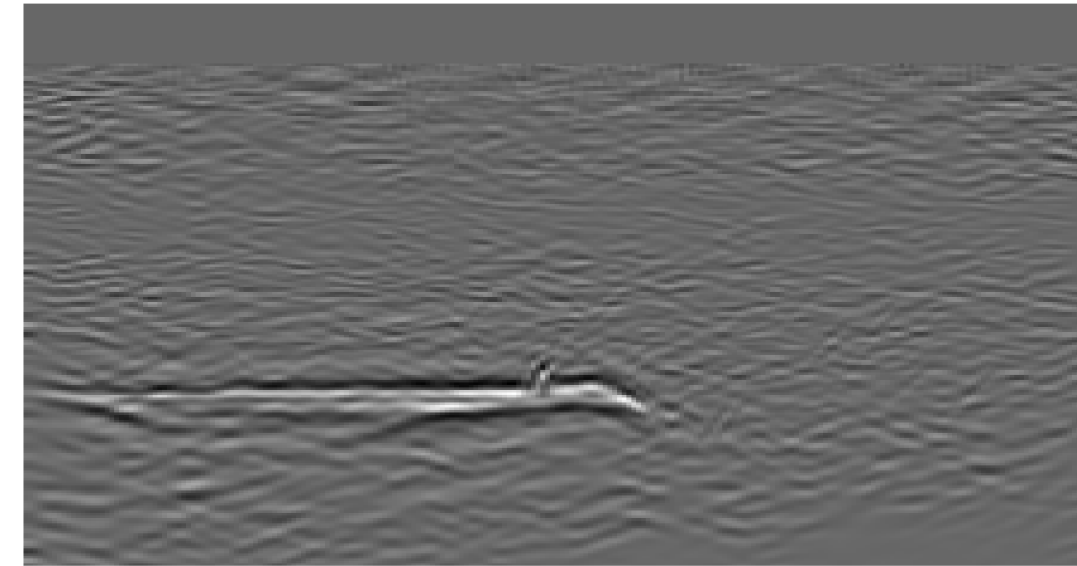
Seismic Image



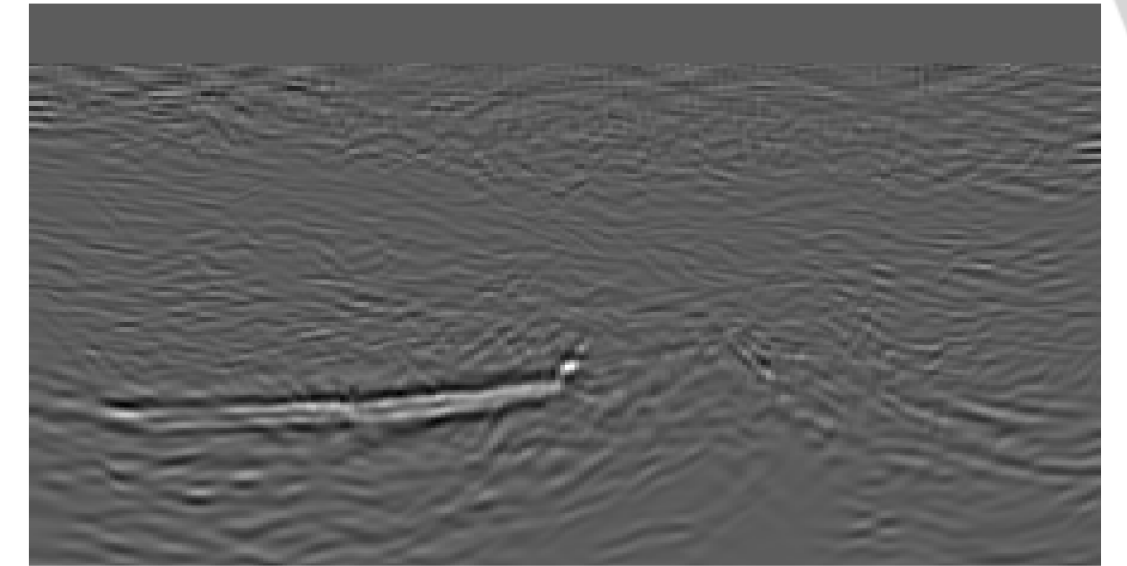
Seismic Image



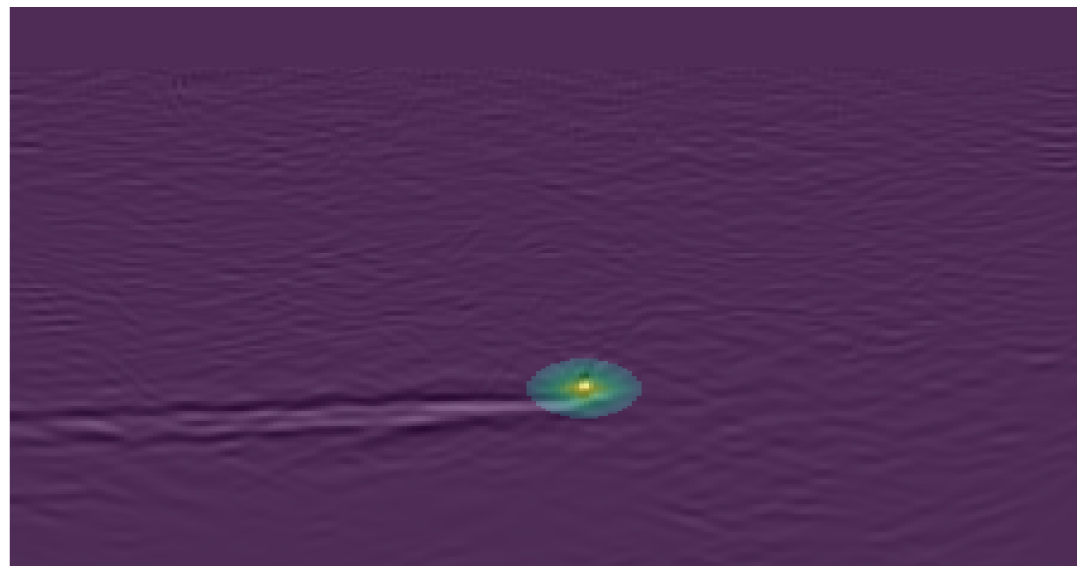
Seismic Image



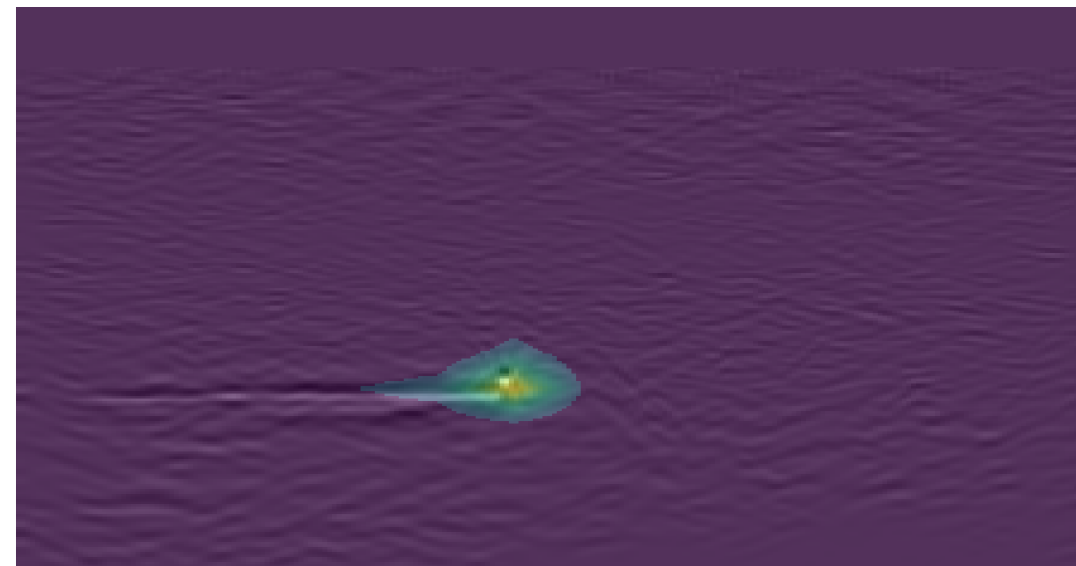
Seismic Image



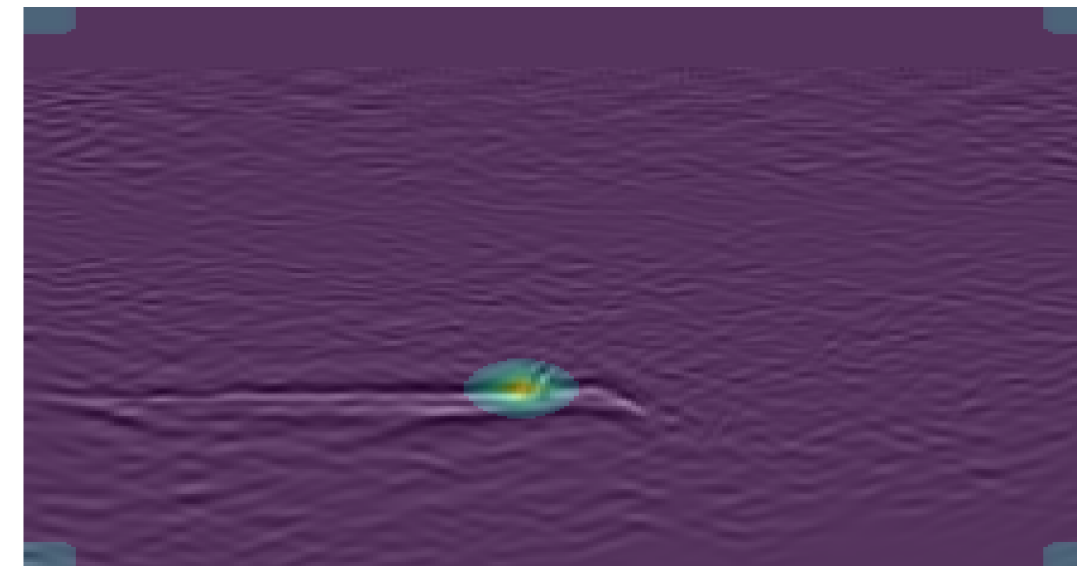
CAM on Seismic Image



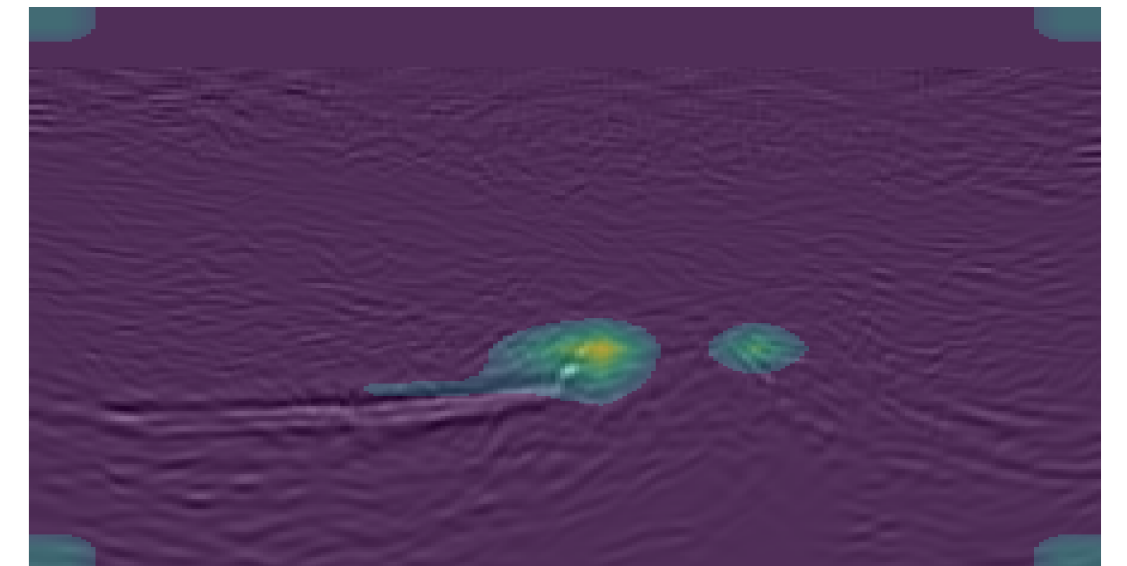
CAM on Seismic Image



CAM on Seismic Image



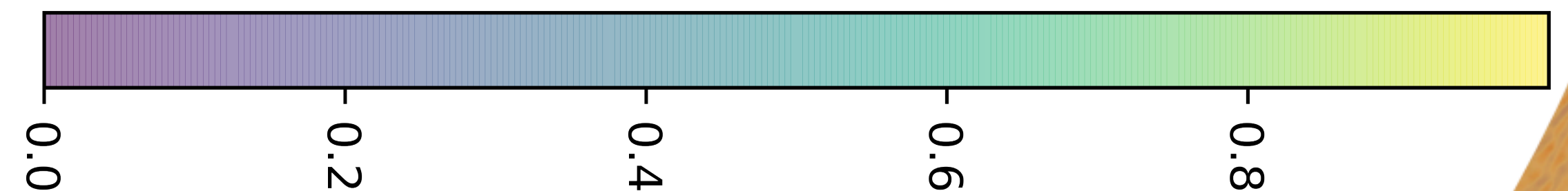
CAM on Seismic Image



Thresholded CAM maps ( $<0.2$ )

Localized areas of (potential) leakage

**importance**

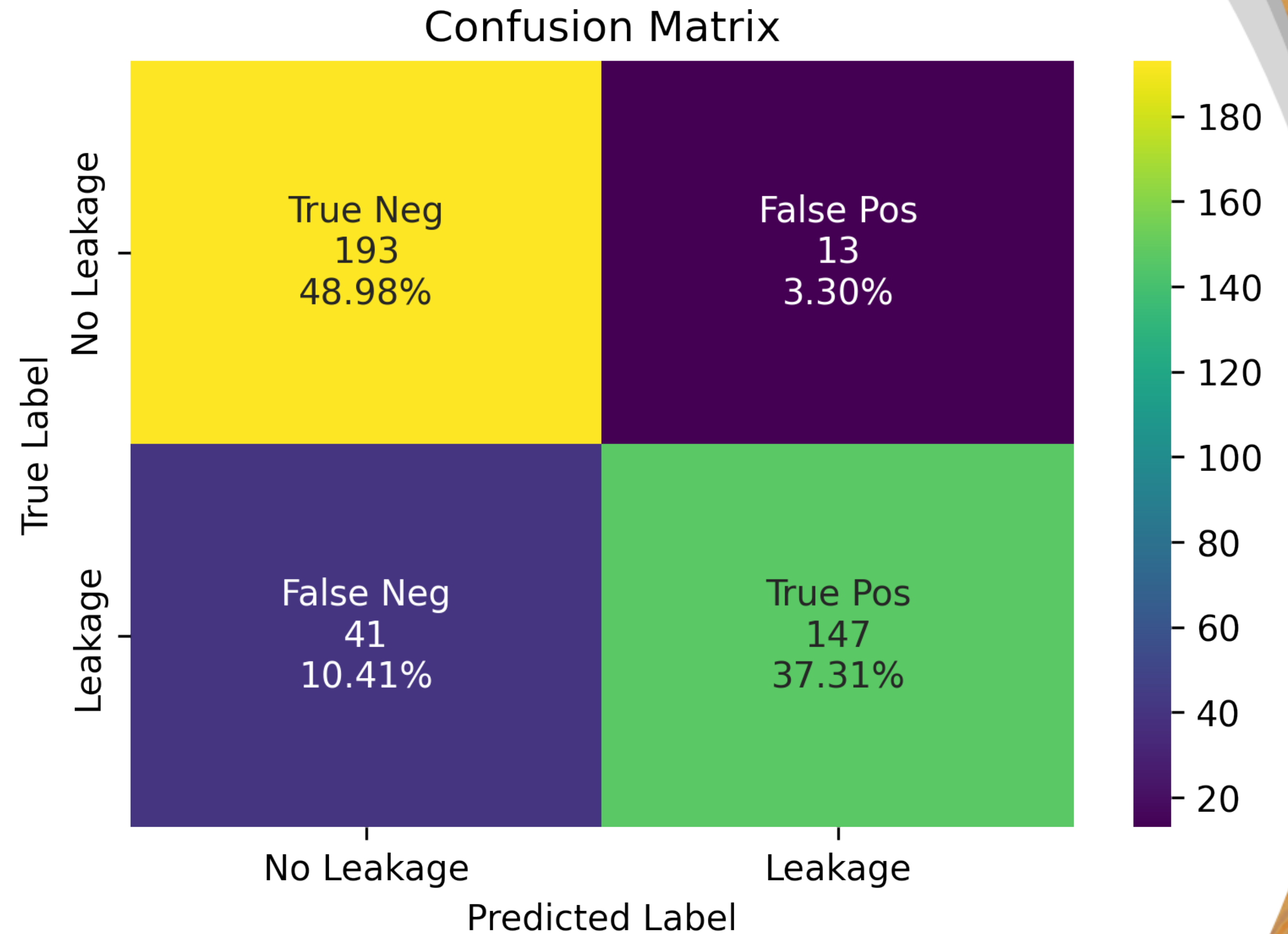




# Results

Overall 86.29% accuracy

- ▶ relied on *dense* receiver sampling
- ▶ relatively *high* percentage *false negatives*
- ▶ fewer *false positives*
- ▶ may need improvement



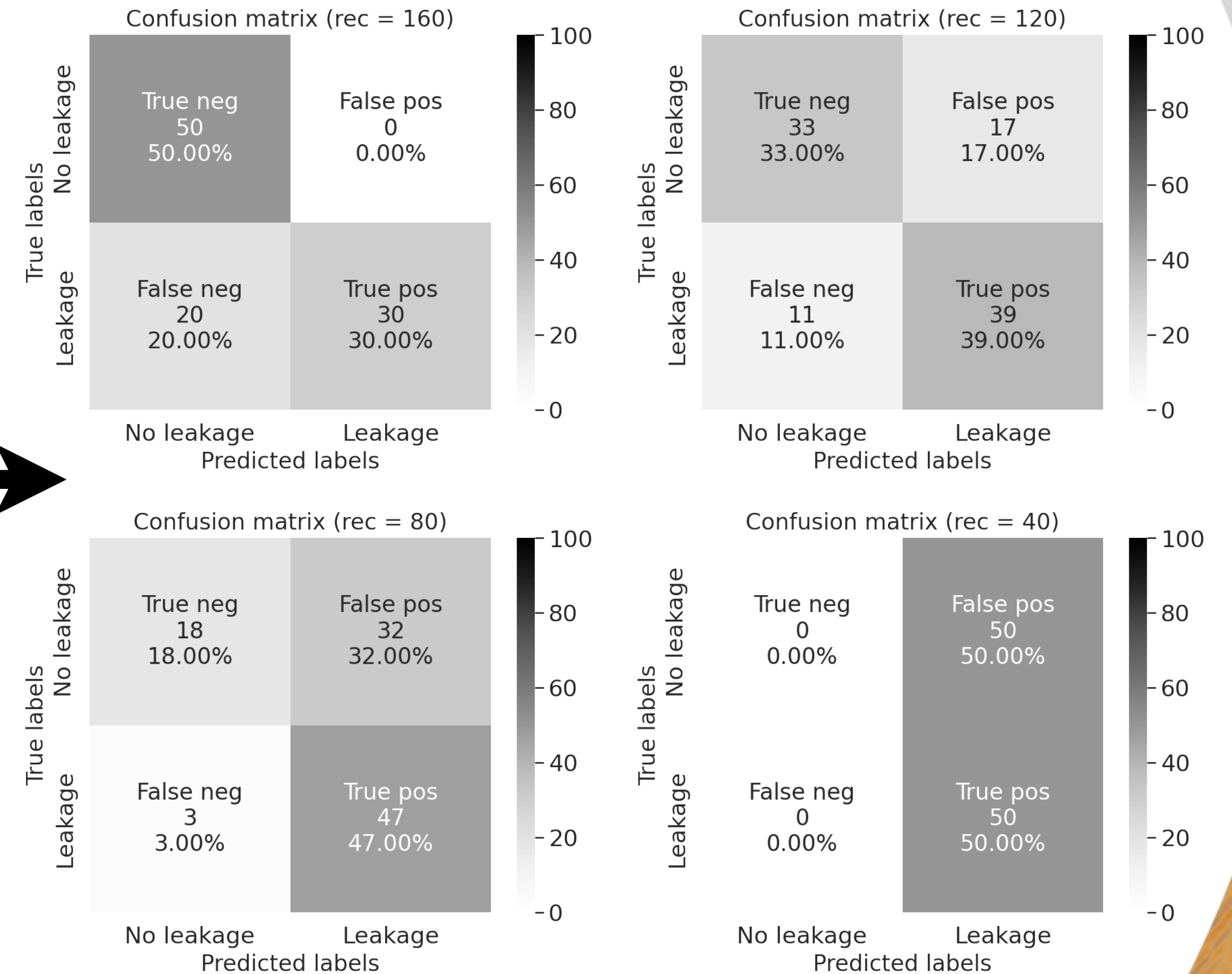
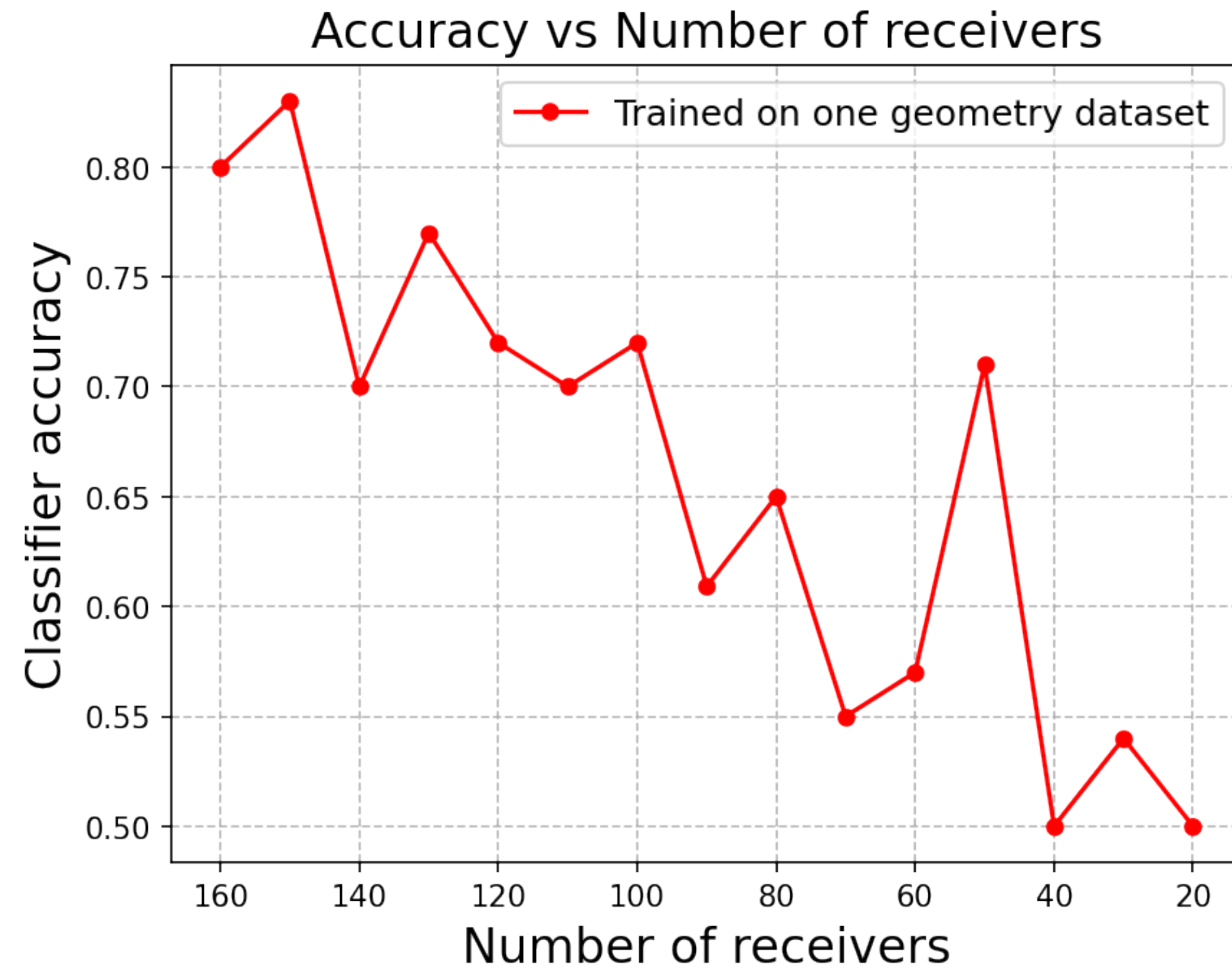


# Improved leakage detection w/ data augmentation



# Problem

## leakage detection deteriorates

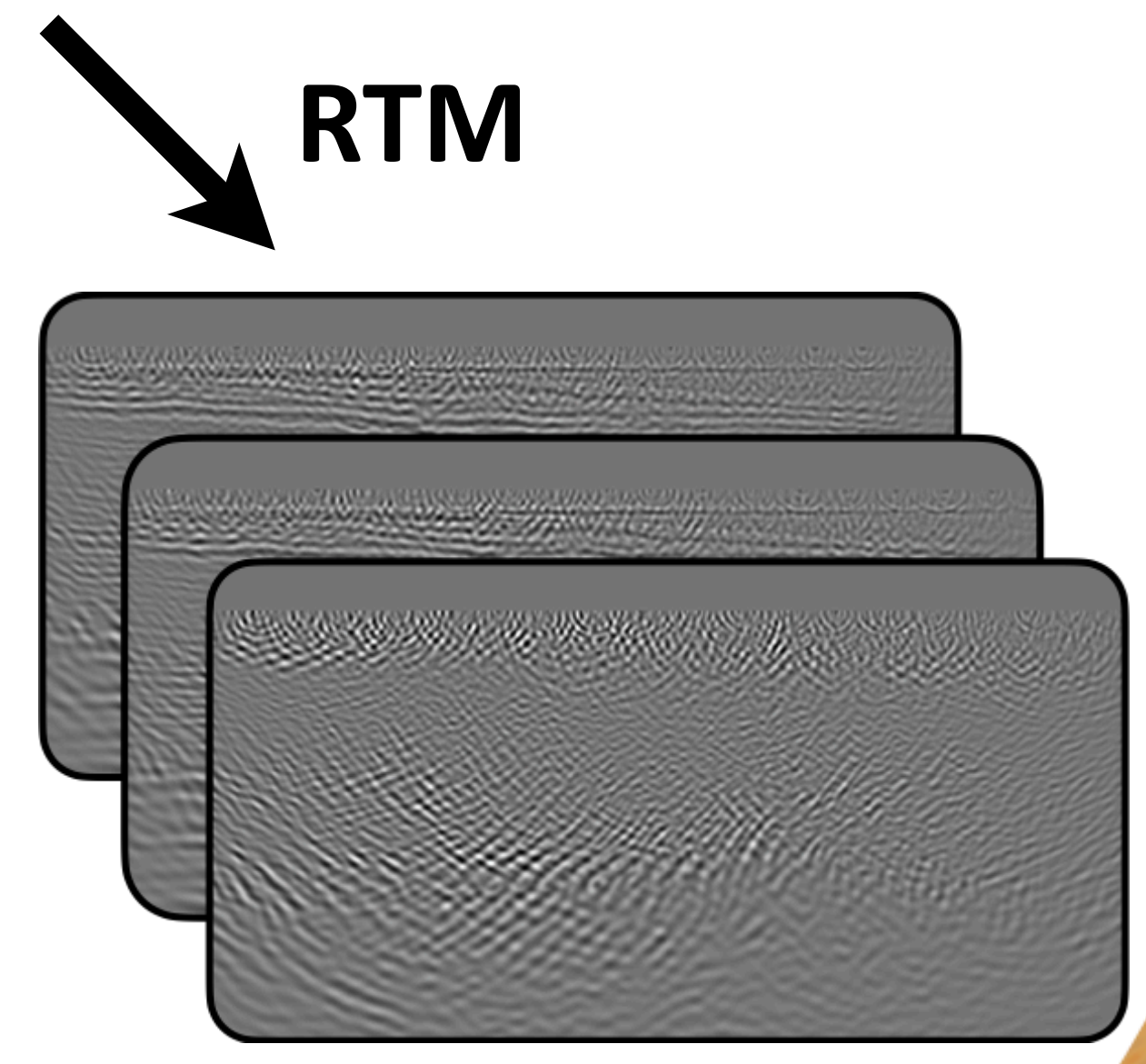
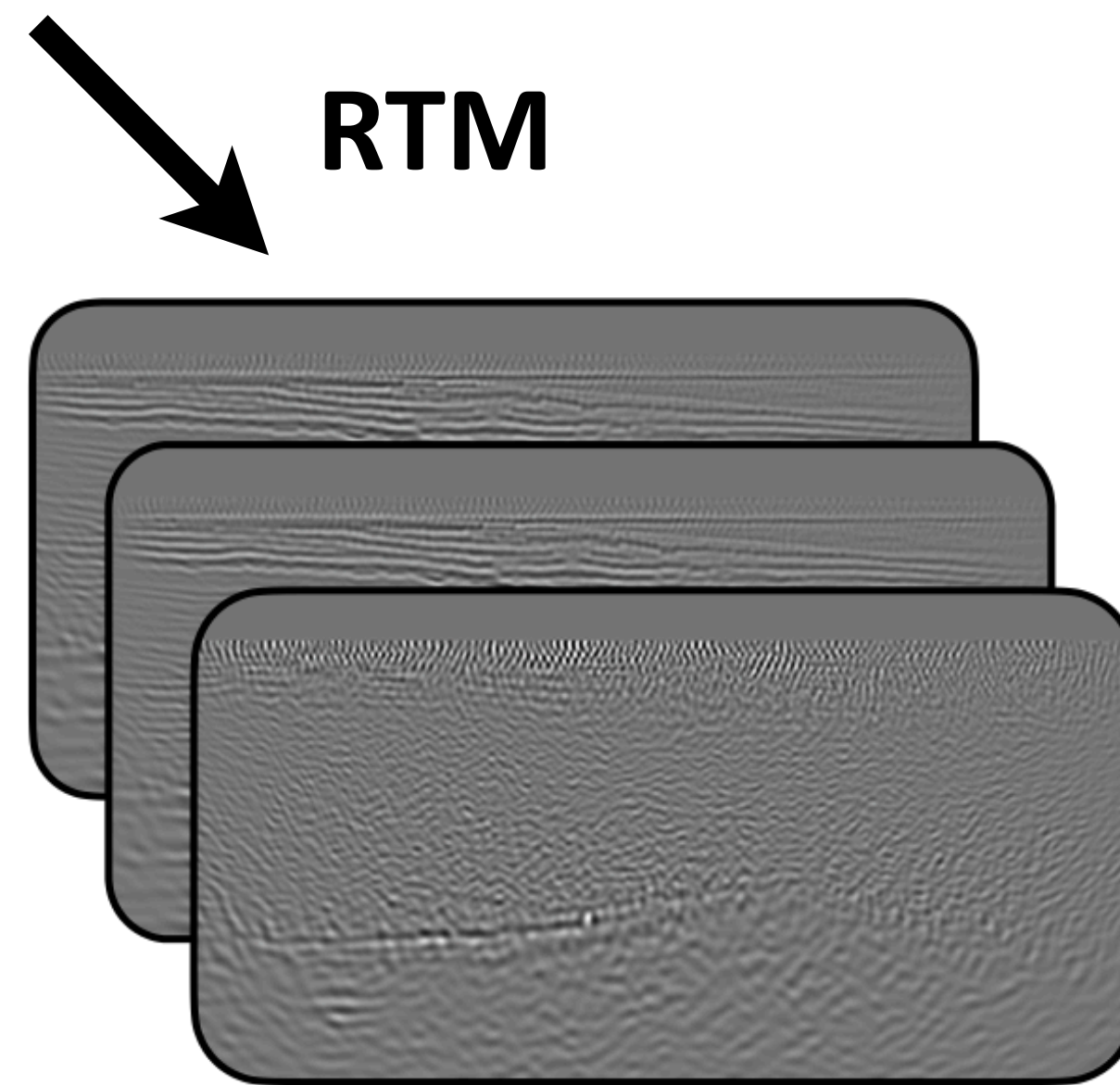
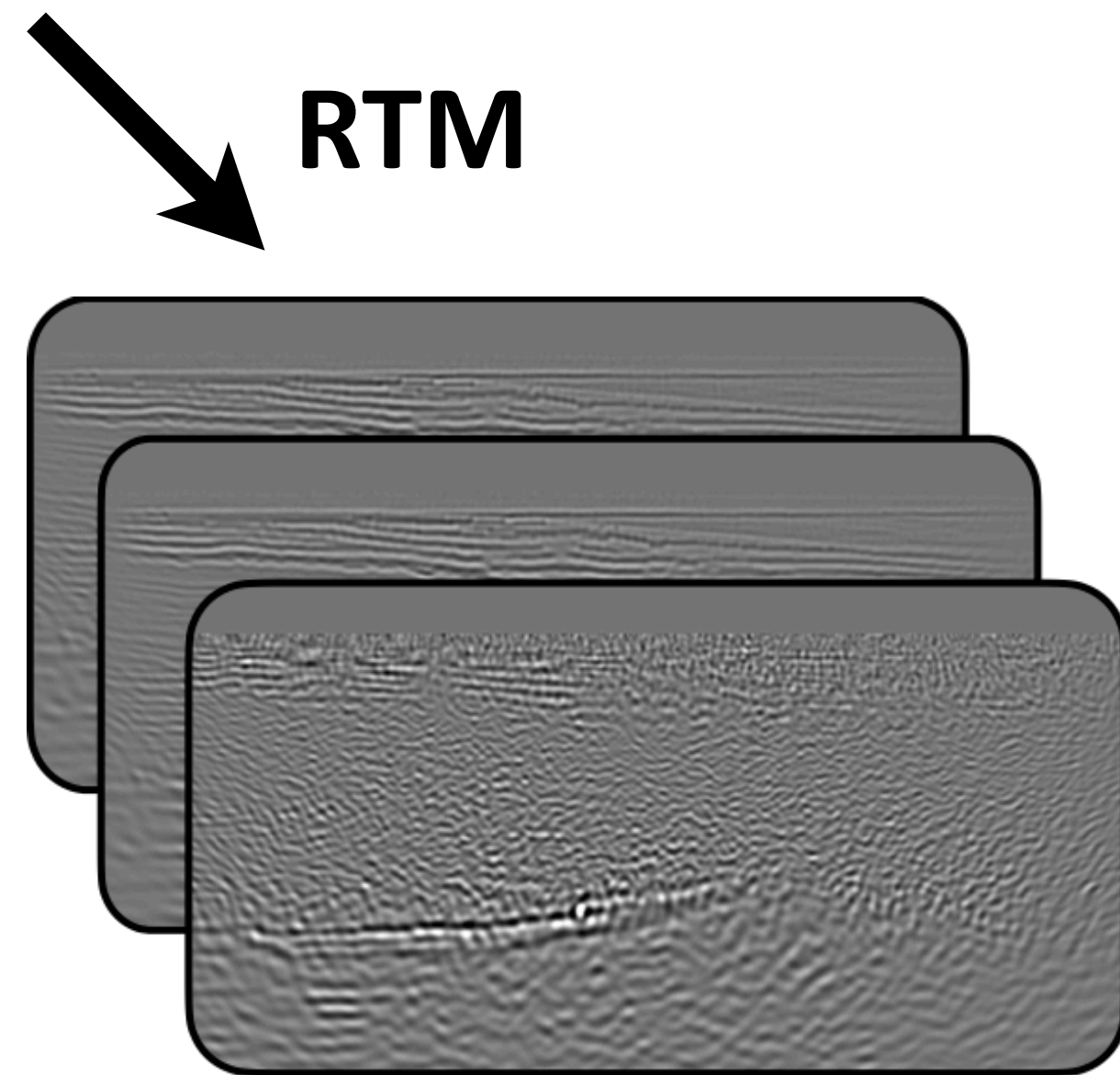
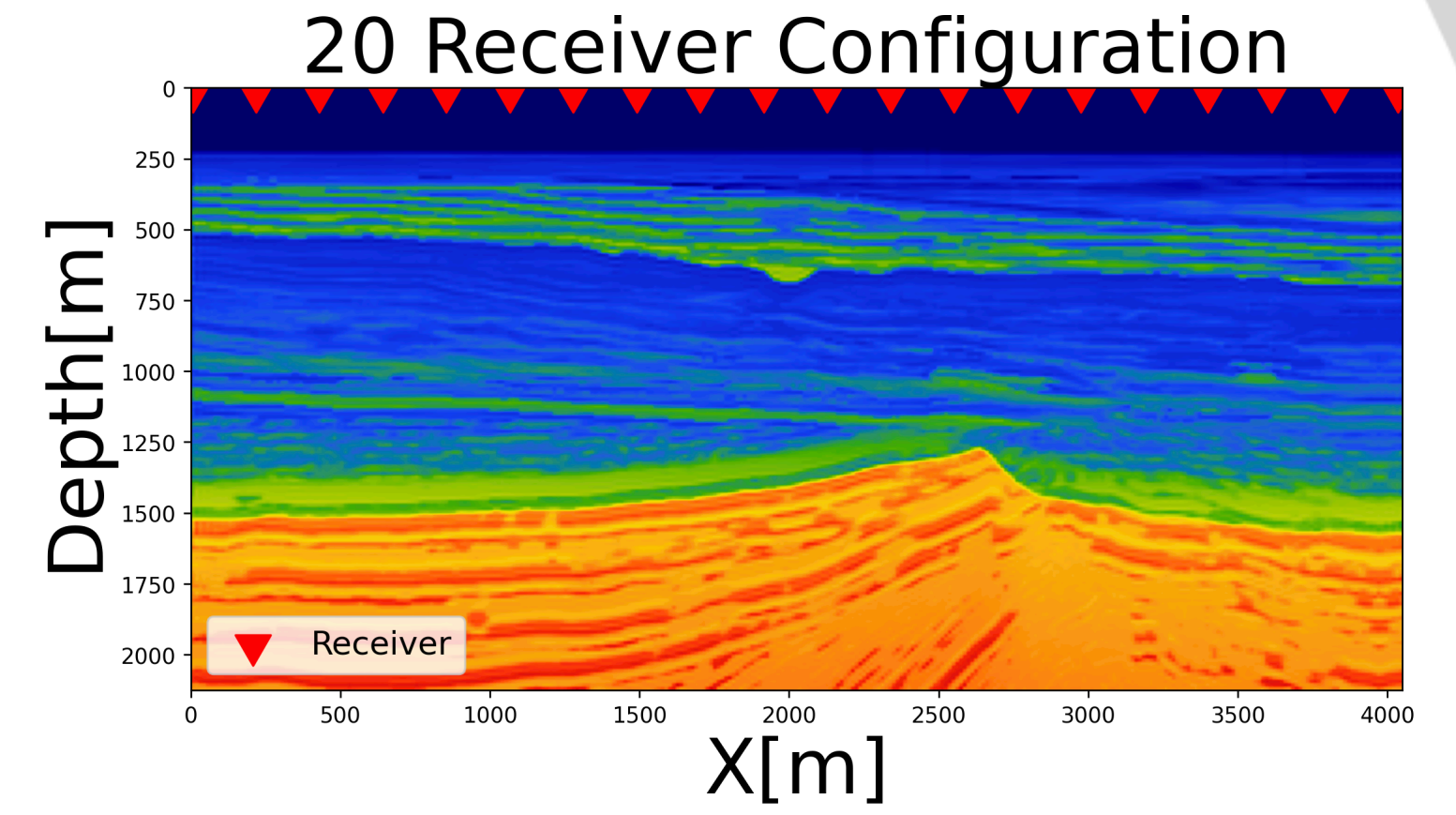
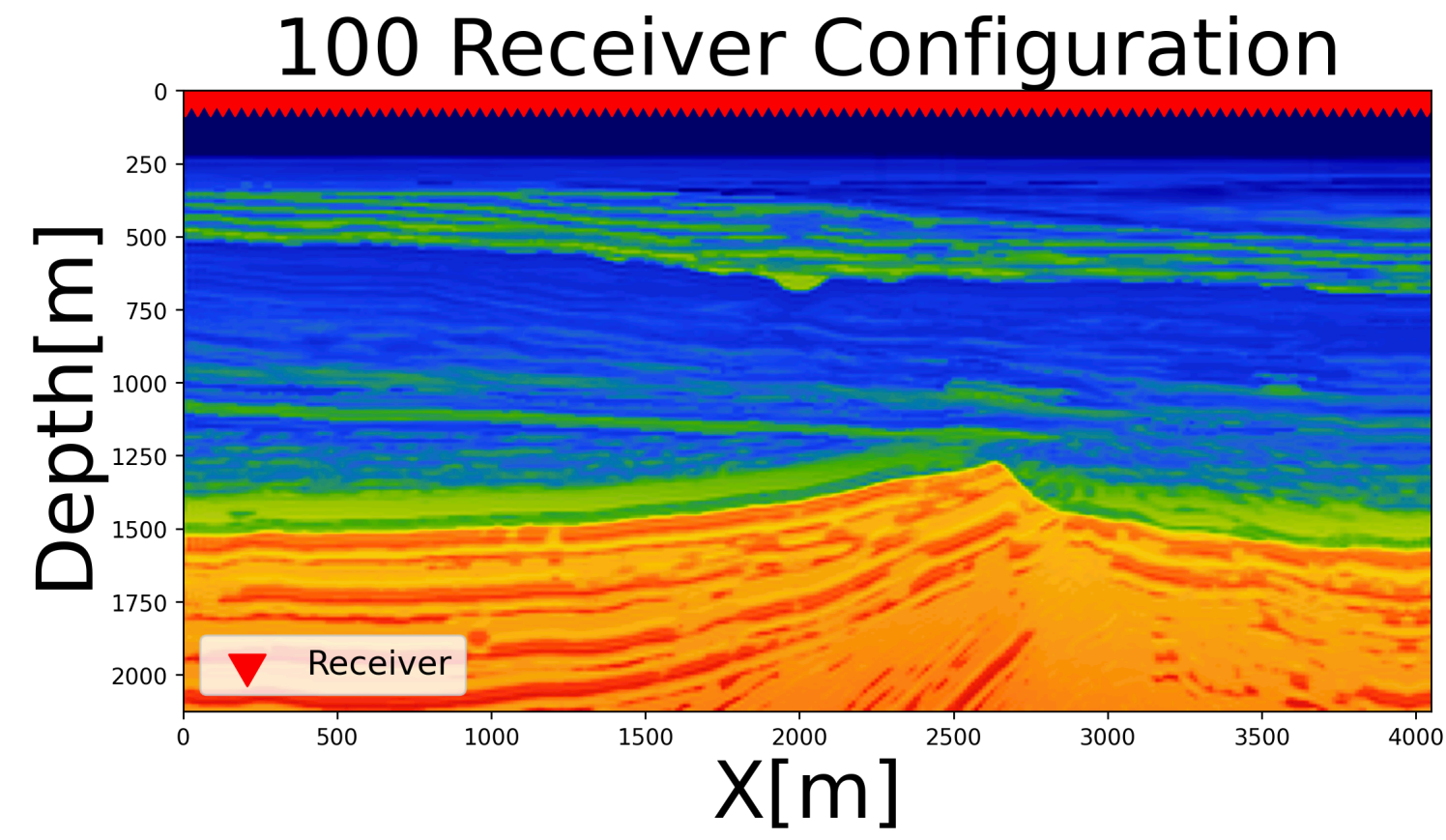
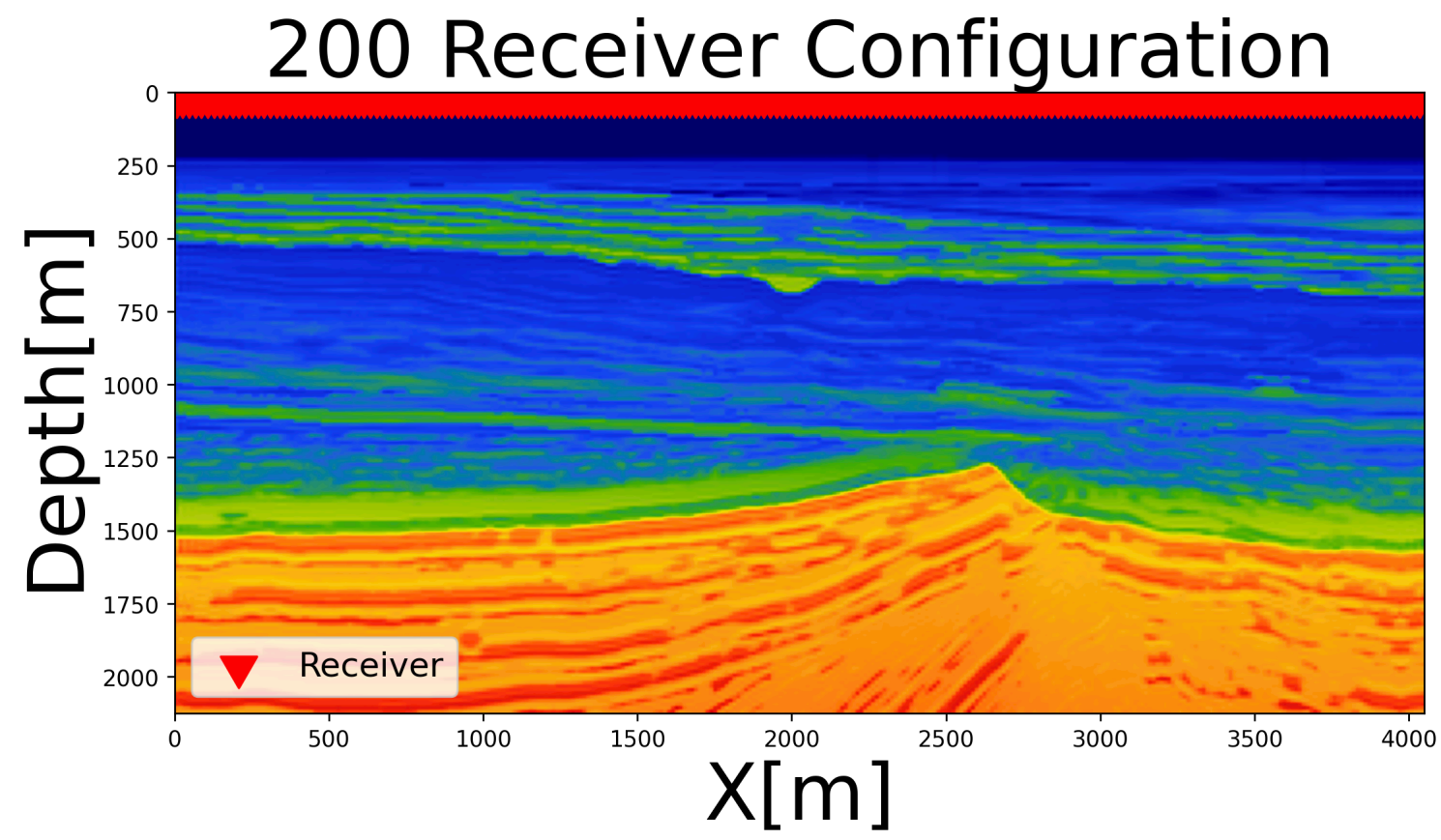


- ▶ accuracy *decreases* w/ receiver *density*
- ▶ solution *augment* training set



# Issue

## sparse receiver sampling

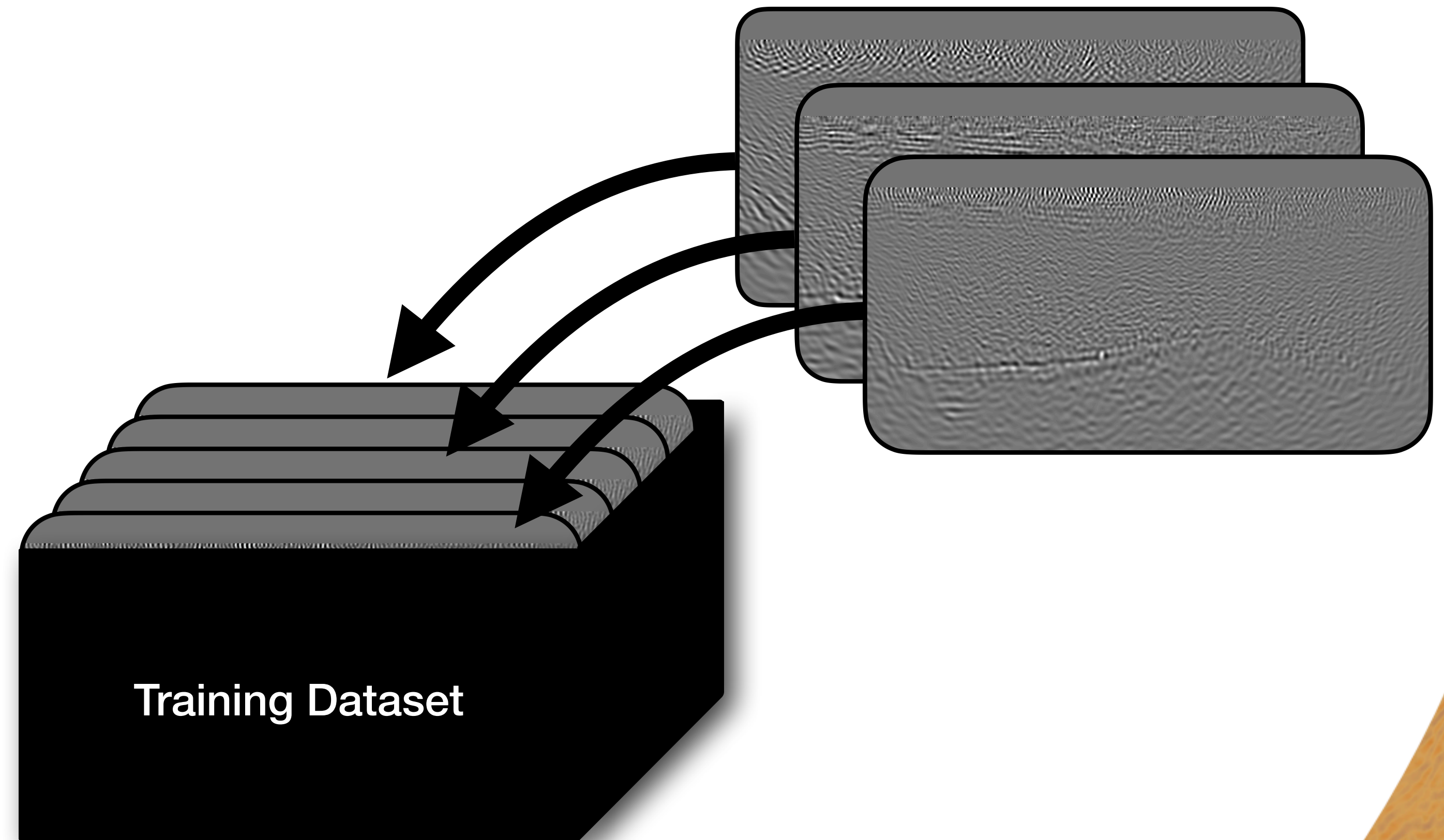




# Solution

## data augmentation

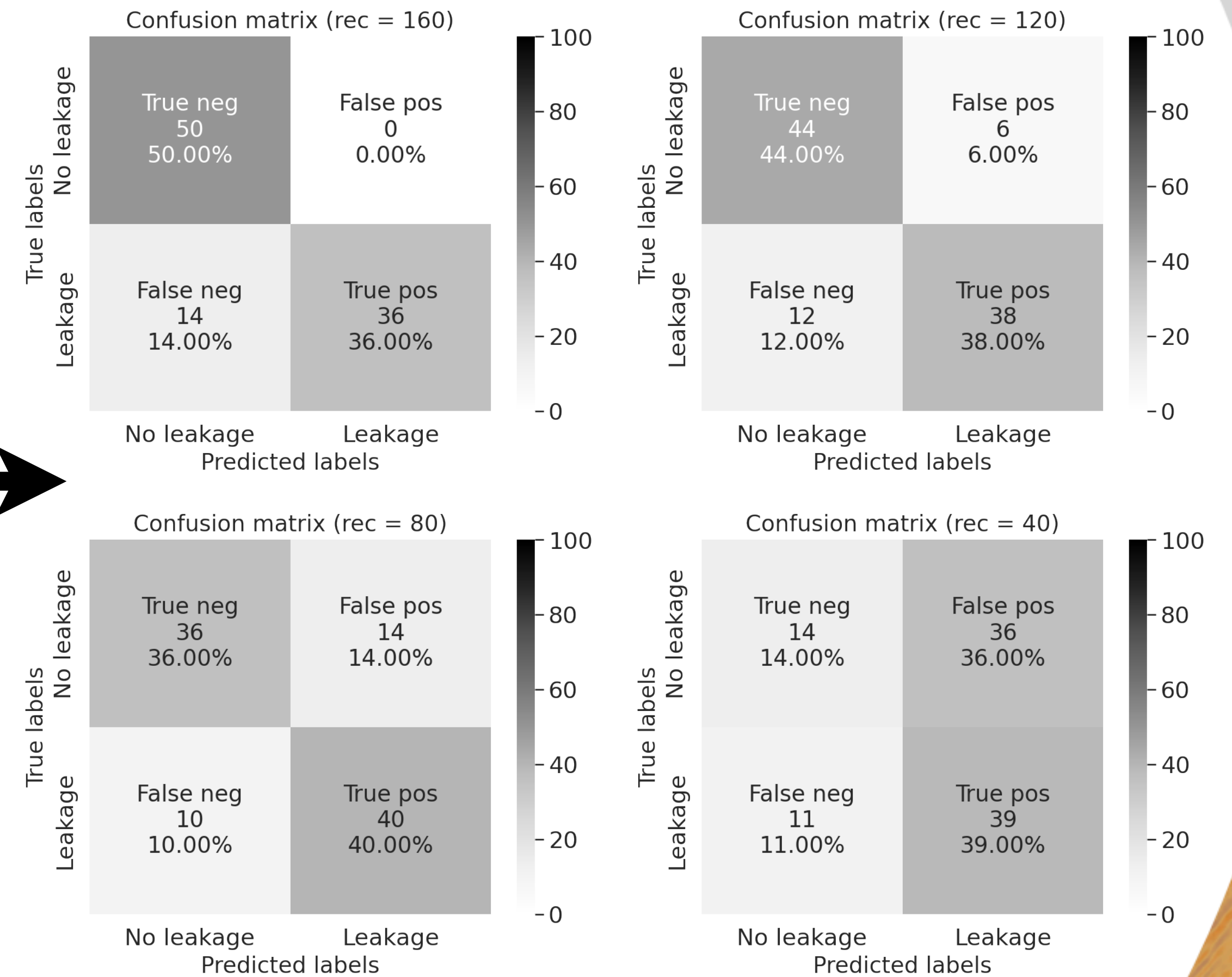
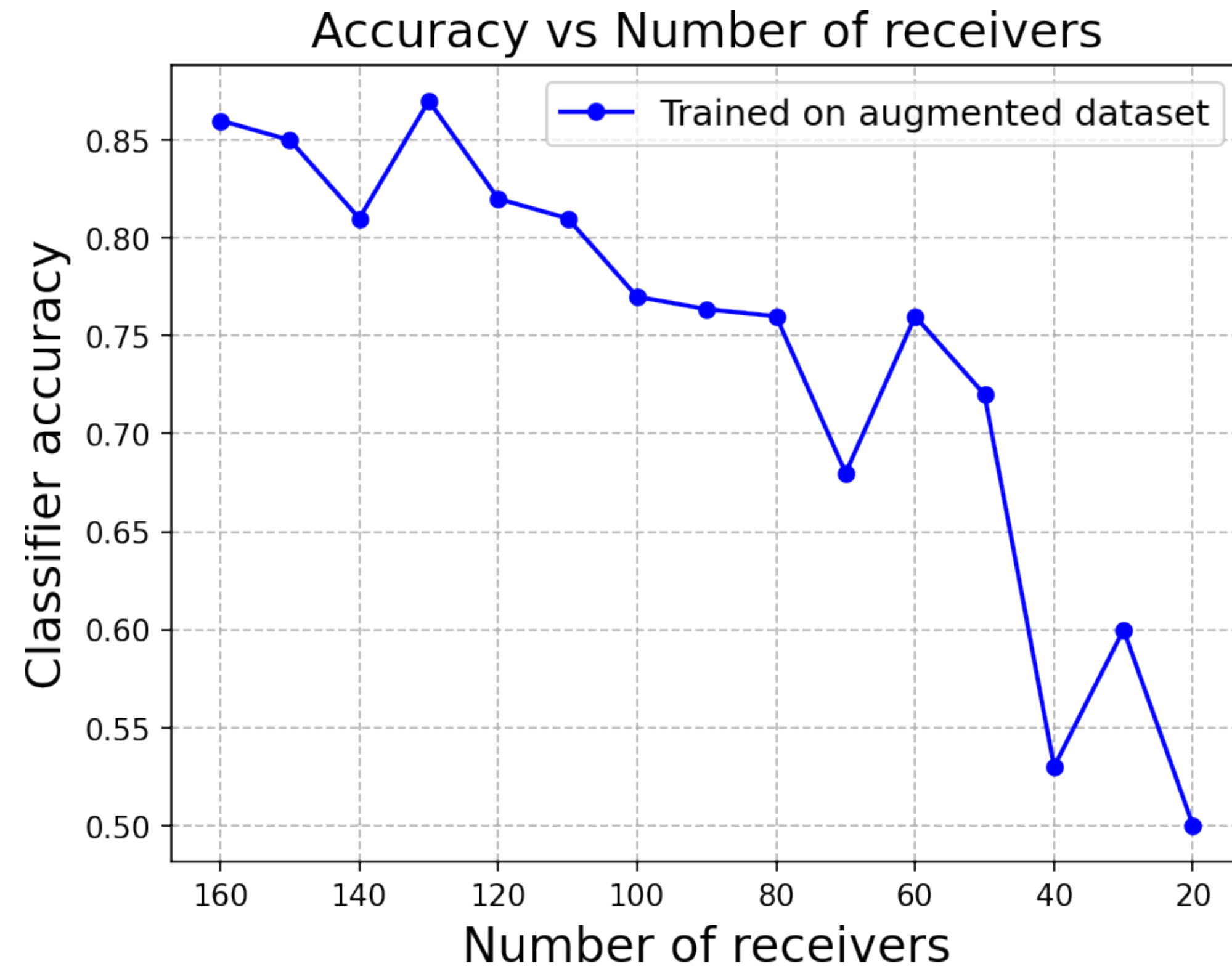
- ▶ produce difference images w/ random number of receivers
- ▶ add new images to training dataset
- ▶ retrain the model w/ augmented dataset
- ▶ test on different receiver configurations





# Results

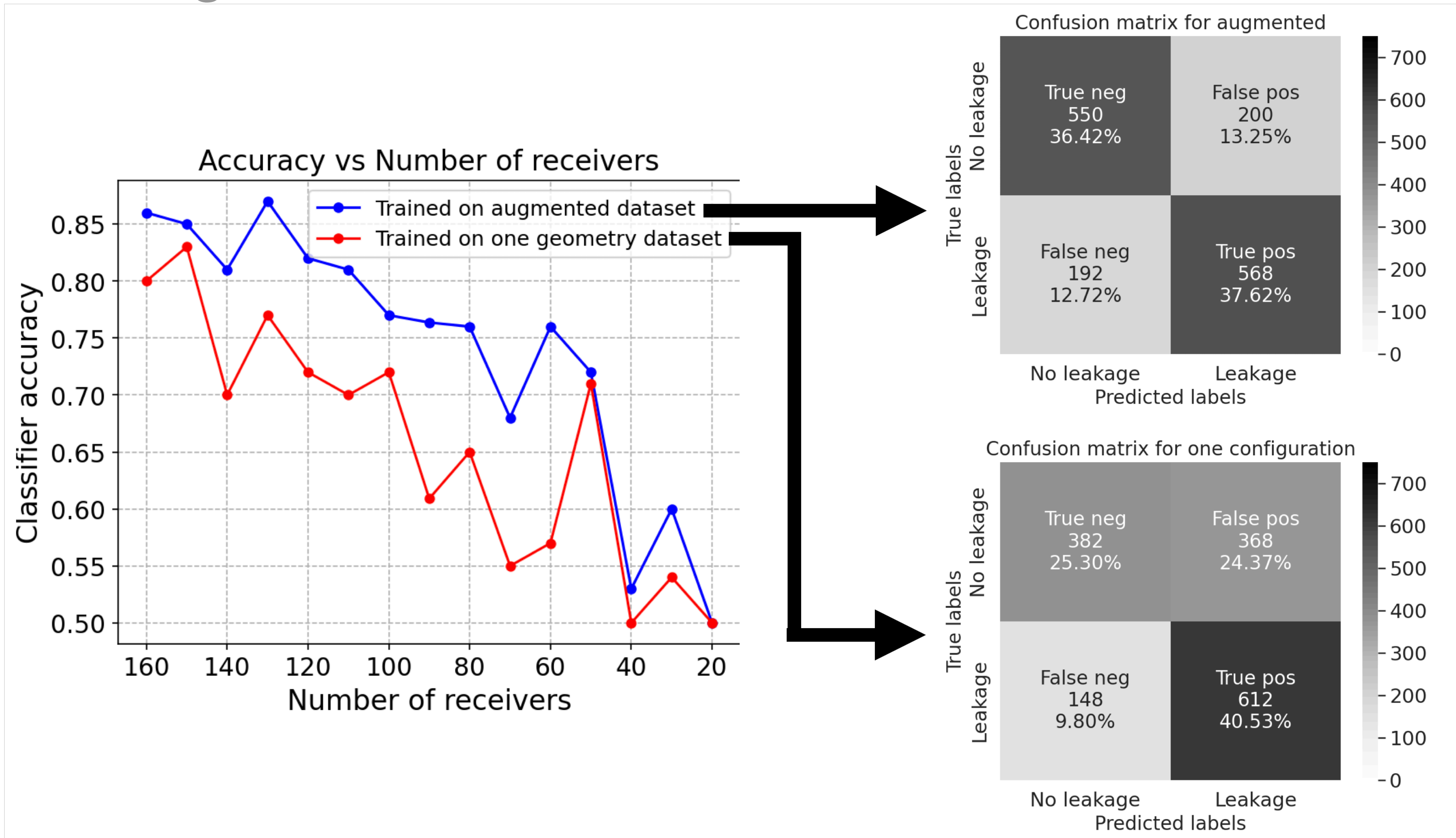
## after data augmentation





# Results

## after data augmentation





# Permeability inversion from time-lapse seismic data

Mathias Louboutin, Ziyi Yin, Rafael Orozco, Thomas J. Grady II, Ali Siahkoohi, Gabrio Rizzuti, Philipp A. Witte, Olav Møyner, Gerard J. Gorman, and Felix J. Herrmann, “[Learned multiphysics inversion with differentiable programming and machine learning](#)”. 2023



# End-to-end inversion permeability

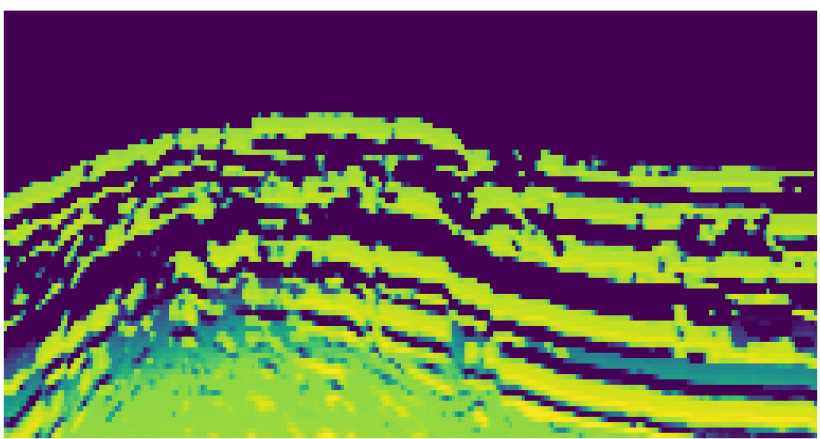
Mathias Louboutin, Ziyi Yin, Rafael Orozco, Thomas J. Grady II, Ali Siahkoohi, Gabrio Rizzuti, Philipp A. Witte, Olav Møyner, Gerard J. Gorman, and Felix J. Herrmann, "Learned multiphysics inversion with differentiable programming and machine learning". 2023

permeability  
**K**

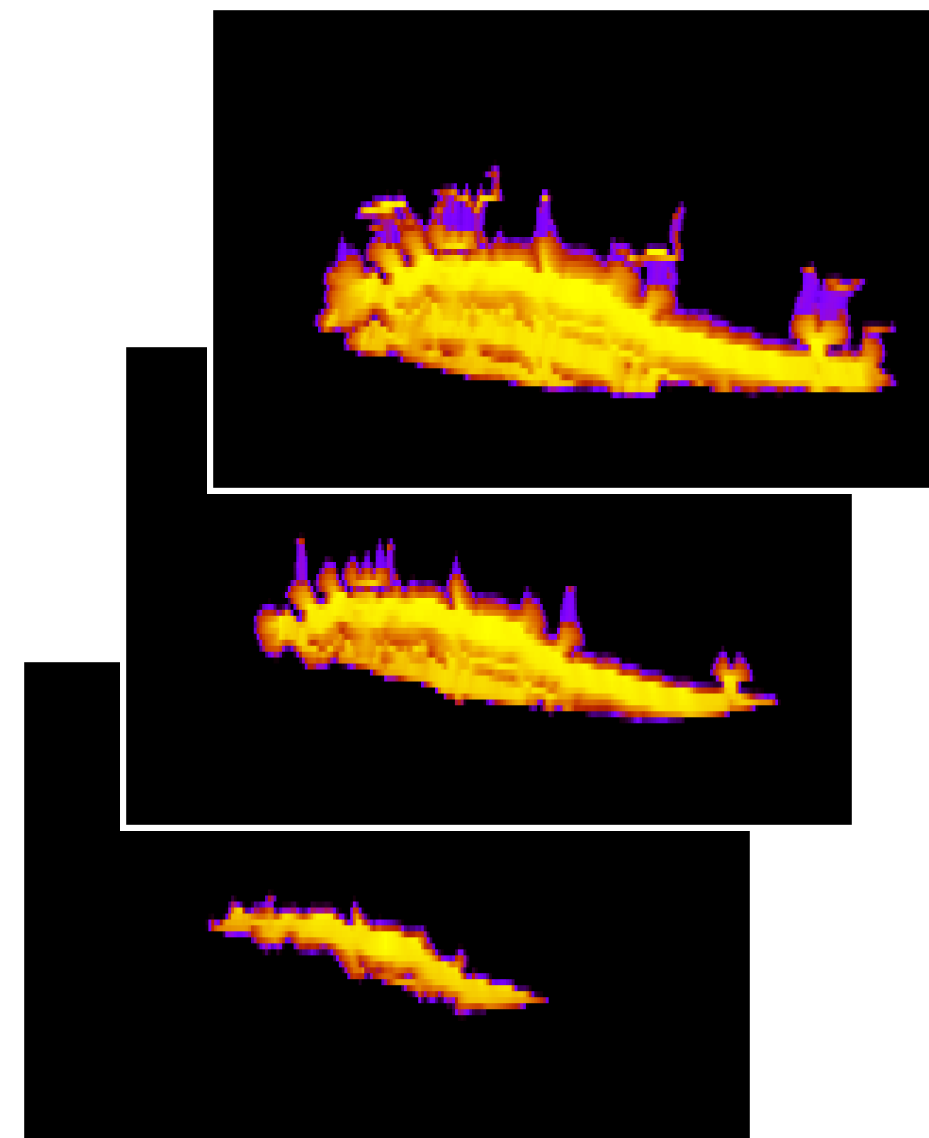
CO<sub>2</sub> concentration  
**c**

wavespeed  
**v**

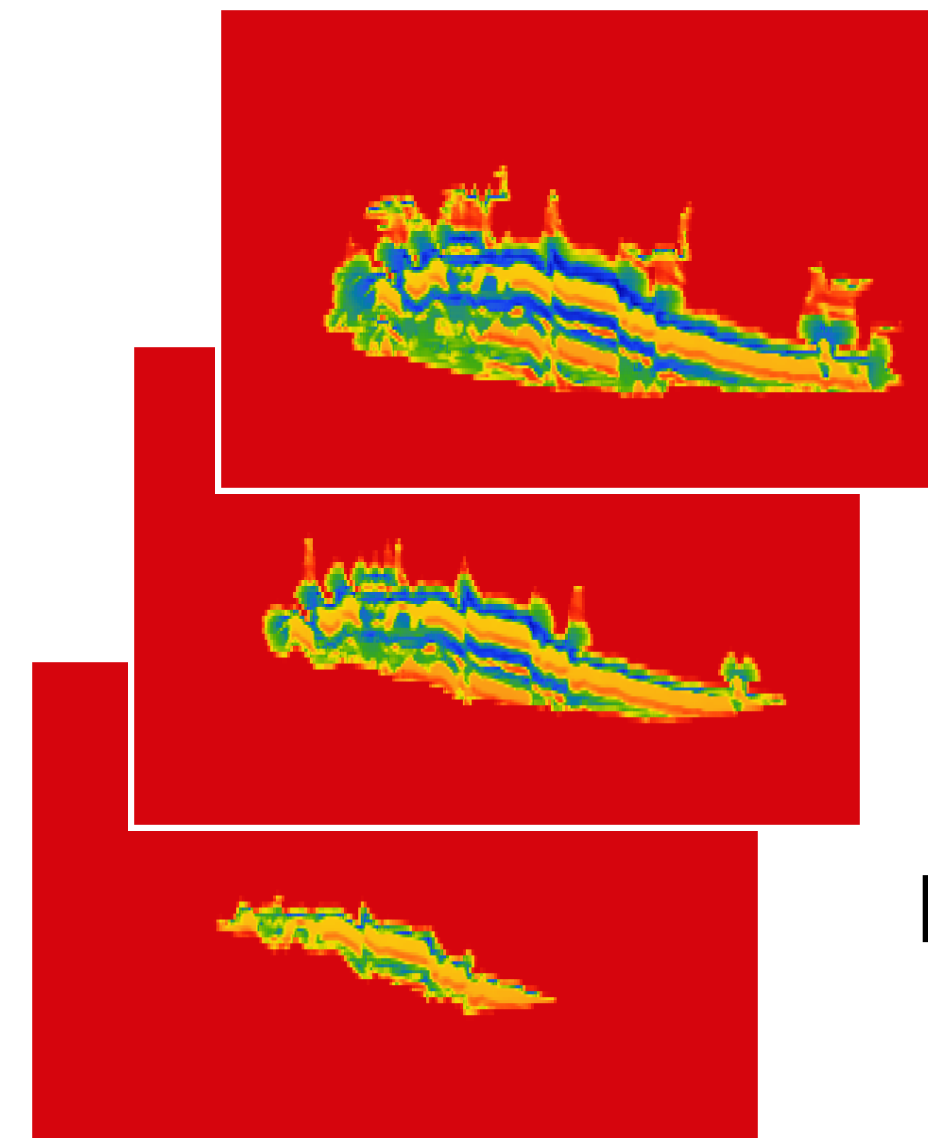
time-lapse data  
**d**



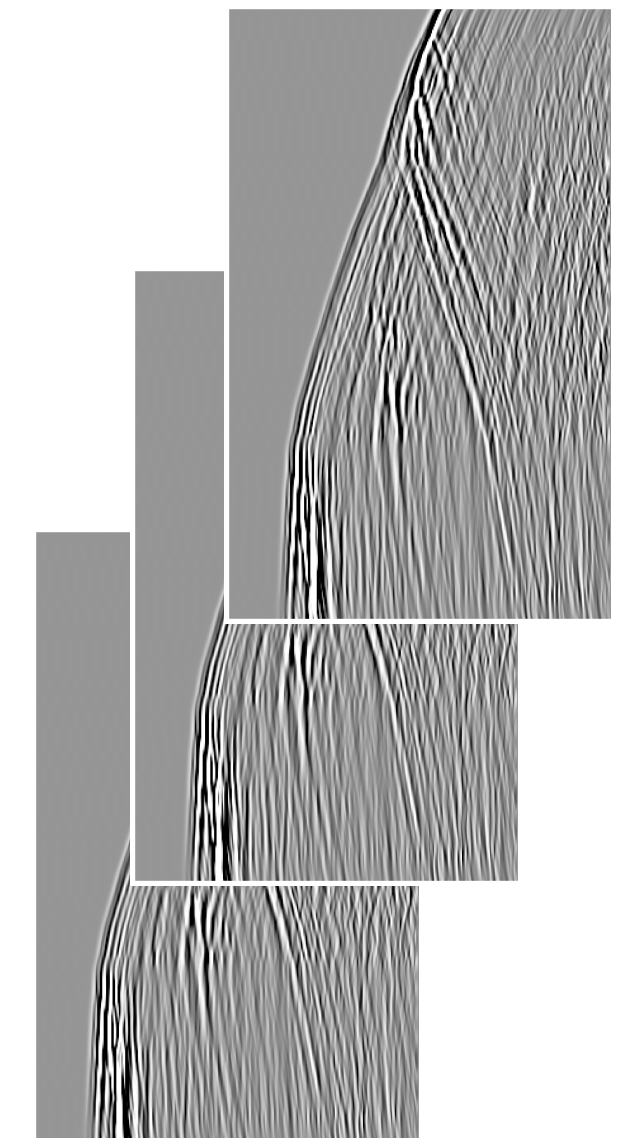
$\mathcal{S}$   
→  
fluid-flow  
physics



$\mathcal{R}$   
→  
rock  
physics



$\mathcal{F}$   
→  
wave  
physics



minimize  
**K**

$$\|\mathcal{F} \circ \mathcal{R} \circ \mathcal{S}(\mathbf{K}) - \mathbf{d}\|_2^2$$



# CO<sub>2</sub> plume predictions & forecast

monitor

year 25

forecast

physical time

year 10

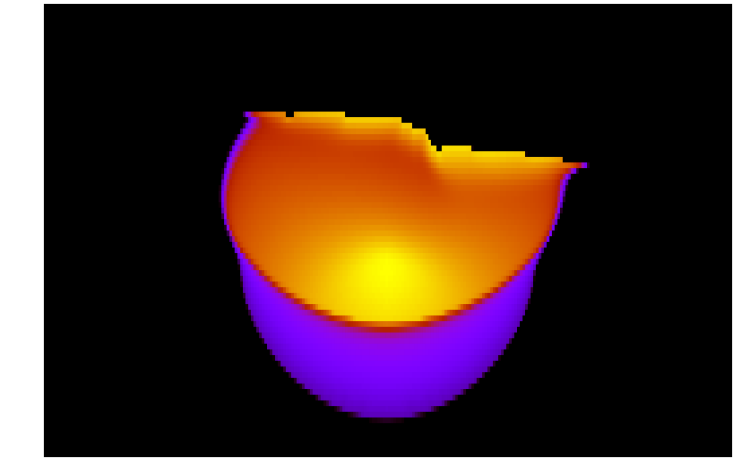
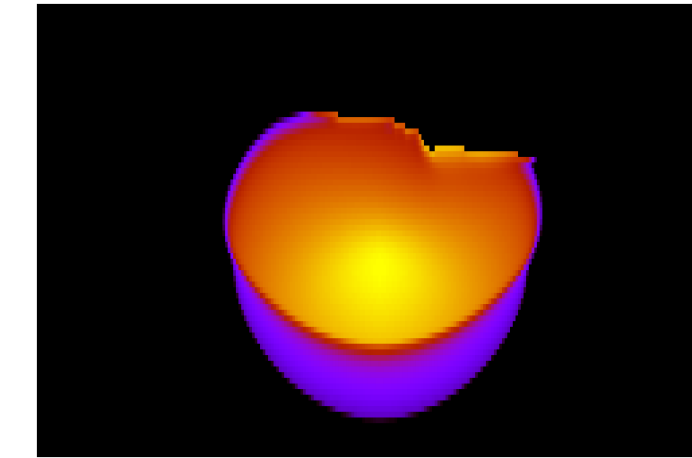
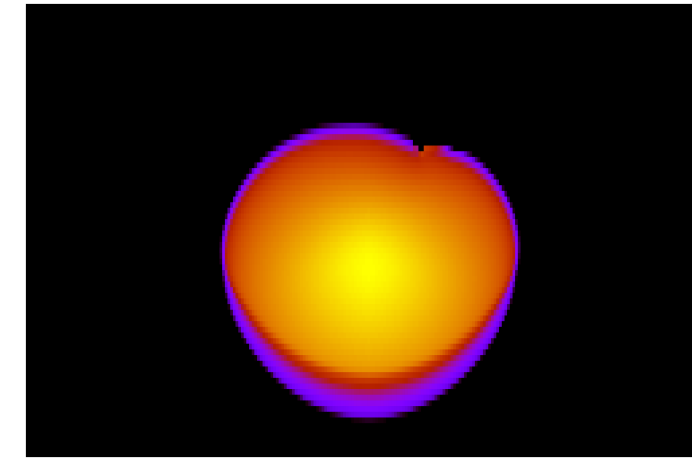
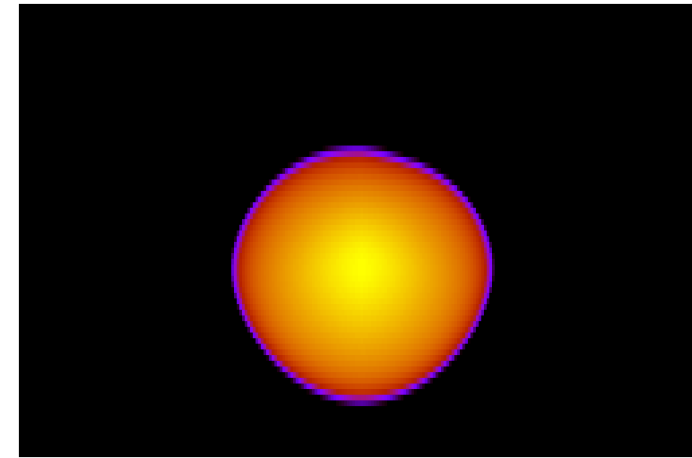
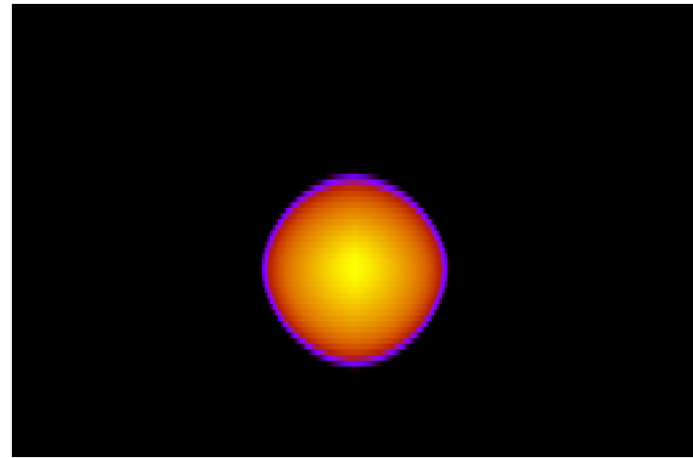
year 20

year 30

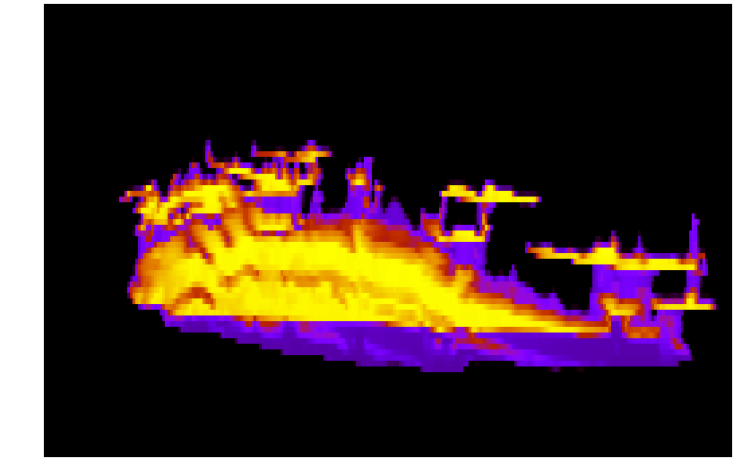
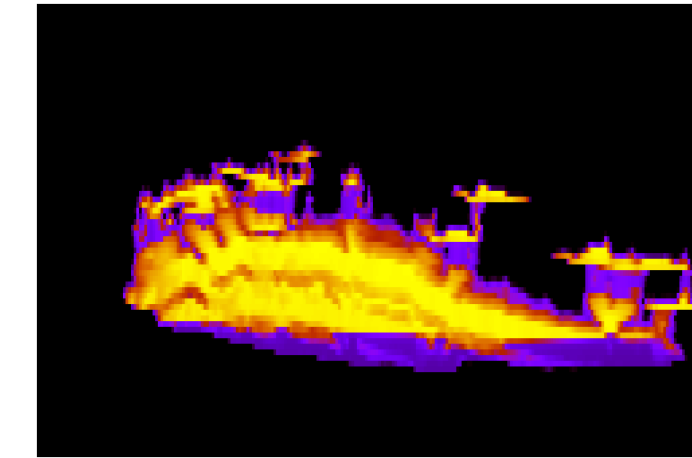
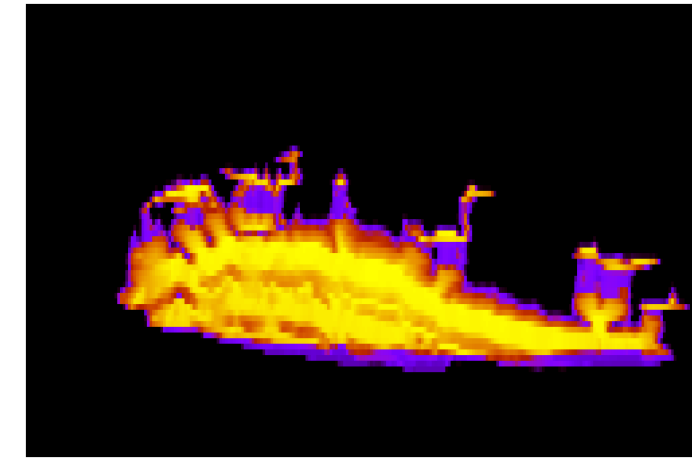
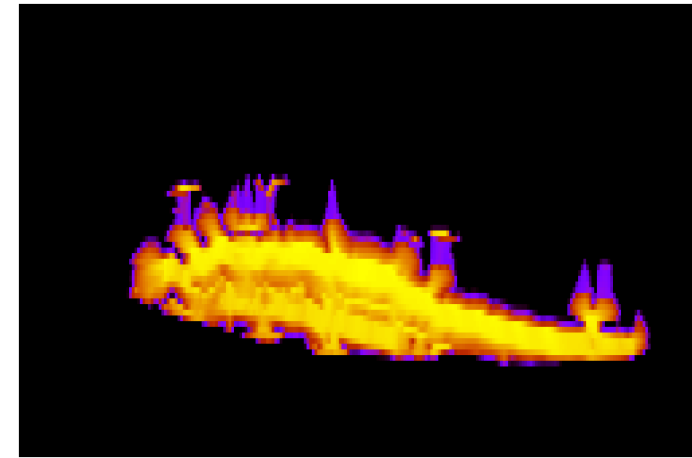
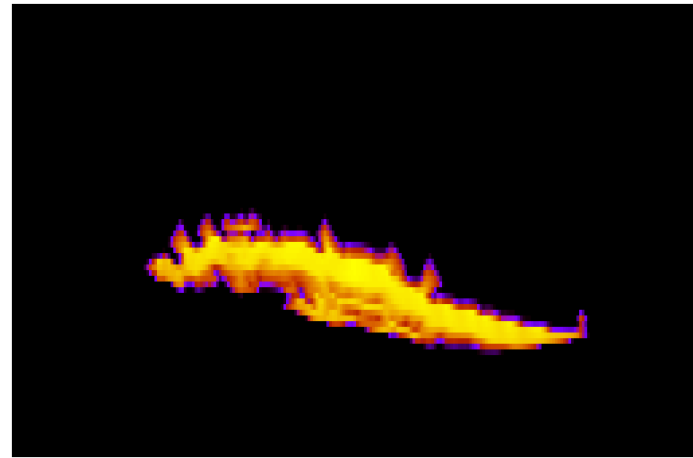
year 40

year 50

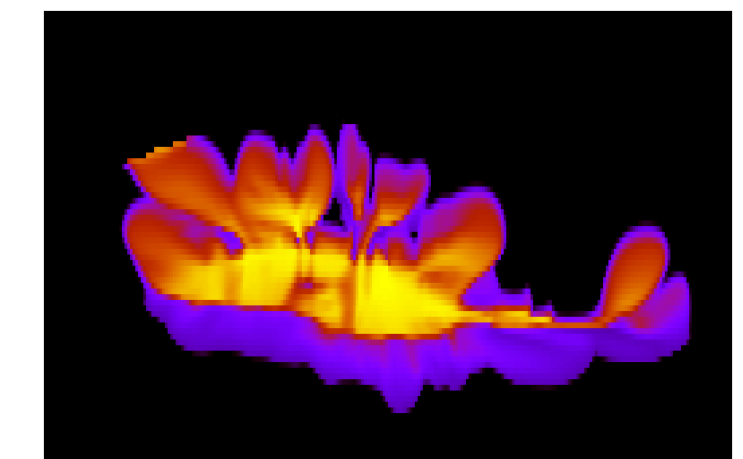
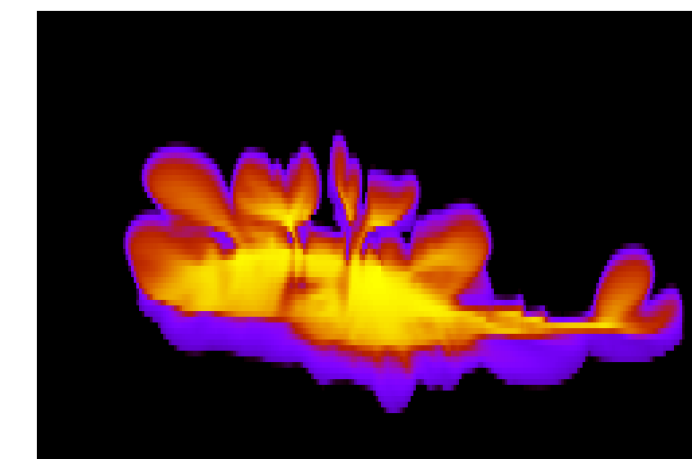
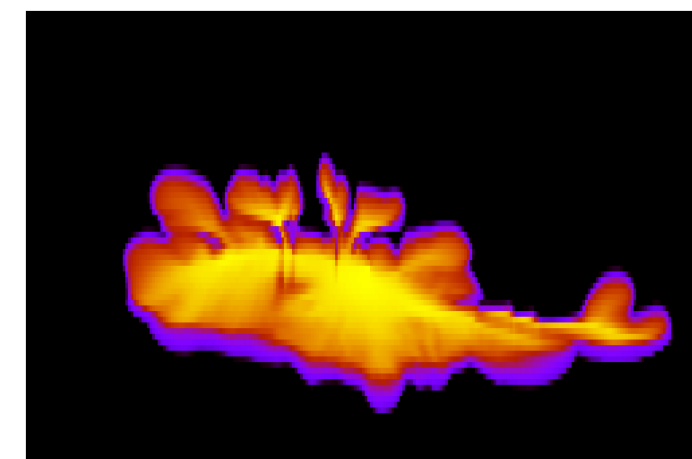
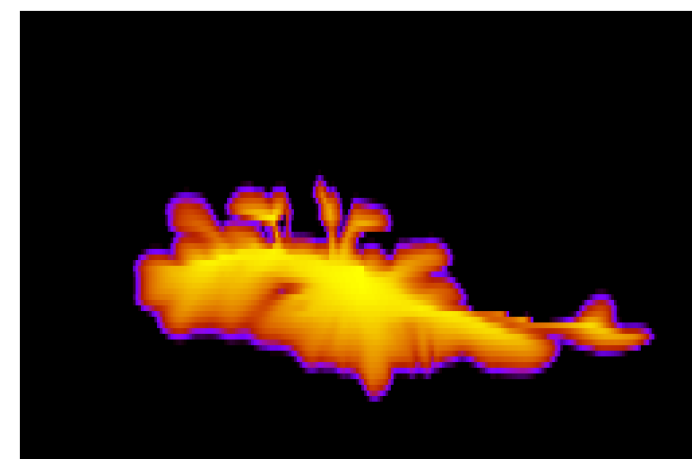
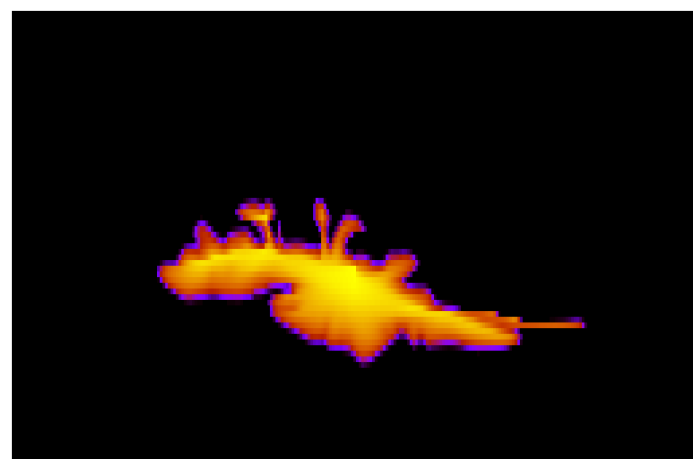
initial



ground truth



inverted

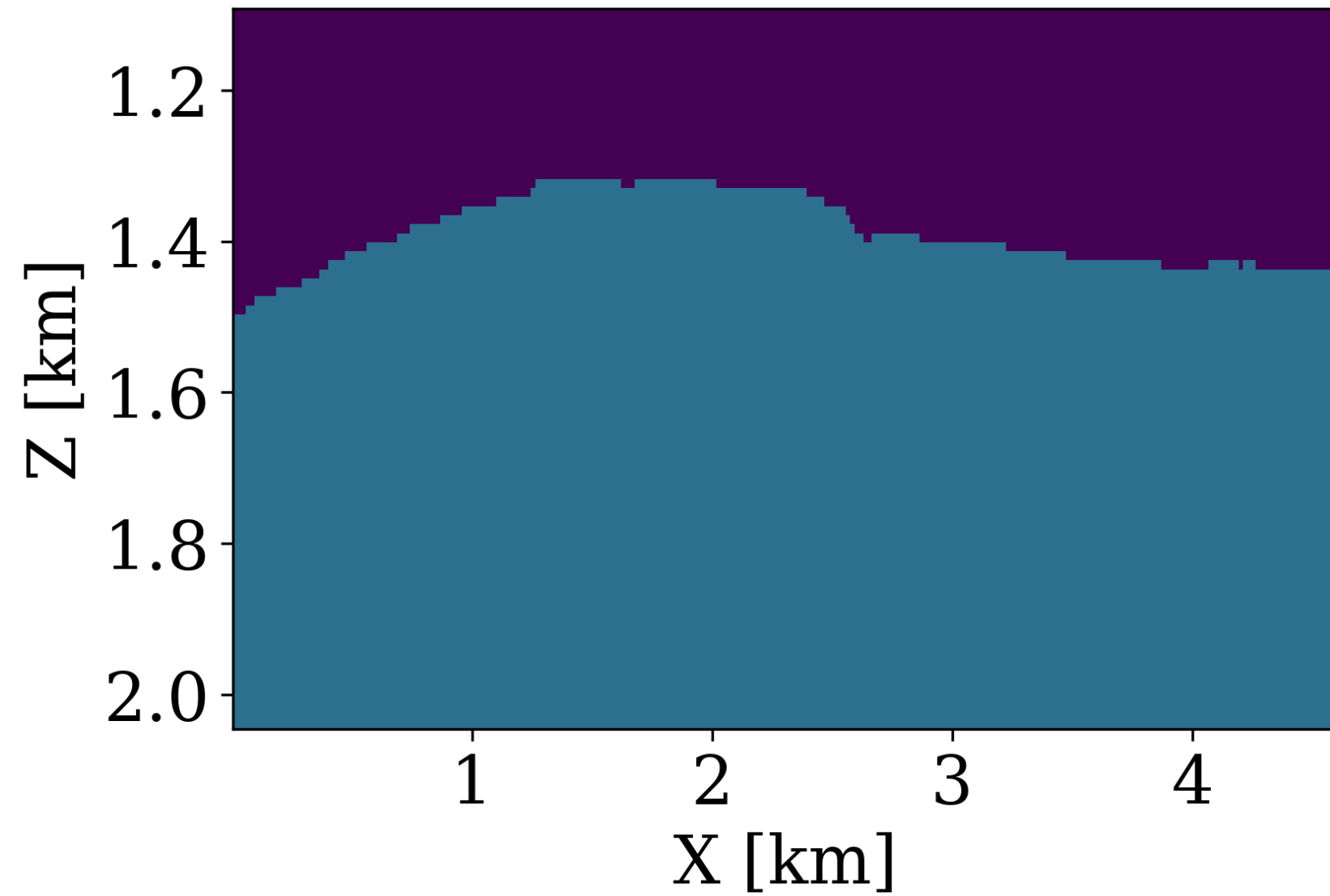




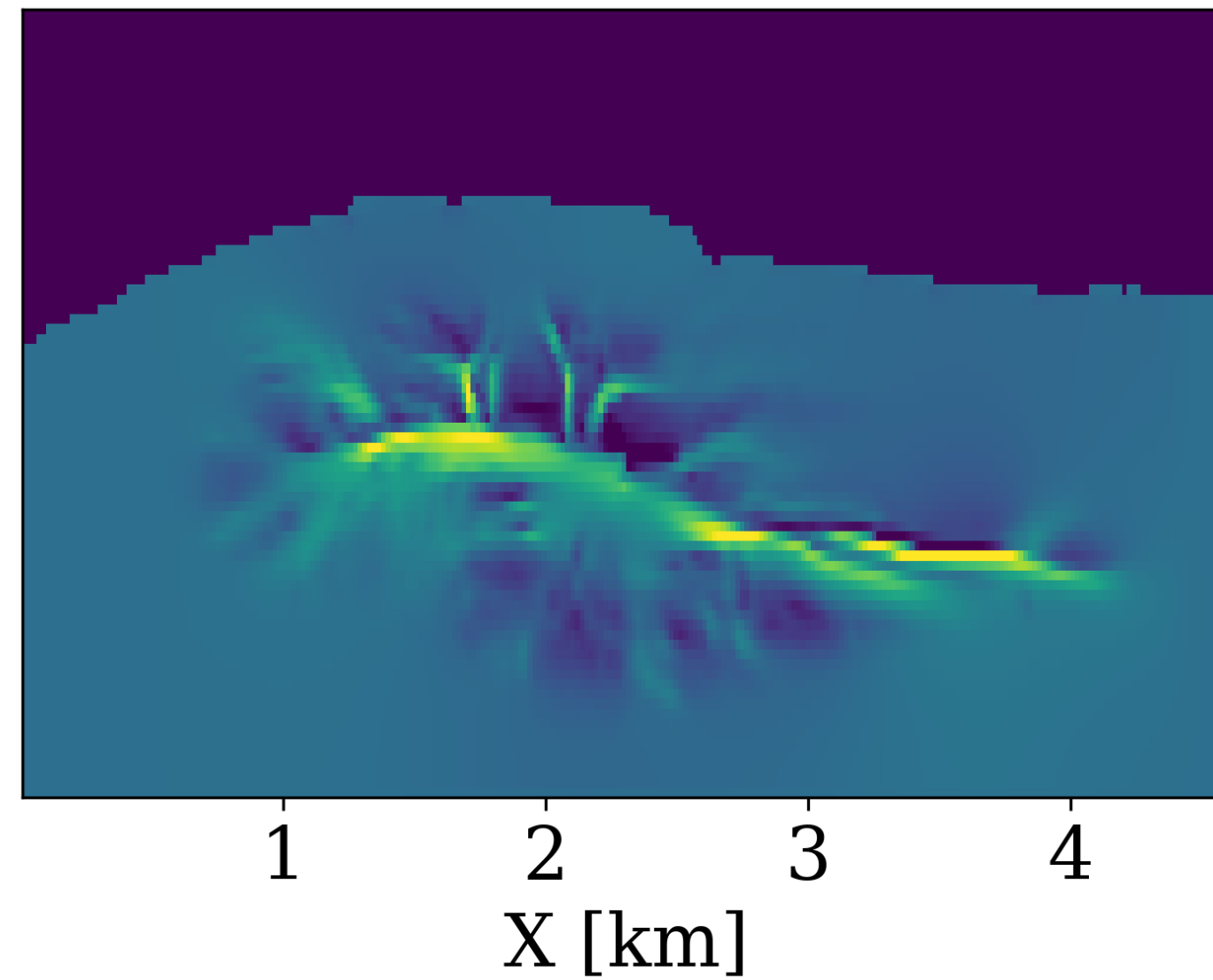
# Permeability inversion

Mathias Louboutin, Ziyi Yin, Rafael Orozco, Thomas J. Grady II, Ali Siahkoohi, Gabrio Rizzuti, Philipp A. Witte, Olav Møyner, Gerard J. Gorman, and Felix J. Herrmann, "Learned multiphysics inversion with differentiable programming and machine learning". 2023

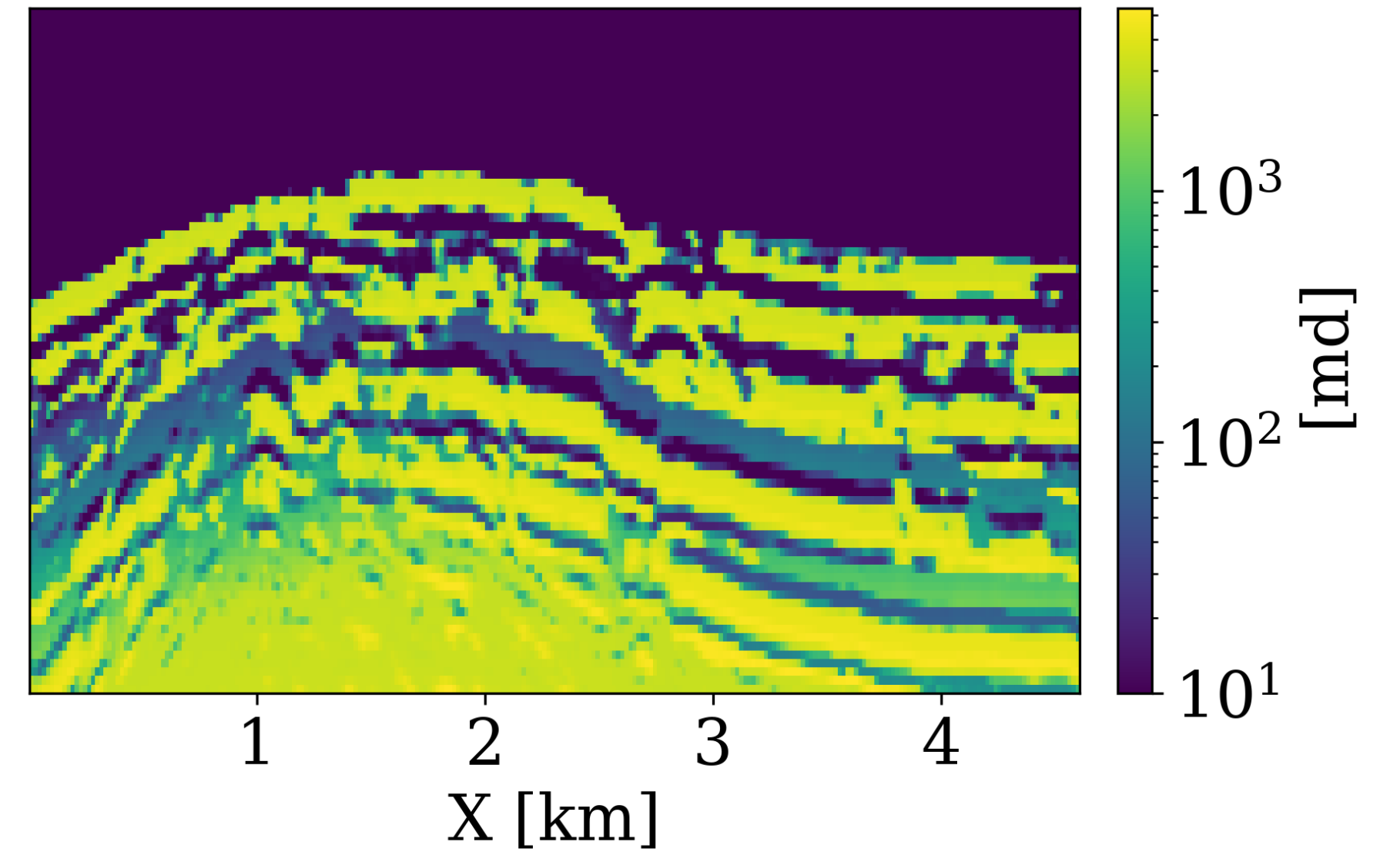
initial



inverted



ground truth



Julia packages can be found on the [SLIM](https://github.com/slimgroup) GitHub page (<https://github.com/slimgroup>).



# Acknowledgements

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<https://slim.gatech.edu/>